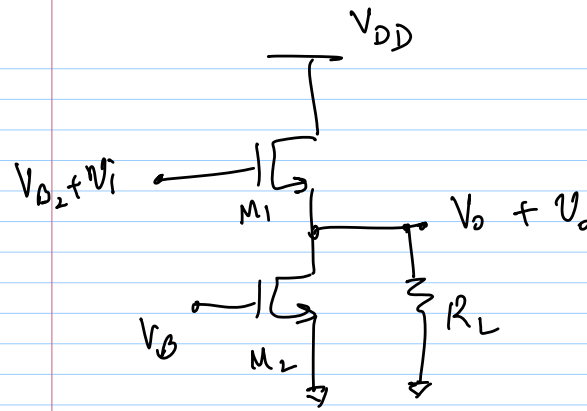
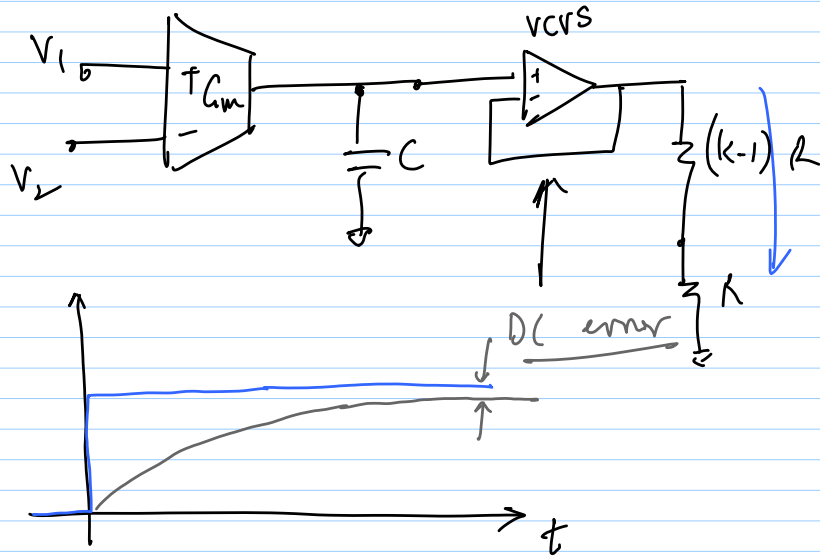


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Lec 18



$$V_{o_{min}} = V_{DSAT2}$$

$$V_{o_{max}} = V_{DD} - V_{DSAT1}$$

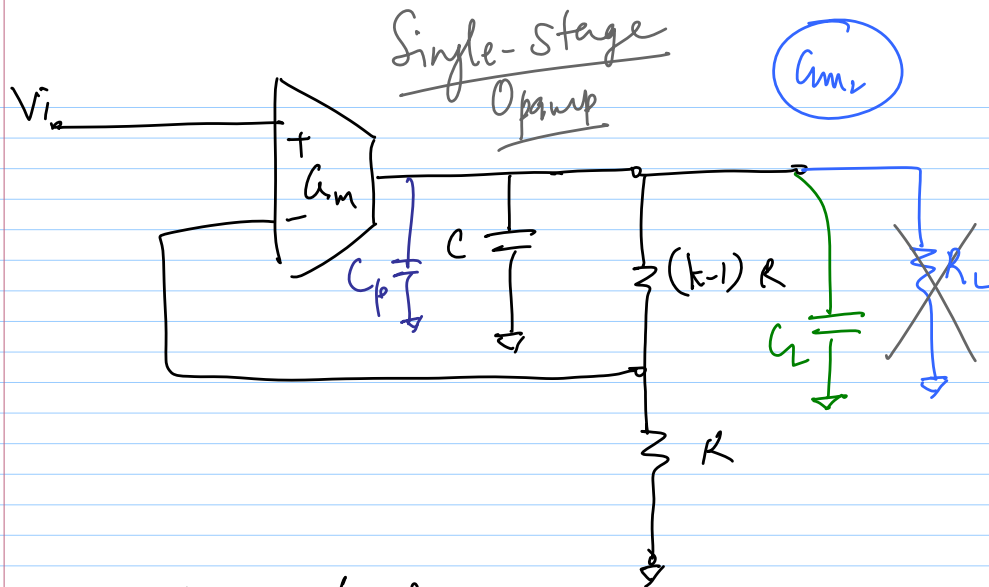
$$\hookrightarrow V_{a1} = V_{DD} + V_{T1}$$

$$V_{o_{max}} = V_{DD} - V_{a2}$$

* Increase R so that gmR is large enough

$gm \uparrow \Rightarrow I_{bias} \uparrow$

$\Rightarrow W/L \uparrow \left\{ \begin{array}{l} \text{par Cap.} \uparrow \\ \text{slower devices} \end{array} \right.$



DC gain $\approx gmR_L$

Single stage Opamp

- 1) DC gain \Rightarrow do not drive Resistive loads
- 2) $G_m = g_{m1}$; $\omega_u = g_{m1}/C_L$
- 3)

