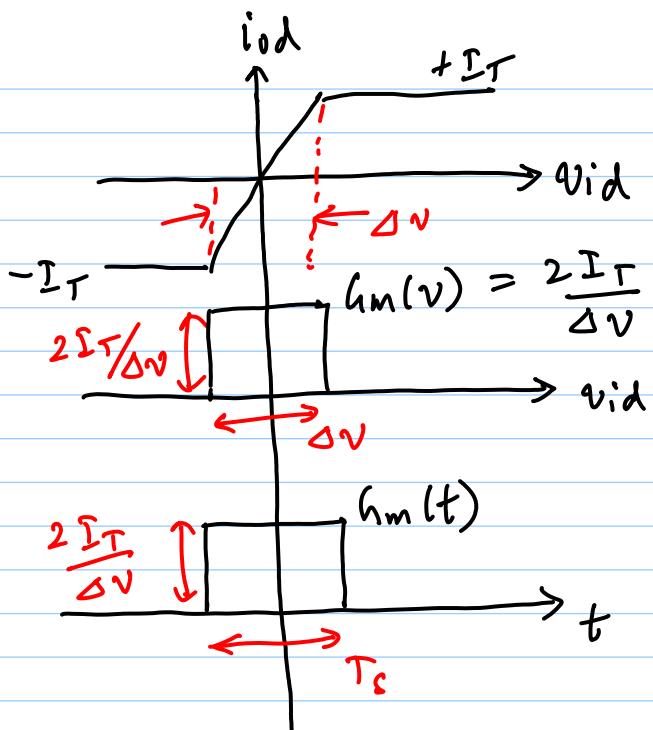
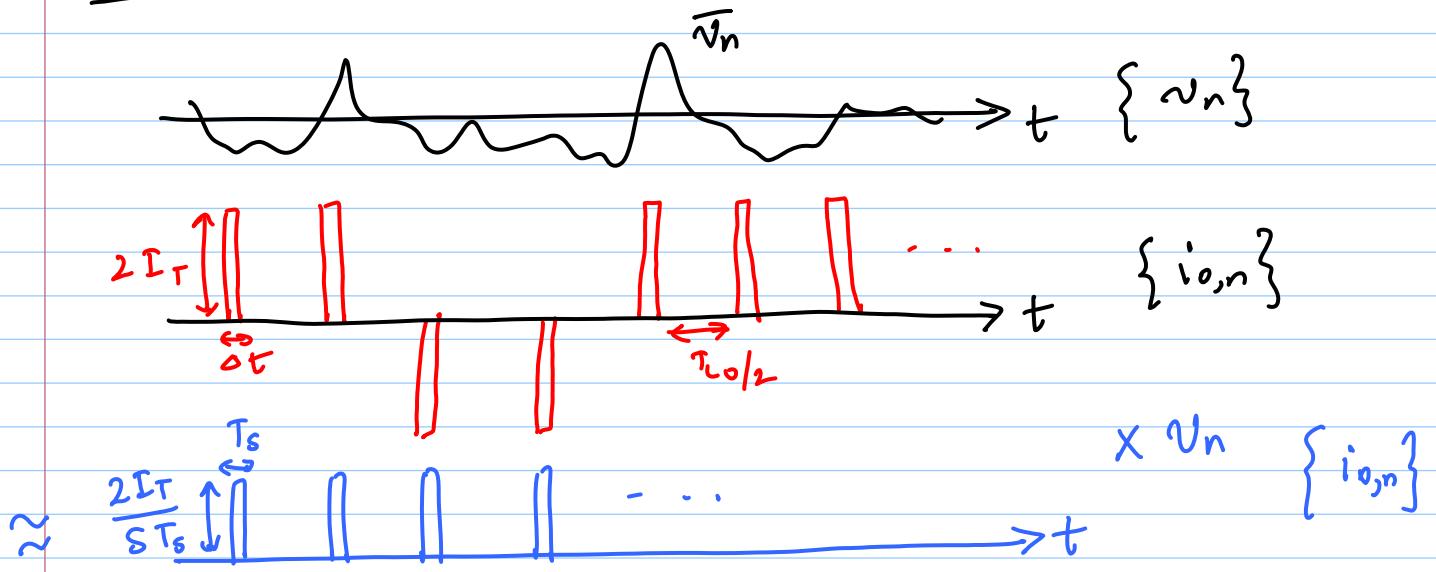


