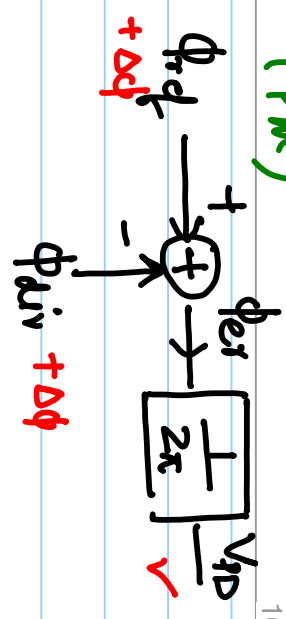
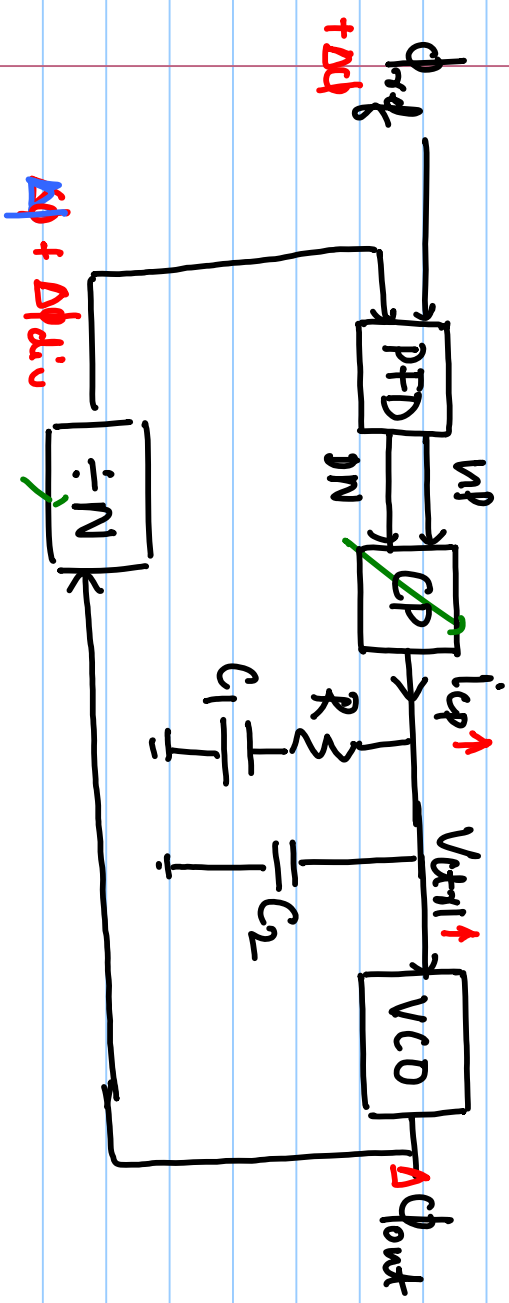


# lecture #20

- Frequency Modulation (FM)
- Phase Modulation (PM)



