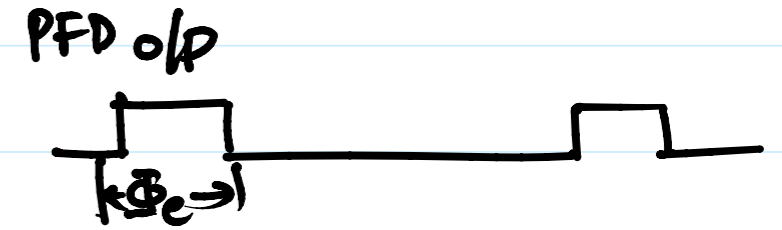
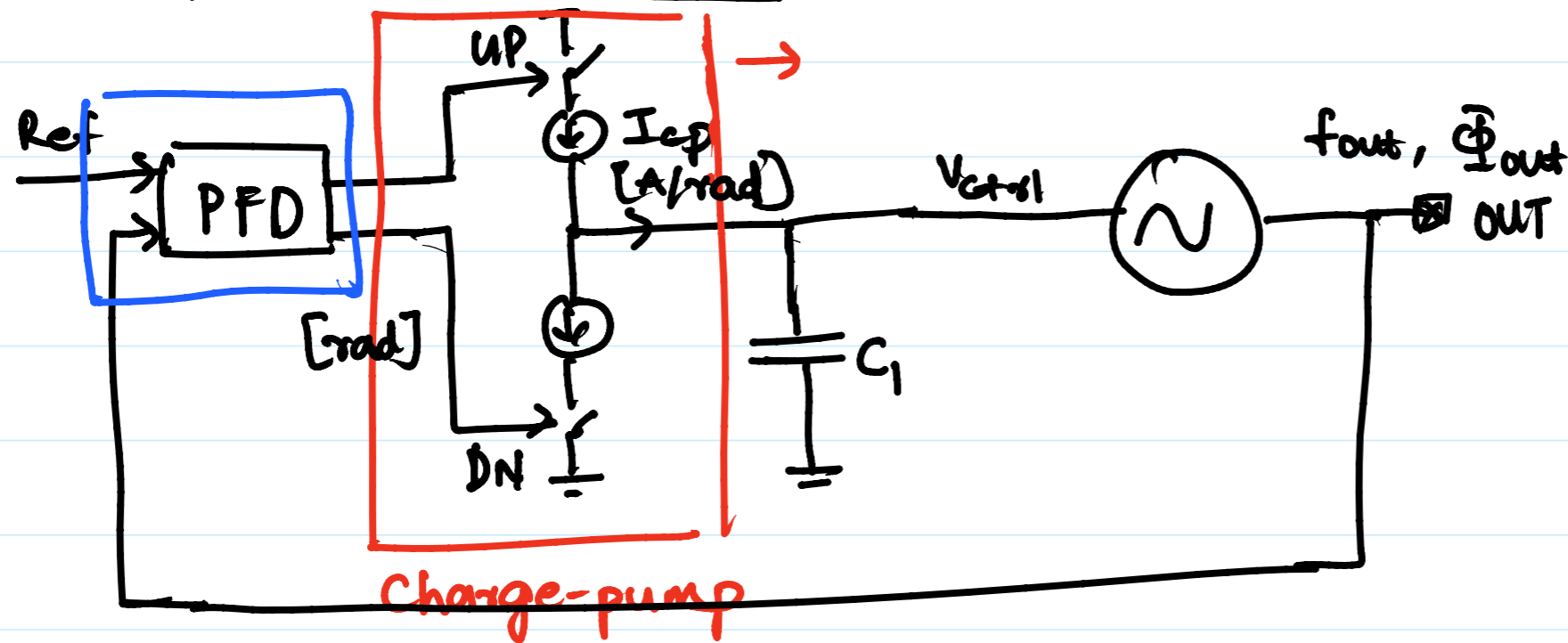