## Lecture 23 : Noise in Mixers (contd.) ; other linearization techniques

### Switch Thermal noise



piecewise linear approx.  
← applies to any  
transconductor

$$\Delta v \ll V_{L0}$$

$$v_{id} = 2V_{L0} \sin \omega_{L0} t$$

$$\Rightarrow g_m = g_m(t) \text{ also}$$

$$T_s = \frac{\Delta v}{S} = \frac{\Delta v}{2V_{L0}\omega_{L0}}$$

$$g_m = \frac{2I_T}{\Delta v} = \frac{2I_T}{ST_s}$$

$$\hat{V_n^2} = \frac{4kT\gamma'}{G_m}$$

It can be shown that:

$$\begin{aligned}\overline{i_{on}^2} &= \frac{2}{T_{LO}} \cdot \left( \frac{2I_T}{S} \right)^2 \cdot \frac{1}{T_S} \hat{V_n^2} \\ &= \frac{4I_T}{S \cdot T_{LO}} \cdot \frac{2I_T}{ST_S} \cdot \frac{4kT\gamma'}{G_m}\end{aligned}$$

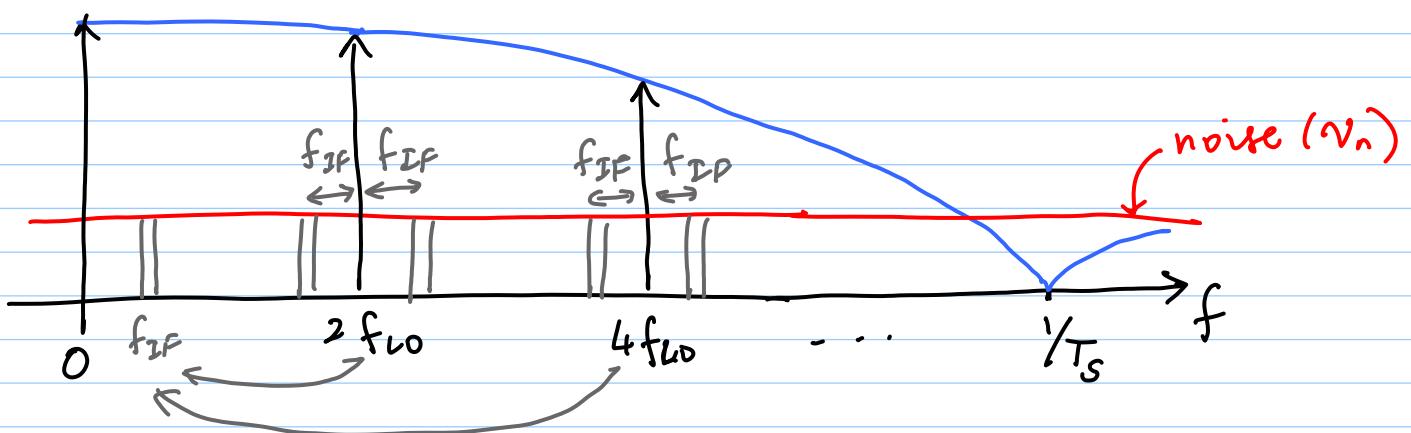
$$= 4kT\gamma' \cdot \frac{4I_T}{ST_{LO}} \quad \left. \begin{array}{l} \text{we want } S \rightarrow \\ \text{be large} \end{array} \right\}$$

$$= 4kT\gamma' \cdot \frac{I_T}{\pi V_{LO}} \quad \left. \begin{array}{l} \text{for a sinusoidal} \\ L_O \end{array} \right\}$$

