

# Resource Allocation in Multi-terminal Wireless Communication Systems

Srikrishna Bhashyam

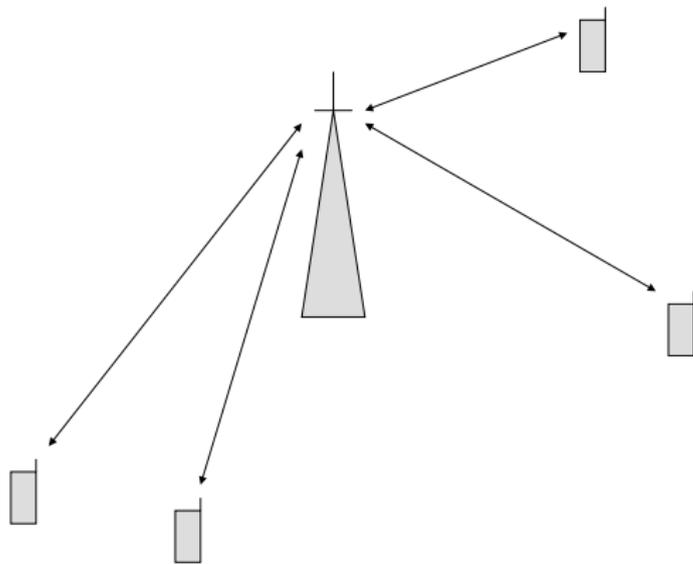
Joint work with:  
Rajesh Sundaresan  
C. Manikandan

Department of Electrical Engineering  
Indian Institute of Technology Madras

Supported by DST

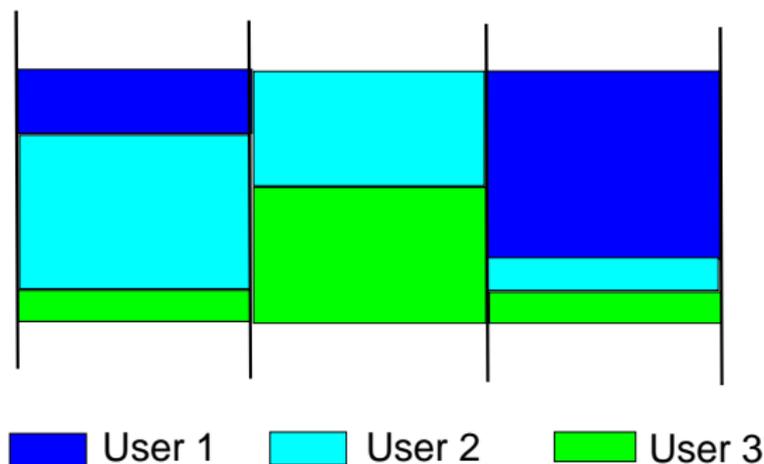
1 Apr 2011

# Cellular Systems



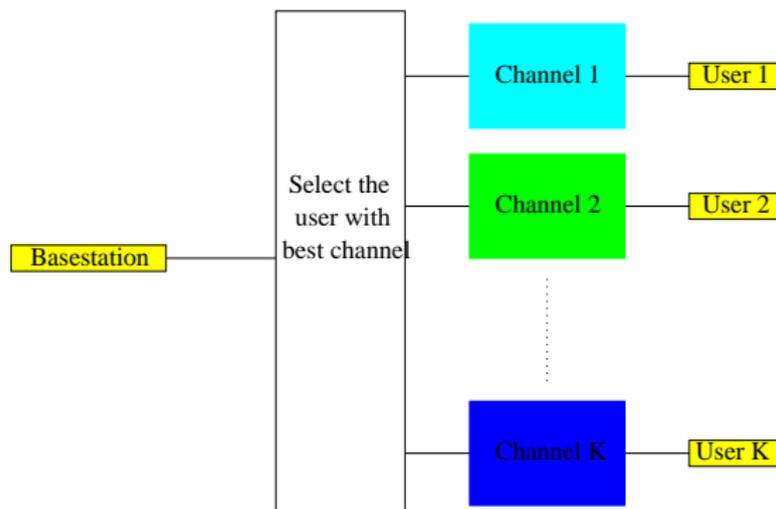
- Time-varying channel
- Resource sharing – Interference constraints

# Dynamic Resource Allocation



- Resources: Time, Bandwidth, Power
- Adaptation to channel and traffic conditions
- Dynamic resource allocation
  - ▶ Reallocation period of the order of a few milliseconds