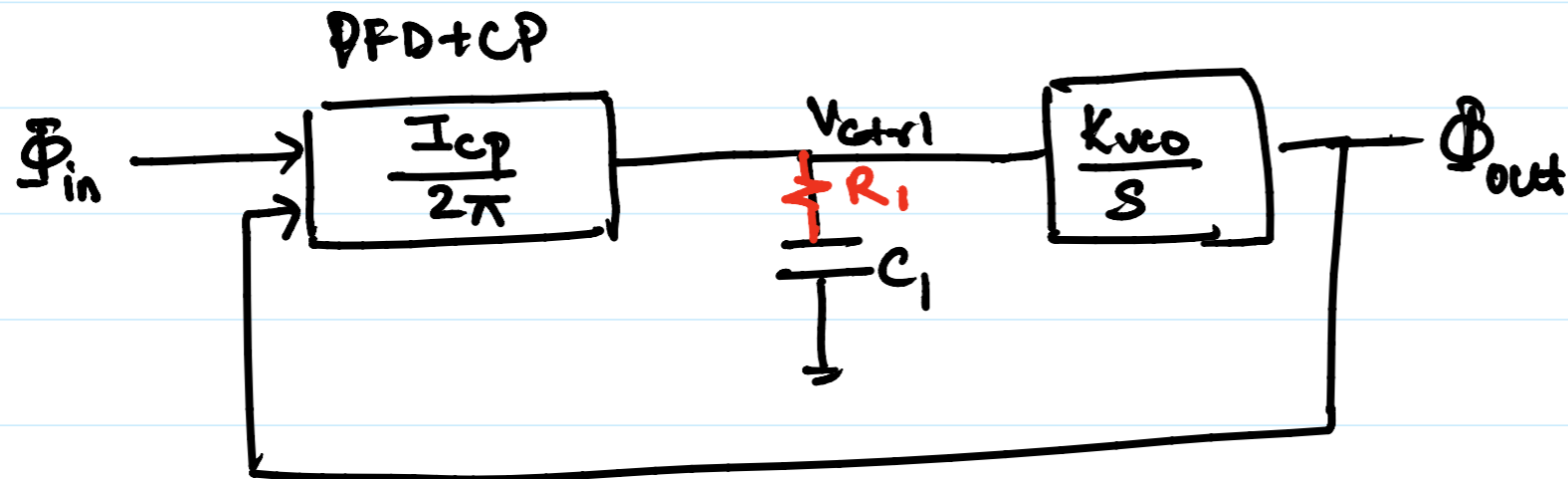


