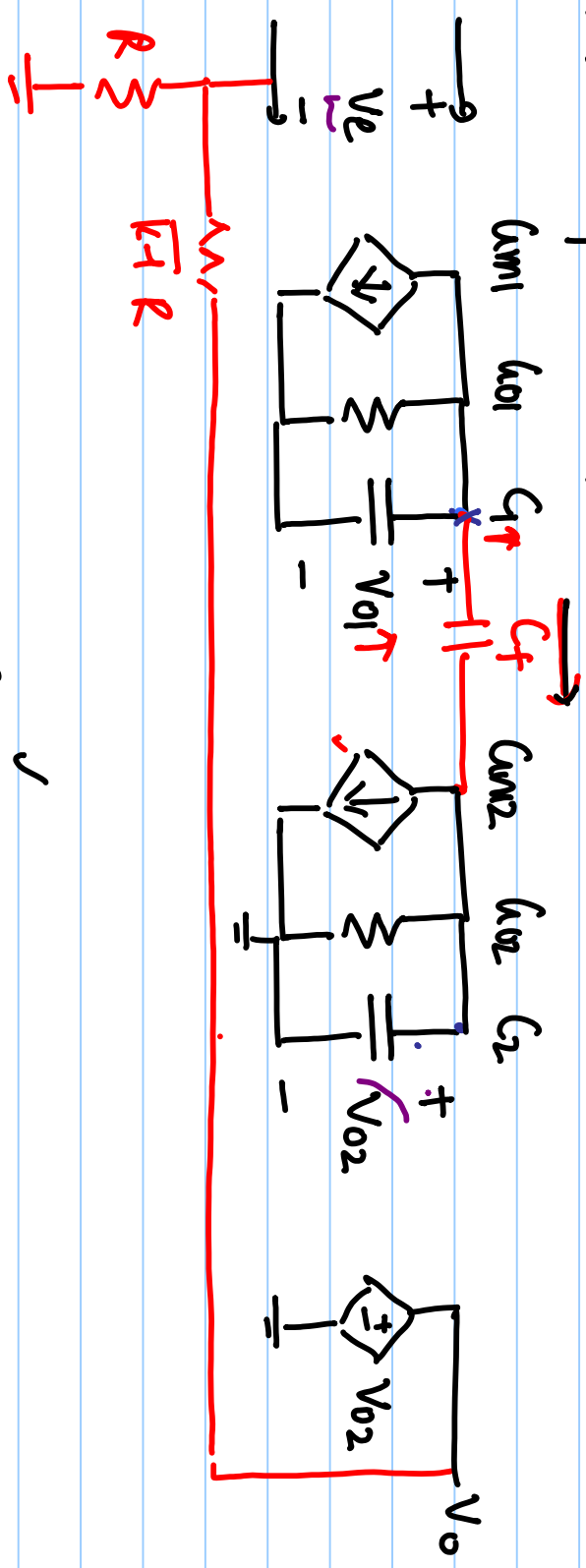


# Lecture # 20

Note Title

01-03-2022

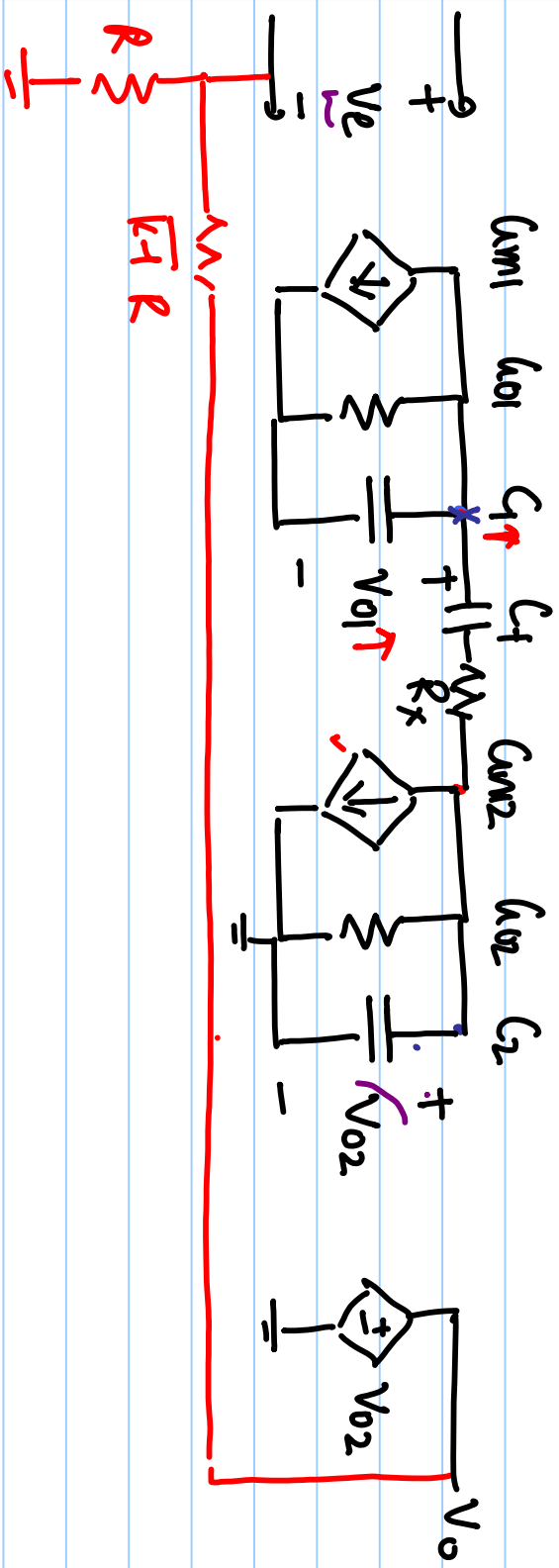
## Miller Compensation



$$\frac{V_0}{V_e} = \frac{g_{m1} g_{m2} (1 - s C_f / g_{m2})}{s^2 (C_1 C_f + C_2 (C_f + C_1 C_2)) + s (C_f g_{m2} + C_f (g_{o1} + g_{o2})) + g_{o1} g_{o2}}$$

$$z_1 = \frac{g_{m2}}{C_f} \quad (\text{R.H.P Zero})$$

$$\angle LG = -\tan^{-1} \left( \frac{\omega}{p_1} \right) - \tan^{-1} \left( \frac{\omega}{p_2} \right) - \tan^{-1} \left( \frac{\omega}{g_{m2} C_f} \right) \xrightarrow{\phi_m'} \phi_m \downarrow$$



$$\frac{1}{sC_f} \rightarrow \frac{1}{sC_f} + R_x = \frac{1 + sC_f R_x}{sC_f}$$

$$N(s) = 1 - \frac{sC_f}{g_m} \rightarrow 1 - \frac{1}{g_m} \left( \frac{1}{\frac{1}{sC_f} + R_x} \right) = 1 - \frac{1}{g_m} \frac{sC_f}{1 + sC_f R_x}$$

