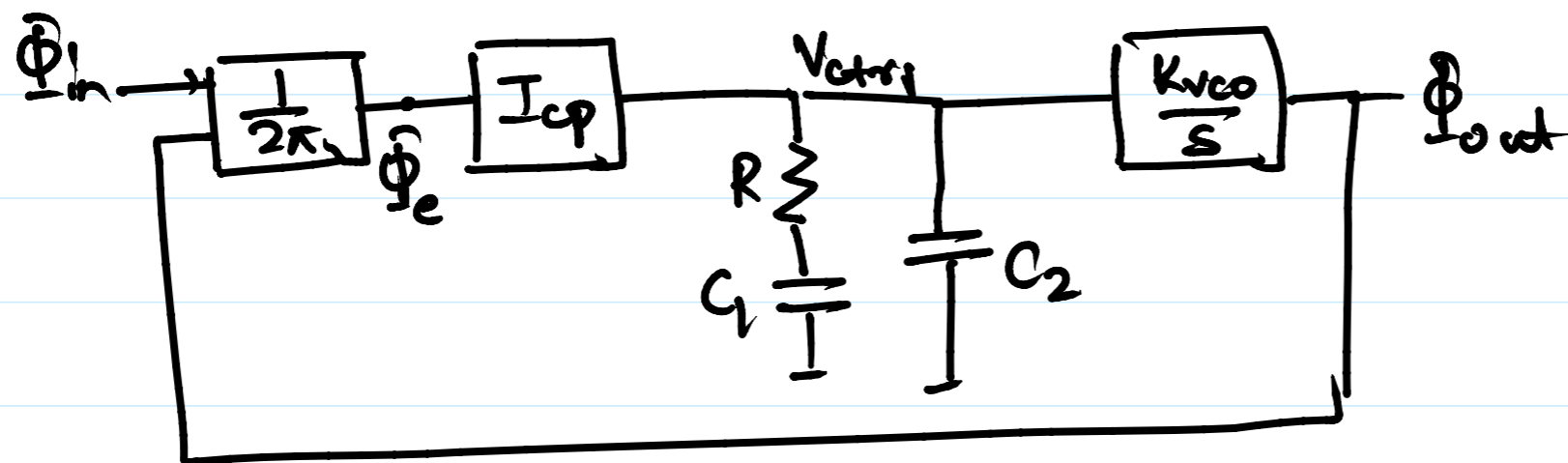
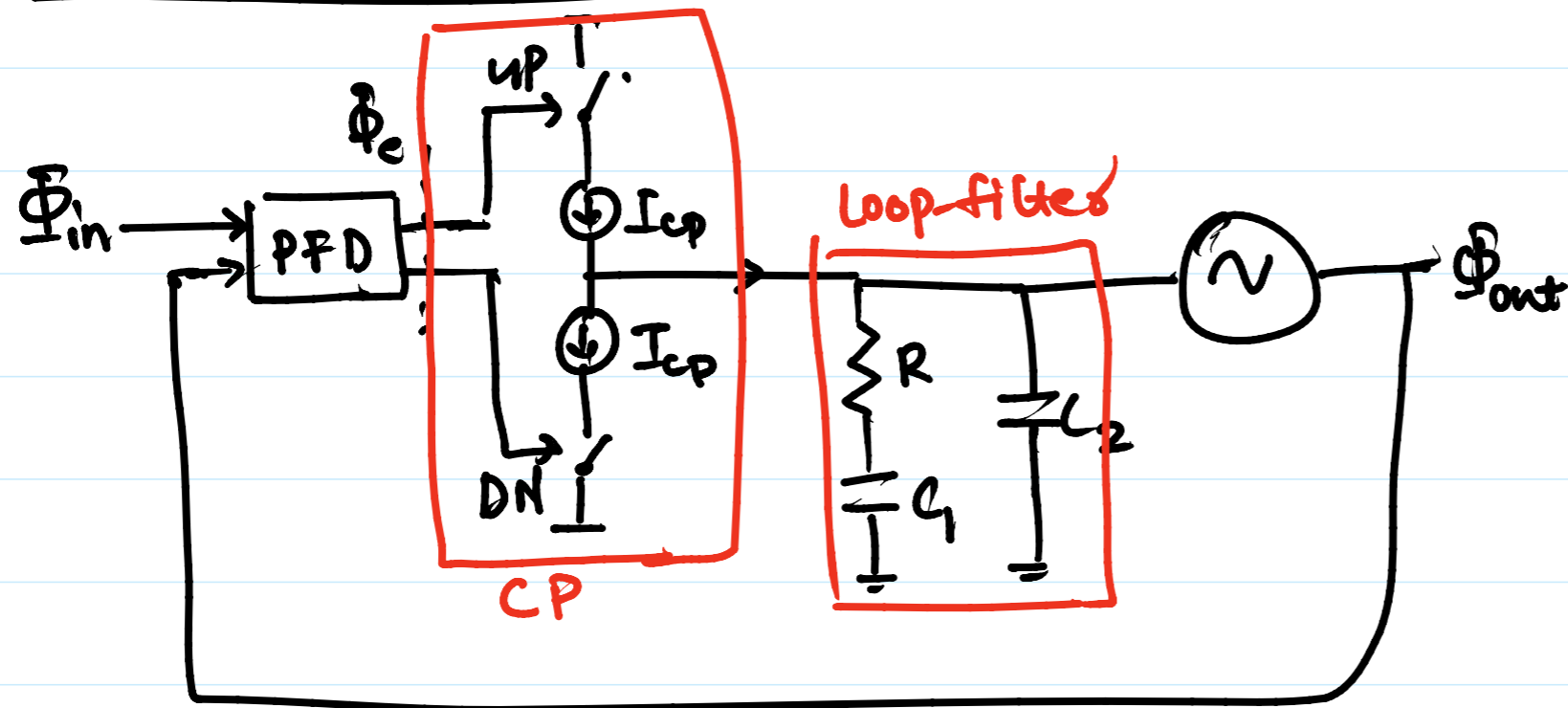


