

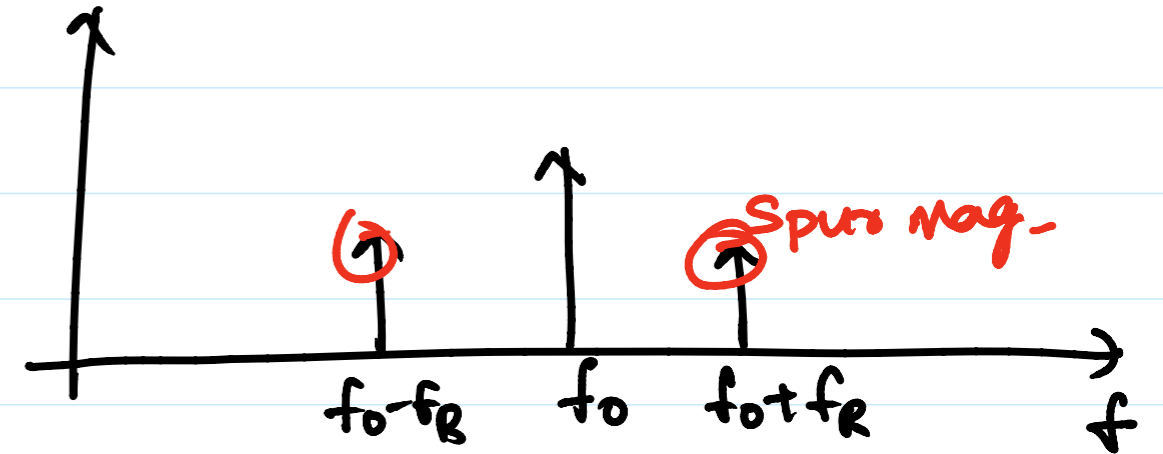
# PLL building blocks. - CP

$$\text{Spur magnitude} = \frac{F_{BW}}{2F_R} \Delta\phi_{os}$$

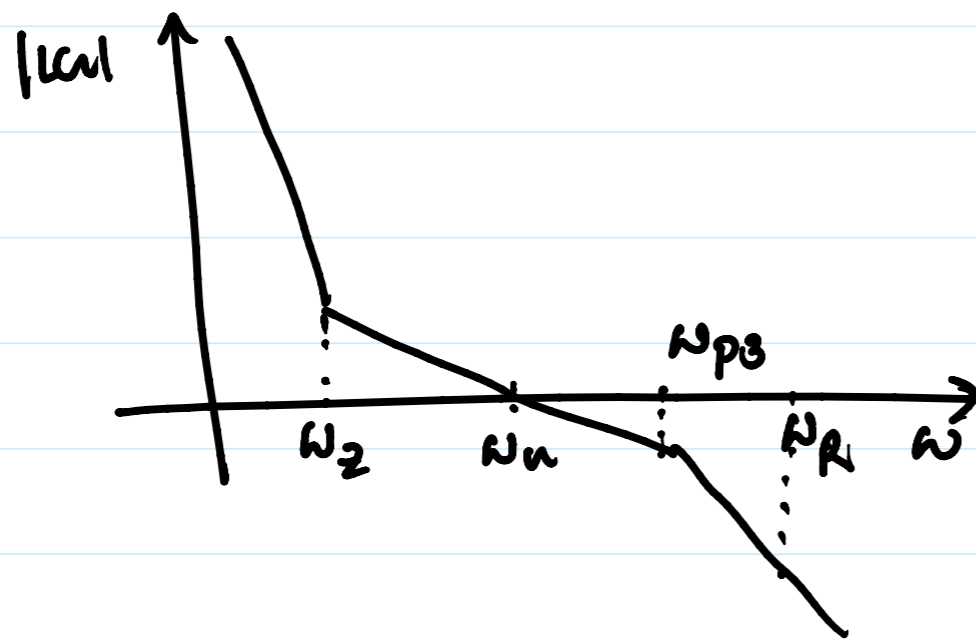
$F_{BW}$ : unity gain bandwidth

$F_R$ : ref. frequency

$\Delta\phi_{os} = \frac{2\pi T_{os}}{T_R}$  : phase offset due to current mismatch ( $I_{up} \neq I_{dn}$ )



$$\text{Spur mag. (in dB)} = 20 \log \left( \frac{F_{BW}}{2F_R} \cdot \Delta\phi_{os} \right) - \underbrace{20 \log \left( \frac{N_R}{N_{p3}} \right)}_{\text{Ref. spur suppression}}$$



