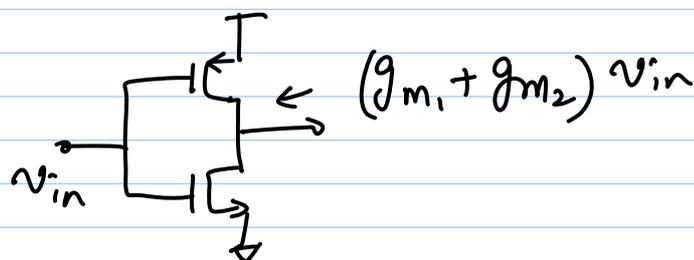
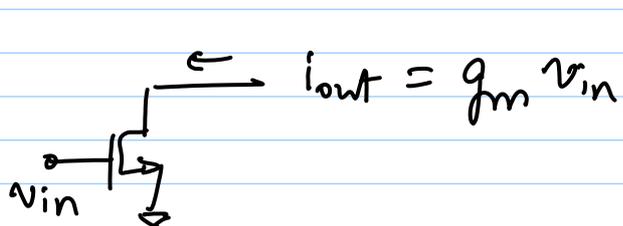


# Lecture 19: LNA Design (final): Introduction to Mixers

## Other ideas to explore (LNAs)

1) Current re-use:



2) Feedback: \* to match  $R_{in} = 50 \Omega$

\* to improve  $11P_3$  (linearity)

issues:  $\rightarrow$  NF may increase substantially  
 $\rightarrow$  Stability may worsen

## Other general rules of thumb

\* Start off with same  $w$  &  $L$  for cascode device; usually cascode gate =  $V_{DD}$

\* Start with  $f_T \geq 10 \times$  operating freq.

\* Model noise accurately (e.g. model may use  $\delta = 2/3$  &  $\delta = 0$ ).

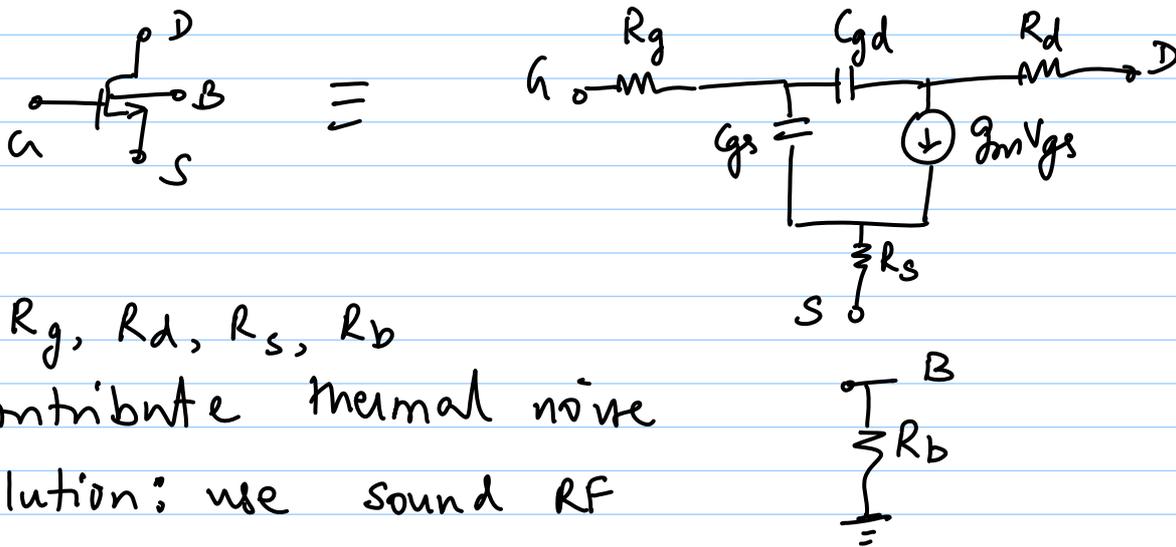
\* Hand calculations are approximations only, so use simulation tools effectively:

$\rightarrow$  Plot  $g_m$ ,  $f_T$  and  $\Gamma$  vs.  $I_{bias}$  and  $w$

$\rightarrow$  Plot NF vs. current density

$\rightarrow$  Usually,  $NF_{opt.} \neq S_{21, opt.} \neq 11P_{3, opt.}$

# Extrinsic sources of noise (mos)



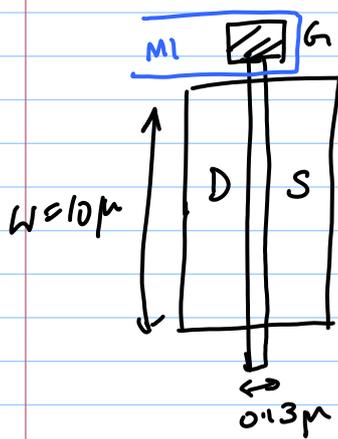
\*  $R_g, R_d, R_s, R_b$  contribute thermal noise