# Charge-pump based PLL

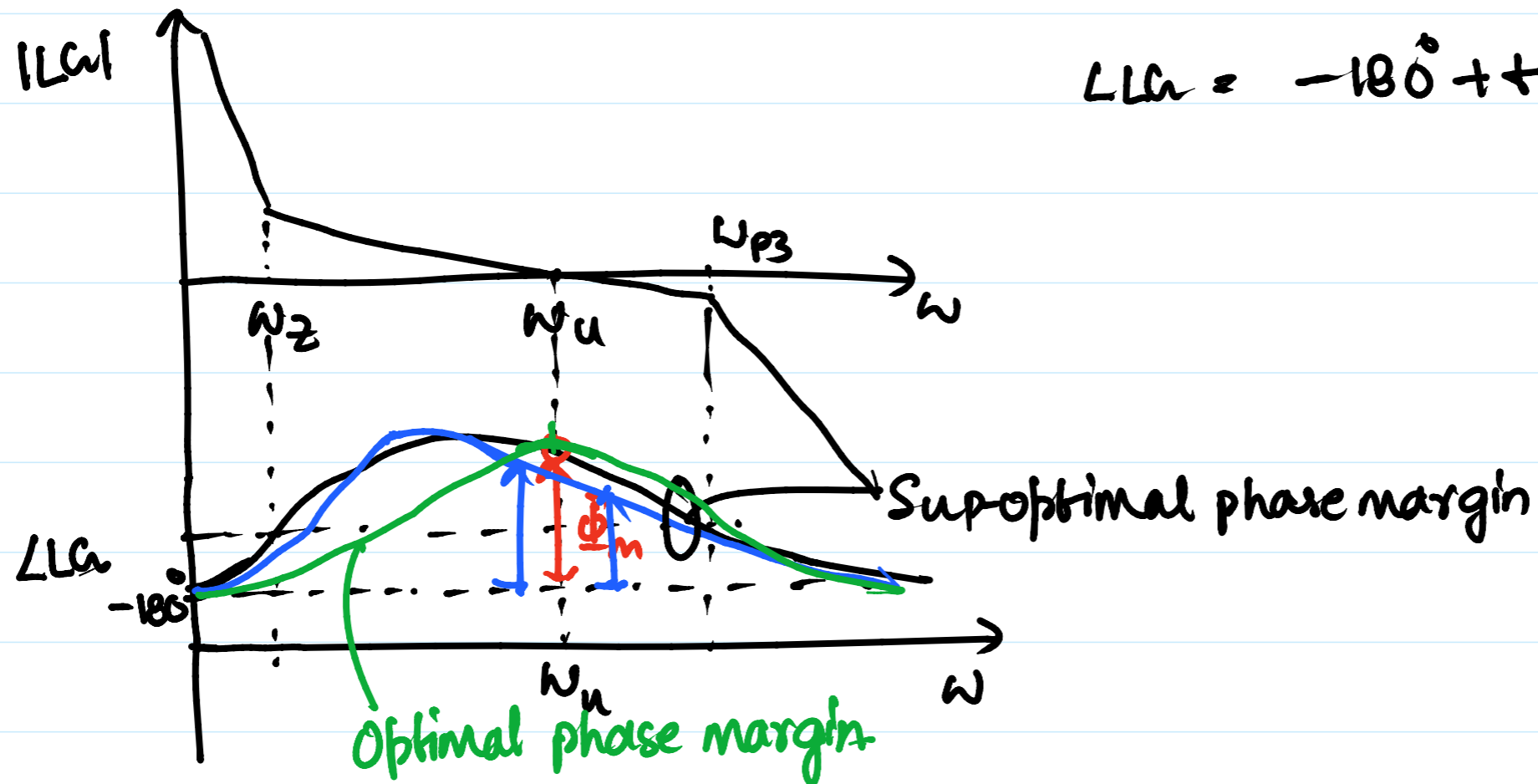


$$LG(s) = \frac{1}{2\pi} \times I_{cp} \times \frac{1}{sC_2} \frac{\left(s + \frac{1}{RC_1}\right)}{\left(s + \frac{1}{\frac{RC_1C_2}{C_1+C_2}}\right)} \frac{K_{vco}}{s}$$

$$= \frac{I_{cp} K_{vco}}{2\pi s^2 C_2} \frac{(s + \omega_z)}{(s + \omega_{p3})}$$

$$\omega_z = \frac{1}{RC_1}, \quad \omega_{p1} = \omega_{p2} = 0, \quad \omega_{p3} = \frac{C_1 + C_2}{RC_1 C_2} = \omega_z \left( \frac{C_1}{C_2} + 1 \right)$$

$$\angle L(s) = -180^\circ + \tan^{-1} \left( \frac{\omega}{\omega_z} \right) - \tan^{-1} \left( \frac{\omega}{\omega_{p3}} \right)$$

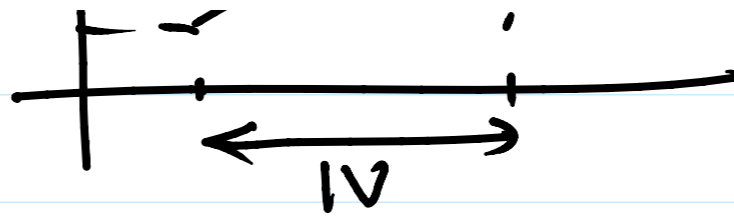


Desired:  $\omega_u, \Phi_m$   
 To find:  $\omega_z, \omega_{p3}, I_{cp}$

$K_{vco}$

$$\Delta F = 1 \text{ GHz}, \quad \Delta V_{ctrl} = (1V) \rightarrow 100 \text{ mV}$$





$$\text{Optimal } \Phi_m \Rightarrow \left. \frac{d\Phi_m}{d\omega} \right|_{\omega=\omega_u} = 0$$

$$\Phi_m = \tan^{-1}\left(\frac{\omega_u}{\omega_z}\right) - \tan^{-1}\left(\frac{\omega_u}{\omega_{p3}}\right) = \angle L_c \Big|_{\omega=\omega_u} - (-180^\circ)$$

$$\frac{d\Phi_m}{d\omega_u} = \frac{1}{\omega_z} \frac{1}{1 + \left(\frac{\omega_u}{\omega_z}\right)^2} - \frac{1}{\omega_{p3}} \frac{1}{1 + \left(\frac{\omega_u}{\omega_{p3}}\right)^2} = 0$$

$$\frac{\omega_z}{\omega_{p3}} \left[ 1 + \left(\frac{\omega_u}{\omega_z}\right)^2 \right] = 1 + \left(\frac{\omega_u}{\omega_{p3}}\right)^2$$