Charge-pump based PLL



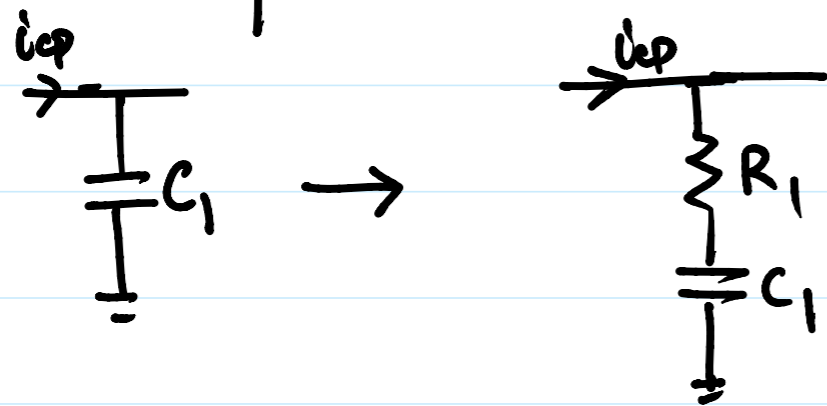
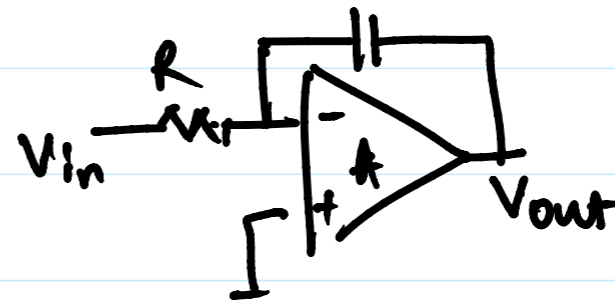
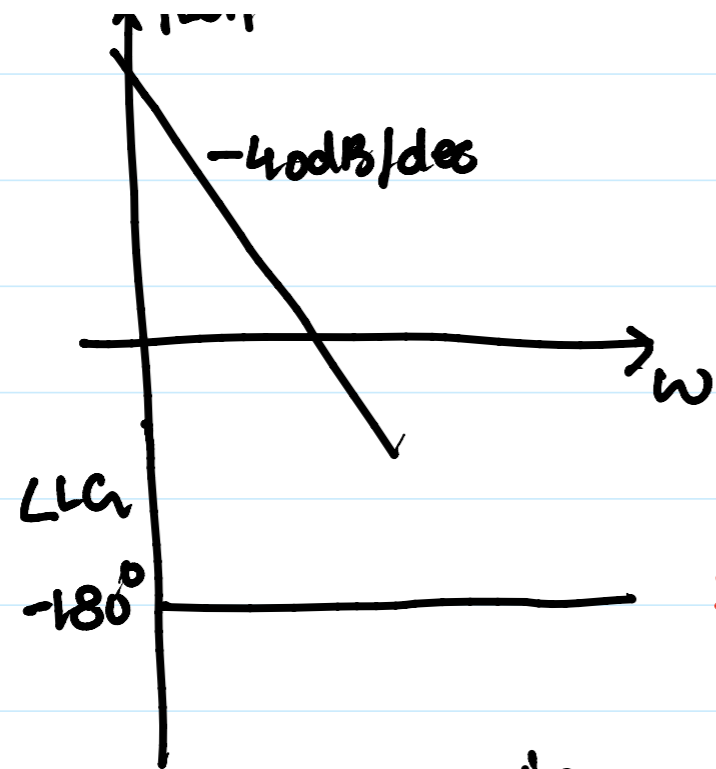
$$[\text{rad}] \times \frac{\text{A}}{\text{rad}} \times \Omega = \text{V}$$

$$[K_{VCO}] = \frac{\text{rad}}{\text{V}}$$



open loop gain, $LG(s) = \left. \frac{\Phi_{out}}{\Phi_{in}} \right|_{\text{open loop}} = \frac{I_{cp}}{2\pi} \frac{1}{sC_1} \frac{K_{VCO}}{s}$

