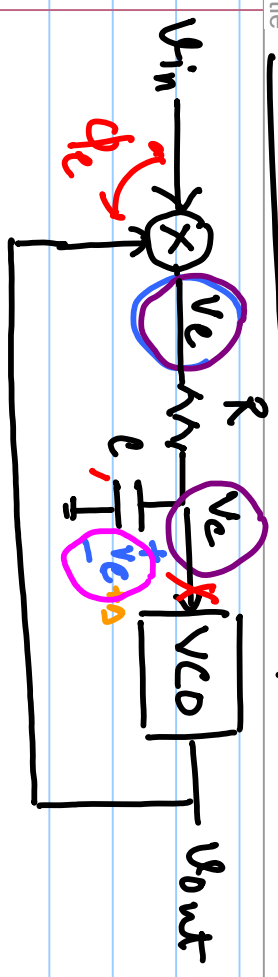


Lecture #7

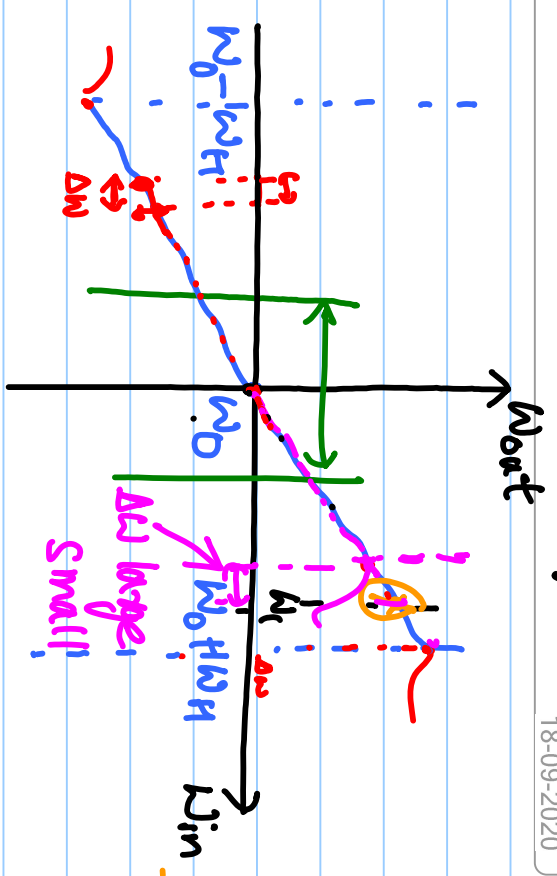
Type-I, Order-2

Hold-in (Tracking) Range



$$V_{in} = \sin(\omega_{int} - \phi_e)$$

$$V_{out} = \cos(\omega_{free} t + \int K_{VCO} \cdot V_e \cdot dt + \phi_{os})$$



$$V_e = \frac{1}{2} \left[\sin(\omega_{in} + \omega_{free} t) \int K_{VCO} V_e dt + \phi_{os} \right]$$

$$+ \sin(\Delta\omega(t) - \int K_{VCO} V_e dt - \phi_{os})$$

$$V_e = \frac{1}{2} \cdot \sin(\Delta\omega(t) - \int K_{VCO} V_e dt - \phi_{os})$$

$2\omega_H$: hold-in range.
 $\Delta\omega$ change is very small!
 $\Delta\omega$ large: PLL loses lock.