# Adapting to the Channel: Maximizing Capacity

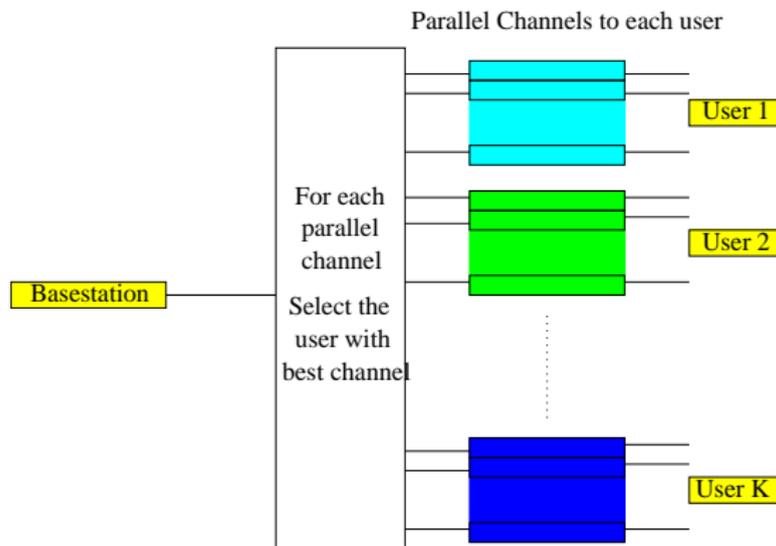


- Infinite backlog assumption
- All power and bandwidth resources to one user
- User with best achievable rate chosen:

$$i = \arg \max_k R_k,$$

where  $R_k$  is the rate that can be supported by user  $k$ .

# Maximizing Capacity: Parallel Channels

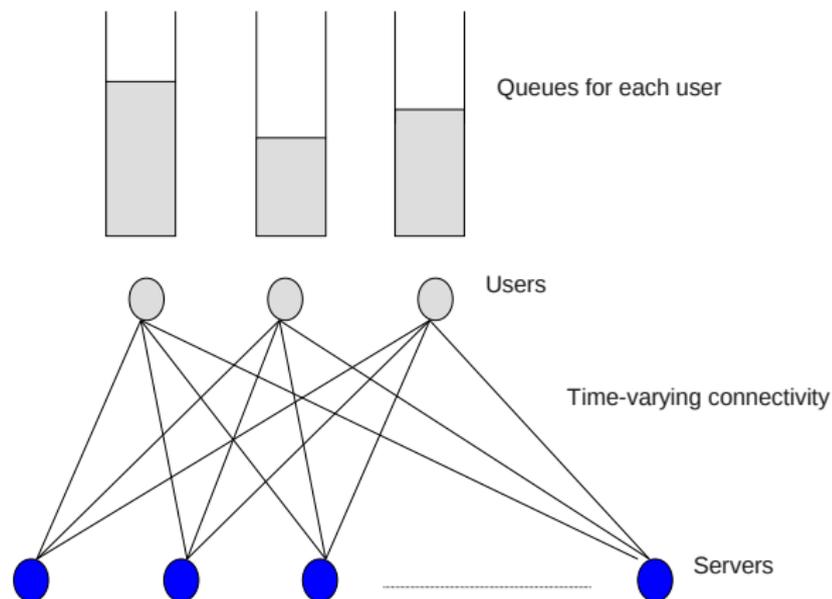


- Bandwidth resources split to achieve parallel channels
- For each channel  $n$ , user with best channel conditions chosen:

$$i_n = \arg \max_k R_{k,n}.$$

- Water-filling power allocation

# Adapting to the Channel and Traffic

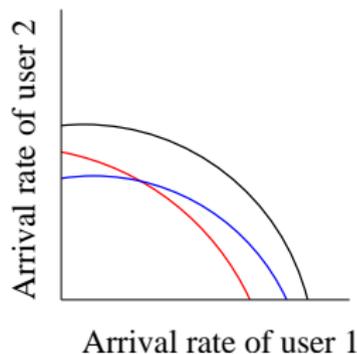


- Multi-Queue Multi-Server Model for each time slot
- Server: Subcarrier/Group of subcarriers/Spreading code

# Resource Allocation/Cross-layer Scheduling Goals

- Scheduling Goals

- ▶ Stability and throughput optimality
  - ★ Stability: Average queue length finite