$$\frac{\omega_z}{\omega_{p3}} - 1 = \omega_u^2 \left[ -\frac{\omega_z}{\omega_{p3}} \cdot \frac{1}{\omega_z^2} + \frac{1}{\omega_{p3}^2} \right]$$

$$\frac{\omega_z}{\omega_{p3}} - 1 = \frac{\omega_u^2}{\omega_{p3}} \left[ -\frac{1}{\omega_z} + \frac{1}{\omega_{p3}} \right]$$

$$= \frac{\omega_u^2}{\omega_z \omega_{p3}} \left[ \frac{\omega_z}{\omega_{p3}} - 1 \right]$$

$$= \vec{\omega}_2 \vec{\omega}_3 \left( \frac{v}{\omega_3} - 1 \right)$$

$$\boxed{\omega_u = \sqrt{\omega_2 \omega_3} = \omega_3 \sqrt{1 + \frac{c_1}{c_2}}}$$

$$\Phi_m = \tan^{-1} \left( \sqrt{1 + \frac{c_1}{c_2}} \right) - \tan^{-1} \left( \frac{\omega_u}{\omega_2 \left( 1 + \frac{c_1}{c_2} \right)} \right)$$

$$\tan^{-1} \left( \frac{1}{\sqrt{1 + \frac{c_1}{c_2}}} \right)$$

$$\Phi_m = \tan^{-1} \left( \sqrt{1 + \frac{c_1}{c_2}} \right) - \tan^{-1} \left( \frac{1}{\sqrt{1 + \frac{c_1}{c_2}}} \right)$$

$$\tan(\Phi_m) = \frac{\sqrt{1 + \frac{c_1}{c_2}} - \frac{1}{\sqrt{1 + \frac{c_1}{c_2}}}}{1 + 1}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$= \frac{\frac{c_1}{c_2}}{2 \sqrt{1 + \frac{c_1}{c_2}}}$$

$$\left(\frac{C_1}{C_2}\right)^2 - 4\left(1 + \frac{C_1}{C_2}\right) \tan^2 \Phi_m = 0$$

$$\frac{C_1}{C_2} = \frac{4 \tan^2 \Phi_m + \sqrt{16 \tan^4 \Phi_m + 16 \tan^2 \Phi_m}}{2}$$

$$= 2 \tan^2 \Phi_m + 2 \tan \Phi_m \sqrt{\tan^2 \Phi_m + 1}$$

$$\boxed{\frac{C_1}{C_2} = 2 \tan \Phi_m \left[ \tan \Phi_m + \sqrt{1 + \tan^2 \Phi_m} \right]}$$

$$\omega_u, \Phi_m, \frac{d\Phi}{d\omega} = 0$$

Design Procedure for type-II, order 3 CP-PLL

$$1.) \omega_u, \Phi_m$$

$$2.) K_C = \frac{C_1}{C_2} = 2 \tan \Phi_m \left[ \tan \Phi_m + \sqrt{1 + \tan^2 \Phi_m} \right]$$