↑ |LG|

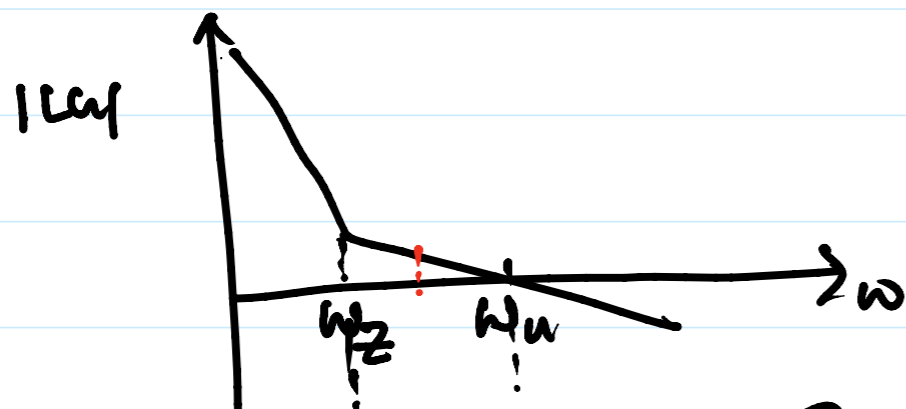


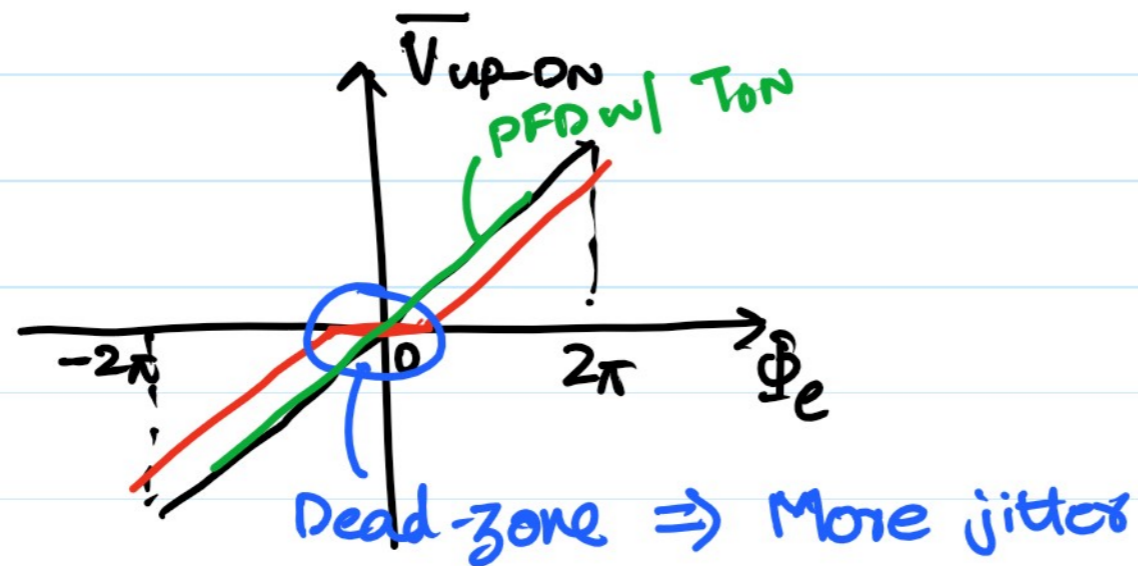
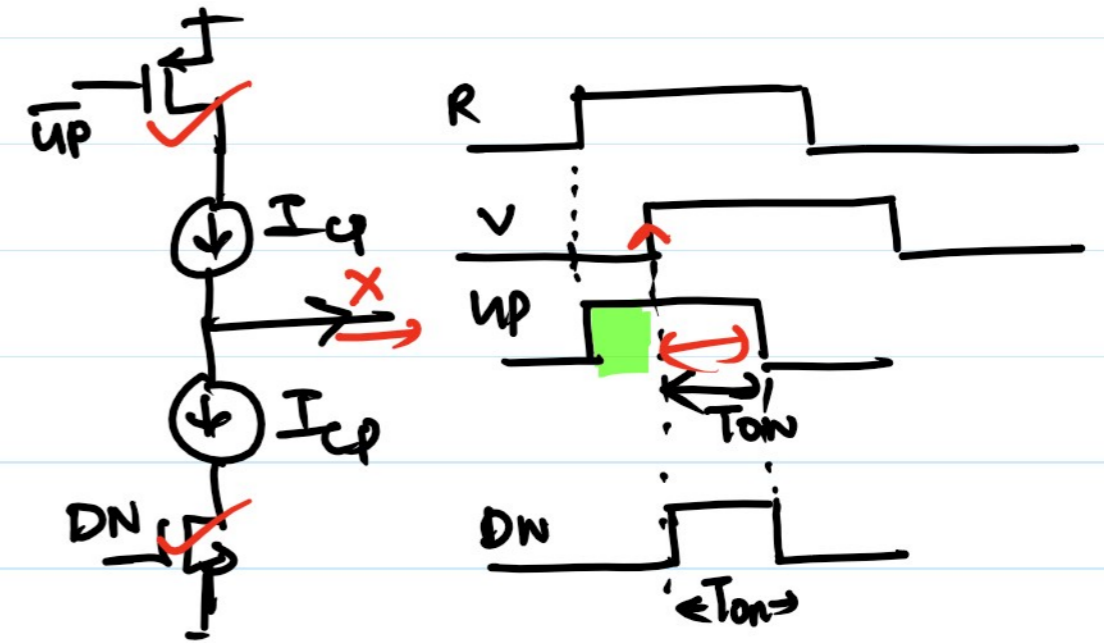
