

Lecture 22: Linearity & Noise of Gilbert Mixers

Sources of NL

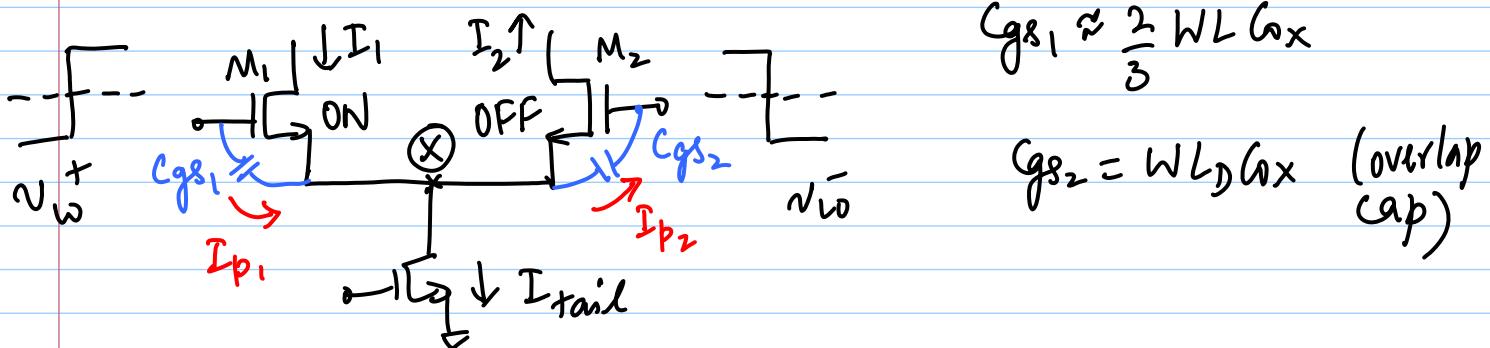
- (i) Transistor or Non-linearity

$$V_{DC} + V_{RF} \xrightarrow{\text{I}} \downarrow I_{out} = I_{DC} + g_{m_0} V_{RF} + g_{m_1} V_{RF}^2 + \dots$$

To improve $|IP_3| \Rightarrow \uparrow V_{DS}$

BUT $\Rightarrow g_{m_0} \downarrow \Rightarrow G_c \downarrow \Rightarrow NF \uparrow$

- (ii) LO switch Non-linearity



$$C_{GS1} \neq C_{GS2} \Rightarrow I_{p1} \neq I_{p2}$$

KCL @ node X

$$I_1 + I_{p1} = I_{p2} + I_T + I_2 \xrightarrow{0} \quad (\text{M}_2 \text{ is OFF})$$

$$\Rightarrow I_1 = I_T + (I_{p2} - I_{p1})$$

$$\simeq I_T - I_{p1} \quad (I_{p1} \gg I_{p2})$$

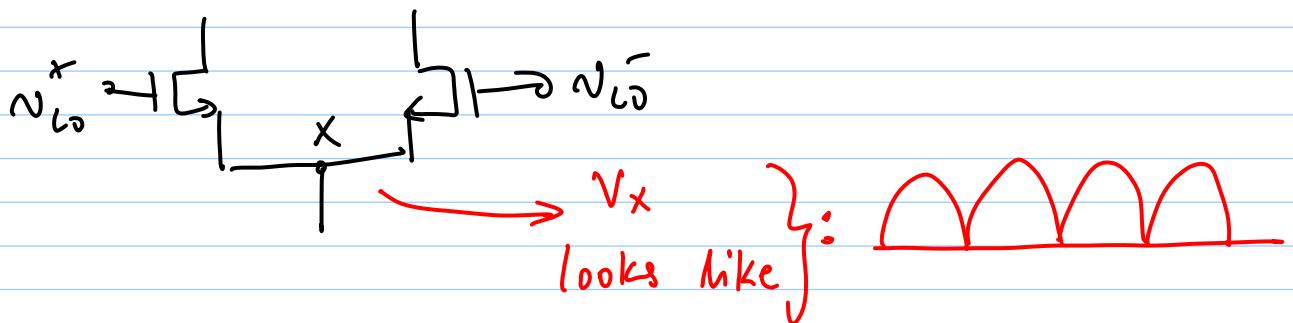
$$= I_T - \underbrace{C_{GS1} \frac{d(V_{L0} - V_X)}{dt}}_{\text{displacement current flowing into current source}}$$