\* does not depend on transistor size!

switch size  $\uparrow \Rightarrow T_S \downarrow \Rightarrow$  wider sampling BW

but as switch size  $\uparrow \Rightarrow$  input referred noise  $\downarrow$



$$\overline{V_{0,n,sw}^2} = 8kT\gamma' \cdot \frac{I_T}{\pi V_{LO}} \cdot R_L^2$$

If other white noise sources are present at the LO part (e.g. LO buffer noise)  $\Rightarrow$  adjust  $\gamma$

### Total noise

$$\overline{V_{on}^2} = \overline{V_{on,R_L}^2} + \overline{V_{on,g_m}^2} + \overline{V_{on,sw}^2}$$

$$= 8kT R_L + 4kT \gamma g_m R_L^2 + 8kT \gamma R_L^2 \cdot \frac{I_T}{\pi V_{LO}}$$

$$= \gamma kT R_L \left\{ 1 + \frac{\gamma g_m R_L}{2} + \gamma \frac{R_L I_T}{\pi V_{LO}} \right\} //$$

### Noise optimisation

Rewrite

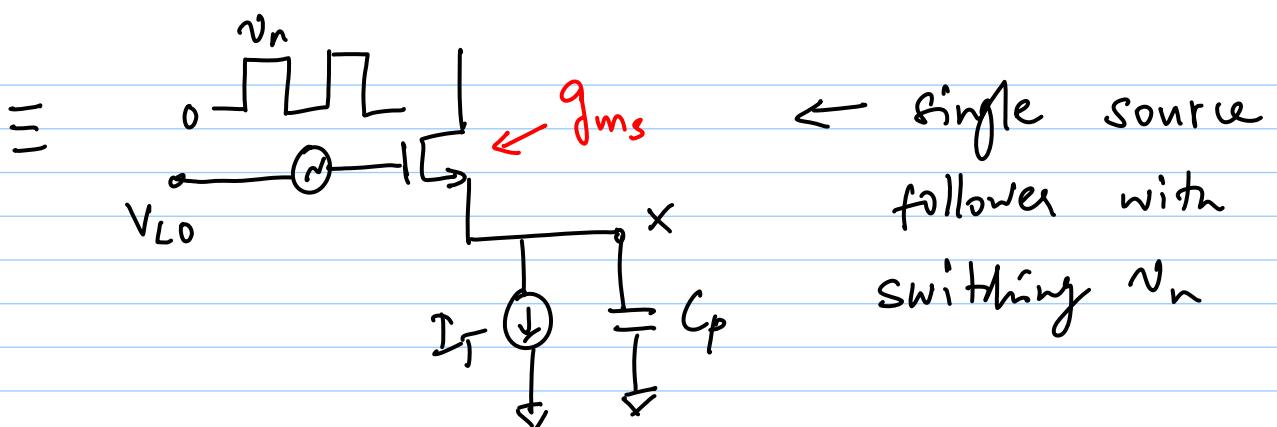
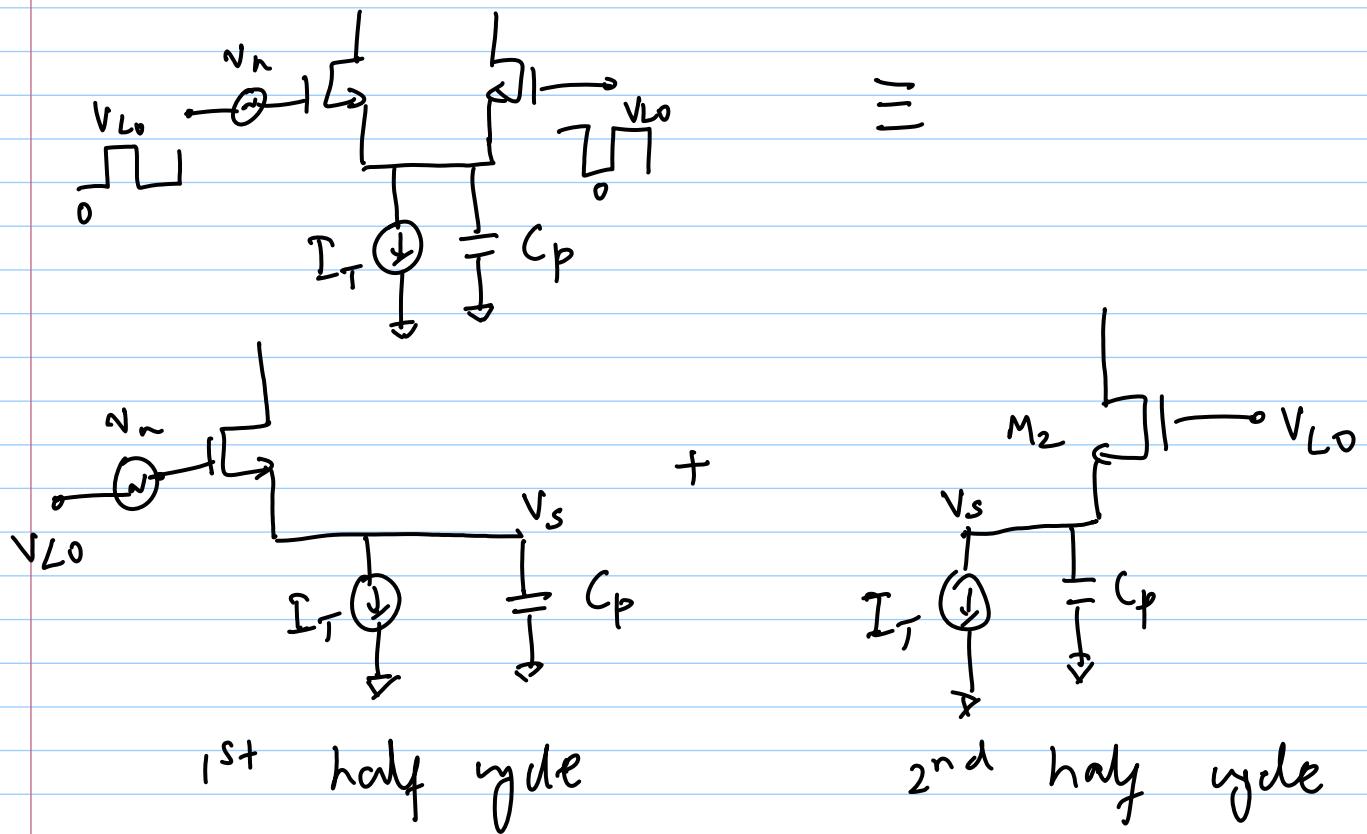
$$\overline{V_{on}^2} = \gamma kT R_L \left\{ 1 + \gamma \frac{R_L I_T}{\pi V_{LO}} + \gamma \frac{R_L \cdot I_T}{2(V_{AS} - V_T)} \right\}$$

\* relative contribution of switch and transconductance stages is:

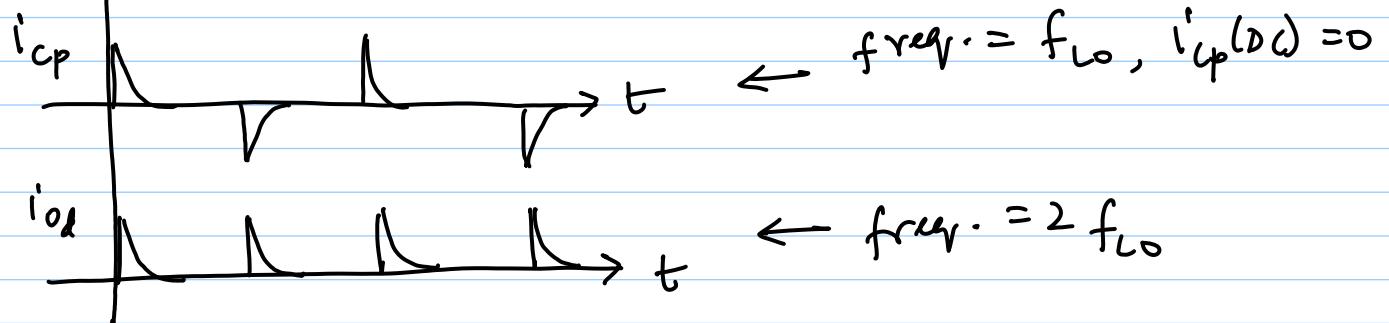
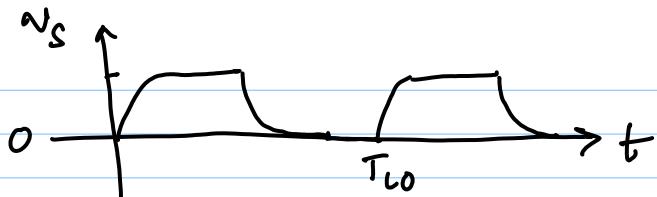
$$\frac{2(V_{AS} - V_T)}{\pi V_{LO}}$$

$\Rightarrow$  as  $(V_{AS} - V_T) \sim V_{LO}$ , they contribute comparable noise  $\leftarrow$  noise-linearity tradeoff

b) Indirect switch noise



$v_n \ll V_{LO} \Rightarrow$  linear assumption is valid  
 time constant @  $x = \frac{C_p}{g_{ms}} \ll T_{LO}$   
 $\Rightarrow V_s$  charges & discharges exponentially  
 every period



$i_{od}$  commutes between  $\pm i_{cp}$

$\Rightarrow$  non-zero DC value

$\Rightarrow$  Flicker noise is present @ output!

$$\bar{i}_{on} = \frac{2}{T_{Lo}} \int_0^{T_{Lo}/2} i_{cp}(t) dt = \frac{2}{T_{Lo}} \int_0^{T_{Lo}/2} C_p \left[ \frac{dV_s(t)}{dt} \right] dt$$

$$= \frac{2}{T_{Lo}} C_p \left[ V_s(T_{Lo}/2) - V_s(0) \right]$$

$$= \frac{2}{T_{Lo}} C_p V_n$$

$$G_c \text{ (flicker noise, indirect)} = \frac{2 C_p}{T_{Lo}} = 2 f_{Lo} C_p$$

$\rightarrow$  increases with  $f_{Lo}$

$\rightarrow$  usually smaller than direct mechanism

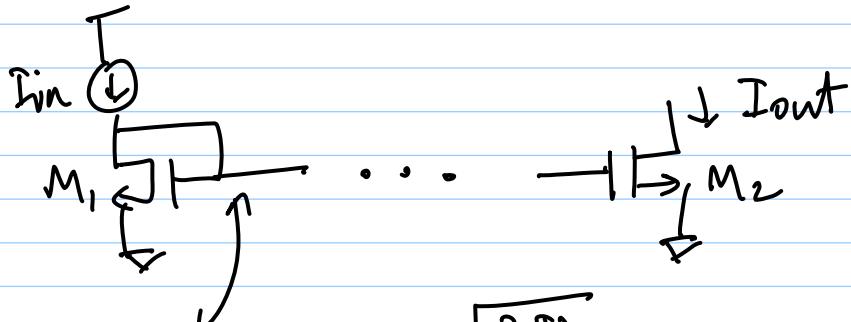
$$\rightarrow SNR = \frac{\frac{2}{\pi} \cdot g_m}{2 f_{Lo} C_p} \cdot \frac{V_{in}}{V_n} \quad \begin{matrix} \text{minimise} \\ C_p \end{matrix}$$

$$If C_p \sim (g_s)_{(g_m)}, SNR \approx 2 \frac{f_T}{f_{Lo}} \cdot \frac{V_{in}}{V_n} \quad \begin{matrix} \leftarrow \text{max.} \\ f_T \end{matrix}$$