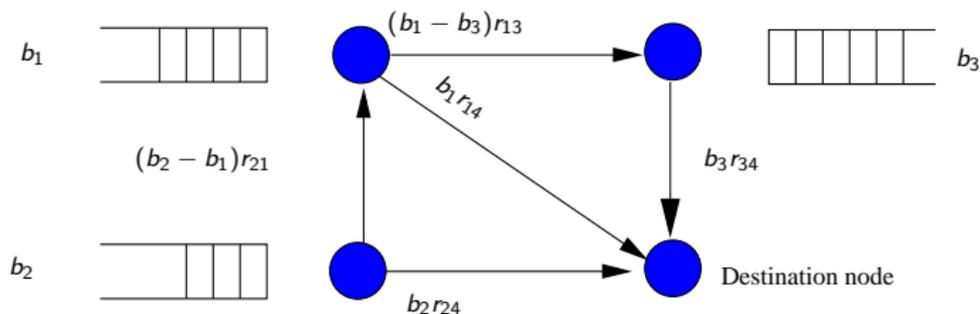


- Stability region of policy 1
- Stability region of policy 2
- Stability region of throughput optimal policy

- ▶ Packet delay constraints
- ▶ Fairness

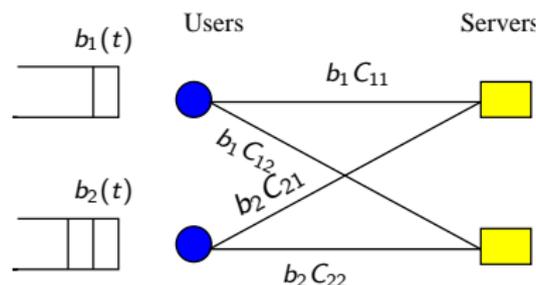
# Stability in a general wireless network

- [Tassiulas et al 1992, Georgiadis et al 2006]
  - ▶ Dynamic backpressure policy



- Interference model: Only certain links can be activated simultaneously
- Scheduling problem: Which links will you activate?
- Solution: **Activate those links such that the sum of their weights is maximum.**

# Dynamic back-pressure policy for our setting

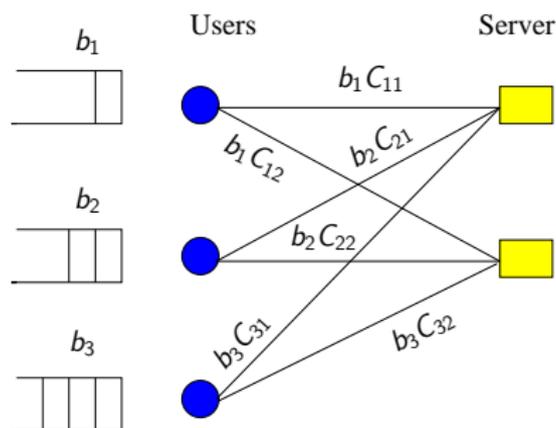


- Only one link per server to be activated. Which links to activate?
- *Solution:*
  - ▶ Make the servers as destination nodes.
  - ▶ Assign the weights for each link as in back-pressure policy.
  - ▶ Activate those links such that the sum of their weights is maximum.

$$\max \sum_k b_n C_{nk}$$

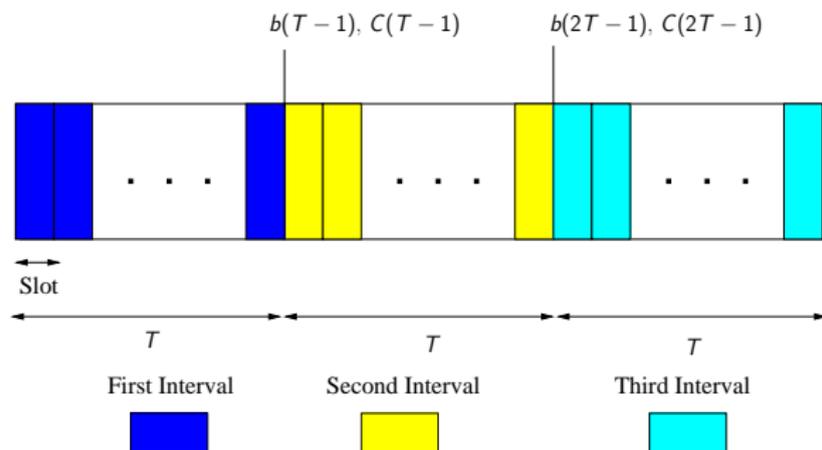
$b_n$ : Backlog of user  $n$ ,  $C_{nk}$ : Capacity of user  $n$  on server  $k$