displacement current flowing into current source

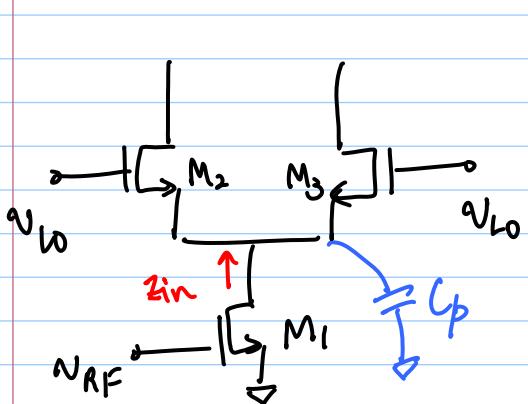
* I_1 is modulated by LO

→ if I_1 becomes small enough, M_1/M_2 may leave saturation \Rightarrow non-linearity

i.e. sharp LO edges & large V_{LO} make linearity worse (opposite of low-noise requirement - we will see this next class)



LO amplitude & LO switch size



* v_{LO} - large enough for 100% current switching

* Switching Speed depends on v_{LO} : $(V_{GS} - V_T) / V_{OV}$

faster switching \leftrightarrow lower V_{OV}

$C_p \uparrow \Rightarrow$ low Z

path for I_{RF}

$\uparrow W_{2,3} \downarrow I_{DC}$

$g_{m_{2,3}} \downarrow \Rightarrow Z_{in} \uparrow$

more I_{RF} through C_p

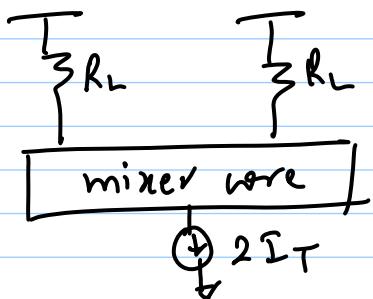
Noise in Gilbert Mixers:

Ref: H. Darabi & A. Abidi, "Noise in RF-CMOS

Mixers: A simple Physical Model", IEEE Journal of Solid-State Circuits, Vol. 35, No. 1, Jan 2000,
pp 15-25

1) Load Noise:

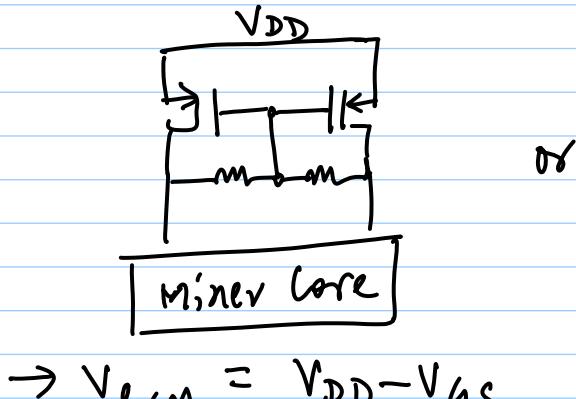
- a) Resistive load:
 $\star \overline{V_{o,n,R_L}} = 8kT R_L \{2 resistors\}$
 \star no 1/f noise (usually)



Issues:

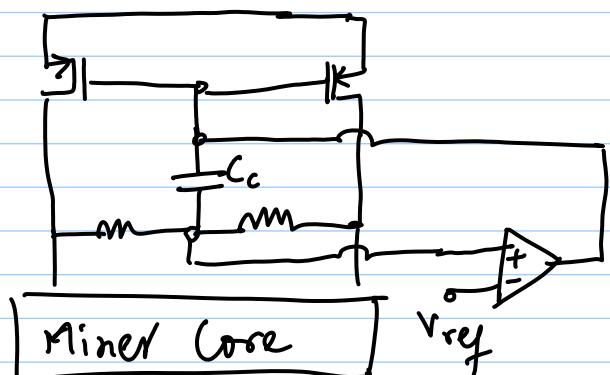
- * voltage headroom: $V_{o,cm} = V_{DD} - I_T R_L$
- * $G_C \propto R_L$