$$Z_1' = \frac{-g_m}{(R_x g_m - 1) C_f} < 0$$

$$= \frac{g_m + sC_f R_x g_m - sC_f}{g_m (1 + sC_f R_x)}$$

$$= \frac{g_m + sC_f (R_x g_m - 1)}{g_m (1 + sC_f R_x)}$$

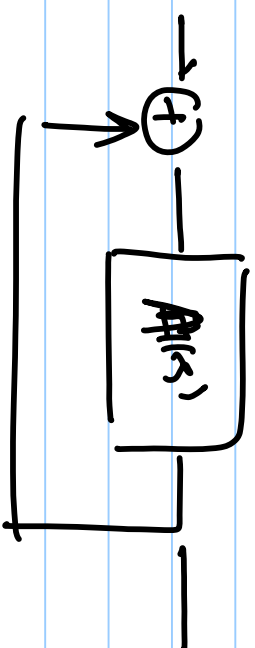
$$\left( R_x - \frac{1}{g_m} \right)$$

$$R_x - 1/g_m > 0$$

$$\begin{aligned}
 \omega_n(s) &= \frac{1}{k} \frac{\frac{G_{m2}}{a_{02}} \frac{G_{m1}}{a_{01}}}{1 + s C_f \left( R_x - \frac{1}{G_{m2}} \right)} \\
 &= \frac{s^3 \frac{C_1}{\omega_{01}} \frac{C_2}{\omega_{02}} \left\{ C_f \left( \frac{\omega_{02}}{C_2} R_x + \frac{\omega_{01}}{C_1} R_x + \frac{C_1 + C_2}{\omega_{01} \omega_{02}} \right) \right.}{+ \frac{C_1 C_2}{\omega_{01} \omega_{02}} \left. + s \left( C_f \left( R_x + \frac{1}{\omega_{01}} + \frac{1}{\omega_{02}} + \frac{G_{m2}}{\omega_{02}} \frac{1}{\omega_{01}} \right) + \frac{C_1 + C_2}{\omega_{01} \omega_{02}} \right) \right.} \\
 &\quad \left. + 1 \right\}
 \end{aligned}$$


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$$H(s) = \frac{1 - s/z_1}{1 + s/p_1}$$

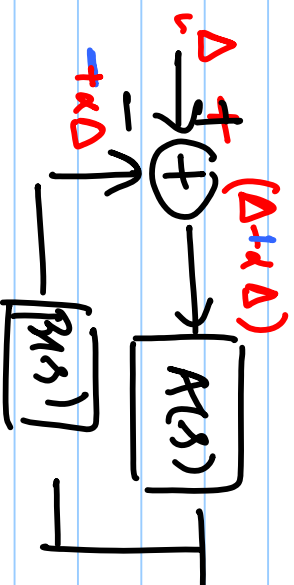
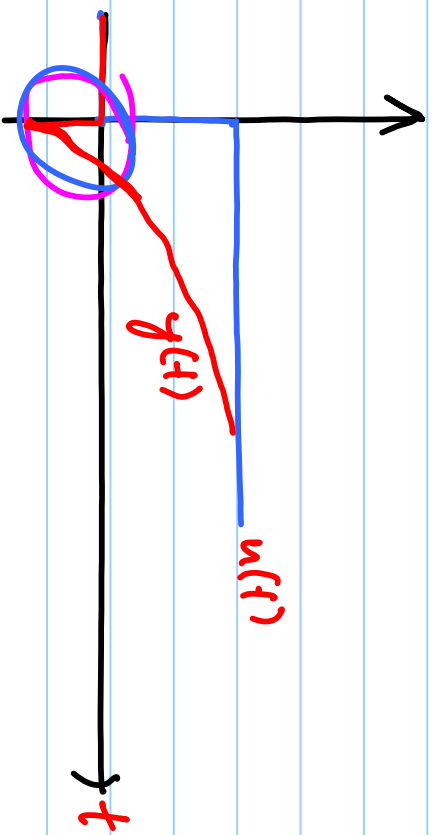


