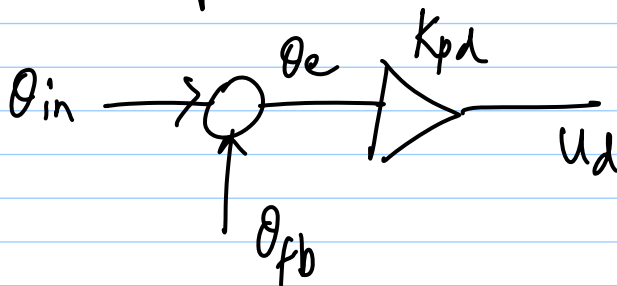
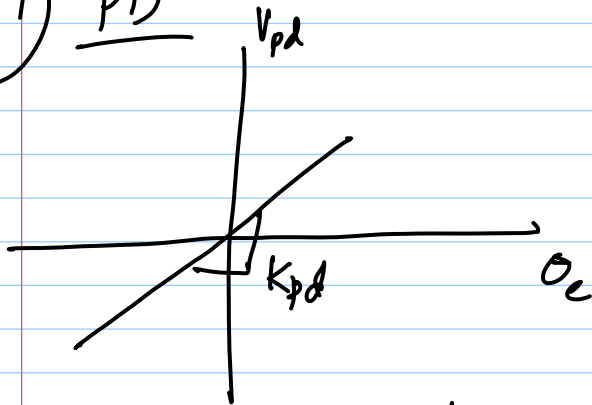


$$\frac{15413}{1}$$

Lec 42

$$\frac{U_d}{\theta_e}(A) = K_{pd}$$

1) PD



2) VCO

$$W_o = W_{free} + K_{vw} \cdot V_i(t)$$

$$w = \frac{d\varphi}{dt}, \quad ; \quad \varphi = \int w dt$$

$$\theta_s = \int K_{V\omega} V_c(t)$$

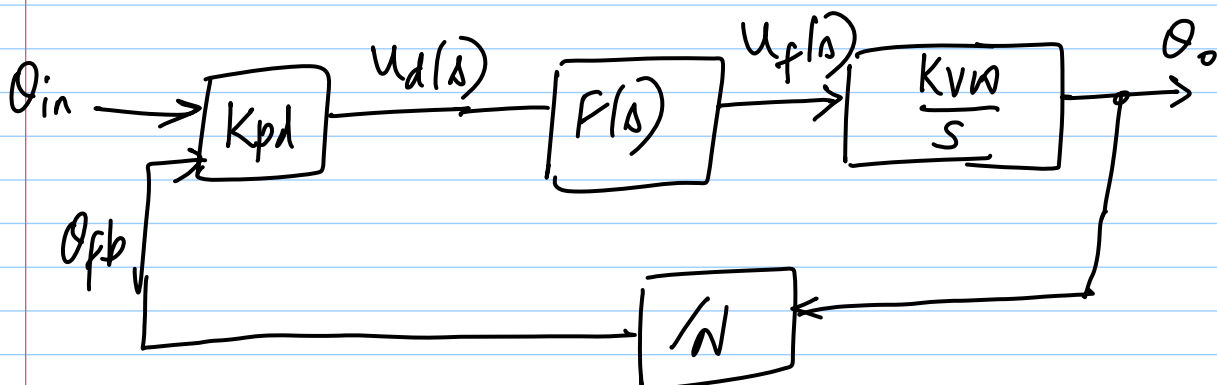
$$\theta_o(s) = \frac{K_{v\omega}}{s} \cdot V_c(s)$$

$$\frac{Q_o}{V_c}(1) = \frac{K_{vw}}{s}$$

3) Divider

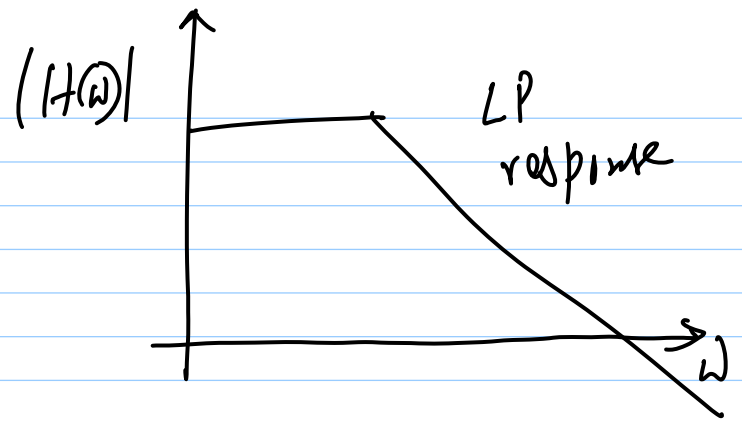
$$\frac{\partial f_b}{\partial \theta}(\lambda) = \frac{1}{N}$$

