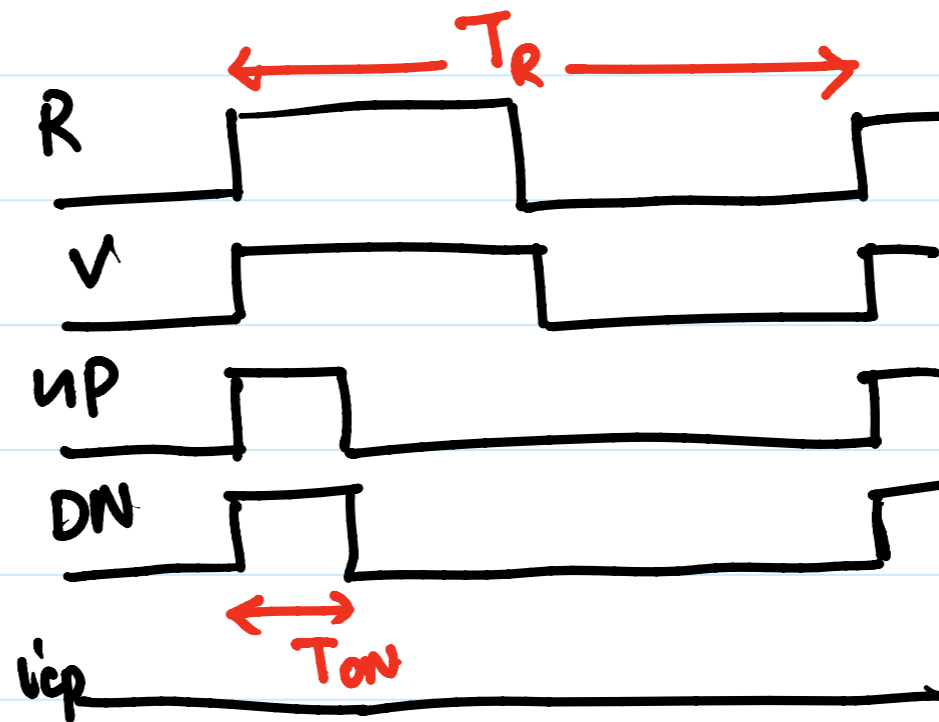
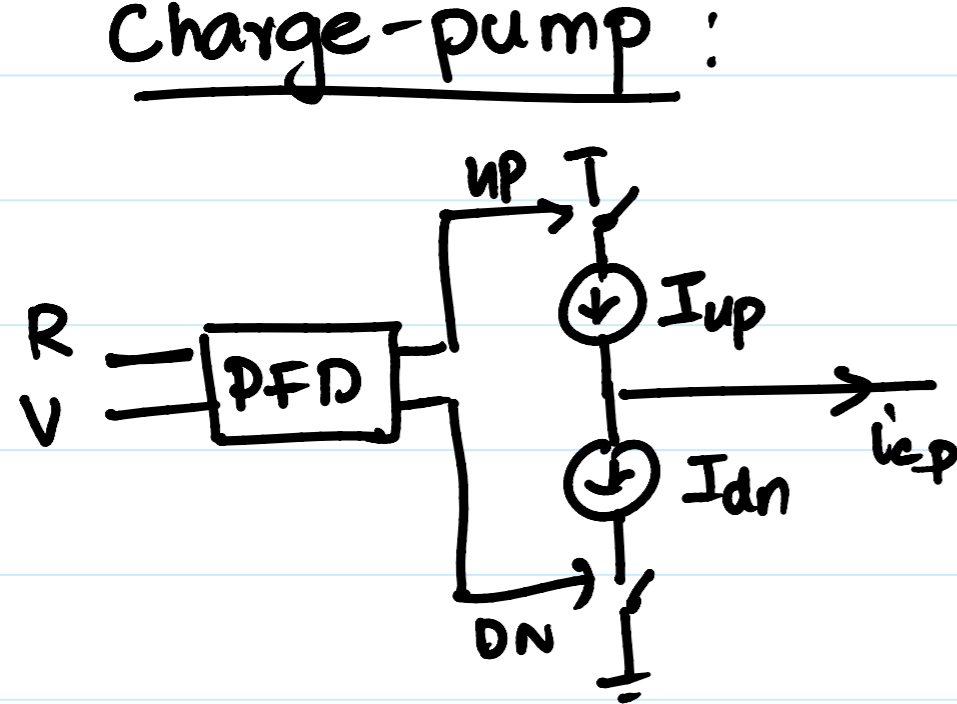
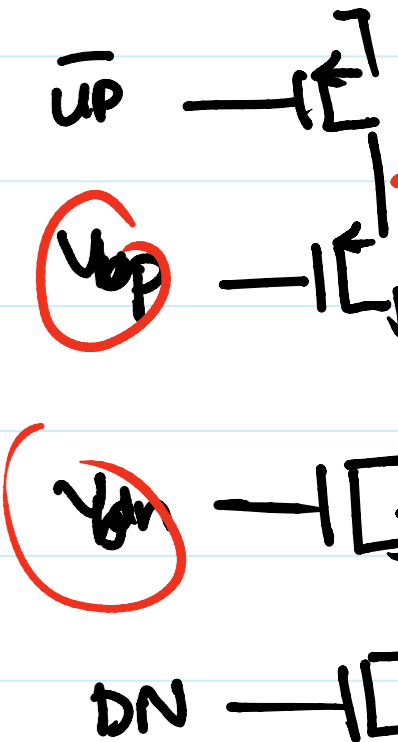