b) PMOS loads



$$\rightarrow V_{o,cm} = V_{DD} - V_{GS}$$

CM-feedbacks



$$\rightarrow V_{o,cm} \leq V_{DD} - V_{D,SAT}$$

\rightarrow best headroom

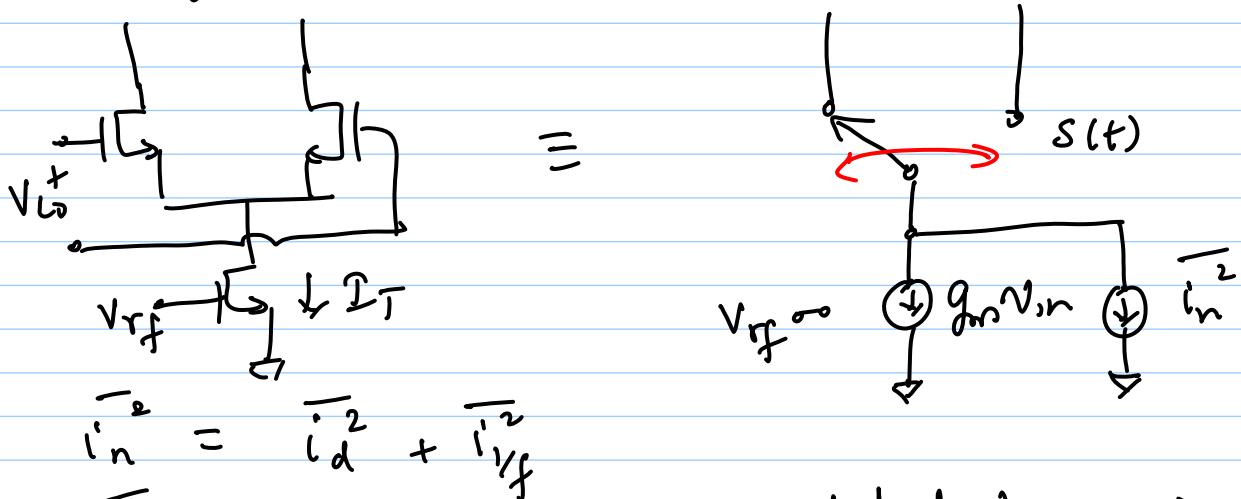
$\rightarrow C_c = \text{Miller compensation cap}$

\star Thermal noise of PMOS

\star 1/f noise impacts Direct conversion or low-IF Rx
(use large PMOSs)

2) Noise from gm stage

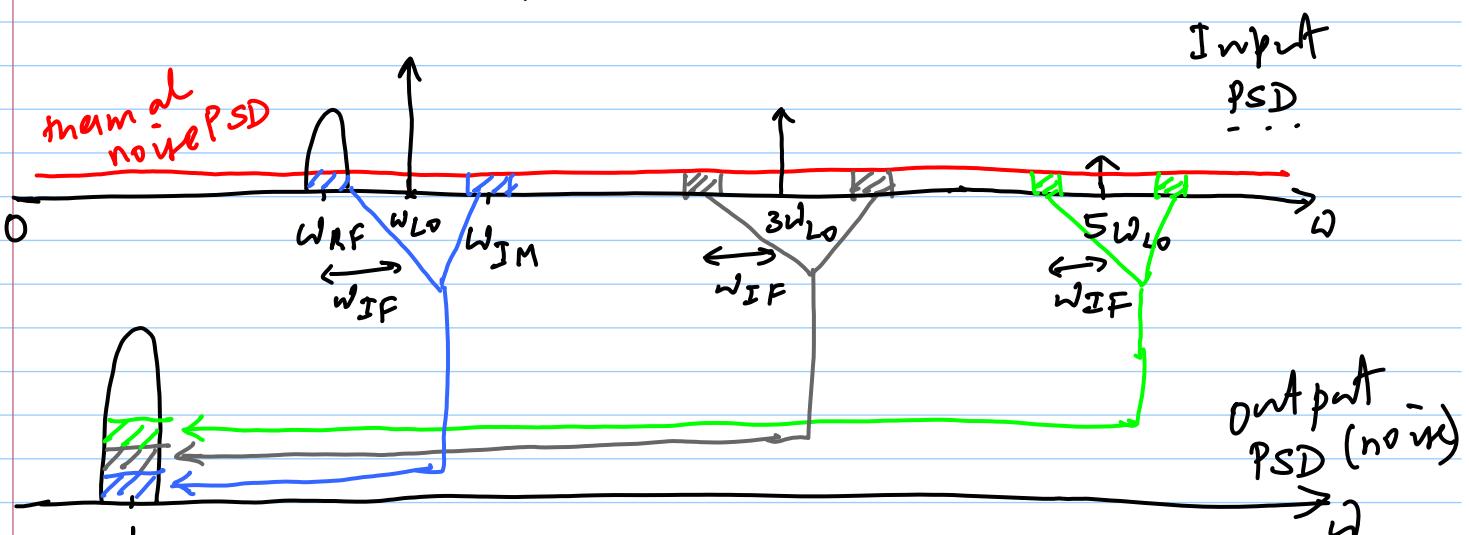
Single-balanced mixer



* $\bar{i_n^2}$ gets amplitude modulated by $s(t)$
 → noise contributions from frequencies
 other than around f_{RF}