$$Y(s) = X(s) H(s)$$

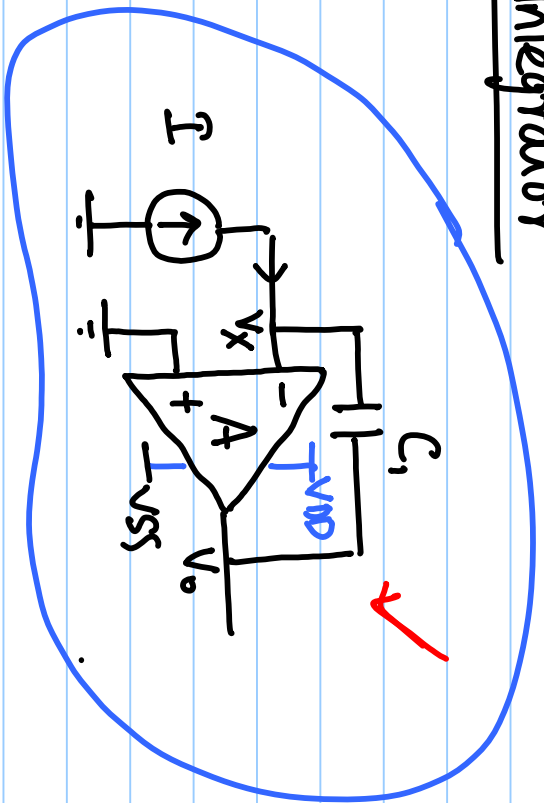
$$\begin{aligned}
 &= \frac{1}{s} \cdot \frac{1 - s/z_1}{1 + s/p_1} = \frac{1}{s} \cdot \frac{p_1}{z_1} \frac{z_1 - s}{p_1 + s}
 \end{aligned}$$

$$\begin{aligned}
 & \left[ \frac{z_1}{s} + \frac{\frac{z_1 + p_1}{-p_1}}{s + p_1} \right] \frac{p_1}{z_1} & z_1 (p_1 - s) - s(z_1 + p_1) \\
 & = \left[ \frac{z_1}{s} - \frac{z_1 + p_1}{s + p_1} \right] \times \frac{1}{z_1} & z_1 p_1 - s p_1 \\
 & & p_1 (z_1 - p_1)
 \end{aligned}$$

$$\begin{aligned}
 y(t) &= \frac{1}{z_1} \left[ z_1 - (z_1 + p_1) e^{-p_1 t} \right] u(t) & \mathcal{F} \left[ \frac{1}{s} \right] \rightarrow \left[ \frac{1}{s} \right] \\
 &= \left[ 1 - \left( 1 + \frac{p_1}{z_1} \right) e^{-p_1 t} \right] u(t) & \mathcal{F} \left[ e^{-p_1 t} \right] \rightarrow \left[ \frac{1}{s + p_1} \right]
 \end{aligned}$$



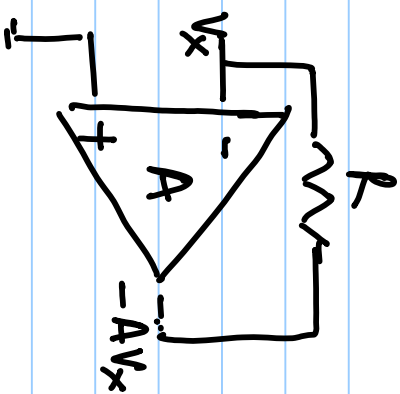
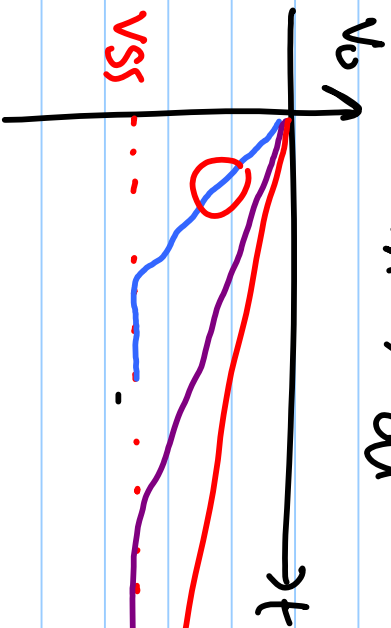
# Integrator



$$I = C_1 \frac{d(V_x - V_0)}{dt}$$

$$= C_1 \frac{d}{dt} \left( -\frac{V_0}{A} - V_0 \right)$$

$$I = -C_1 \left( \frac{1}{A} + 1 \right) \frac{dV_0}{dt}$$



$$I = C_1 \frac{d}{dt} (V_x - V_{SS})$$

$$I = C_1 \frac{dV_0}{dt}$$

$$\frac{dV_0}{dt} = \frac{I}{C_1}$$

$$V_0 = \frac{I}{C_1} t$$

