

15-3-13

Lec 38

Bandgap Reference

* Create V/I that is independent of P, V, T variations

$$V = \alpha_1 V_1 + \alpha_2 V_2$$

$$\frac{\partial V}{\partial T} = 0 \Rightarrow \alpha_1 \frac{\partial V_1}{\partial T} + \alpha_2 \frac{\partial V_2}{\partial T} = 0$$

↓
 -ve T.C.

↑
 +ve T.C.

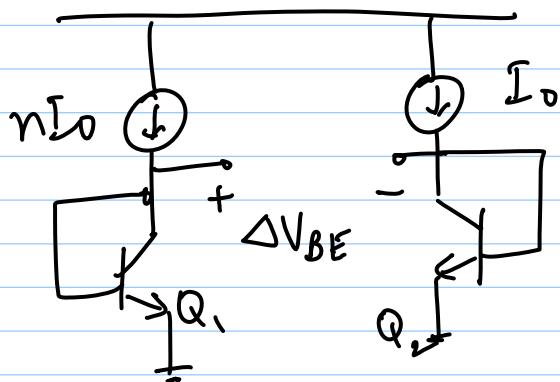
$$V_{BE} = V_T \ln \left(\frac{I_C}{I_S} \right) ; \quad V_T = \frac{kT}{qV}$$

$$\begin{aligned} \frac{\partial V_{BE}}{\partial T} &= \frac{(4+m)}{T} I_S + \frac{Eg}{kT^2} \cdot I_S \\ &= \underbrace{V_{BE}}_{T} - (4+m)V_T - \frac{Eg}{qV} \end{aligned}$$

$$V_{BE} = 0.75V, \quad T = 300K,$$

$$\frac{\partial V_{BE}}{\partial T} \approx -1.5mV/K$$

positive T_C



$$\Delta V_{BE} = V_{BE1} - V_{BE2}$$

$$= V_T \ln \left(\frac{n I_0}{I_s} \right)$$

$$- V_T \ln \left(\frac{I_0}{I_s} \right)$$

$$= V_T \ln(n)$$

$$\frac{\partial}{\partial T} (\Delta V_{BE}) = \frac{k}{q} \ln(n) \quad (\text{true temp})$$

$$\frac{k}{q} = 0.087 \text{ mV/K}$$

$$V_{ref} = \alpha_1 V_1 + \alpha_2 V_2$$

$$= \alpha_1 V_{BE} + \alpha_2 (V_T \ln n)$$

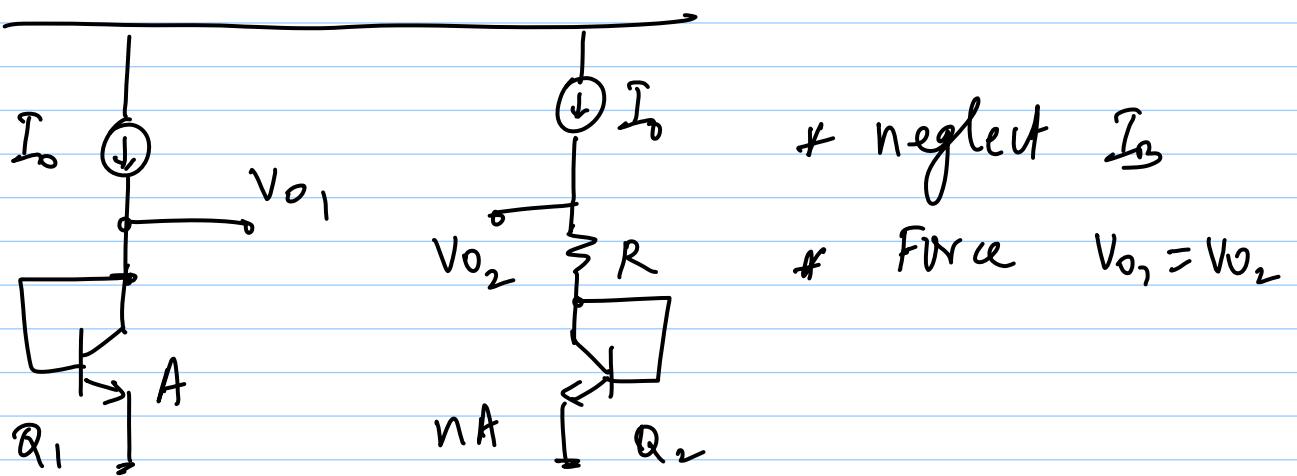
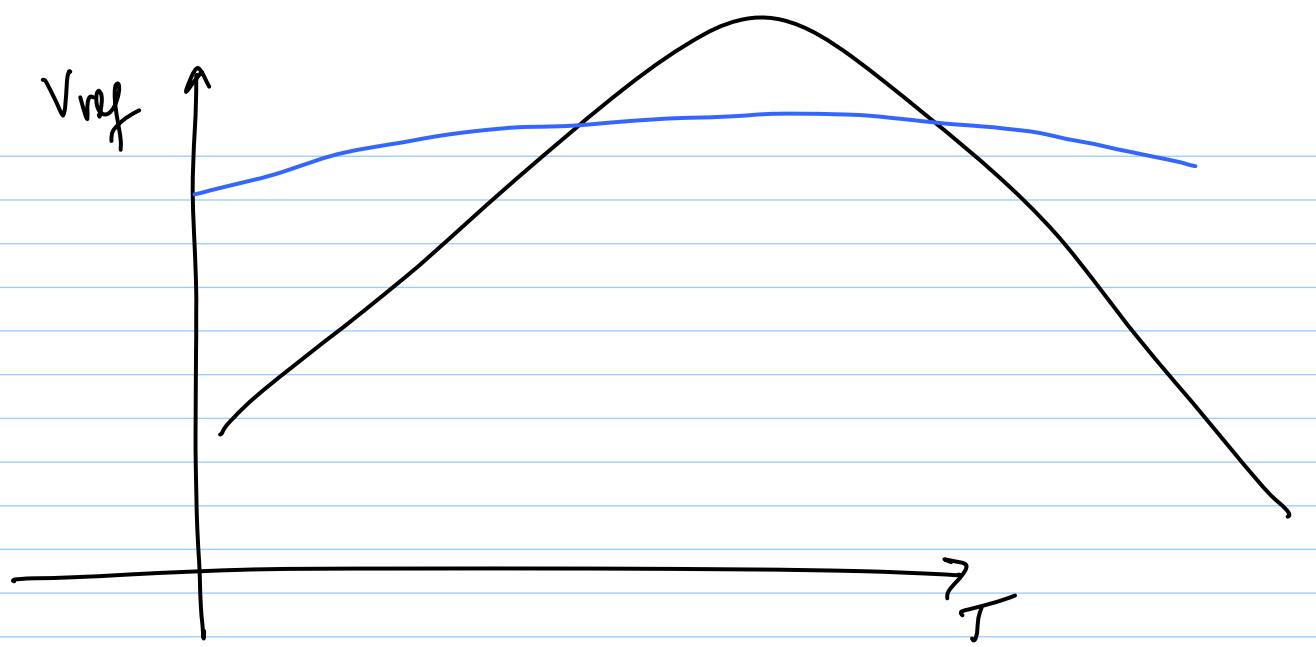
Set $\alpha_1 = 1$