(a) thermal noise

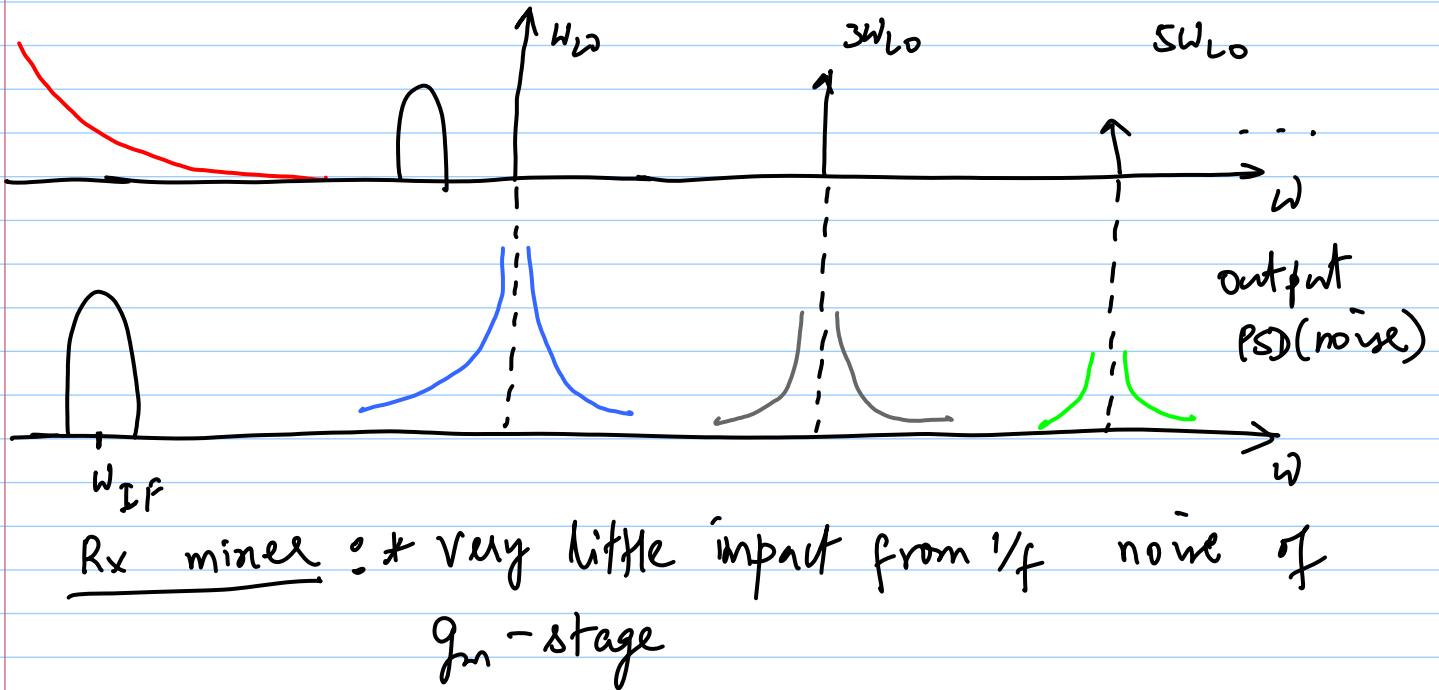
$$s(t) = \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{1}{n} \sin(n\omega_{LO}t), \quad n=\text{odd}$$



$$\frac{\bar{n}_{\text{out}, \text{gm}}^2}{\Delta f} \simeq \frac{4KJ \gamma^2}{g_m} \times \left(\frac{2}{\pi} g_m R_L \right)^2 \times 2 \times \left(1 + \frac{1}{3^2} + \frac{1}{5^2} + \dots \right) \underbrace{\bar{h}_c^2}_{\text{Input noise PSD}} = \pi e / 4$$