# Two Throughput Optimal Policies



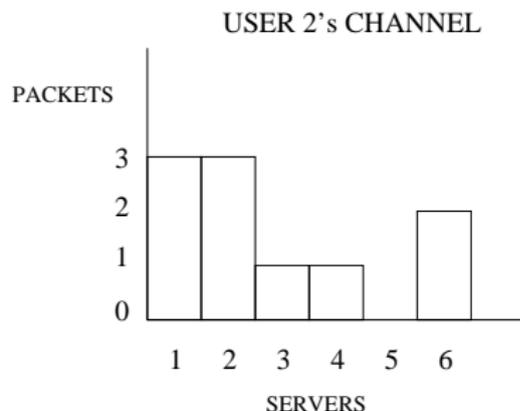
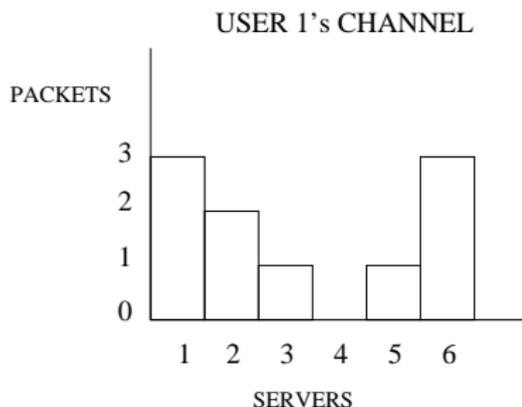
- Policy 1: Dynamic backpressure policy
- Policy 2: **Improving delay performance**
  - ▶ Update queue information after each server is scheduled

# Using Delayed Information



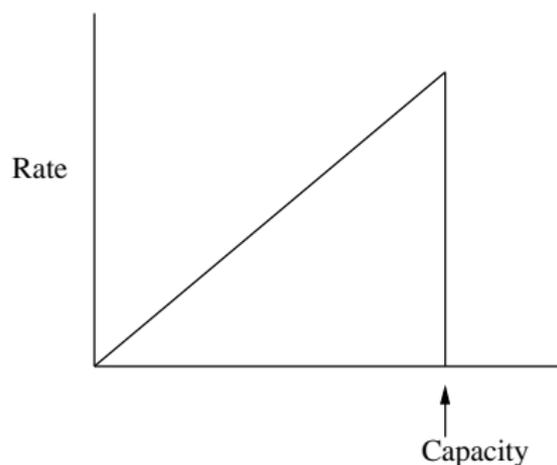
- Time-slots are grouped into intervals
- Channel and queue information available only once in  $T$  slots

# Channel model



- $C_{nk}$ : channel capacity of user  $n$  on server  $k$ .
- $C_{nk} \in \{0, 1, 2, 3\}$ .

# Loss model



Packets sent

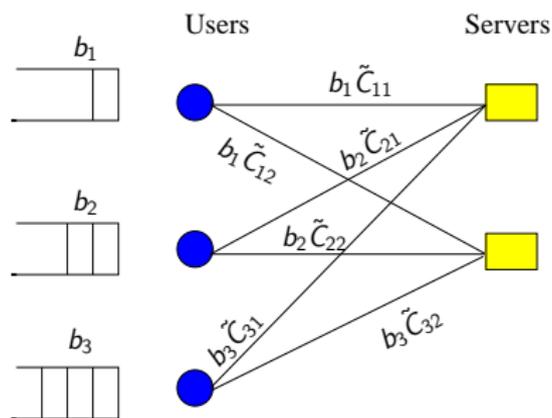
$R_{nk}$	0
$R_{nk} \leq C_{nk}$	$R_{nk} > C_{nk}$

- $R_{nk}$ : number of packets user  $n$  transmits on server  $k$ .
- $C_{nk}(IT - 1)$ : channel information available at the start of  $l^{th}$  interval.