# PLL building blocks.

## Charge-pump :



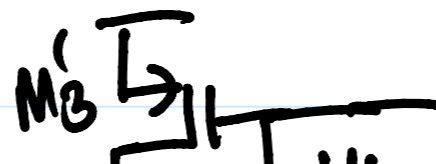
$$i_{cp} = I_{up} - I_{dn}$$

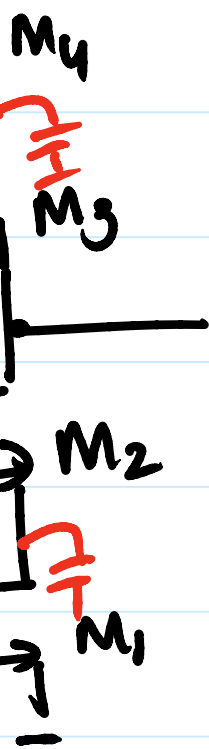


- Mismatch between  $I_{up}$  &  $I_{dn}$ ,  $I_{up} \neq I_{dn}$   
(Static errors)

$M_1, M_4$  are  
 $M_2, M_3$  are

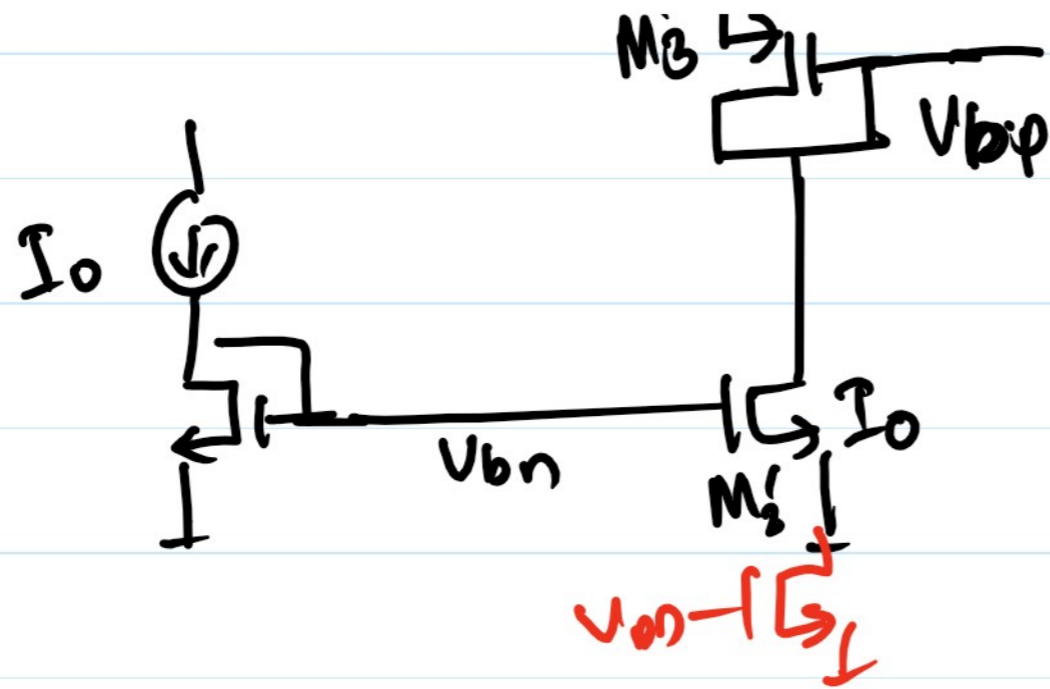
- Dynamic error : Charge-sharing during transient  
clock- f