$$\overline{v_{o_n, g_m}^2} = 4kTg_m R_L^2$$

b) $1/f$ noise



* Switching pair mismatch \Rightarrow some $1/f$ noise remains @ baseband

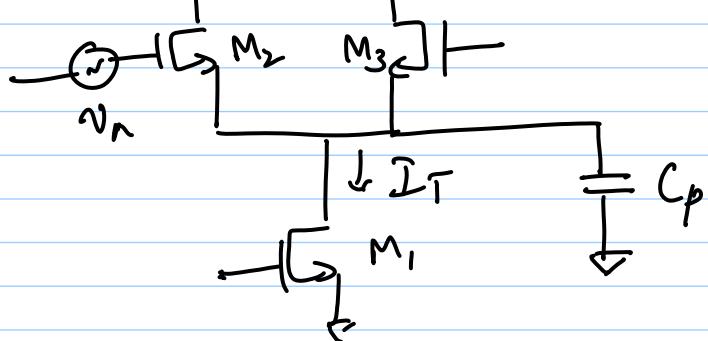
Tx mixer: desired signal = ω_{BB}
 * ($1/f$ noise + BB signal) gets up-converted
 * $1/f$ noise does matter \Rightarrow design g_m stage with large area

3) Noise from switching pair:

\rightarrow more complicated to analyse

\rightarrow no noise contribution when current is completely switched (like a cascode)

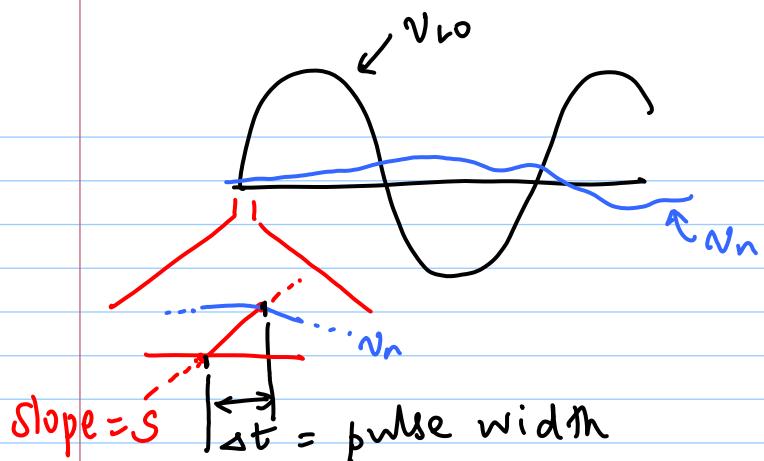
a) Direct switch noise



→ If C_p is large, switching devices do contribute noise even when fully on.
 { Ref. HW3 problem 3 }

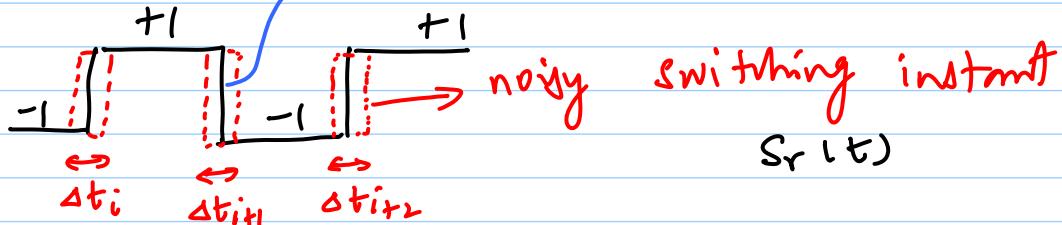
→ Both devices contribute noise during switching phase

→ $\bar{v}_n = \text{single input-referred noise source}$
 that captures noise of both switches $M_2 - M_3$
 * \bar{v}_n modulates the switching time instant



$$\Delta t = \frac{v_n(t)}{s} \quad \begin{matrix} \text{slope } @ \\ \text{switching instant} \end{matrix}$$

$\text{slope } = s \quad \Delta t = \text{pulse width}$



$$\equiv \text{ideal switching } s_i(t)$$

$$+ \dots + \text{pulse train } p(t)$$

$$s_r(t) = \delta(t) + p(t)$$

$p(t)$ = pulse train of height = +1 or -1

$$\text{width } \Delta t = \frac{v_n(t)}{S}$$

$$\text{rate} = 2\omega_{L0}$$

\bar{i}_{on} \Rightarrow pulses of amplitude $2I_T$

average value of output current over one period:

$$\begin{aligned}\bar{i}_{on} &= \frac{2}{T} \times 2I_T \times \Delta t = \frac{2}{T_{L0}} \times 2I_T \times \frac{V_n}{S} \\ &= 4I_T \cdot \frac{V_n}{S \cdot T_{L0}} \quad \left\{ T_{L0} = \frac{2\pi}{\omega_{L0}} \right\}\end{aligned}$$

