Fractional-N PLL

Dtuider $\quad N / N+1$

$\{Q N \mid Q N 2, Q P I Q P 2\}$
$P=0$, Fin is high.

$$
10,01
$$

$$
\begin{aligned}
& Q N 1^{+}=Q P 1 \\
& Q N 2^{+}=Q P 2 \cdot P \\
& Q P 1^{+}=\overline{Q N 1} \cdot \overline{Q N 2} \\
& Q P 2^{+}=Q N
\end{aligned}
$$



Divide-by-3: $P=1$


$$
\begin{aligned}
& Q P 1^{+}=Q \overrightarrow{N I} \cdot \overrightarrow{Q N 2} \\
& Q P 2^{+}=Q N 1 \\
& Q N 1^{+}=Q P 1 \\
& Q N 2^{+}=Q P 2 \cdot P
\end{aligned}
$$



$$
\begin{array}{ccccc}
P_{1} & P_{0} & \text { Divi } & \text { Div2 } & \text { Div } \\
0 & 0 & \div 2 & \pm 2 & \pm 4
\end{array}
$$


$\Rightarrow$ Seamless switehing across whole range


$$
\begin{aligned}
n_{\text {Sd }}(z)= & n_{\text {frac }}(z) \text { STF }(z) \\
& +q(z) \text { NTF }(z)
\end{aligned}
$$

$$
n_{s q}[k]=x[k]+q[k]
$$

$$
\Rightarrow \quad n_{\text {frac }}(2)-(N T F(2)-1) \times-q(2)=n_{s a}(2)-q(2)
$$