switches

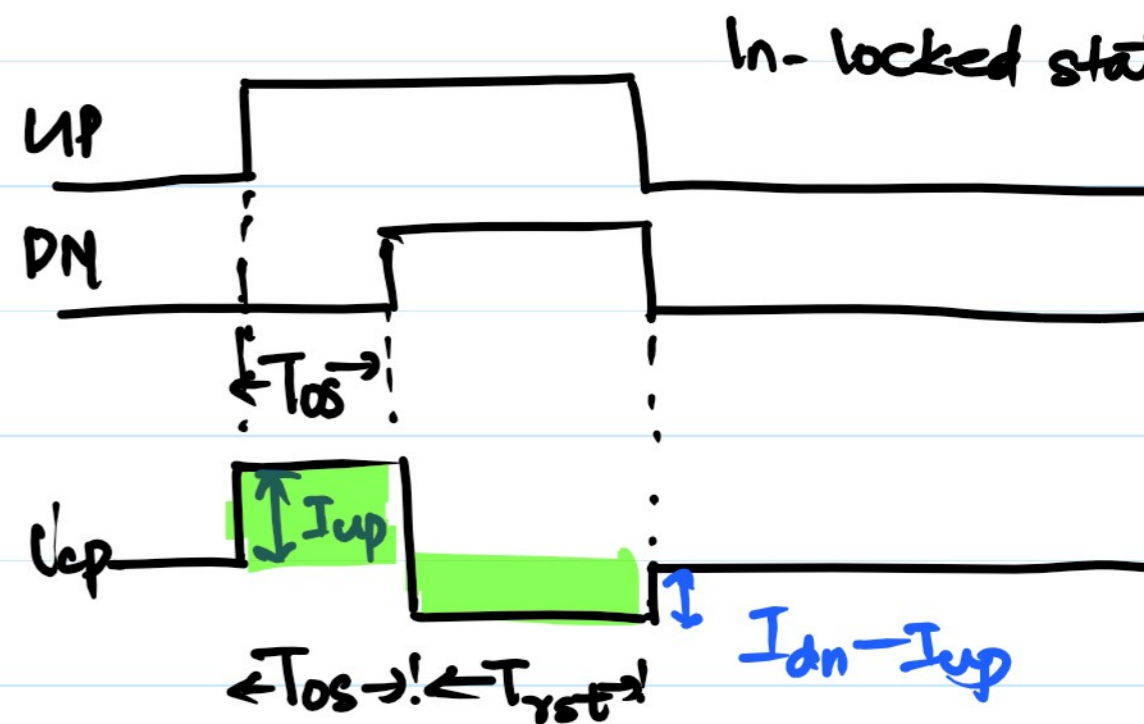
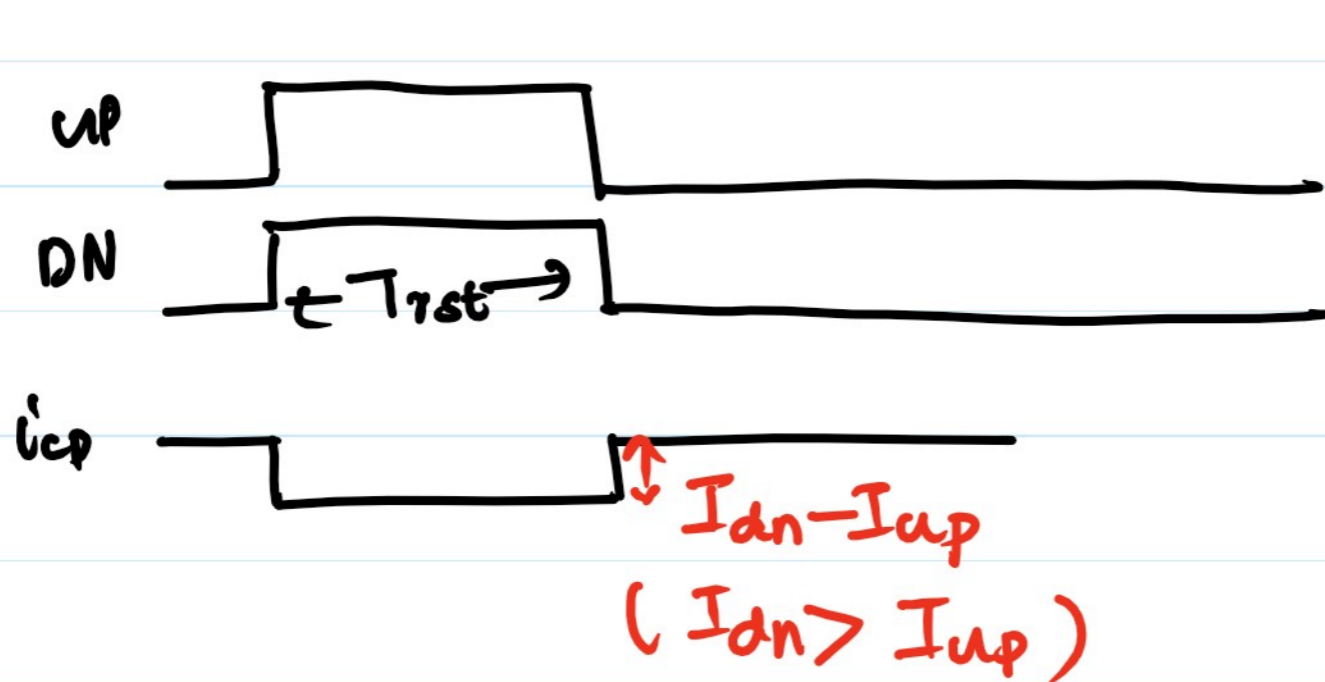
current source