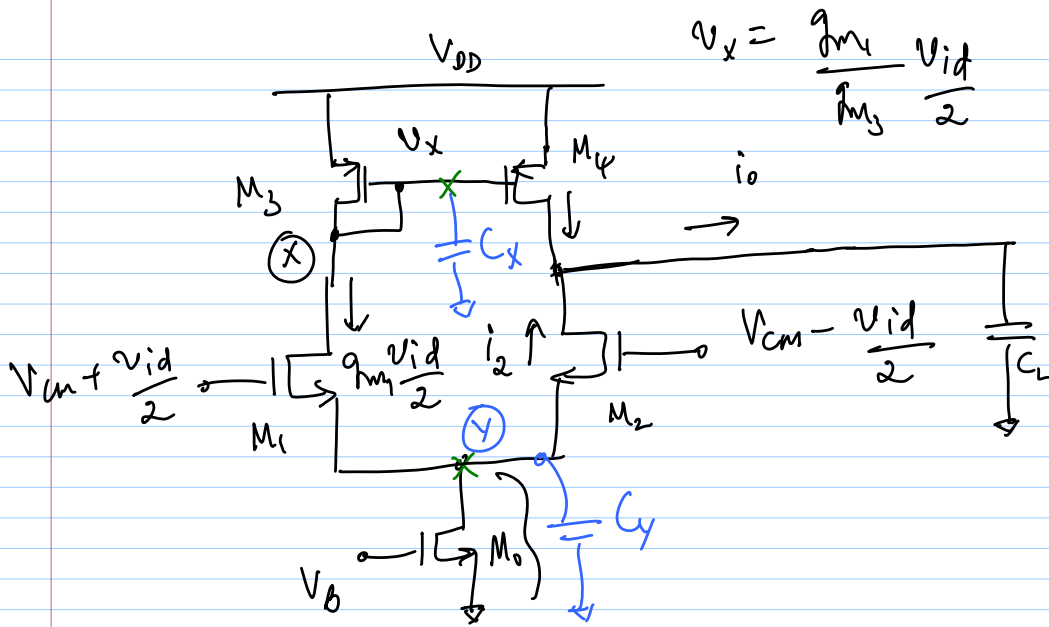
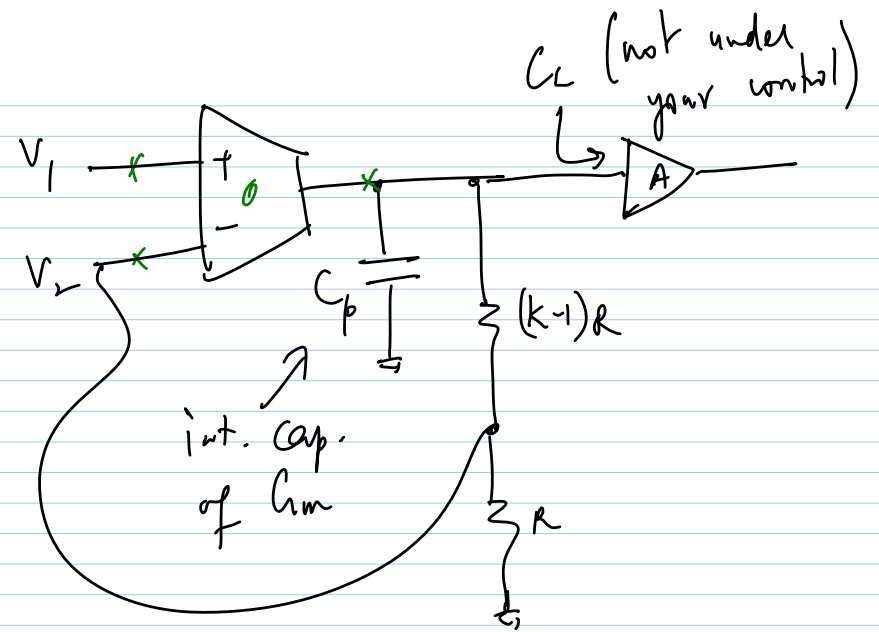
Load cap C_L

↳ acts as integrating cap

↑ If you have $C \neq C_L$

$$W_u = \frac{g_m'}{k + C_L} \quad g_m' \rightarrow g_m$$

$$W_u = \frac{g_m}{C_L}$$



$$i_4 = g_{m4} v_x = g_{m1} \frac{v_{id}}{2} \quad (g_{m4} = g_{m3})$$

$$i_2 = g_{m2} \frac{v_{id}}{2}$$

$$i_o = i_2 + i_4 = g_{m1} v_{id}$$

$$\underline{\text{No } C_L} \Rightarrow v_o = i_o \cdot r_o = g_{m1} v_{id} (r_{ds1} || r_{ds2})$$

No r_o $\Rightarrow v_o = i_o \cdot \frac{1}{sC_L}$

$$= \frac{g_{m1} v_{id}}{sC_L}$$

Actual det

$$\frac{v_o}{v_{id}} \stackrel{(n)}{=} \frac{g_{m1}}{g_o + sC_L} = \frac{g_{m1} r_o}{1 + sC_L r_o}$$