$$\dot{\phi}_e(t) = \Delta\omega(0) - K_{VCO} \int V_e \cdot dt - \phi_{os}$$

$$\frac{s\omega_0 - \omega_{free}}{K_{VCO}} = V_e = \frac{1}{2} \sin(\phi_e)$$

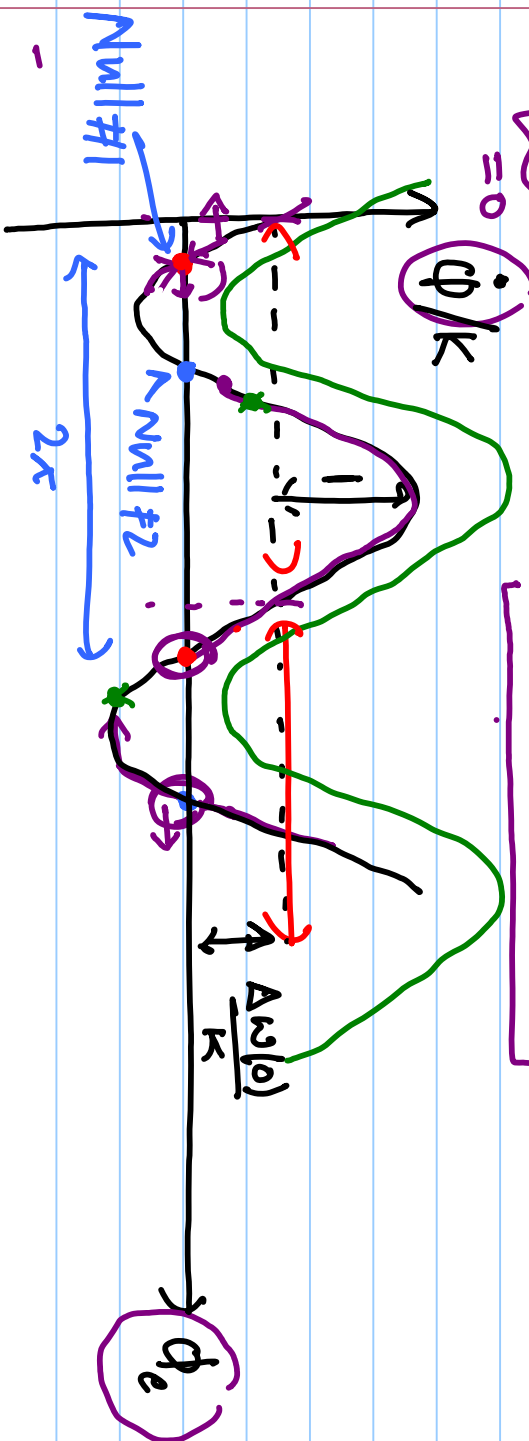
$$\dot{\phi}_e(t) = \Delta\omega(0) - K_{VCO} V_e = \Delta\omega(0) - K_{VCO} \cdot K_{PD} \sin(\phi_e)$$



$$T = \frac{2\pi}{\Delta\omega(0)}$$

∞ \underline{V}

$$\frac{d\phi}{dt} = \frac{\dot{\phi}}{k} = \frac{\Delta\omega(0)}{k} - \sin(\phi_e) \quad \checkmark$$