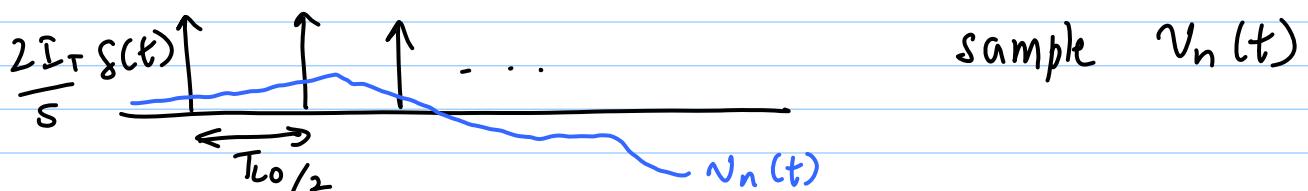
$$\neq L_0 \text{ signal} = \pm V_{L0} \sin \omega_{L0} t \Rightarrow v_{L0d} = 2V_{L0} \sin \omega_{L0} t$$

$$\Rightarrow \text{slope} = \frac{dv_{L0d}}{dt} = 2V_{L0} \cdot \omega_{L0} \cos \omega_{L0} t$$

$$\begin{aligned}s &= \text{slope @ switching time } (t = n\pi / \omega_{L0}) \\ &= 2V_{L0} \cdot \omega_{L0}\end{aligned}$$

$$\begin{aligned}\Rightarrow s \cdot T &= 2V_{L0} \omega_{L0} \cdot T_{L0} \\ &= 4\pi V_{L0}\end{aligned}$$

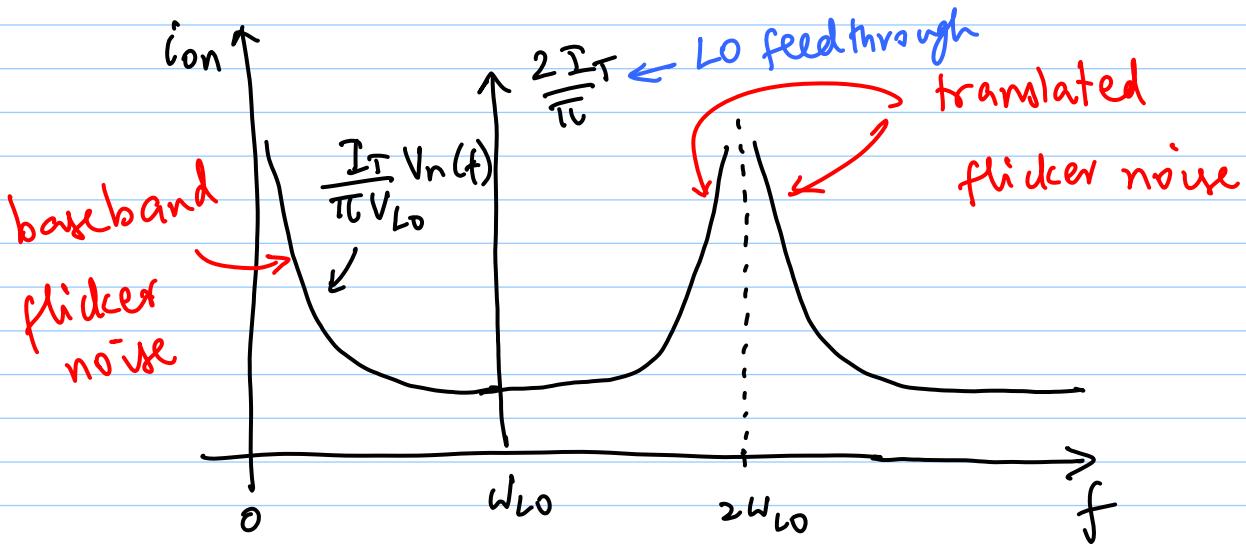
$\frac{\Delta t}{T_{L0}} \ll 1 \Rightarrow$ pulses are approximated by ideal δ -function impulses that



$$i_{on}(f) = \frac{4I}{ST_{co}} V_n(f)$$

$$= \frac{1}{\pi} \cdot \frac{I_T}{V_{LO}} V_n(f) \quad \text{Sampled images appear @ } n \cdot (2f_{LO})$$

Flicker noise



V.C. mixer (T_x) \rightarrow no $1/f$ noise from switches
 @ f_{LO}
 \rightarrow $1/f$ noise of G_m stage is present