## Additional linearisation techniques

### 1) Predistortion

simplest example = current mirror

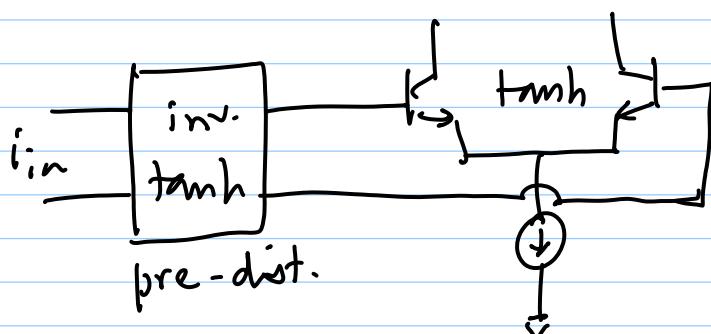


$$V_{AS} = V_{T_1} + \sqrt{\frac{2I_{in}}{K'_1 \left(\frac{W_1}{L_1}\right)}} \quad \leftarrow \text{square root function}$$

$$I_{out} = \frac{k'_2}{2} \left( \frac{w_2}{l_2} \right) (V_{AS_2} - V_{T_2})^2 \quad \leftarrow \text{square function}$$

$$I_{out} = \frac{k'_2}{2} \left( \frac{w_2}{l_2} \right) \left\{ \sqrt{\frac{2I_{in}}{K'_1 \left(\frac{W_1}{L_1}\right)}} + (V_{T_1} - V_{T_2}) \right\}^2$$

\*  $I_{out} \leftrightarrow I_{in}$  depends on matching



overall det-  
is linear

### 2) Piecewise approximation

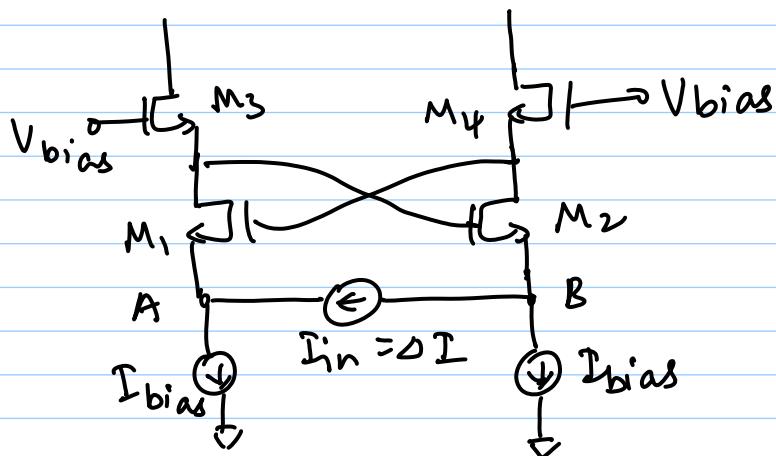
e.g. multi-tanh (already covered  
in class)

### 3) Feedback

MOSFET

Cross-guad

(Tektronix)



Goal: Synthesise  
short-ckt. between  
A & B (+ve feedback)