Spur suppression:

$F_{BW} \downarrow$ ,  $N_{p3} \downarrow$

$F_R \uparrow$

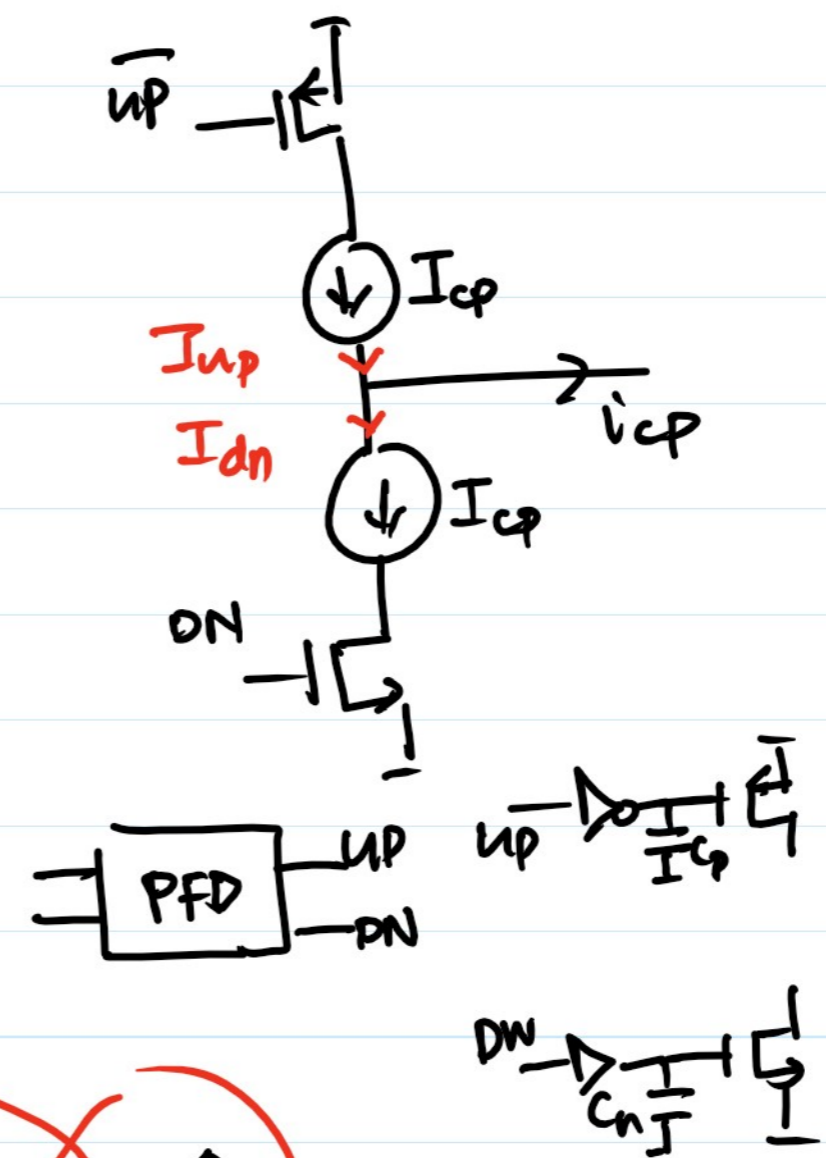
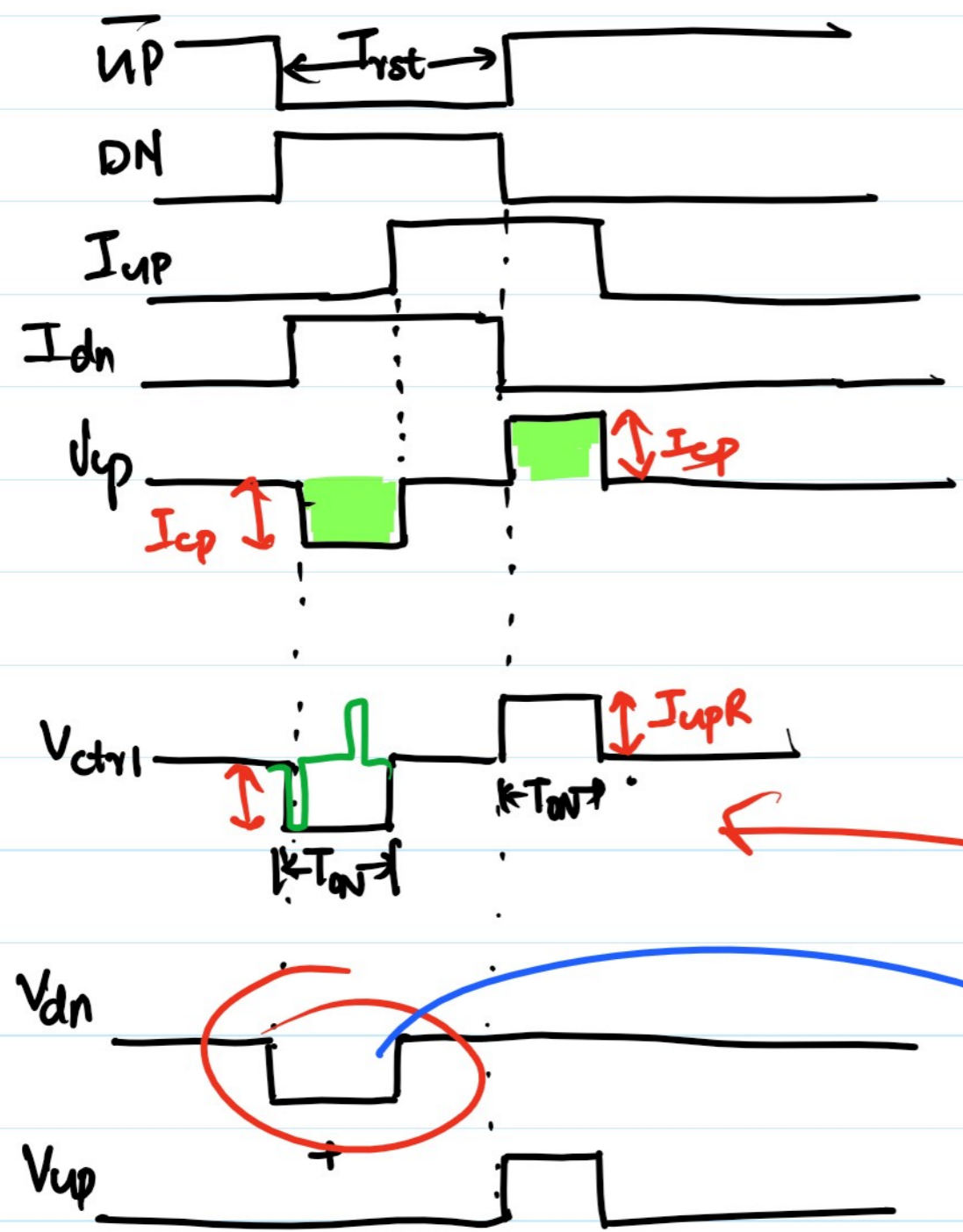
\* Slow response