Mismatch between  $M_2$  &  $M_2'$ ,

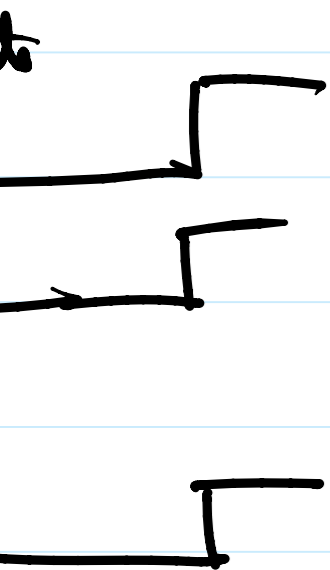
-  $\overline{UP} / DN \rightarrow I_{up}/I_{dn}$  delay

a) Mismatch between  $I_{up}$  &  $I_{dn}$



$$I_{up} \cdot T_{os} = (I_{dn} - I_{up}) T_{rst}$$

$M_3$  &  $M'_3$

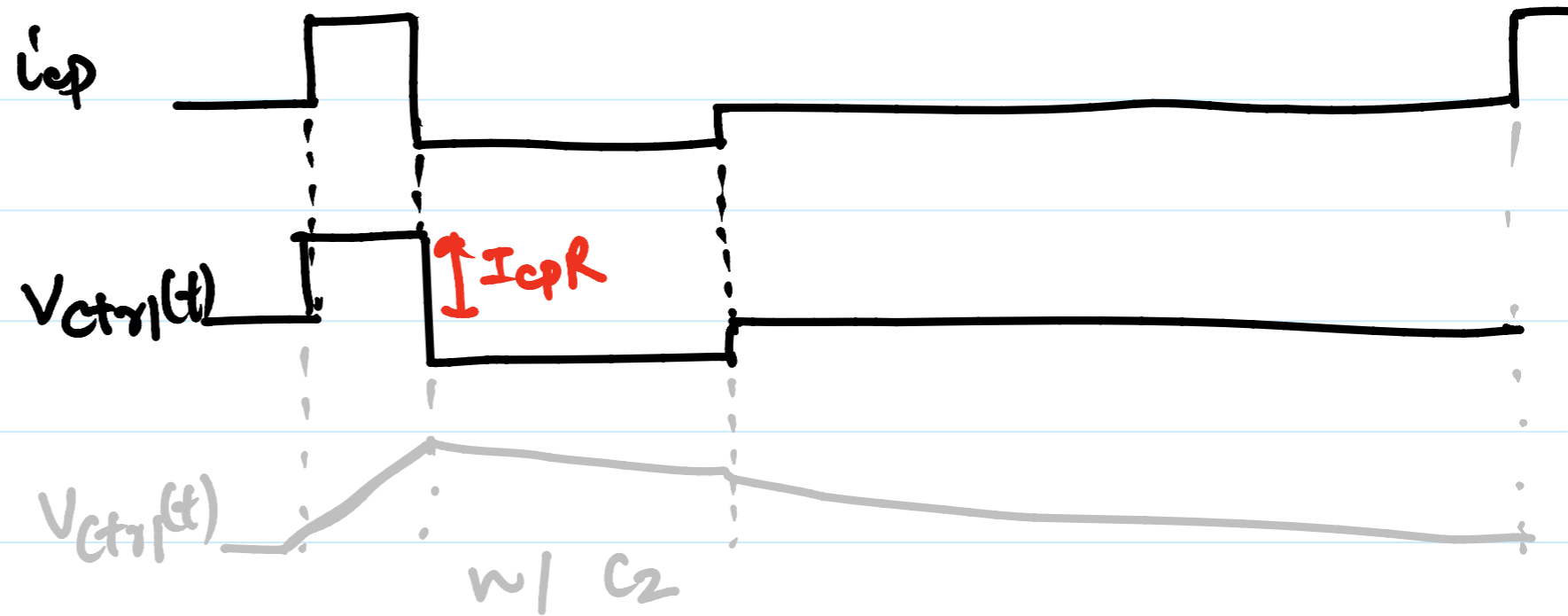
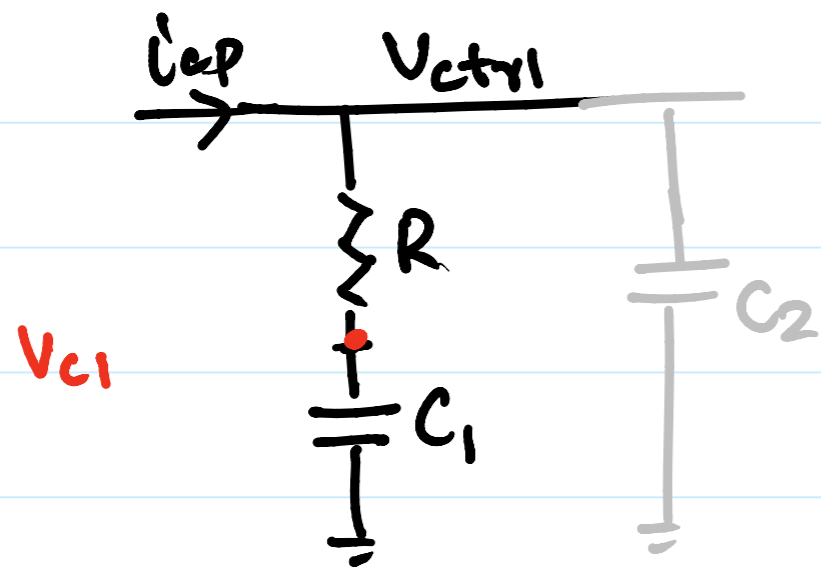