$$V_{PD} = \frac{1}{2\pi} \phi_{er} = \frac{1}{2\pi} (\phi_{rd} - \phi_{div})$$

$$\Rightarrow \text{For } +\phi_{er} = \Delta\phi$$

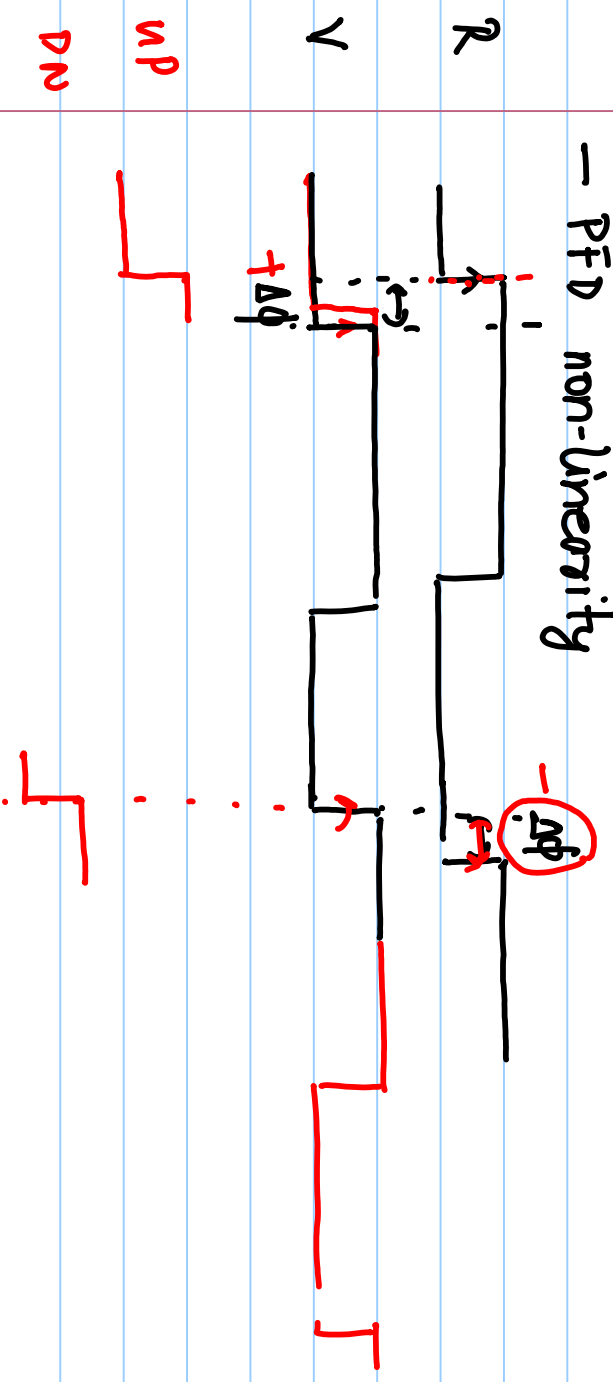
$$V_{PD} = \frac{1}{2\pi} \cdot \Delta\phi$$