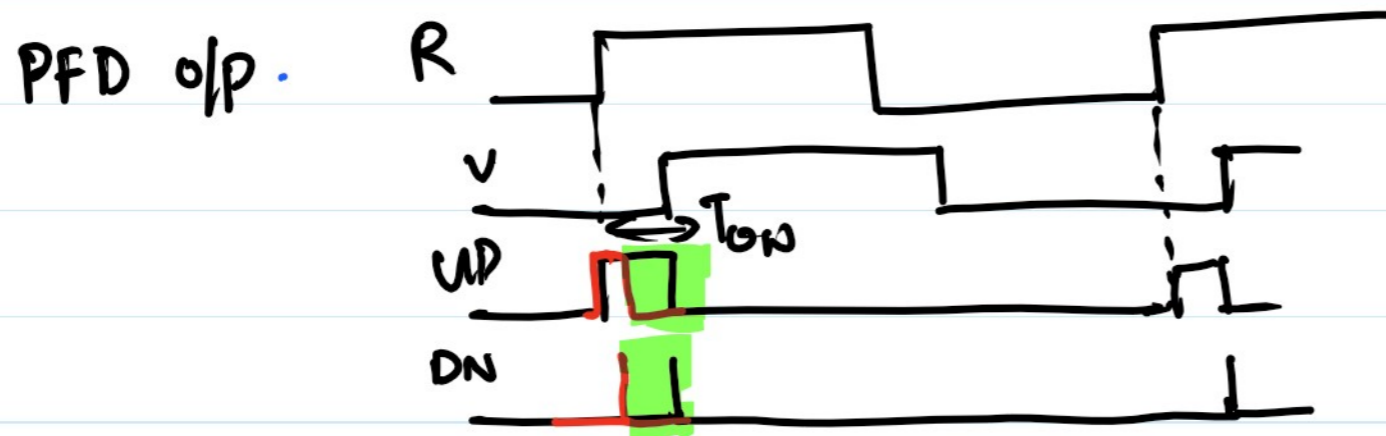
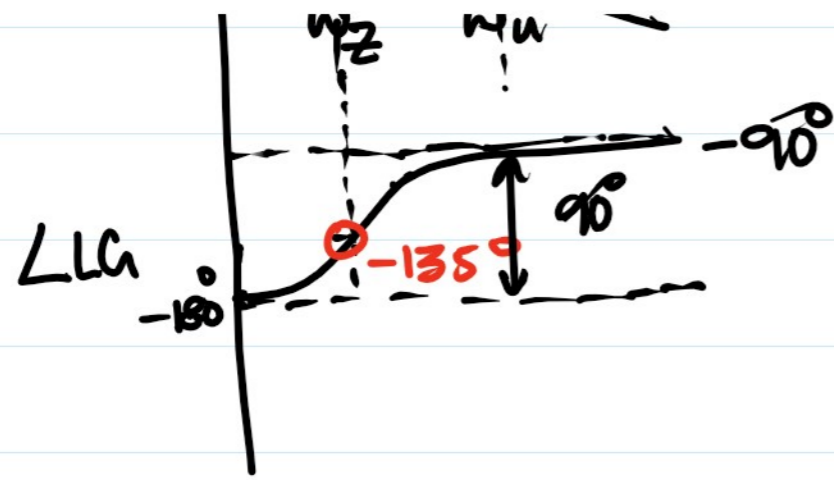
$$V_{ctrl}(s) = I_{cp} \left(R_1 + \frac{1}{sC_1} \right)$$