# Results

- Retain throughput optimality of dynamic backpressure policy
- Two policies: Policy 1 and Policy 2
- Comparison with KLS policy [Kar et al 2007]

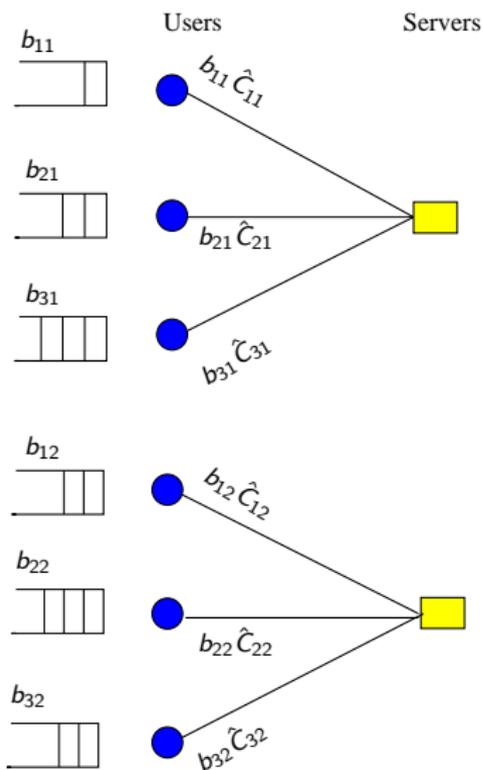
## Policy 1 & Policy 2



$$\begin{aligned} \text{Define } \tilde{C}_{nk} &= \max_r E [T_{nk}(t) | C_{nk}(IT - 1)] \\ &= \max_r r \Pr\{r \leq C_{nk} | C_{nk}(IT - 1)\} \end{aligned}$$

- Policy 1 is the dynamic back pressure policy for our setting
- Assignment changes every slot
- Policy 2: Update queue information after each server is scheduled

# KLS Policy



- Virtual queue for each user-server pair
- Define  $\hat{C}_{nk}(IT)$  as

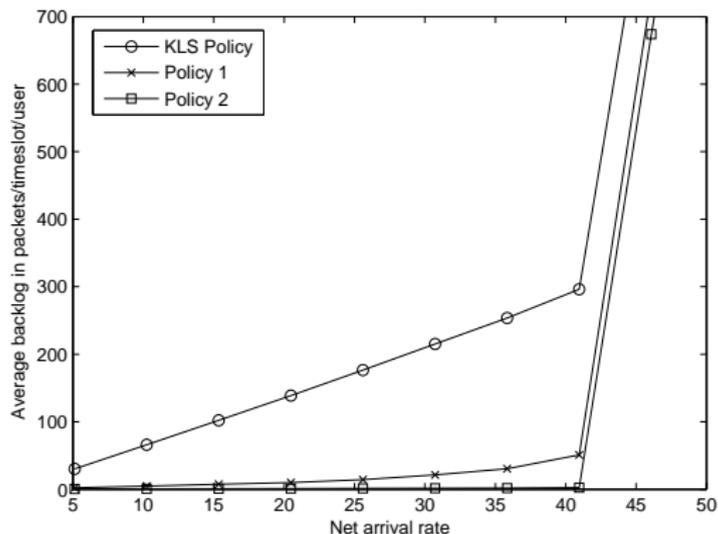
$$\frac{1}{T} \mathbb{E} \left[ \sum_{t=IT}^{(l+1)T-1} C_{nk}(t) \middle| C_{nk}(IT-1) \right]$$

- Assignment changes once in  $T$  slots

# Simulation setup

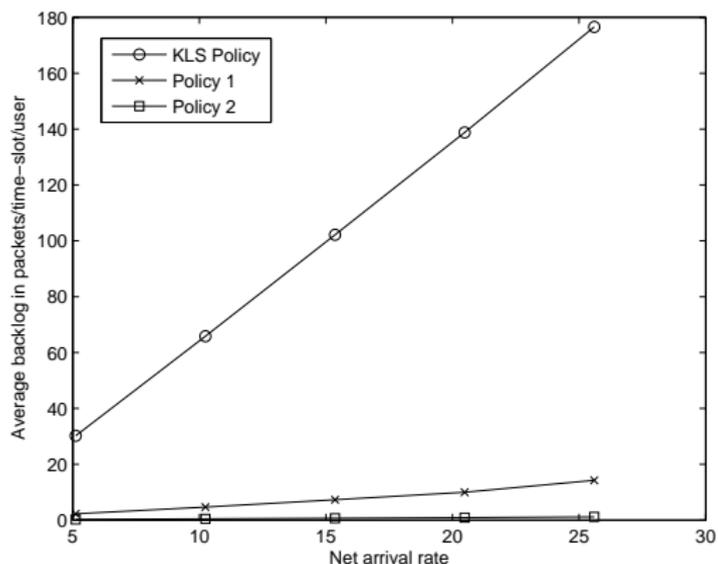
- Truncated Poisson arrivals
- 128 users and 16 servers
- Markov fading channel with probability transition matrix
- Backlog and delay are used as metrics for comparison
- Simulations for both symmetric and asymmetric arrivals
  - ▶ Symmetric case shown here