\* Noise

\* Reduced  $\Phi_m$

\* More power

- Delay between  $I_{up}$  &  $I_{dn}$

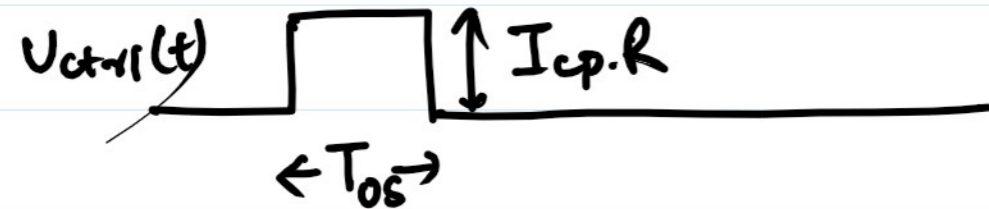


$$V_{ctrl}(s) = V_{dn}(s) - e^{-sT_{rst}} V_{dn}(s)$$

$$= (1 - e^{-sT_{rst}}) V_{dn}(s)$$

$$= [1 - (1 - sT_{rst})] V_{dn}(s) \quad ; \quad |sT_{rst}| \ll 1$$

$$= (sT_{rst}) V_{dn}(s)$$



$$V_{ctrl} = \sum_{n=1}^{\infty} \frac{2I_{cp} \cdot R}{n\pi} \sin\left(n\pi \frac{T_{0s}}{T_R}\right) \cos(n\omega_R t)$$

For mismatch between  $I_{up}$  &  $I_{dn}$  delays

$I_{up}$  delay : Delay from UP signal to  $I_{up}$  o/p.

$$V_{ctrl}(t) = \frac{2I_{cp} \cdot R}{\pi} \sin\left(\pi \frac{T_{0s}}{T_R}\right) \left(\frac{2\pi}{T_R} \cdot T_{rst}\right)$$

$$V_{ctrl}(t) = \frac{2I_{cp} R}{\pi} \sin\left(\pi \frac{T_{0s}}{T_R}\right) \cos(\omega_R t)$$

$$\frac{d(V_{ctrl}(t))}{dt} = \frac{2I_{cp} R}{\pi} \sin\left(\pi \frac{T_{0s}}{T_R}\right) (-\omega_R \sin(\omega_R t))$$

$$V_{ctrl}(t) = \frac{2I_{cp} \cdot R}{1} \frac{T_{0s}}{T_R} \frac{2\pi}{T_R} T_{rst}$$

$$\begin{aligned}
 V_{out} &= A \cos \left( K_{vco} \int V_o + 2 I_{cp} \cdot R \frac{T_{on}}{T_R} \cdot 2\pi \frac{T_{rst}}{T_R} \cdot \cos(\omega_{rt}) \cdot dt \right) \\
 &= A \cos \left( \omega_{ot} + \frac{2 I_{cp} \cdot R \cdot K_{vco}}{\omega_R} \cdot \frac{T_{on}}{T_R} \cdot \frac{2\pi T_{rst}}{T_R} \sin(\omega_{rt}) \right) \\
 &= A \cos \left( \omega_{ot} + \underbrace{2 I_{cp} \cdot R \cdot K_{vco} \frac{T_{on}}{T_R} \cdot T_{rst}}_{\beta'} \sin(\omega_{rt}) \right)
 \end{aligned}$$

$$\text{Spur mag.} = \frac{\beta'}{2} = \frac{2 I_{cp} R K_{vco}}{T_R} \cdot T_{on} \cdot T_{rst} \times \frac{1}{2}$$

$$= \frac{F_{BW}}{2} \cdot \left( 2\pi \frac{T_{on}}{T_R} \right) \cdot T_{rst}$$

$$= \frac{F_{BW}}{2} \cdot \Delta\phi_{on} \cdot T_{rst}$$

$$\text{Spur mag.} = 20 \log \left( \frac{F_{BW}}{2} \cdot \Delta\phi_{on} \cdot T_{rst} \right) - 20 \log \left( \frac{\omega_R}{\omega_{p3}} \right)$$

Spur Suppression due to 3<sup>rd</sup> pole