$$\Delta\phi_e \text{ +ve}$$

$$\frac{d\phi_e}{dt} = -ve$$

$$\frac{\Delta\omega(0)}{k} < 1 \Rightarrow$$

$$\boxed{\Delta\omega(0) < k}$$

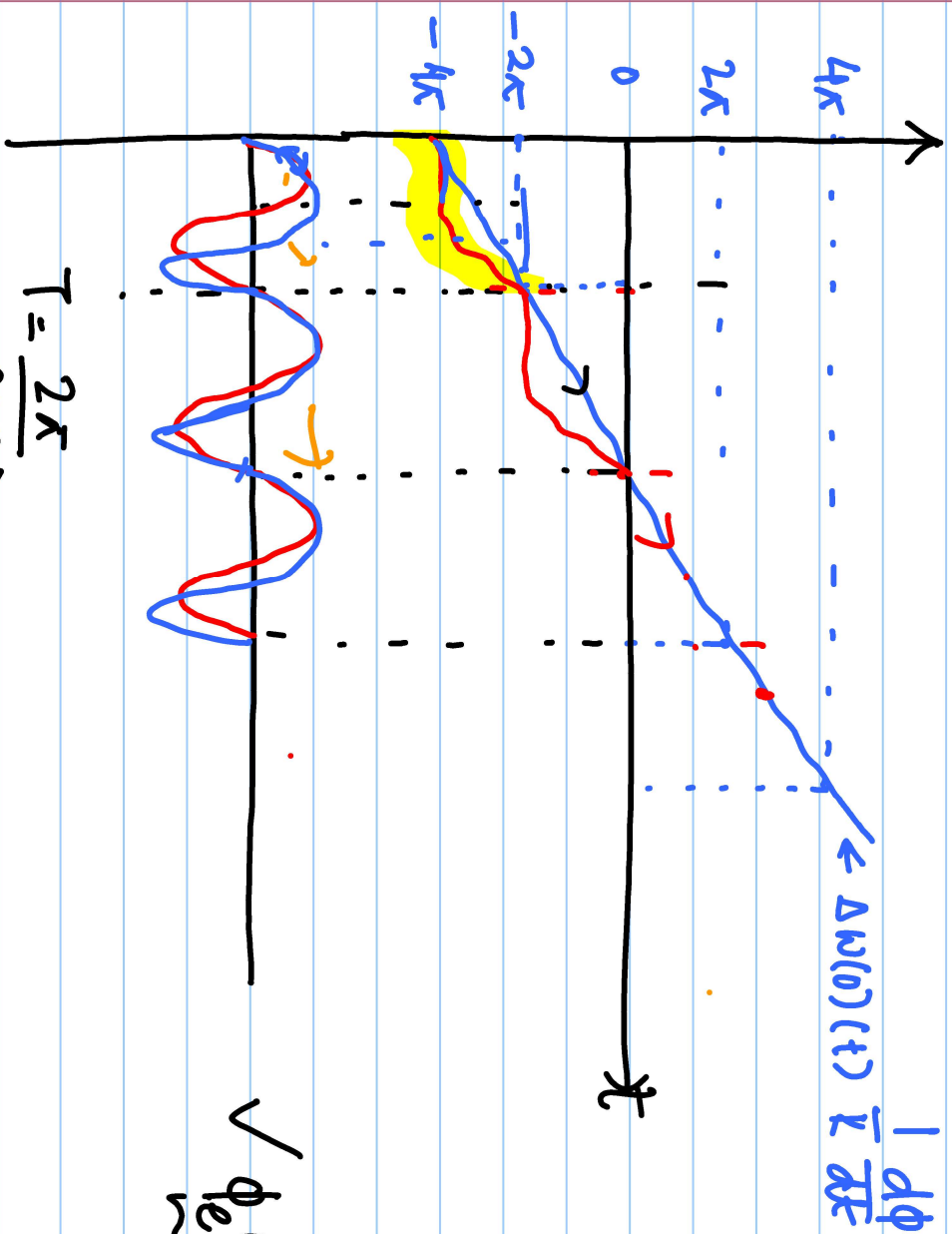
lock-in range

$$\Delta\omega(0) > k$$

Pull-in range $\Delta\omega_p$: w/ cycle slipping and w/o cycle slipping

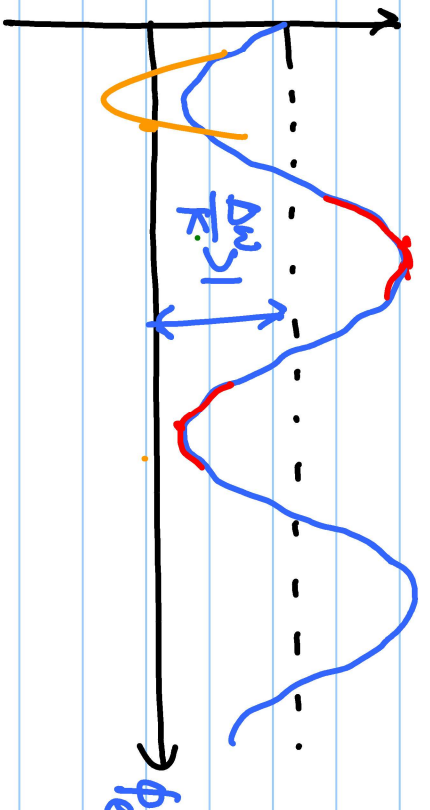
w/ ϕ_e exceeding 2π and w/o ϕ_e exceeding 2π