$$I_{up} \cdot T_{os} = (I_{dn} - I_{up}) T_{rst}$$

$$\frac{T_{os}}{T_{rst}} = \frac{I_{dn} - I_{up}}{I_{up}} = \frac{\Delta I}{I}$$

$$T_{os} = \frac{\Delta I}{I} T_{rst}$$

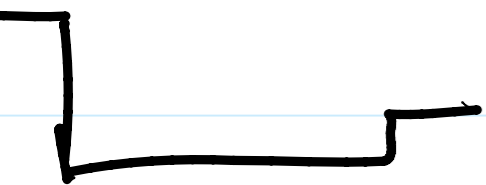
$$\Delta \phi_{os} = 2\pi \cdot \frac{T_{os}}{T_R} = 2\pi \cdot \frac{\Delta I}{I} \frac{T_{rst}}{T_R} \quad ; \quad T_R - \text{Ref. per}$$



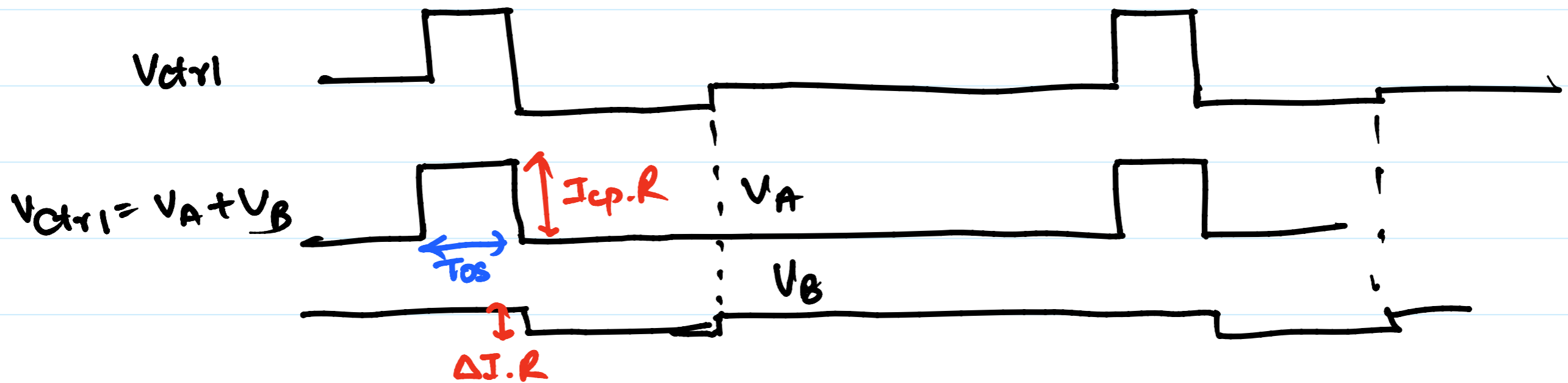
$$i_{cp} = C_1 \frac{dV_{c1}}{dt}$$

$$V_{c1} = \frac{1}{C_1} i_{cp} t$$

ried



$$v_{ctrl} = \frac{1}{C_1} \dot{i}_{cp} t + \dot{i}_{cp} \cdot R$$



$$v_{ctrl} = v_A + v_B \approx v_A = a_0 + \sum_n a_n \cos(n\omega_R t)$$

$\omega_R$ : ref. fr

$$a_0 = I_{cp} \frac{T_{os}}{T_R}$$

For  $n=1$

$$v_{ctrl} = \frac{2 I_{cp} R}{\omega_R T_R} \sin\left(2\pi \frac{T_{os}}{T_R}\right) \cos(\omega_R t)$$

$$\approx \frac{2 I_{cp} R}{\omega_R T_R} \left(2\pi \frac{T_{os}}{T_R}\right) \cos(\omega_R t)$$

$$\int_0^{T_R} (I_{cp} R) \cos(m\omega_R t) \cdot dt$$

$$= \int_0^{T_R} \sum_n a_n \cos(n\omega_R t) \cdot dt$$

$$\frac{I_{cp} R \times \sin(m\omega_R t) \Big|_0^{T_{os}}}{m\omega_R} = \frac{a_m}{n} \int_0^{T_R} 1 - \cos(2n\omega_R t) dt$$