$$= I_{cp} \frac{(1 + sR_1C_1)}{sC_1}$$

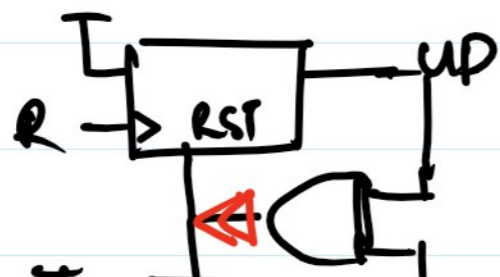
$$= \frac{I_{cp}}{sC_1} (1 + sR_1C_1)$$

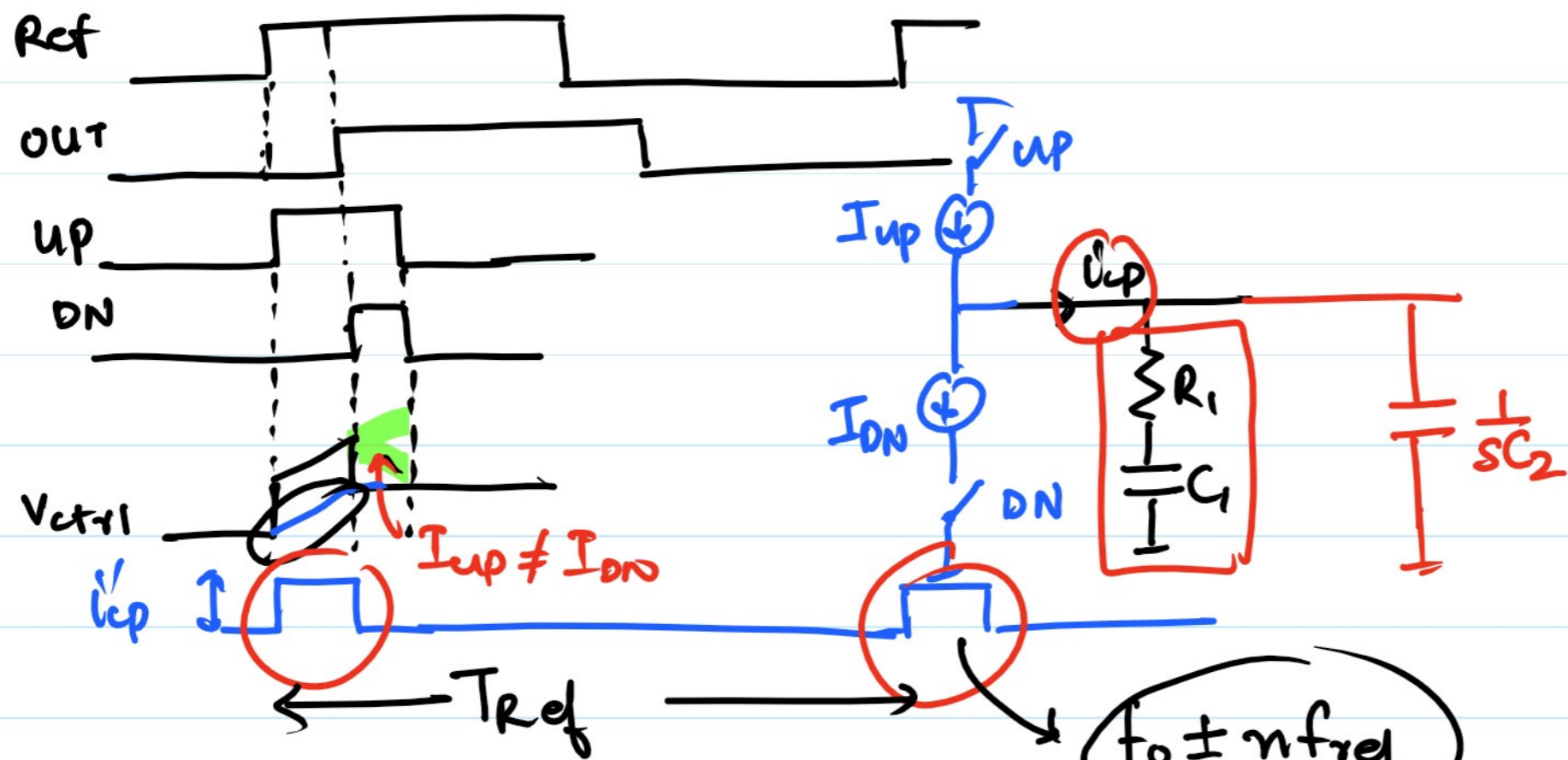
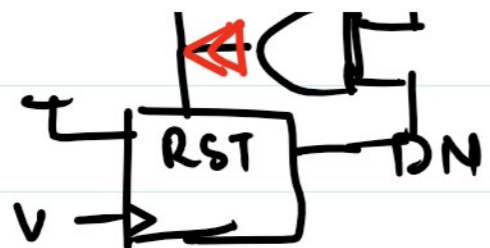
$$LC(s) = \frac{I_{cp}}{2\pi} \frac{1 + sR_1C_1}{sC_1} \frac{K_{vco}}{s} ; \omega_z = \frac{1}{R_1C_1}, \omega_{p1} = \omega_{p2} = 0$$





