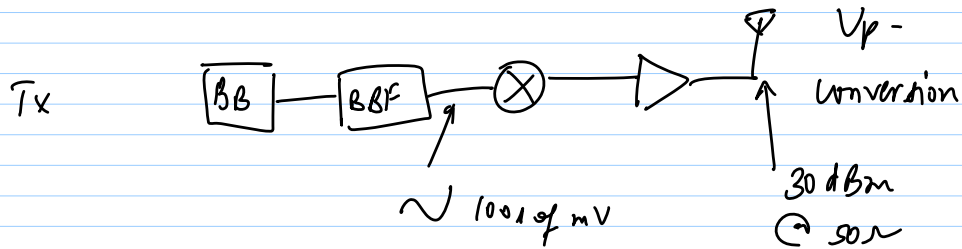
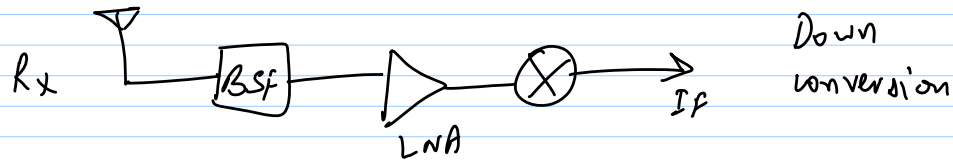


16-9-13

Lec 19  
Mixers



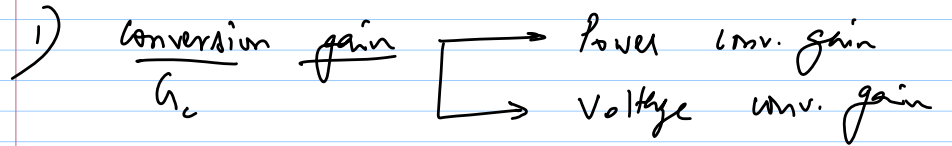
\* Multiplication

$$x_{RF}(t) = A_{RF} \cos \omega_{RF} t \quad ; \quad x_{LO}(t) = A_{LO} \cos \omega_{LO} t$$

$$x_{IF}(t) = x_{RF}(t) \times x_{LO}(t)$$

$$= \frac{A_{RF} A_{LO}}{2} \left[ \cos(\omega_{LO} - \omega_{RF})t + \cos(\omega_{LO} + \omega_{RF})t \right]$$