* finite dc gain = $g_{m1} r_o = g_m / g_o$

* Swing limits

* noise

* Slew rate

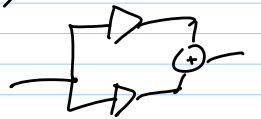
* Non-dominant poles & zeros

C_y - No pole due to V_G

C_x - $v_x = i_i \left(\frac{1}{g_{m3}} \parallel \frac{1}{sC_x} \right)$

$$= \frac{i_i}{g_{m3} + sC_x}$$

$$i_4 = g_{m4} \cdot v_x$$



$$i_4 = \frac{g_{m4} \cdot g_{m1} v_{id}/2}{g_{m3} + sC_x}$$

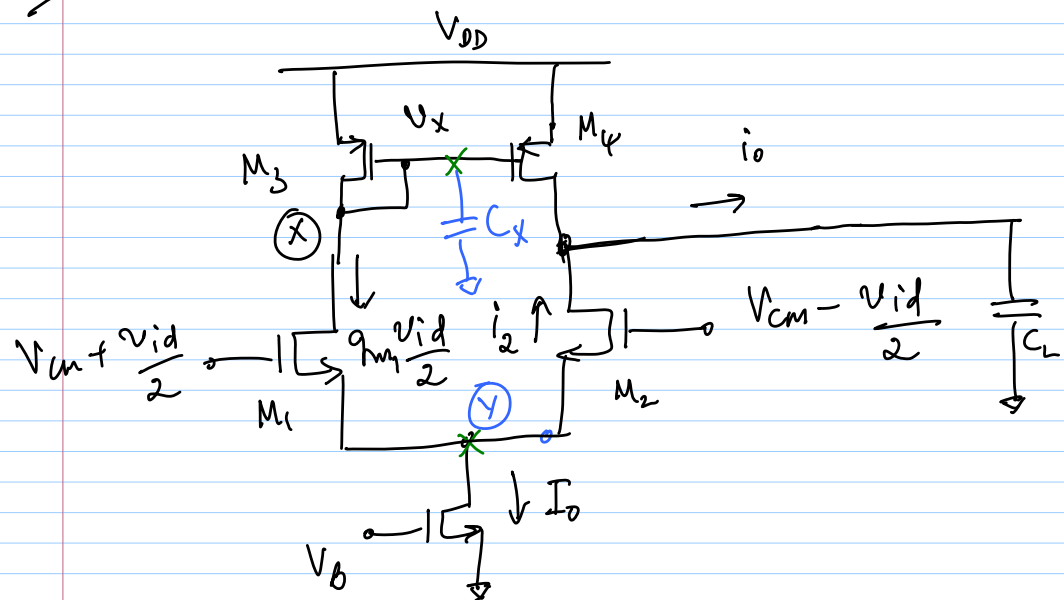
$$i_2 = g_{m1} v_{id}/2$$

$$i_o = i_4 + i_2$$

$$= g_{m1} \frac{v_{id}}{2} \left[1 + \frac{g_{m4}}{g_{m3} + sC_x} \right]$$

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Lec 19



$$\begin{aligned}
 i_o &= i_2 + i_4 \\
 &= g_{mL} \frac{v_{id}}{2} + \frac{g_{m4} g_{m1} v_{id} / 2}{g_{m3} + sC_x} \\
 &= g_{m1} \frac{v_{id}}{2} \left[1 + \frac{g_{m3}}{g_{m3} + sC_x} \right]
 \end{aligned}$$

$$v_o = \frac{i_o}{g_o + sC_L}$$

$$\frac{v_o}{v_{id}} = \frac{g_{m1}}{2} \left[1 + \frac{g_{m3}}{g_{m3} + sC_x} \right] \frac{1}{g_o + sC_L}$$

$$= \frac{g_{m1}}{2} \cdot \frac{1}{g_o + sC_L} \cdot \frac{2g_{m3} + sC_x}{g_{m3} + sC_x}$$

Dominant pole (ω_p) ω_z, ω_p

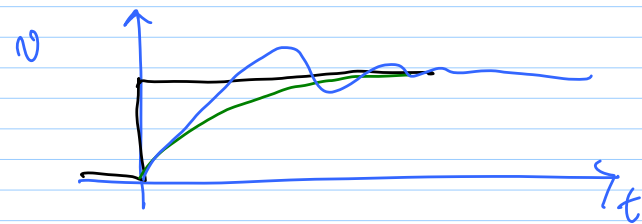
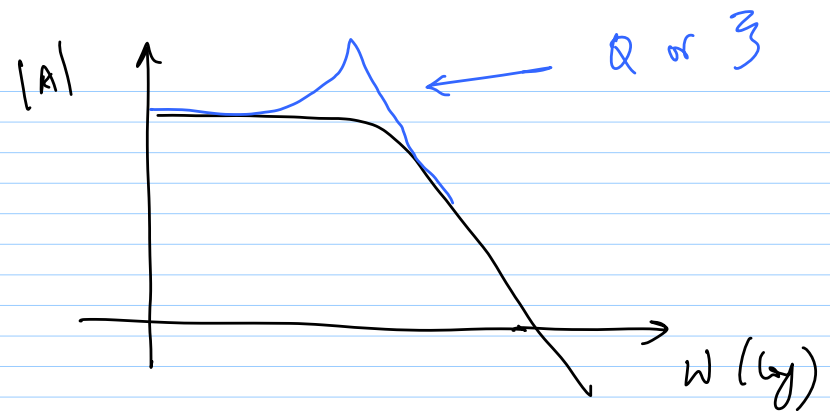
$$\omega_p = \frac{-g_{m3}}{C_x} ; \omega_z = -\frac{2g_{m3}}{C_x} = 2\omega_p$$