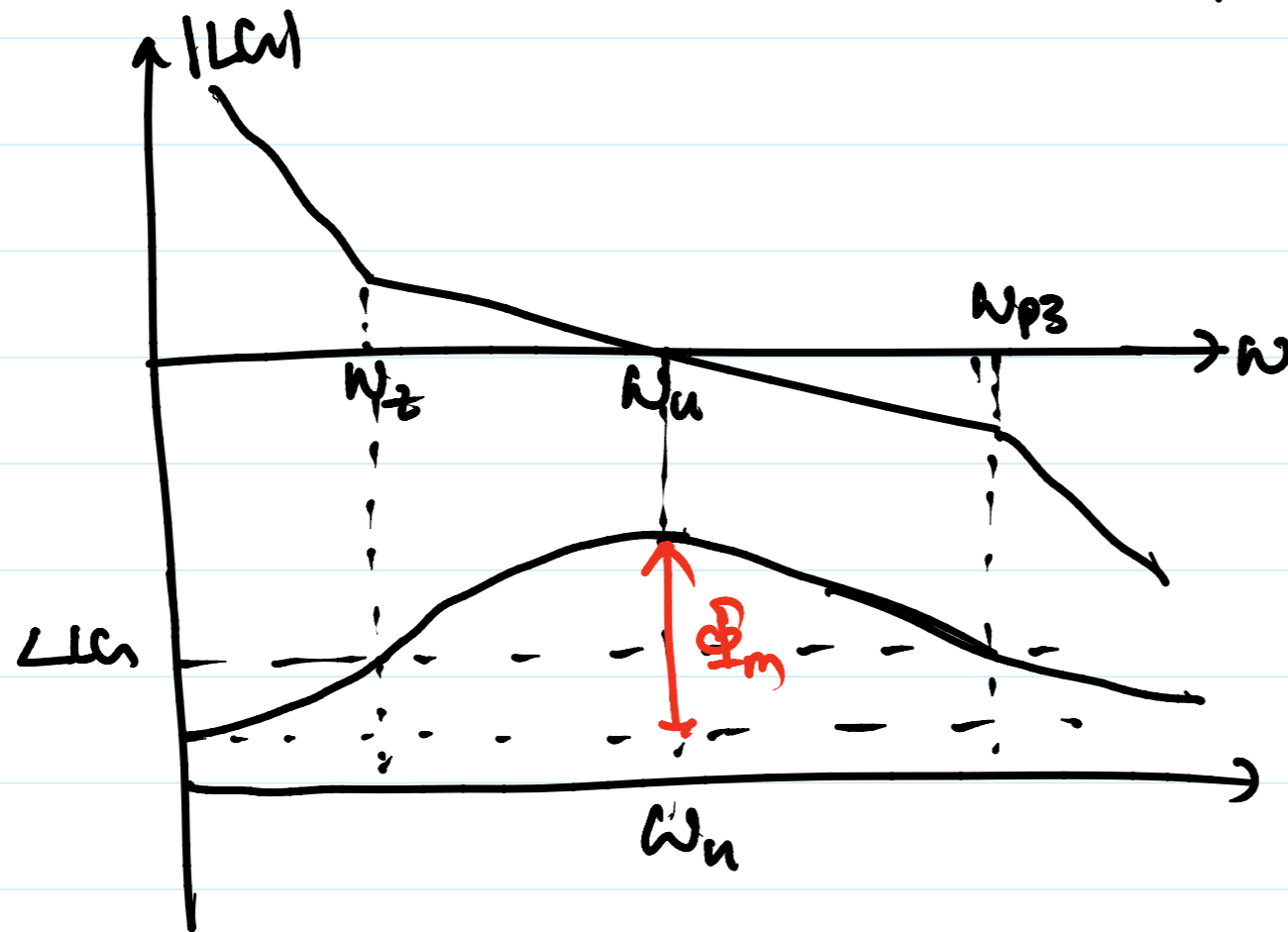
$$3.) \omega_z = \frac{\omega_u}{\sqrt{1 + K_C}}, \quad \omega_{p3} = \omega_z (1 + K_C)$$

4) Choice for R - based on noise

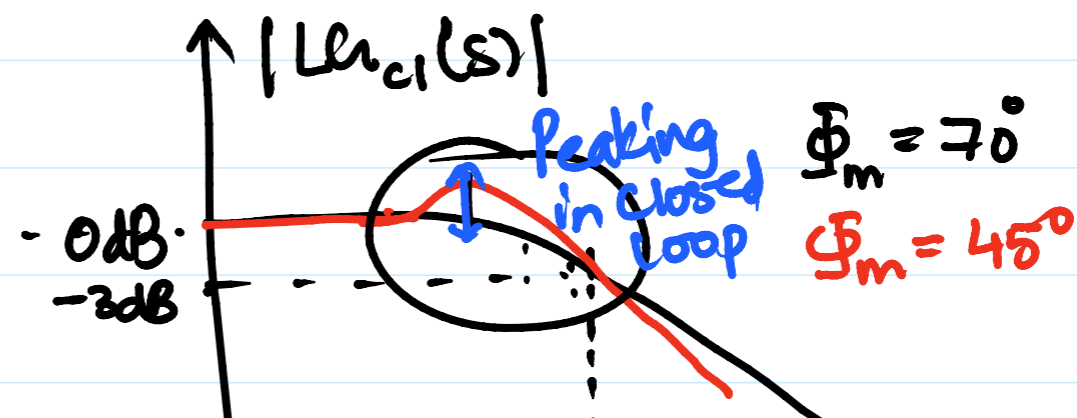
$$\omega_z = \frac{1}{RC_1} \Rightarrow C_1 \xrightarrow{K_c} C_2$$