## Average backlog comparison: Slow fading, $T = 8$



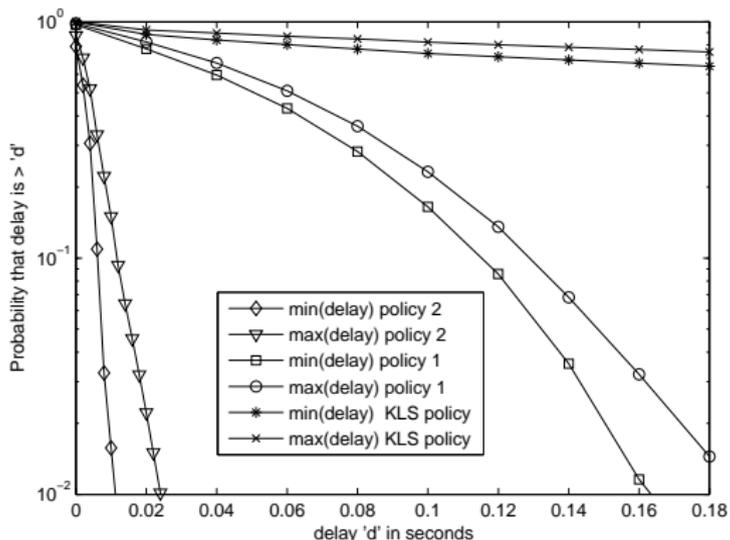
- All the policies have similar stability region.

## Average backlog comparison for low traffic



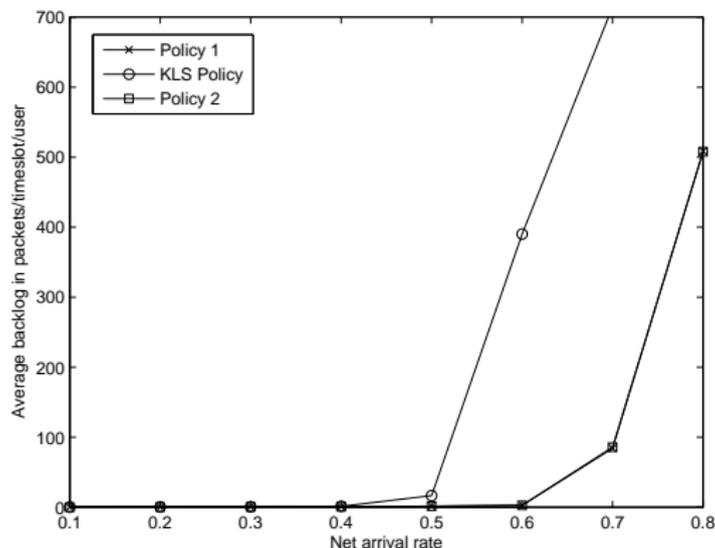
- At low traffic, proposed policies outperform KLS policy.

# Delay comparison



- Net arrival rate = 25.6,  $T = 4$

# Comparison of stability regions: Fast fading



- 2 queues, 1 server,  $T = 2$ , states are  $\{0, 1\}$
- Probability transition matrix:  $\begin{bmatrix} \delta & 1 - \delta \\ 1 - \delta & \delta \end{bmatrix}$ ,  $\delta = 0.1$

# Fairness and Utility Maximization

- Arrival rate vector outside stability region
  - ▶ Support a fraction of the traffic
  - ▶ Optimize utility based on long term throughput
  - ▶ Flow control to get stabilizable rates + stabilizing policy
  - ▶ Fairness based on choice of utility function
    - ★ Proportional fairness

# Possible Extensions

- More physical layer options
  - ▶ Multiple antennas
  - ▶ Power allocation across resources (servers)
  - ▶ Interference processing vs. Interference avoidance
  - ▶ Multi-cell scenario: Centralized vs. Distributed methods
- Requirements
  - ▶ Lower complexity/approximate solutions to optimization problem
  - ▶ Appropriate reduction search space of physical layer modes

# Summary

- Adapting to the channel
- Adapting to the channel and traffic
  - ▶ Dynamic backpressure policy
- Adapting to imperfect information
  - ▶ Conditional expected rate in backpressure policy
- Possible extensions
  - ▶ Approximate lower complexity solutions
  - ▶ Appropriate choice of physical layer modes