$q$

$t$

$$\cos(m\omega_p t) dt$$

$$\sin(\omega_p t) dt$$



$$= \frac{2I_{cp}R}{\omega_R T_R} \overbrace{\Delta\phi_{os} \cdot \cos(\omega_R t)}$$

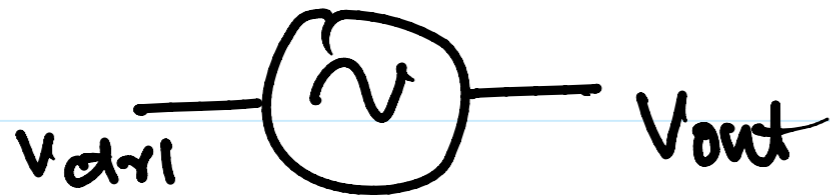
$$= \frac{I_{cp}R}{\pi} \Delta\phi_{os} \cos(\omega_R t)$$

$$= \frac{u_m}{2} \int_0^{2\pi} 1 - \cos(2n\omega_R t) dt$$

$$\Rightarrow a_n = \frac{2I_{cp} \cdot R}{n \omega_R T_R}$$

$$a_n = \frac{2I_{cp} \cdot R}{n \omega_R T_R} \sin(2n\omega_R t)$$

$$= \frac{I_{cp} R}{n\pi} \sin(2n\pi)$$



$$v_{out} = A \cos\left(\cdot \quad k_{vco} \cdot \int v_{ctrl} \cdot dt\right)$$

$$= A \cos\left(\underbrace{k_{vco} \int v_0 + \frac{2I_{cp} \cdot R}{\omega_R T_R} \cdot \Delta\phi_{os} \cdot \cos(\omega_R t) dt}_{\beta}$$

$$= A \cos\left(\omega_0 t + \underbrace{\frac{2I_{cp} \cdot R}{\omega_R T_R} \cdot \Delta\phi_{os} \cdot k_{vco} \int \cos(\omega_R t) dt}_{\beta}$$