Solution: use sound RF

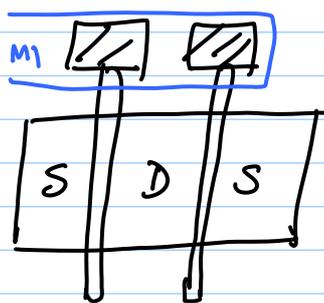
layout techniques

- 1)  $R_g$  - use multifinger devices to reduce  $R_g$   
- contacts on both sides of gate

e.g.  $\frac{W}{L} = \frac{10\mu}{0.13\mu}$  ;  $R_{metal} \ll R_{poly}$

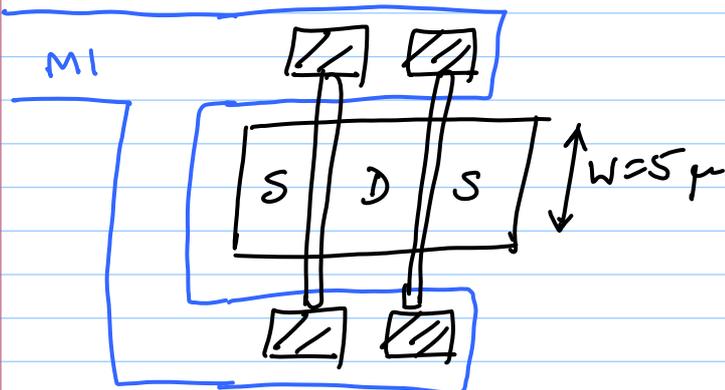
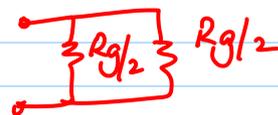


$R_g$  vs.



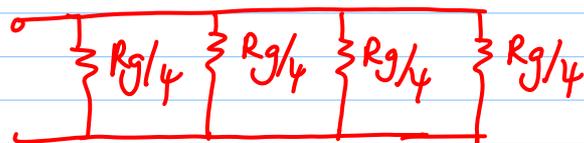
$\frac{R_g}{4}$

(worse approx.)



$\frac{R_g}{16}$

(worse approx.)



Accurate expression: (takes distributed effects into account)

$$R_g = K \cdot \frac{R_{sh} \cdot W}{n^2 L} \left. \begin{array}{l} K = \frac{1}{3} \text{ for 1-side gate contact} \\ K = \frac{1}{12} \text{ for 2-sided gate contact} \end{array} \right\}$$

→  $R_{sh}$  = sheet resistance

→  $n$  = number of fingers

- 2)  $R_b$  — use more number of substrate contacts  
— thermal noise of  $R_b$  can modulate backgate of MOS  
— can impact gain & NF

$$\overline{i_{nd,sub}^2} = 4kT R_b \cdot g_{mbs}^2 \Delta f$$

### Introduction to Mixers:

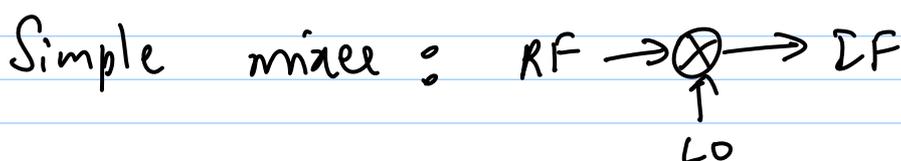
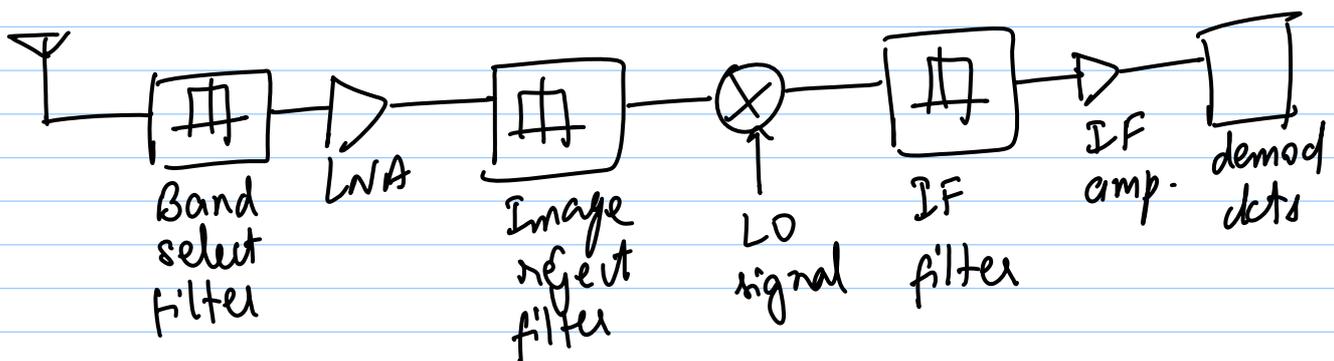
\* Mixers are used for freq. translation