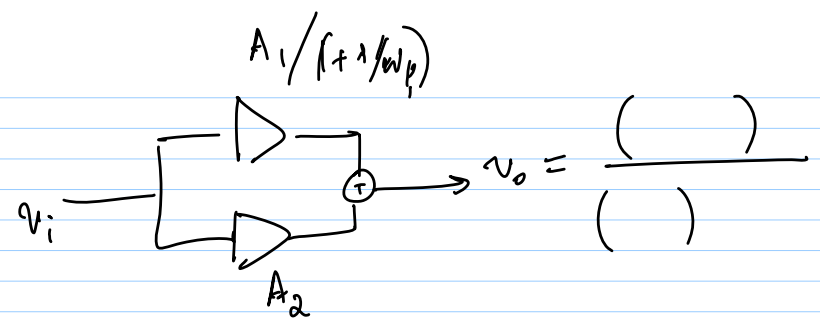
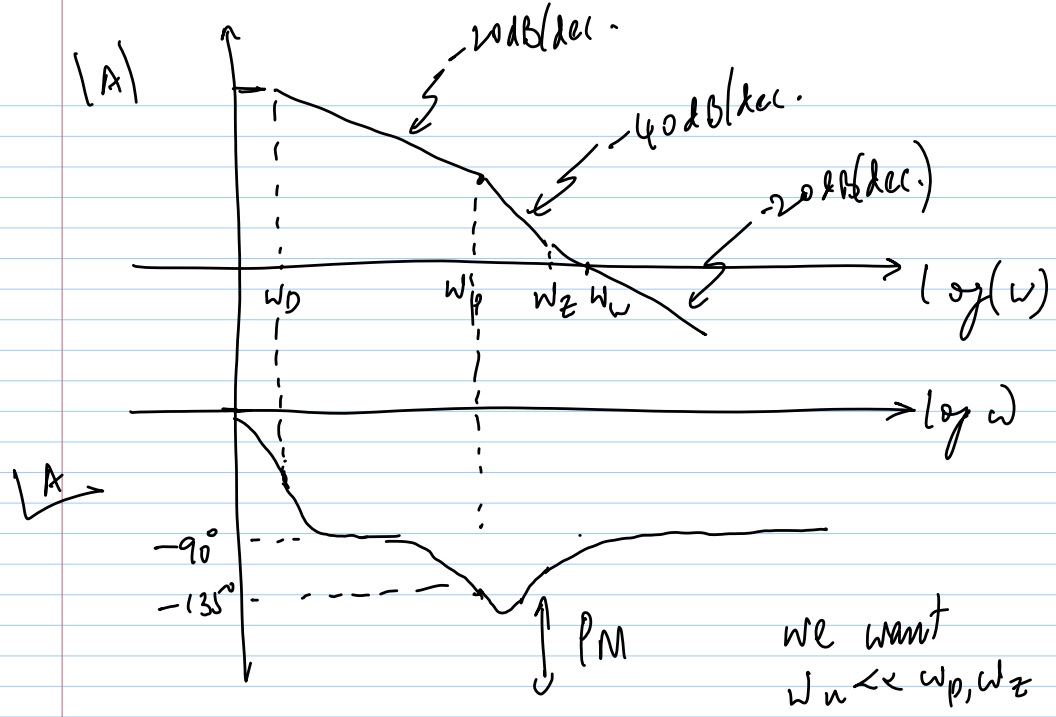
$$|w_H| = \frac{g_{m1}}{C_L} ; |w_D| = \frac{g_o}{C_L}$$

$$BW = \frac{\omega_u}{k} ;$$

$$\omega_p = \frac{-g_{m3}}{C_x} ; \omega_z = -\frac{2g_{m3}}{C_x} = 2\omega_p$$

Unity gain $\Rightarrow \omega_p \Rightarrow \omega_u$





* Multiple paths w/ different freq. response w phase shifts

$$\omega_D = \frac{g_{m1}}{C_L}, \quad \omega_u = \frac{g_{m1}}{C_L}$$

$$\omega_p = \frac{g_{m3}}{C_x}; \quad \omega_z = \frac{2g_{m3}}{C_x}$$

$\omega_p \rightarrow \omega_u$

$$\frac{g_{m3}}{C_x} \rightarrow \frac{g_{m1}}{C_L}$$

- 1) $\uparrow C_L \Rightarrow \omega_u \downarrow$ X
- 2) $\uparrow g_{m3} \Rightarrow \uparrow \left(\frac{\omega}{L}\right)_3 \Rightarrow C_x \uparrow$ X
- 3) $\downarrow C_x \Rightarrow \left(\frac{\omega}{L}\right)_3 \downarrow$ @ same I_D
 $V_{DSAT3,4} \uparrow$
hit swing limits
- 4) $\downarrow g_{m1} \Rightarrow \downarrow \left(\frac{\omega}{L}\right)_1 \Rightarrow \omega_u \downarrow$

↑ I_0 is the only way to improve available BW of the opamp.

CM limits

1) Input CM:

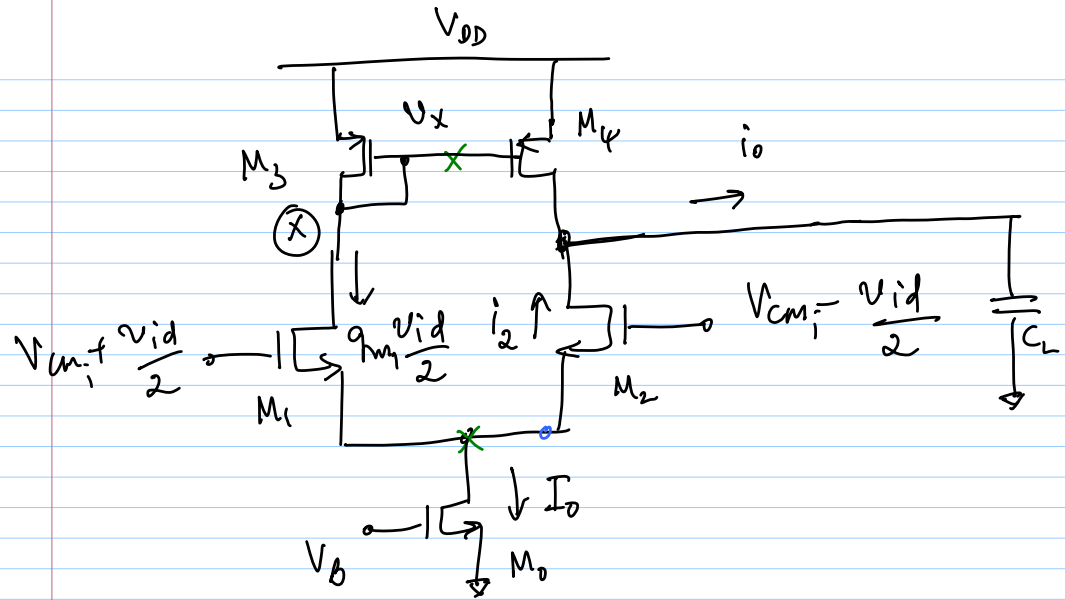
$$V_{CMi}(\min) = V_{DSAT_0} + V_{ASr}$$

$$V_{CMi}(\max) = V_{DD} - V_{S_{Q3}} + V_{T_1}$$

2) Output CM:

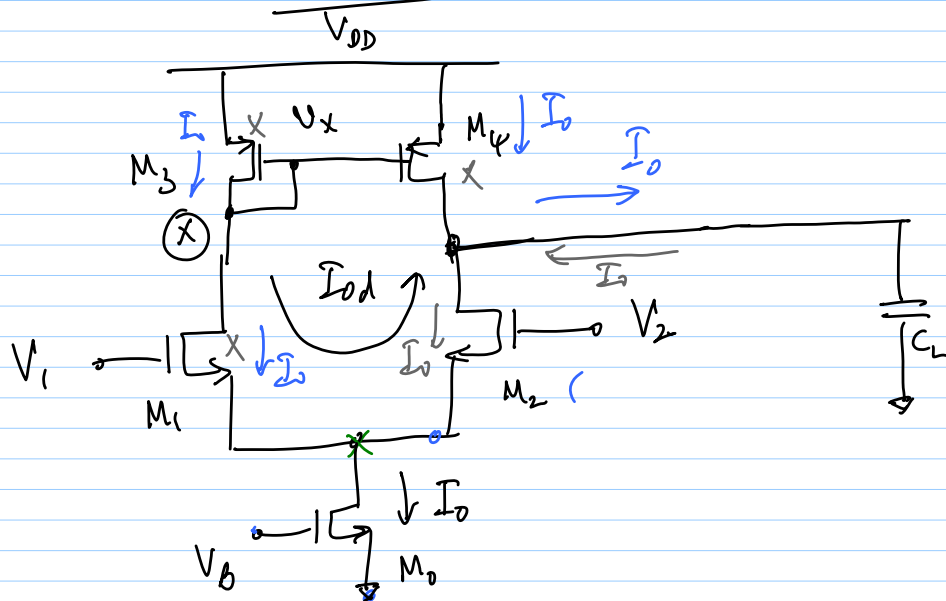
$$V_{CMo}(\min) = V_{CMi} - V_{T_1}$$

$$V_{CMo}(\max) = V_{DD} - V_{OSAT_3}$$



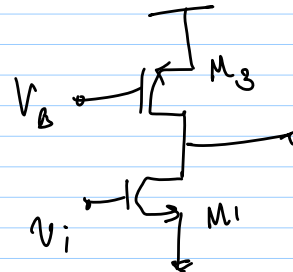
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Lec 20



* Noise

$$\bar{e}_n^2 = \frac{16kT}{3} \left[\frac{1}{g_{m1}} + \frac{g_{m3}}{g_{m1}^2} \right]$$