Linear PLL model



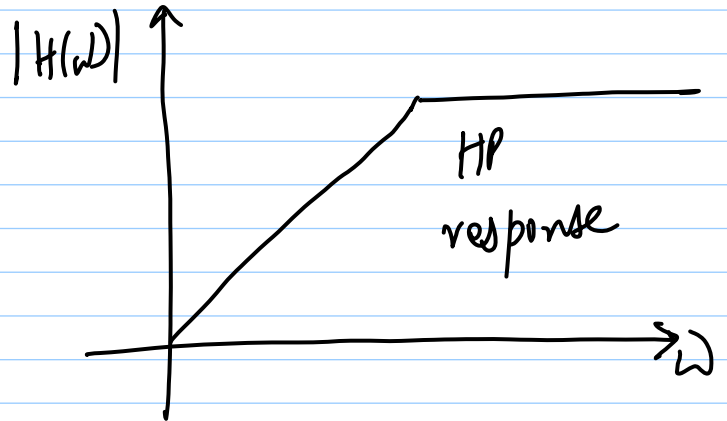
$$* \quad H(n) = \frac{\theta_{fb}}{\theta_{in}} (n)$$

$$= \frac{K_{pd} K_{vw} F(s)/N}{s + K_{pd} K_{vw} F(s)/N}$$



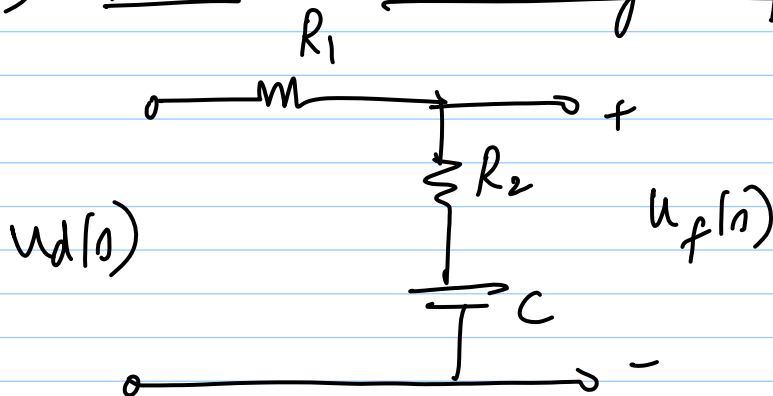
$$* H_e(s) = \frac{\theta_e(s)}{\theta_{in}} = 1 - H(s)$$

$$= \frac{s}{s + K_{pd} K_{vw} F(s)/N}$$



Loop Filters F(s)

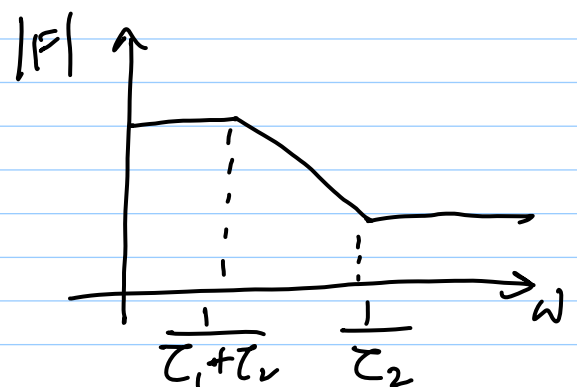
1) Passive Lead-lag filter



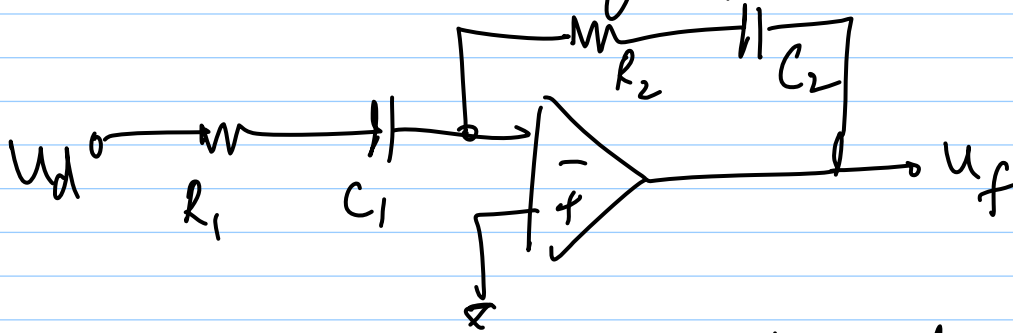
$$\tau_1 = R_1 C$$

$$\tau_2 = R_2 C$$

$$F(s) = \frac{1 + s\tau_2 \text{ (lead)}}{1 + s(\tau_1 + \tau_2) \text{ (lag)}}$$

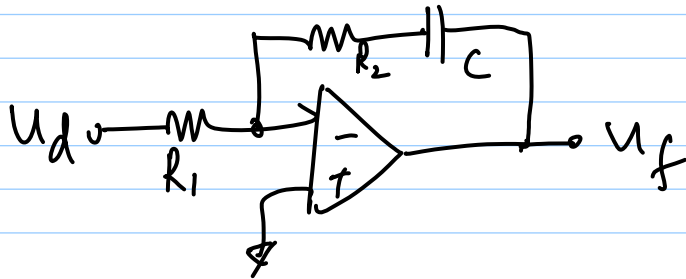


2) Active lead lag filter



$$K_a = C_1 / C_2; \quad F(s) = K_a \cdot \frac{1 + s\tau_2}{1 + s\tau_1}$$

3) Active PI filter (proportional + Integral)



$$F(s) = \frac{1}{R_1} \left[\frac{1 + sCR_2}{sC} \right] = \frac{1 + s\tau_2}{s\tau_1}$$

* for the PI filter

$$H(s) = \frac{\frac{K_{pd} K_{v\omega}}{N} \cdot \frac{(1 + s\tau_2)}{\tau_1}}{s^2 + s \cdot \frac{K_{pd} K_{v\omega} \tau_2 / N}{\tau_1} + \frac{K_{pd} K_{v\omega} / N}{\tau_1}}$$

$\left(s^2 + 2\zeta\omega_n s + \omega_n^2 \right)$