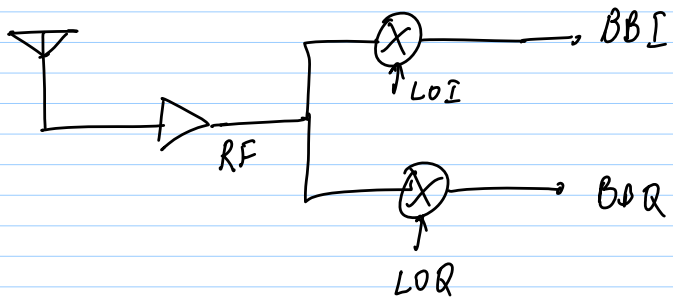
Metrics



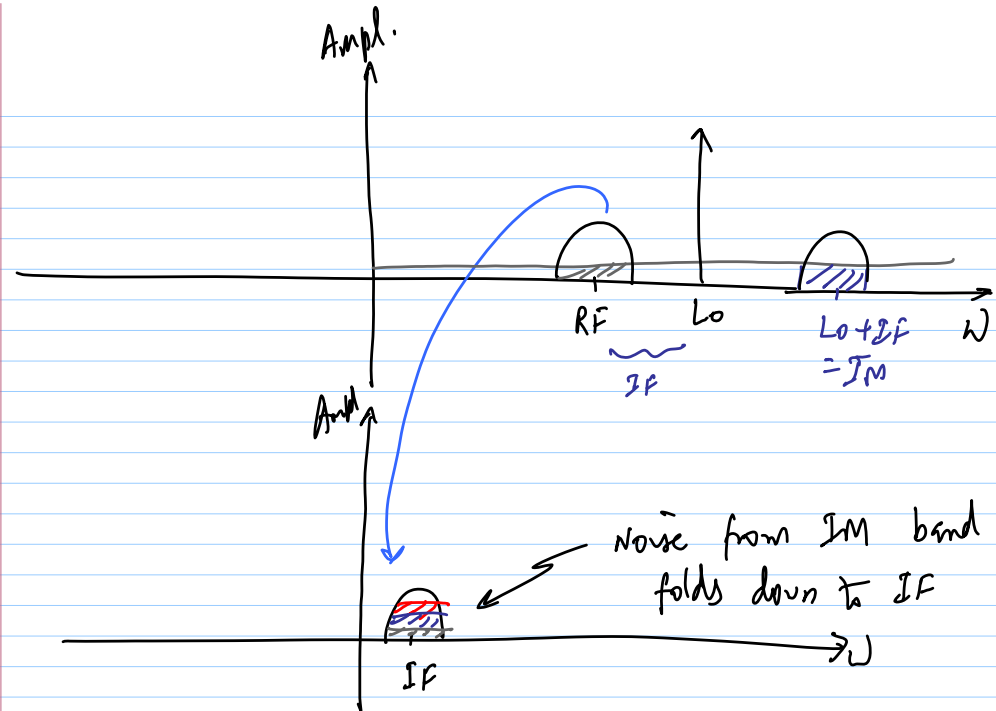
$$G_c = \frac{A_{LO} A_{RF}/2}{A_{RF}} = \frac{A_{LO}}{2} \quad ; \quad G_c < 1 \text{ is possible}$$

2) NF

$$NF = \frac{SNR @ RF \text{ port}}{SNR @ IF \text{ port}} \quad (\text{diff. freq.})$$



$$NF = \frac{SNR_{RF}}{SNR_I} = \frac{SNR_{RF}}{SNR_Q}$$



NF of ideal wireless mixer is already 3dB!

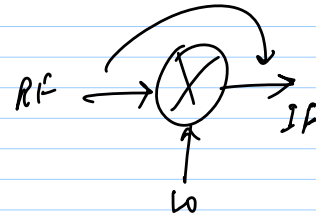
$$NF_{SSB} = NF_{DSB} + 3dB$$

RF sig only in RF band

Sig in RF & Im bands

### 3) Linearity

$1IP_3, 1IP_2, P1-dB$



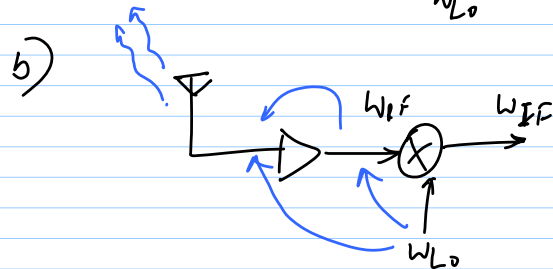
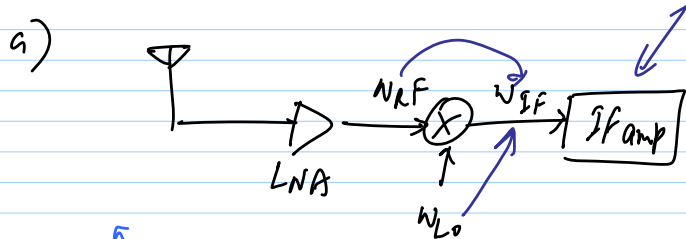
\* AM radio