$$I_2 = I_4 = I_{bias} + \Delta I$$

$$I_1 = I_3 = I_{bias} - \Delta I$$

$$\Rightarrow V_{hs_2} = V_{hs_4} = V_{hs} + \Delta V_{hs}$$

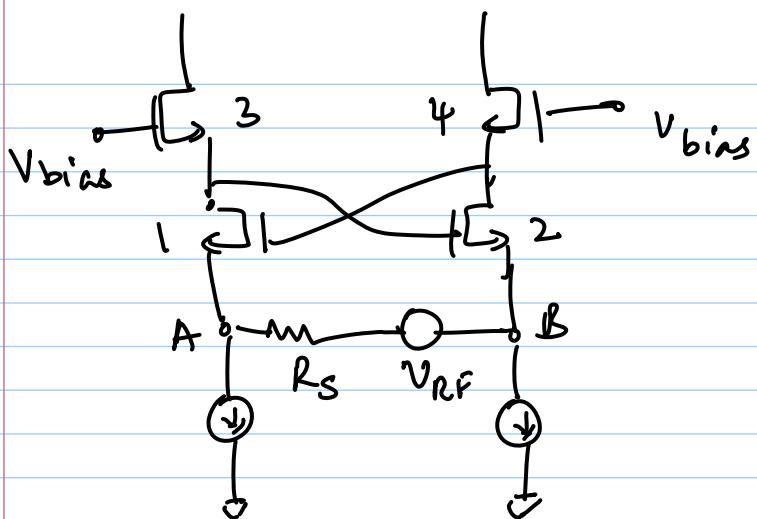
$$V_{hs_1} = V_{hs_3} = V_{hs} - \Delta V_{hs}$$

\* assume same W/L ratios

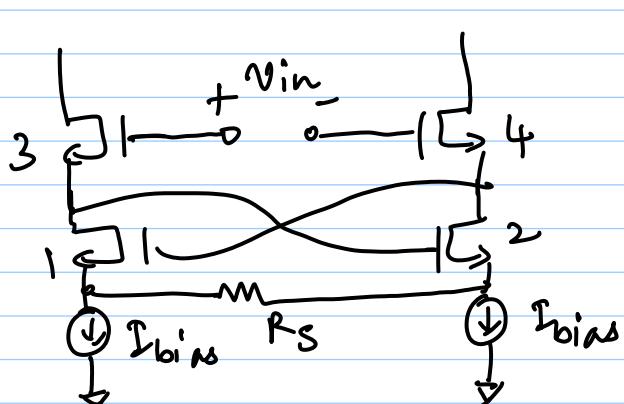
\* assume  $\Delta V_{hs}$  is linear with  $\Delta I$

$$\begin{aligned} V_{AB} &= (V_{bias} - V_{hs_4} - V_{hs_1}) - (V_{bias} - V_{hs_3} - V_{hs_2}) \\ &= (V_{hs_2} - V_{hs_4}) + (V_{hs_3} - V_{hs_1}) \\ &\stackrel{\Delta I}{=} 0 \end{aligned}$$