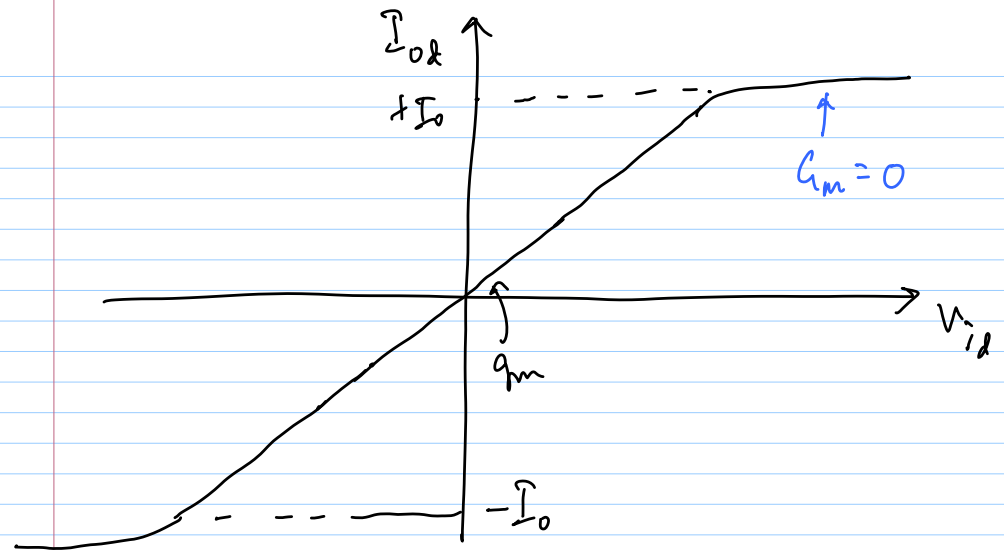
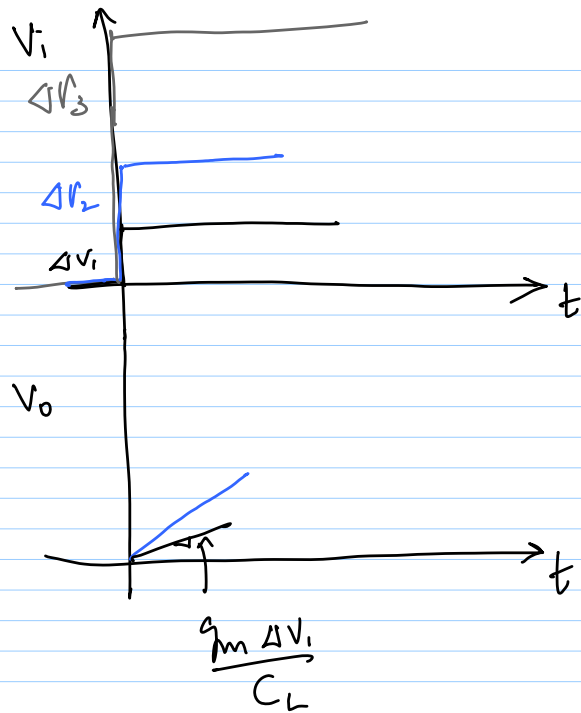
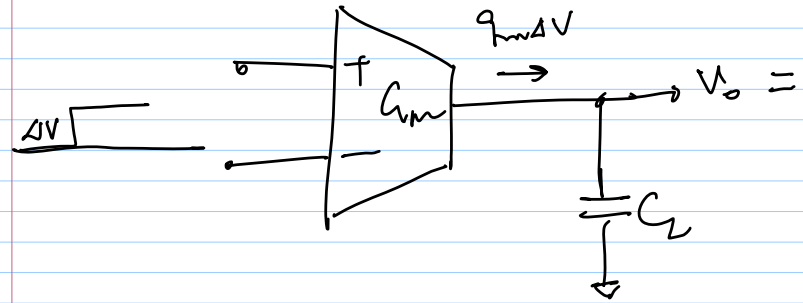
$$\frac{8kT}{3} \left[\frac{1}{g_{m1}} + \frac{g_{m3}}{g_{m1}^2} \right]$$

* Offset

$$V_{os} = \Delta V_{T,1,2} + \frac{g_{m3}}{g_{m1}} \Delta V_{T,3,4}$$

$$\sigma_{os}^2 = \sigma_{V_{T,1,2}}^2 + \left(\frac{g_{m3}}{g_{m1}} \right)^2 \sigma_{V_{T,3,4}}^2$$

* Slew Rate $\leftarrow \frac{dV_o}{dt}$



$$I_{out(max)} = I_0$$

$$+ve \text{ Slew rate} = \frac{I_0}{C_L} \text{ (V/s)}$$

$$-ve \text{ SR} = -\frac{I_0}{C_L} \text{ (V/s)}$$

3/3/14

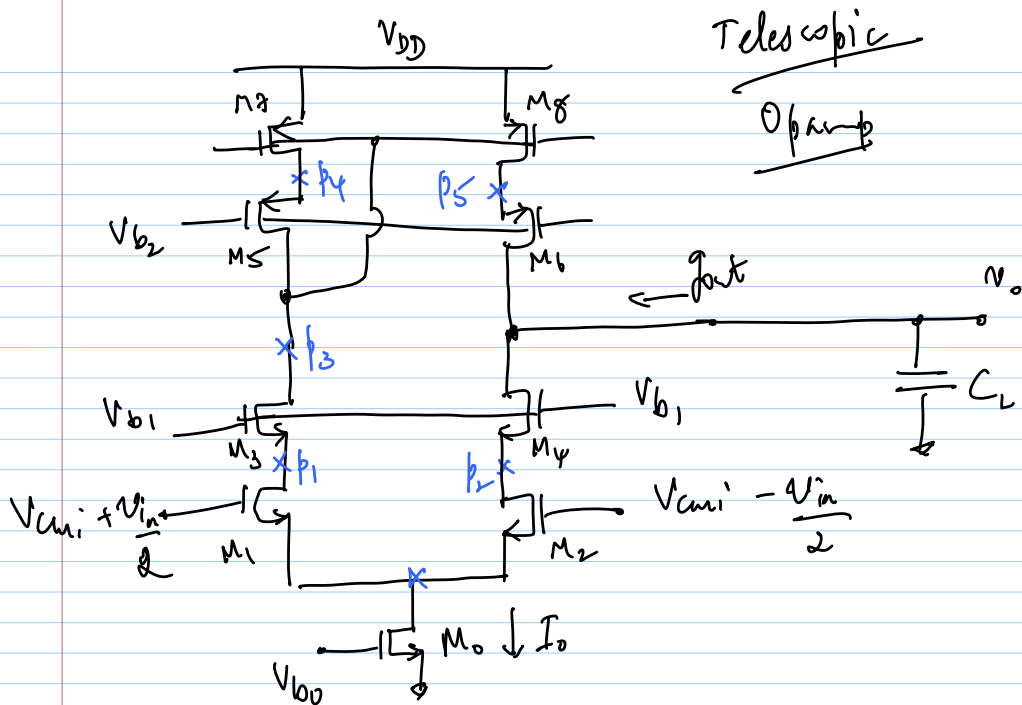
Lec 21

* DC performance - R load

* DC gain - no DC error

$g_m \leftarrow$ affects ω_u

$g_o \leftarrow$ increased through cascode



$$1) \quad r_{out} = (g_{m4} r_{ds4}) r_{ds2} \parallel (g_{m6} r_{ds6}) r_{ds8}$$