$$IF = 455kHz; f_{RF} = 910kHz$$

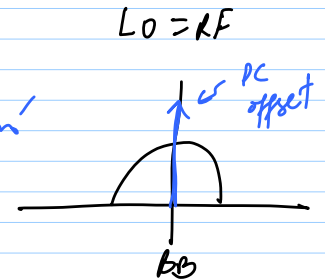
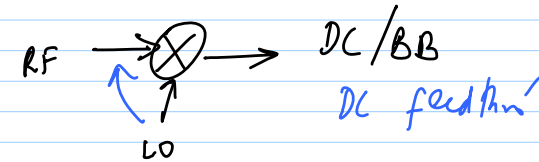
$$\Rightarrow f_{LO} = 1365kHz$$

$$\text{Cubic NL} - (2\omega_{RF} - \omega_{LO}) = \omega_{IF}$$

### 4) Isolation



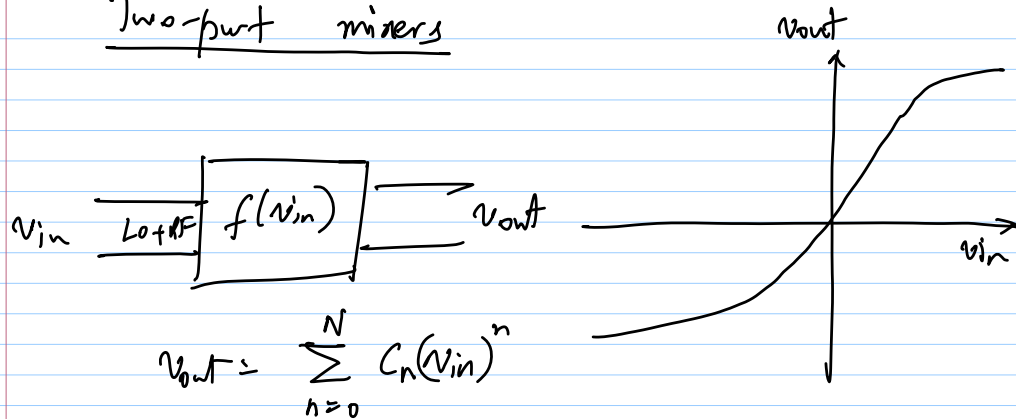
### 5) DCR



### 5) Spurs

- spurious tones  
undesired freq. components  
@ mixer o/p

## Two-port mixers



$$v_{out} = \sum_{n=0}^N C_n (v_{in})^n$$

\* DC terms - even order NL

\* harmonics of inputs  $m\omega_{LO}$  &  $m\omega_{RF}$   
- filter out

\* IM terms

-  $\omega_{RF} \pm \omega_{LO} \rightarrow$  desired terms for mixing

\*  $p\omega_{RF} \pm q\omega_{LO}$  - undesired IM terms

## Square-law Mixer

$C_i = 0$  for  $i \neq 1, 2$

$$v_{out} = C_1 v_{in} + C_2 v_{in}^2$$

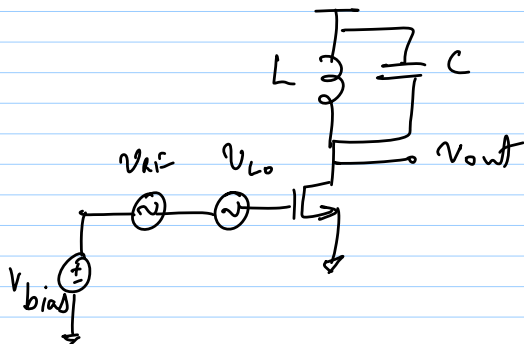
$$v_{in} = v_{RF} \cos \omega_{RF} t + v_{LO} \cos \omega_{LO} t$$

cross term in square term:

$$= 2C_2 v_{RF} v_{LO} \cos \omega_{RF} t \cos \omega_{LO} t$$

$$= C_2 v_{RF} v_{LO} [\cos(\omega_{LO} - \omega_{RF})t + \cos(\omega_{LO} + \omega_{RF})t]$$

### example 1



### example 2