$$R_{AB} = \frac{V_{AB}}{\Delta I} = 0 \leftarrow \text{ideal short ckt.}$$



$$\Delta I = \frac{V_{RF}}{R_S} \quad (\text{very linear})$$

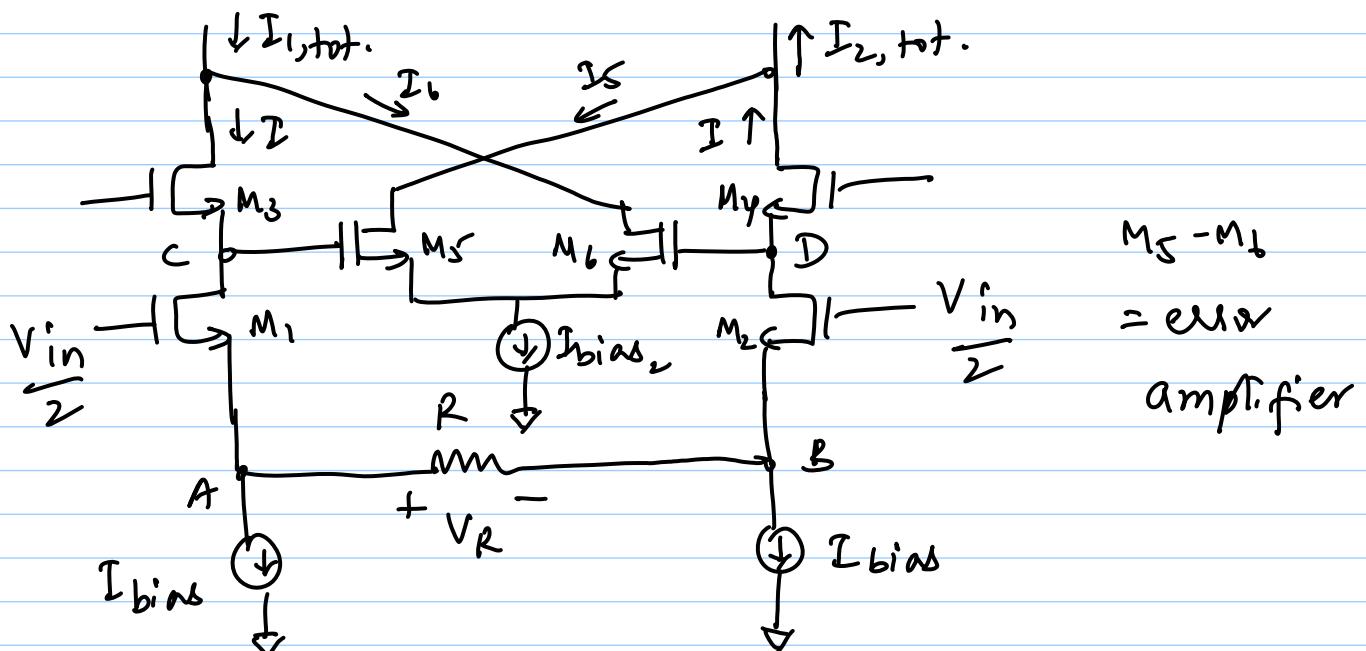


alternative version

\* inputs applied to  
M<sub>3</sub>-M<sub>4</sub> gates  
 $G_{m,\text{eff.}} = 1/R_S$

4) Feedforward — no BW, stability limitations

Cascode topology (Tektronix)



$M_5 - M_6$   
= error  
amplifier

$$V_R = V_{AB} = \left( \frac{V_{in}}{2} - V_{AS_1} \right) - \left( -\frac{V_{in}}{2} - V_{AS_2} \right)$$

$$= V_{in} - (V_{AS_1}, -V_{AS_2})$$

$$\Delta V_{AS_{1,2}} = V_{AS_1} - V_{AS_2}$$

$$= \sqrt{\frac{2(I_{Bias} + \Delta I)}{k' (W/L)}} - \sqrt{\frac{2(I_{Bias} - \Delta I)}{k' (W/L)}}$$

$$= \sqrt{\frac{2I_{bias}}{k'(W/L)}} \left\{ \sqrt{1 + \frac{\Delta I}{I_{bias}}} - \sqrt{1 - \frac{\Delta I}{I_{bias}}} \right\}$$

$$\approx (V_{AS} - V_T) \left\{ \left( 1 + \frac{\Delta I}{2I_{bias}} \right) - \left( 1 - \frac{\Delta I}{2I_{bias}} \right) \right\}$$

$$\approx (V_{AS} - V_T)_{1,2} \cdot \frac{\Delta I}{I_{bias}}$$

$$I = \frac{V_R}{R} = \frac{V_{in}}{R} - \underbrace{\frac{\Delta V_{AS_{1,2}}}{R}}$$

error term

\* Voltage gain from

$$+\frac{V_{in}}{2} \text{ to } \textcircled{C} = -1 \Rightarrow V_C = -\frac{V_{in}}{2}$$

$$-\frac{V_{in}}{2} \text{ to } \textcircled{D} = -1 \Rightarrow V_D = \frac{V_{in}}{2}$$

$$I_6 = g_{m_6} \frac{V_{in}}{2} = g_{m_5} \frac{V_{in}}{2}$$

$$I_5 = -g_{m_5} \frac{V_{in}}{2}$$

$$I_{1,\text{tot.}} = I + I_6$$

$$= \frac{V_{in}}{R} - \frac{\Delta V_{AS1,2}}{R} + g_{m5} \frac{V_{in}}{2}$$

$$I_{2,\text{tot.}} = I - I_5$$

$$= \frac{V_{in}}{R} + \frac{\Delta V_{AS1,2}}{R} - g_{m5} \frac{V_{in}}{2}$$

set this term = 0  
 by design