$$@ 300K \quad (\alpha_2 \ln n) (0.087 \text{ mV/K}) = 1.5 \text{ mV/K}$$

$$\alpha_2 \ln n \approx 17.2$$

$$V_{ref} = V_{BE} + (17.2) V_T$$

$$\approx 1.25V @ 300K$$



$$V_{BE_1} = V_{BE_2} + I_o R$$

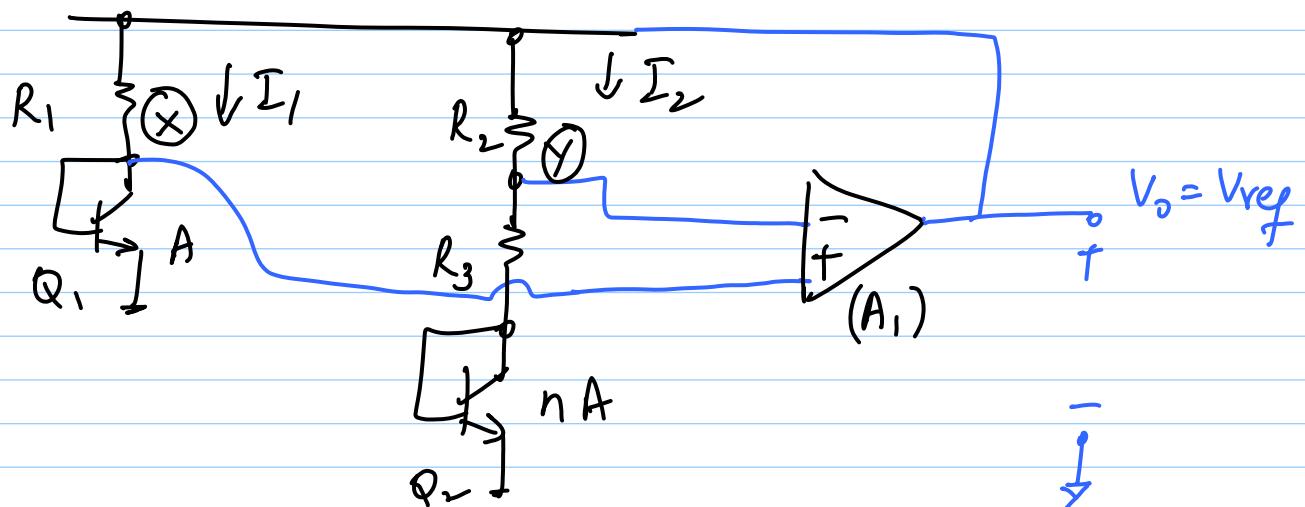
$$\Rightarrow I_o R = V_T \ln(n)$$

$$V_{o_2} = V_{BE_2} + V_T \ln(n)$$

$$\ln(n) = 17.2 \Rightarrow n \text{ is very large}$$

* For $V_{o1} = V_{o2}$

\rightarrow Use an opamp in -ve f.b.



$$V_x = V_y \quad (\text{due to -ve f.b.})$$

$$I_2 R_3 = V_{BE_1} - V_{BE_2} = V_T \ln(n)$$

$$I_2 = \frac{V_T \ln(n)}{R_3} \quad \begin{array}{l} \text{PTAT current} \\ \text{(proportional to} \\ \text{absolute temp.)} \end{array}$$

$$V_o = V_{BE_2} + \frac{V_T \ln(n)}{R_3} (R_2 + R_3)$$

$$= V_{BE_2} + V_T \ln(n) \left[1 + \frac{R_2}{R_3} \right]$$

for zero TC

$$\left(1 + \frac{R_2}{R_s}\right) \ln(n) = 17.2$$

e.g. $n = 31$, $\frac{R_2}{R_s} = 4$