Tx → up conversion of BB signals to IF/RF

Rx → down-conversion of RF signals to IF/BB

### Down-conversion mixers

Superhet. receiver



$$\left. \begin{aligned} x_{RF}(t) &= A_{RF} \cos \omega_{RF} t \\ x_{LO}(t) &= A_{LO} \cos \omega_{LO} t \end{aligned} \right\} x_{IF}(t) = x_{RF}(t) \cdot x_{LO}(t)$$

$$\begin{aligned} x_{IF}(t) &= (A_{RF} \cos \omega_{RF} t) \cdot (A_{LO} \cos \omega_{LO} t) \\ &= \frac{A_{RF} A_{LO}}{2} \left[ \underbrace{\cos(\omega_{LO} - \omega_{RF})t}_{\text{desired IF term}} + \cos(\omega_{LO} + \omega_{RF})t \right] \end{aligned}$$

Metrics

1)  $G_c \equiv$  conversion gain =  $\frac{\text{IF amplitude (desired IF)}}{\text{RF amplitude}}$

$$G_c = \frac{A_{RF} A_{LO} / 2}{A_{RF}} = \frac{A_{LO}}{2}$$

$G_c < 1$  may be ok in several cases  
(depending on NF)

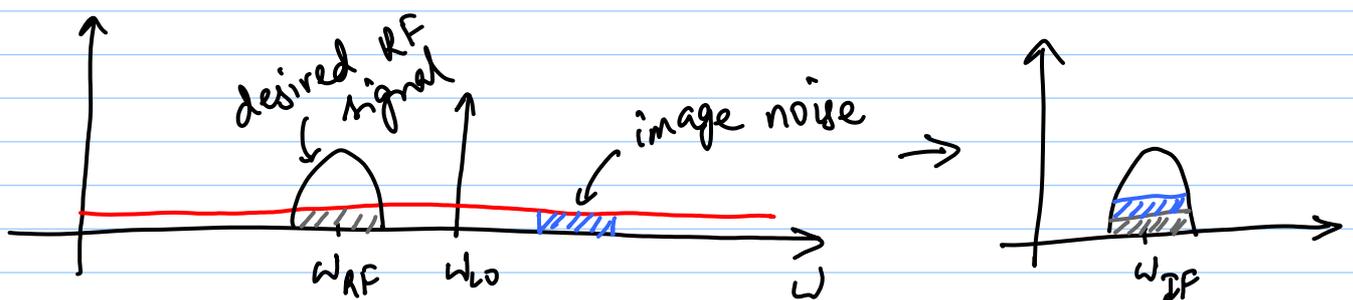
$\Rightarrow$  Passive Mixers

2) Noise Figure NF

$$NF = \frac{\text{SNR @ RF port}}{\text{SNR @ IF port}}$$

\* Beware of image frequencies when computing NF of mixers

$\rightarrow$  Even if there is no image signal @  $\omega_{IM}$ , noise from  $\omega_{IM}$  still contributes to NF!



\*  $NF_{DSB}$  is measured with useful RF signal at both  $\omega_{RF}$  &  $\omega_{IF}$  (i.e.  $\omega_{LO} \pm \omega_{IF}$ )

\*  $NF_{SSB}$  is measured with useful RF signal only at one freq. (either  $\omega_{LO} + \omega_{IF}$  or  $\omega_{LO} - \omega_{IF}$ )

$\Rightarrow NF_{SSB} = NF_{DSB} + 3dB$  (noise power adds as mean-square)

$\Rightarrow$  check carefully to see which NF is quoted!

$NF_{SSB}$  is the accurate metric in most cases

\* Note that even if mixer is noiseless,  $NF_{SSB} = 3dB!$

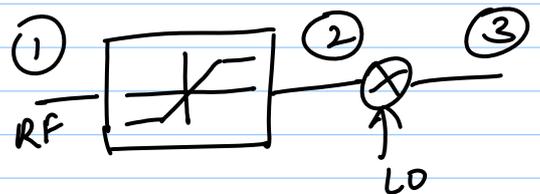
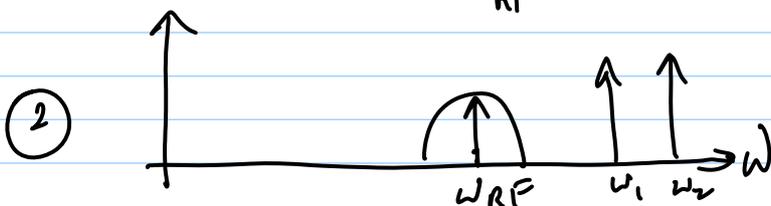
typical values are

$NF_{SSB} \sim 10-15dB$

$\Rightarrow$  LNA needs to precede mixer to keep  $NF_{tot.}$  low.