$$DC \text{ gain} = g_{m1} r_{out} \Rightarrow DC \text{ gain (1-stage opamp)}$$

$$2) \quad \omega_u = g_{m1} / C_L ; \quad \omega_{pole} = \frac{1}{r_{out} C_L} = \frac{g_{out}}{C_L}$$

(same)

(much lower)

loads more like an ideal \int

$$3) V_{cmi}(\min) = V_{DSAT0} + V_{GS1}$$

$$V_{cmi}(\max) = V_{b1} - V_{GS4} + V_{T2}$$

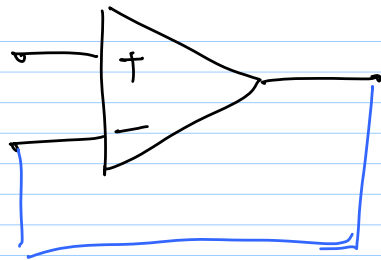
$$4) V_{cm0}(\max) = V_{DD} - V_{DSAT7} - V_{DSAT5}$$

$$V_{cm0}(\min) = V_{b1} - V_{T4}$$

$$5) \text{Slew rate} = \pm \frac{I_o}{C_L}$$

6) Note: Almost the same @ low freq.

$$\frac{16kT}{3} \left[\frac{1}{g_{m1}} + \frac{g_{m7}}{g_{m1}^L} \right]$$



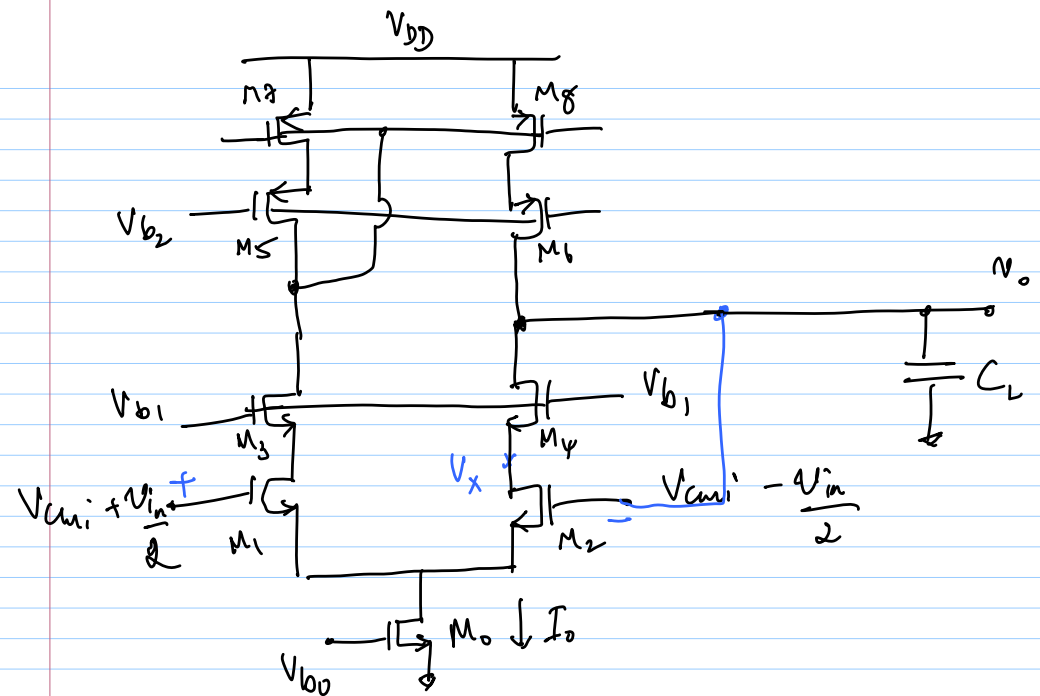
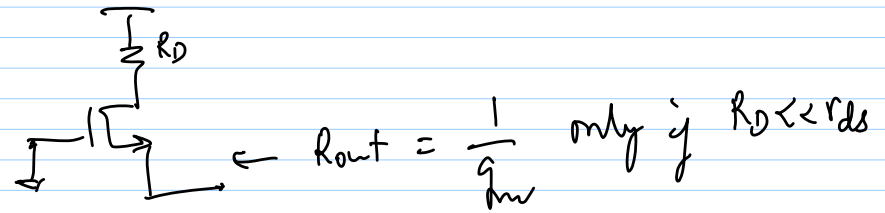
VA
amp.