$$\phi_e = \Delta\omega(0) \cdot t - \int K\nu_{c0} v_e \cdot dt$$



↑

$$v_e = \frac{1}{2} \sin(\phi_e)$$



$$\Delta\omega(0) < K$$

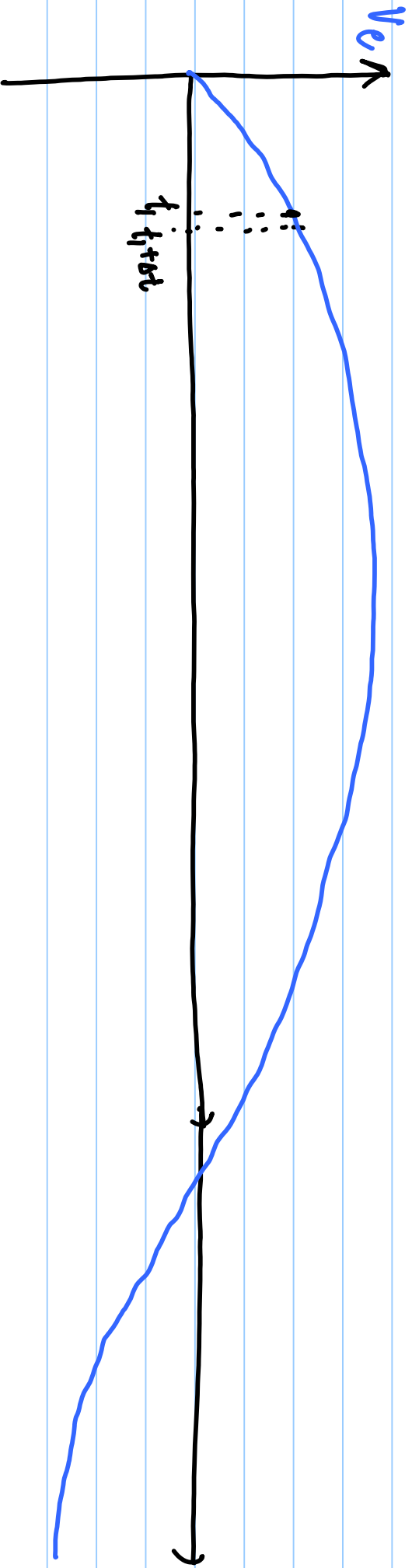
$$v_e = v_e = \frac{1}{2} \sin(\phi_e)$$

$$\checkmark \phi_e(t) = \Delta\omega(0)t - \frac{K\nu_{c0}}{2} \int \sin(\phi_e(t)) dt$$

$$\approx \Delta\omega(0)t - \frac{K\nu_{c0}}{2} \int \sin(\Delta\omega(t)) dt$$

$$\phi_e(t) = \Delta\omega(0) \cdot t + \frac{K_{VCO}}{2} \underbrace{\left(\underbrace{\cos(\Delta\omega \cdot t)}_{\Delta\omega'} \right)}$$

ϕ



$$\phi_e(t) = \Delta\omega(0) \cdot t - \frac{K_{VCO}}{2} \int \sin(\phi_e(t)) dt$$

at $t=0$: $\phi_e = 0$

at $t=0+\Delta t$: $\phi_e = \Delta\omega(0) \cdot \Delta t - \frac{K_{VCO}}{2} \int \sin(\phi_e) dt$

at $t=0+2\Delta t$: $\phi_e = \Delta\omega(0) \cdot 2\Delta t - \frac{K_{VCO}}{2} \int \sin(\phi_e) dt$