* Minimum T_{on} time for PMOS/NMOS switches to switch ON





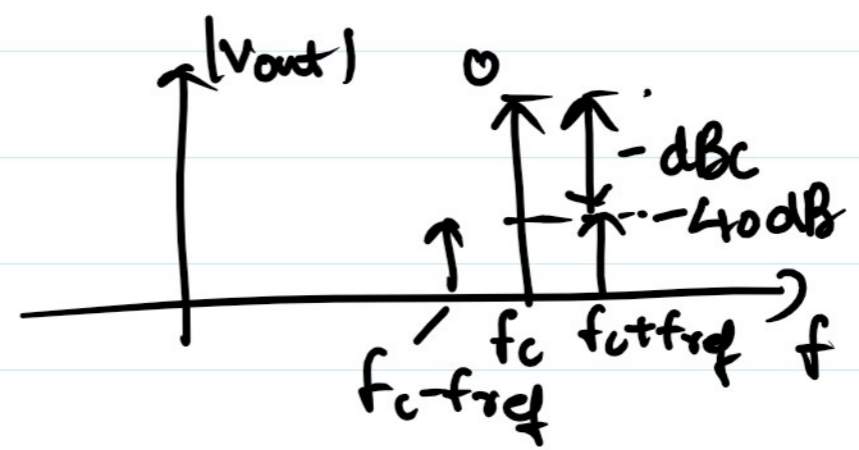
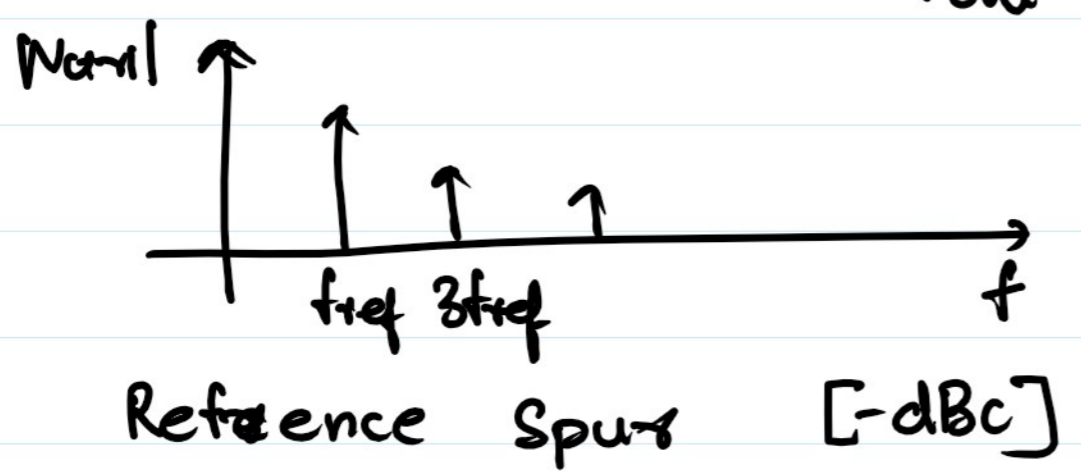
$$\left| \frac{1}{\omega_{ref} C_2} \right| \ll \left| R_1 + \frac{1}{j\omega_{ref} C_1} \right|$$