7) Offset

$\sigma_{v0}^2 = \text{Same as before}$

$$\sigma_{v_{T1,2}}^2 + \left(\frac{g_{m7}}{g_{m1}} \right)^2 \sigma_{v_{T7,8}}^2$$

8) ND poles & zeros



$$V_{o_{min}} (V_{cm_{min}}) = V_{b1} - V_{T4}$$

$$V_{o_{max}} (V_{cm_{max}}) = V_x + V_{T2} = V_{b1} - V_{A54} + V_{T2}$$

$$V_x = V_{b1} - V_{A54}$$

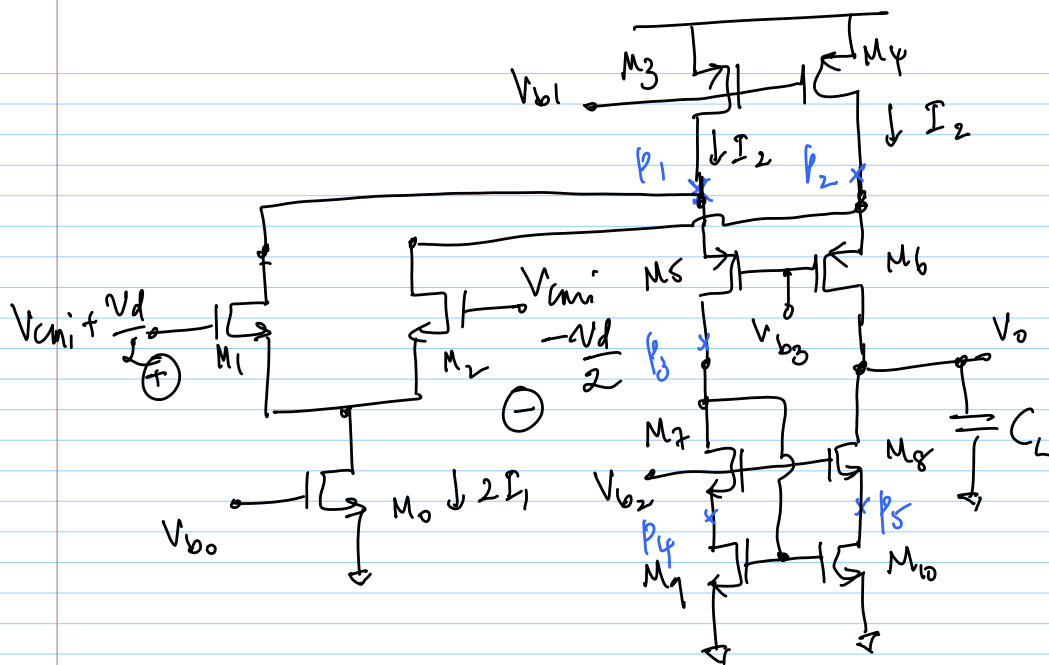
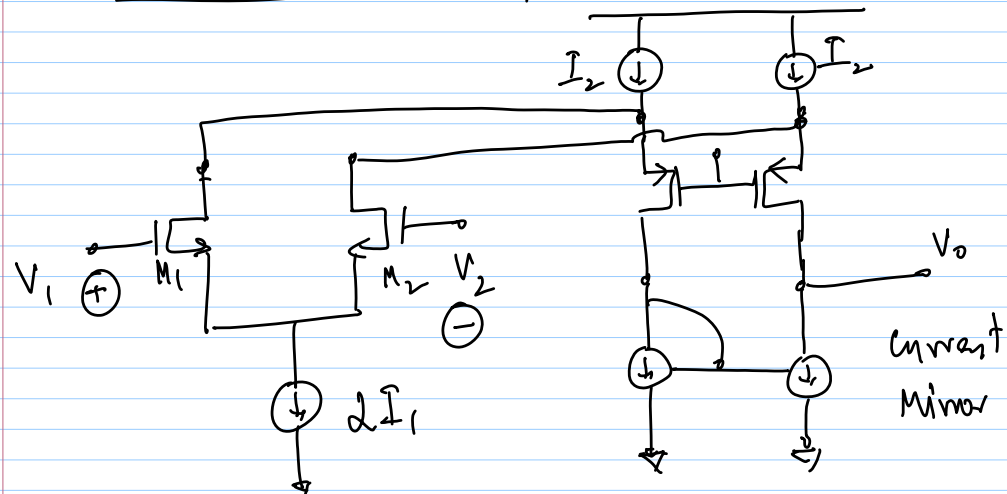
$$\Delta V_o = V_{T2} + V_{T4} - V_{A54}$$

$$\Delta V_o = V_{T2} - V_{DSAT4} \quad \sim \text{Couple of } 100 \text{ mV}$$

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Lec 22

Folded Cascode Opamp



1) DC gain:

$$R_{out} = (g_{m8} r_{ds8}) r_{ds10} \parallel (g_{m6} r_{ds6}) (r_{ds2} \parallel r_{ds4})$$

slightly lesser than folded cascode opamp

$$DC \text{ gain} = g_{m1} R_{out}$$

2) $\omega_u = \frac{g_{m1}}{C_L}$; $\omega_D = \frac{g_{out}}{C_L}$

3) ND poles & zeroes $\rightarrow p_1, -p_5$

$$4) V_{cm1}(\min) = V_{DSAT2} + V_{CS1}$$

$$V_{cm1}(\max) = V_{b3} + V_{ohs} + V_{T1}$$

$$5) V_{cm0}(\min) = V_{DSAT8} + V_{DSAT10}$$

$$V_{cm0}(\max) = V_{b3} + V_{T6}$$

6) Noise

$$\overline{e_n^2} = \frac{16kT}{\delta} \left[\frac{1}{g_{m1}} + \frac{g_{m3}}{g_{m1}^2} + \frac{r_{m9}}{g_{m1}^2} \right]$$

7) offset - HW

8) Slow Rate