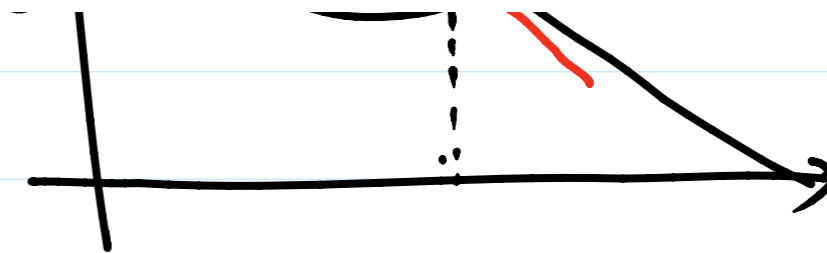
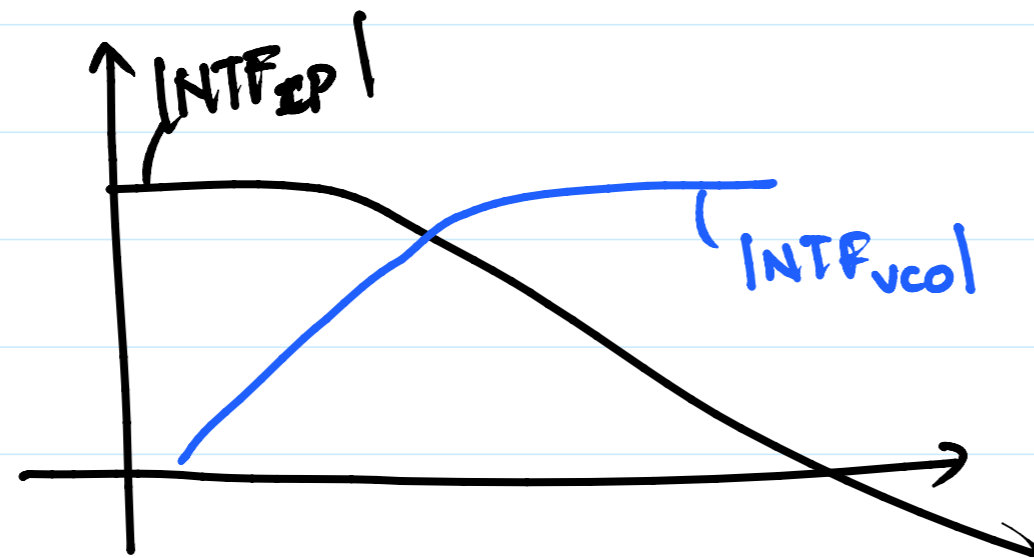
$$5) |LC(\omega_u)| \approx 1 \Rightarrow \left| \frac{I_{cp} K_{vco}}{2\pi \omega_u^2 C_2} \right|^2 \frac{\omega_u^2 + \omega_z^2}{\omega_u^2 + \omega_{p3}^2} \approx 1$$