$$= A \cos\left(\omega_0 t + \frac{\beta}{\omega_R} \sin(\omega_R t)\right)$$

$n\omega_r t) dt$

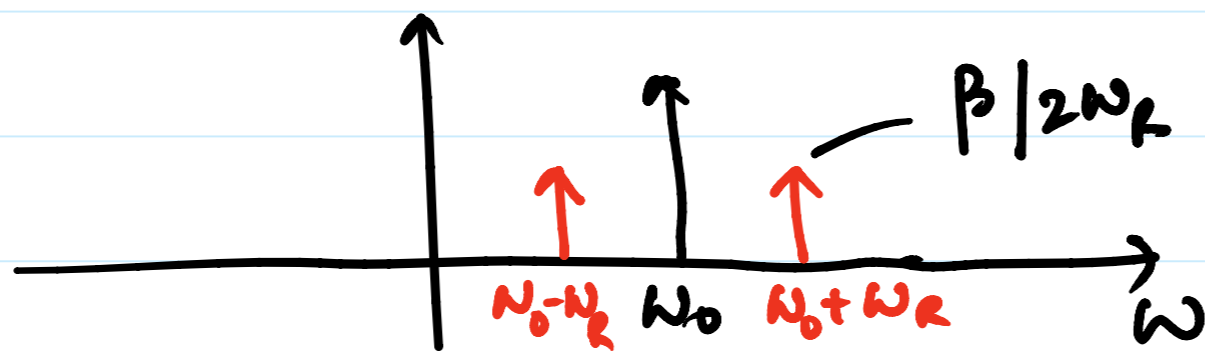
$\sin(n\omega_r T_{os})$

$(n\pi \frac{T_{os}}{T_R})$

$(\frac{T_{os}}{T_R}) \checkmark$

$t)$

$$\begin{aligned}
 &= A \cos(\omega_0 t) \cos\left(\underbrace{\frac{\beta}{\omega_R}}_{\approx 0} \sin(\omega_R t)\right) - A \sin(\omega_0 t) \sin\left(\frac{\beta}{\omega_R} \sin(\omega_R t)\right) \\
 &= A \cos(\omega_0 t) - A \sin(\omega_0 t) \cdot \frac{\beta}{\omega_R} \sin(\omega_R t) \\
 &= A \cos(\omega_0 t) + \frac{A}{2} \frac{\beta}{\omega_R} \left( \cos(\overline{\omega_0 + \omega_R} t) - \cos(\overline{\omega_0 - \omega_R} t) \right) \\
 &= A \cos(\omega_0 t) + \underbrace{A}_{\text{blue circle}} \times \frac{\beta}{2\omega_R} \left[ \cos(\overline{\omega_0 + \omega_R} t) - \cos(\overline{\omega_0 - \omega_R} t) \right]
 \end{aligned}$$