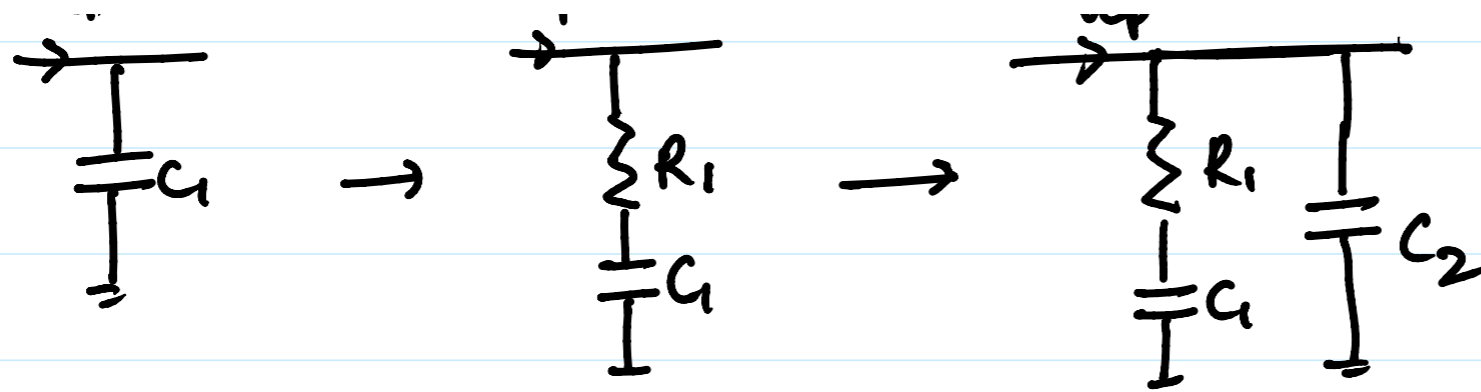
Ref. Spur Mag. ↓ ⇒ C₂ ↑
 Stability ⇒ C₂ ↓

$$f_0 \pm n f_{ref}$$

$$f_{out} = K_{VCO} \cdot V_{ctrl}$$

$$= K_{VCO} \cdot \left[\sum V_n \sin(n \omega_{ref} t) \right]$$





$$Z = \left(\frac{1 + sR_1C_1}{sC_1} \parallel \frac{1}{sC_2} \right)$$

$$= \frac{1 + sR_1C_1}{sC_2 + sC_1 + s^2R_1C_1C_2}$$

$$\omega_z = \frac{1}{R_1C_1}$$

$$\omega_{p1} = \omega_{p2} = 0$$

$$\omega_{p3} = \frac{1}{R_1 \frac{C_1C_2}{C_1 + C_2}}$$

$$Z = \frac{1}{s(C_1 + C_2)} \cdot \frac{1 + sR_1C_1}{1 + \frac{sR_1C_1C_2}{C_1 + C_2}}$$

$$= \frac{\left(s + \frac{1}{R_1C_1} \right)}{\left(s + \frac{C_1 + C_2}{R_1C_1C_2} \right)} \cdot \frac{1}{sC_2}$$