$$\Rightarrow I_{cp}$$

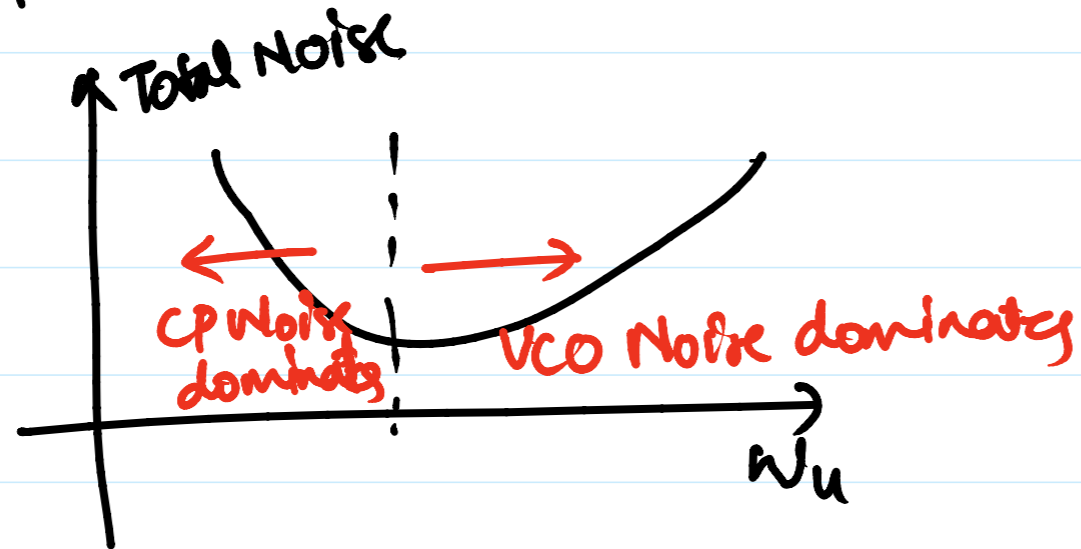


$$LC_{cl} = \frac{\Phi_{out}(s)}{\Phi_{in}(s)} = \frac{LC(s)}{1 + LC(s)}$$

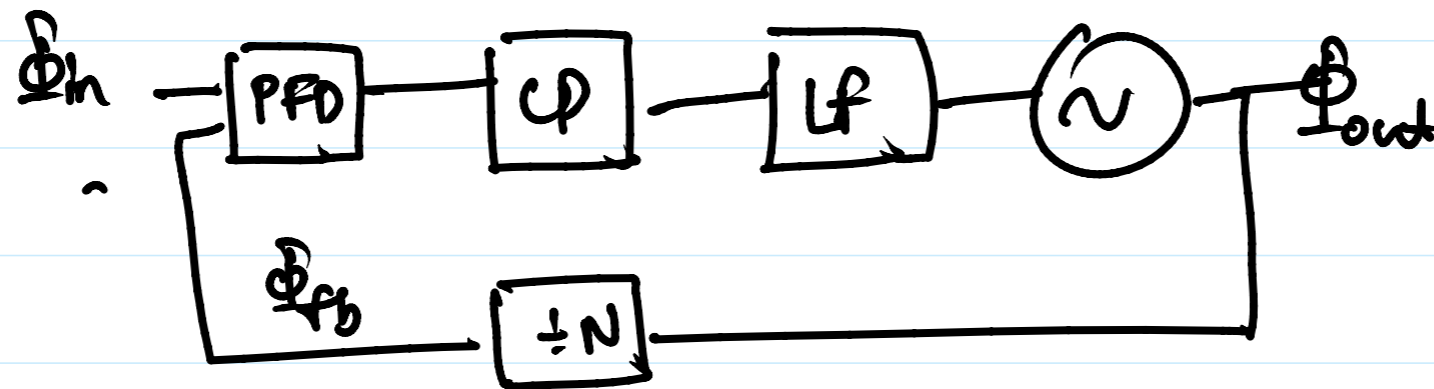


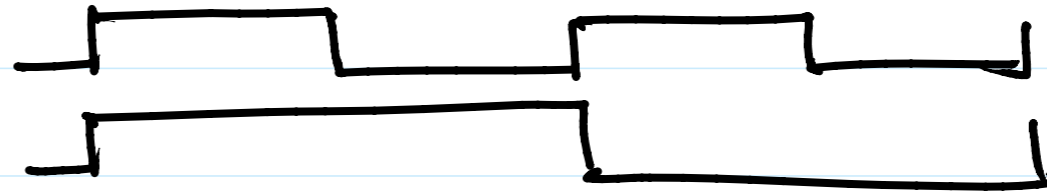
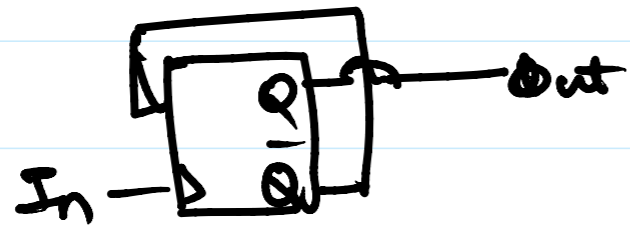


$NTF_{CP}$  = Noise Transfer function for Charge pump



Charge-pump PLL as clock multiplier





$$f_{out} = N f_{ref}$$

$$L_n = \frac{I_{cp} K_{vol}}{2\pi s^2 C_2} \frac{s + \omega_z}{s + \omega_{p3}} \times \frac{1}{N}$$