$$\frac{\beta}{2\omega_R} = \frac{2 I_{cp} \cdot R}{\omega_R T_R} \cdot \Delta\phi_{os} \cdot k_{vco} \cdot \frac{1}{2\omega_R}$$

$$\frac{B}{\omega_R T} \cdot \sin(\omega_R t)$$

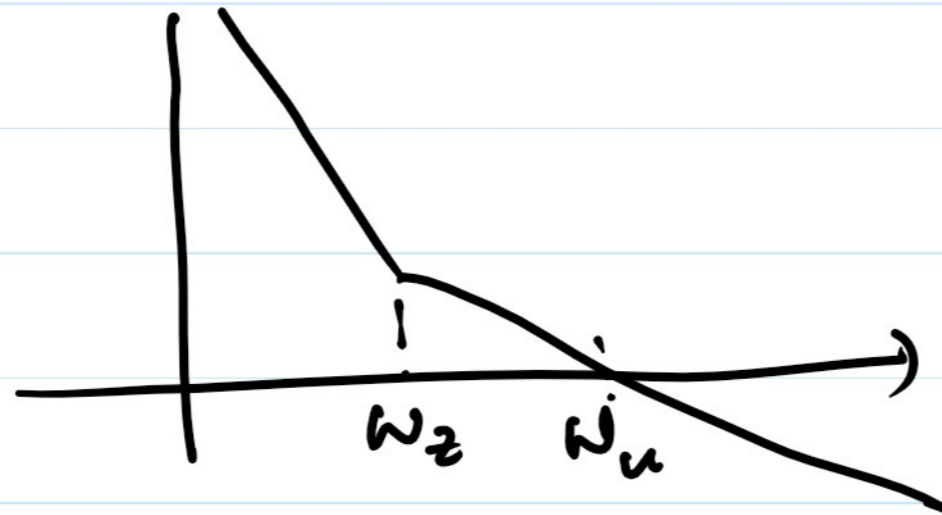
$$\sin(\omega_R t)$$

$$\omega_R t$$

$$= \frac{2 I_{cp} \cdot R}{\omega_R T_R} \cdot \frac{2\pi \cdot T_{os}}{T_R} \times \frac{K_{vco}}{2 \cdot \frac{2\pi}{T_R}}$$

$$= \frac{I_{cp} \cdot R}{2 \omega_R T_R} T_{os} \cdot K_{vco} = \frac{I_{cp} \cdot R \cdot K_{vco}}{2\pi} \cdot \frac{T_{os}}{(2/T_R) T_R} =$$

$$L_G = \frac{I_{cp}}{2\pi} \left( R + \frac{1}{sC_1} \right) \frac{K_{vco}}{s} = \frac{I_{cp}}{2\pi} \frac{K_{vco}}{sC_1} \frac{(1+sRC_1)}{s}$$



$$|L_G(j\omega)| = \frac{I_{cp}}{2\pi} \frac{K_{vco}}{\omega_u s T} R C_1 =$$

$$\omega_u = \frac{I_{cp} R \cdot K_{vco}}{2\pi}$$

$$\text{Spur magnitude} = \frac{\bar{F}_{BW}}{2\bar{F}_R} \Delta\Phi_{os}$$

$$\frac{2\pi F_{BW}}{2 \cdot F_R} \cdot \frac{T_{OS}}{T_R} = \frac{F_{BW}}{2F_R} \Delta\phi_{OS}$$

= 1