$$\text{For } \phi_{er} = -\Delta\phi$$

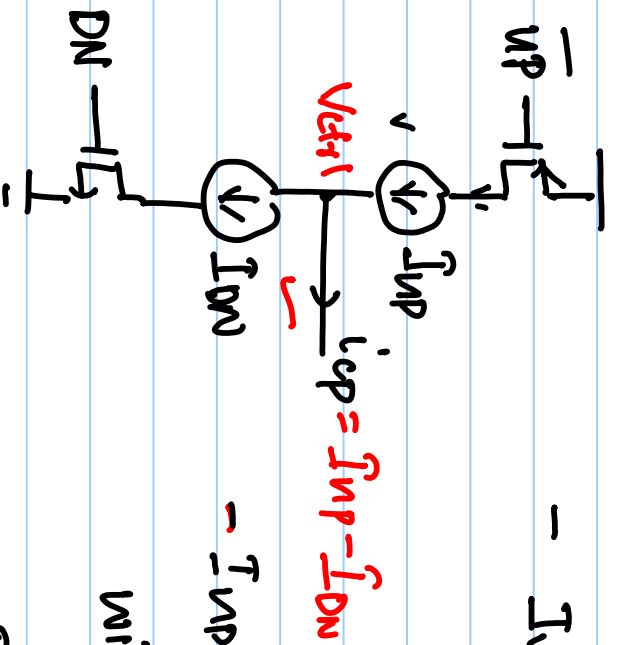
$$V_{PD} = -\frac{1}{2\pi} \Delta\phi$$

- Dead-zone of PFD

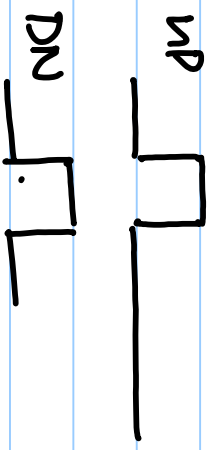
- PFD non-linearity



# Non-linearity in CP



-  $I_{MP} \neq I_{DN}$

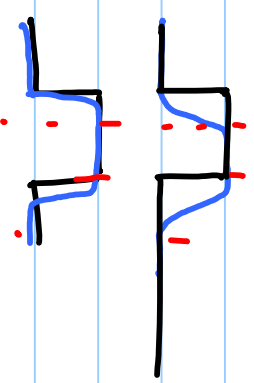


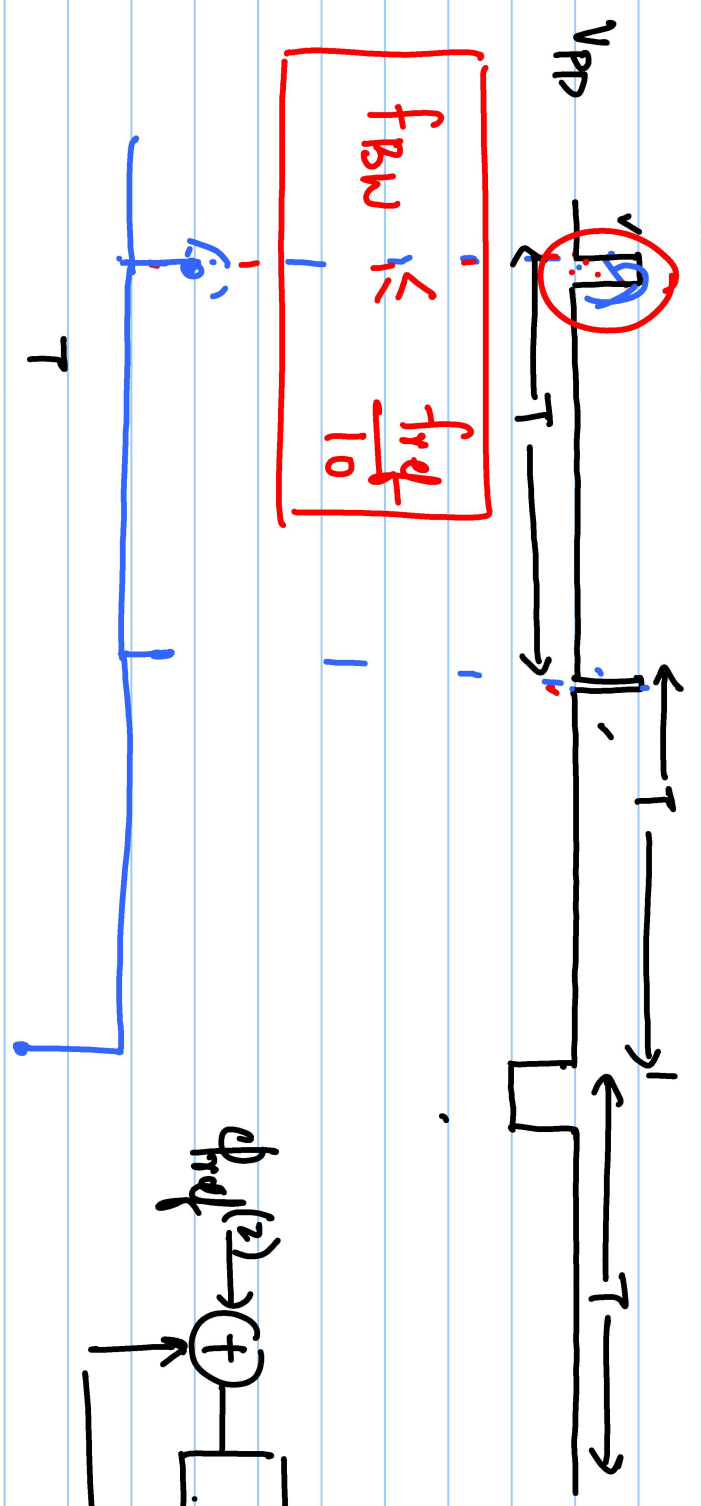
-  $I_{MP} = I_{DN}$

with  $V_{GS1} = 0.9V$

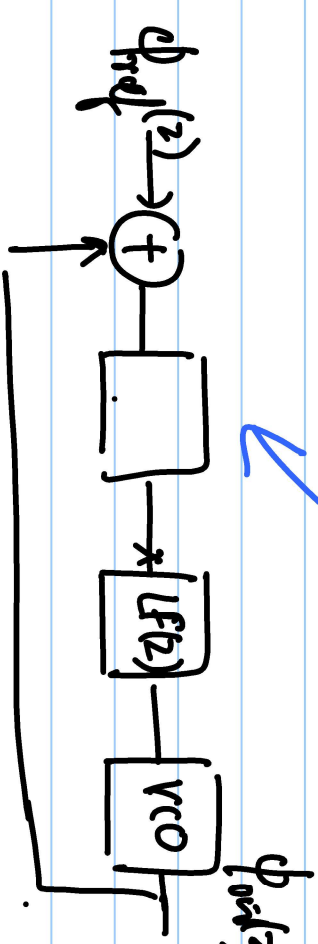
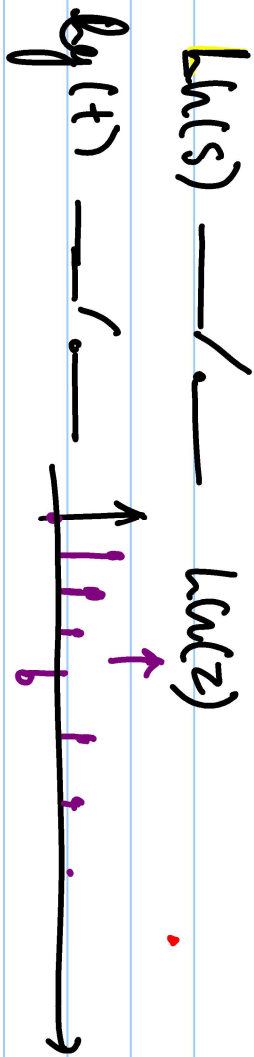
with  $V_{GS1} = 0.9V + \Delta V \Rightarrow I_{MP} \neq I_{DN}$

-  $I_{MP} = I_{DN}$



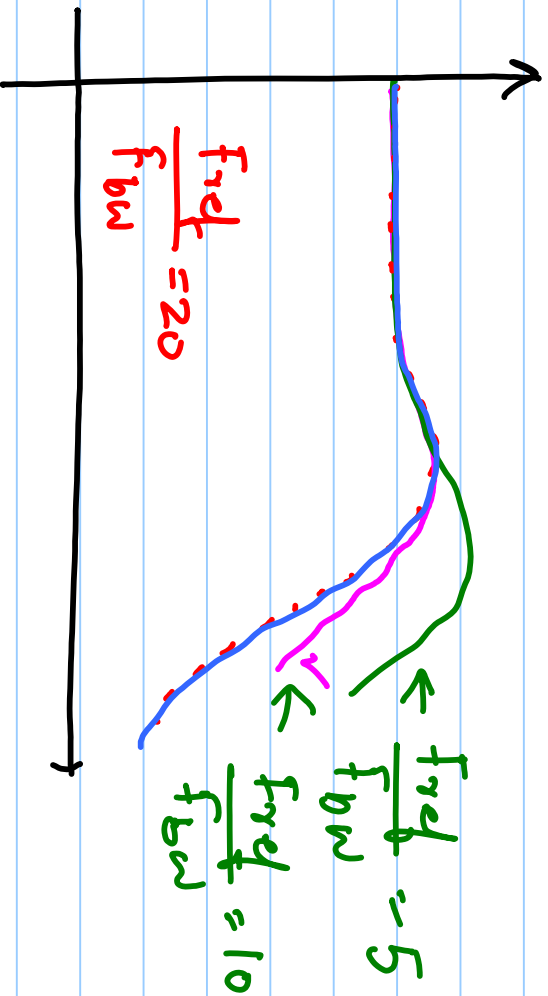


$$f_{BW} \leq \frac{f_{ref}}{10}$$



$$M(z) = K \frac{z^2 \left( \frac{C_1(1-a)}{C_1 + \tau_2} + \frac{2\kappa}{RC_1 \omega_i} \right) - z \left( \frac{C_1(1-a)}{C_1 + \tau_2} + \frac{2\kappa}{RC_1 \omega_i} a \right)}{z^3 - z^2(2+a) + z(1+2a) - a}$$

$$a = \exp(-\omega_p T) \quad \text{and} \quad k = \frac{K_{vco} \tau_p RC_1}{\omega_i \tau_c (\tau_2)}$$



$$\frac{\phi_{out}}{\phi_{req}} = \frac{K_{vc}}{(1+s/\omega_p)}$$

$$\boxed{\omega_p = \frac{\omega_{req}}{10}}$$

$$\Delta \phi_{req} = \Delta \phi_{(0)} u(t) \implies \Delta \phi_{out}(t) = K_{vc} \omega_p (1 - e^{-\omega_p t}) \Delta \phi_{(0)}$$