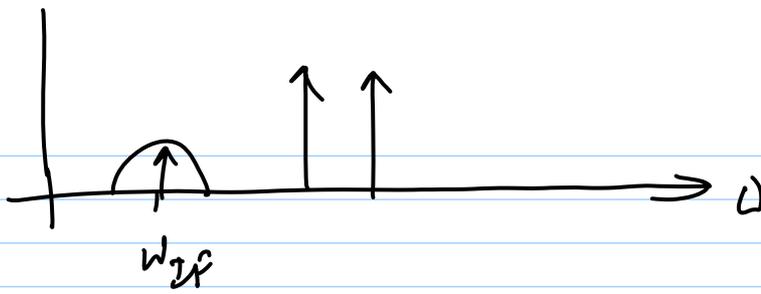
3) Linearity: measured as  $1IP_3/0IP_3$  at appropriate frequency (RF/IF)

RF path non-linearity:



$IM_3$  component falls at desired  $\omega_{RF}$

3



\* Cubic non-linearity can cause problems even with a single input!

e.g. AM radio

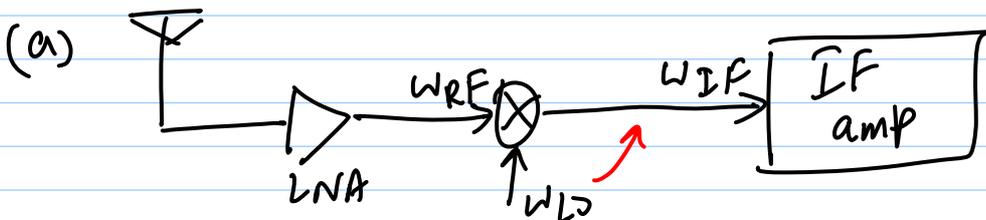
$$IF = 455 \text{ kHz}; f_{ch} = 910 \text{ kHz}$$

$$\Rightarrow f_{LO} = 1365 \text{ kHz}$$

cubic nonlinearity - generates  $(2\omega_{RF} - \omega_{LO})$  term

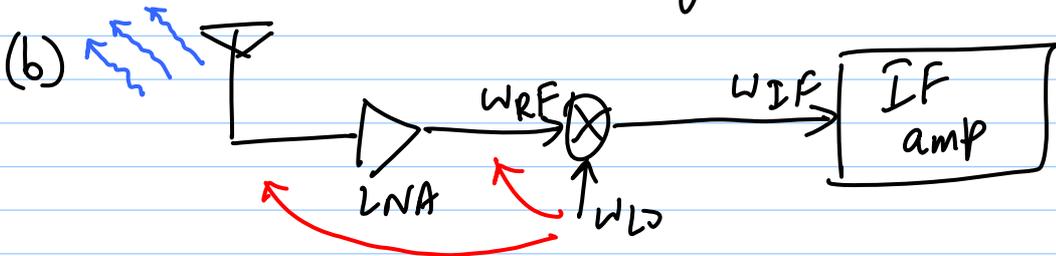
In this case,  $2\omega_{RF} - \omega_{LO} = 455 \text{ kHz} = \omega_{IF}$ !

#### 4) Isolation:



\*  $\omega_{LO} \gg \omega_{RF}, \omega_{IF}$

\* LO-IF feed through would saturate IF amp.



LO-RF feed through (reverse isolation)

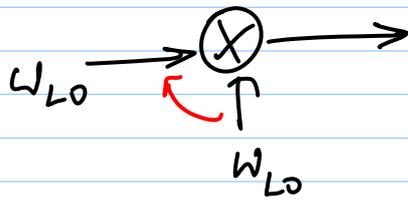
\* Re-radiation of LO & its harmonics

\* Usually,  $A_{LO} \gg A_{RF}$

Direct-conversion (Homodyne) receiver:

$$\omega_{RF} = \omega_{LO}, \quad \omega_{IF} = 0$$

we want only  $\omega_{RF}$  @ BB



"self-mixing"

→ low-freq. term that depends on LO only

→ can be larger than desired RF signal

## 5) Spurs

Mixers, by nature produce a bunch of freq. components

\* Undesired freq. components @ mixer output are called spurious signals or 'spurs'

\* Highly tedious in practice:

if there are  $m$  &  $n$  harmonic numbers @ RF & LO frequencies respectively,

$$f_{spur} = m f_{RF} + n f_{LO} \quad \text{for all combinations of signs of } m \text{ \& } n$$