

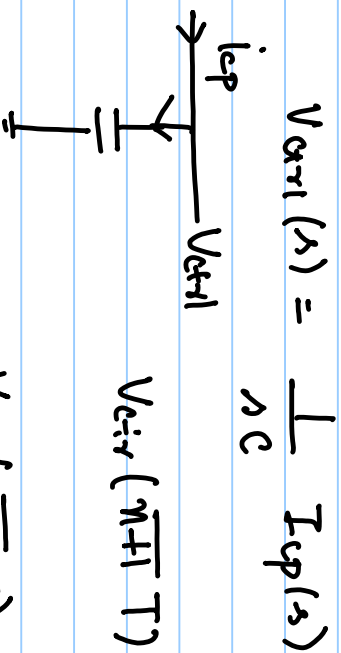
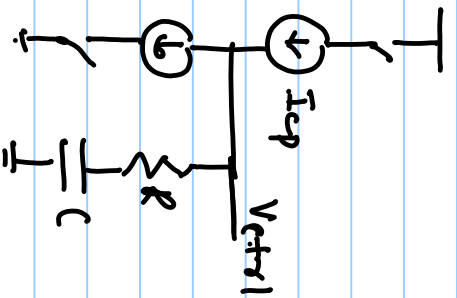
# Lecture #42

## Digital PLLs

Large size of cap.

$$\frac{V_{err}}{I_{cp}} = R + \frac{1}{sC}$$

— Split-tuned PLL  
 — Capacitor multiplication process variation.



$$V_{err}(s) = \frac{1}{sC} I_{cp}(s)$$

$$V_{err}(n+1T) \approx V_{err}(nT) + \int_0^{\Delta t} I_{cp} \cdot dt \quad \checkmark$$

$$V_{err}(n+1T) = V_{err}(nT) + \frac{I_{cp}}{C} \cdot \Delta t(n)$$

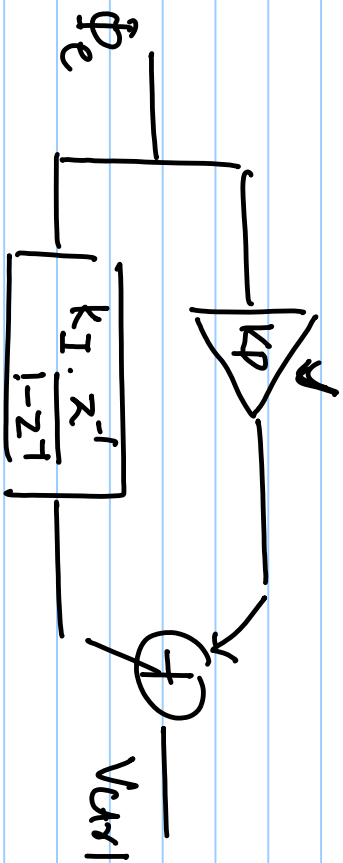
$$+ \frac{I_{cp}}{C} \sum_{i=0}^{n-1} \frac{\Delta t(i)}{T} \cdot \frac{T}{2\pi}$$

$$\checkmark V_{err}(n+1T) = V_{err}(nT) + \frac{I_{cp}}{C} \cdot \frac{T}{2\pi} \Phi_e(nT) \quad \checkmark$$

$$z^{-2} V_{err}(z) = V_{err}(z) + \frac{1 \cdot 0126}{c \cdot 2\pi} \Phi_e(z)$$

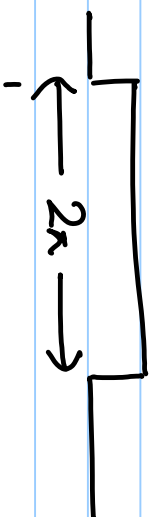
$$\frac{V_{err}(z)}{\Phi_e(z)} = \frac{1 \cdot 0126}{c \cdot 2\pi} \cdot \frac{1}{z-1}$$

$$= \frac{k_I \cdot z^{-1}}{1-z^{-1}}$$



$\Phi_e$ : # of bits 4 bits

$$\frac{V_{err}(z)}{\Phi_e} = K_p + \frac{k_I \cdot z^{-1}}{1-z^{-1}}$$



$\Phi_e = 0$  rad/s  $\rightarrow$  0000

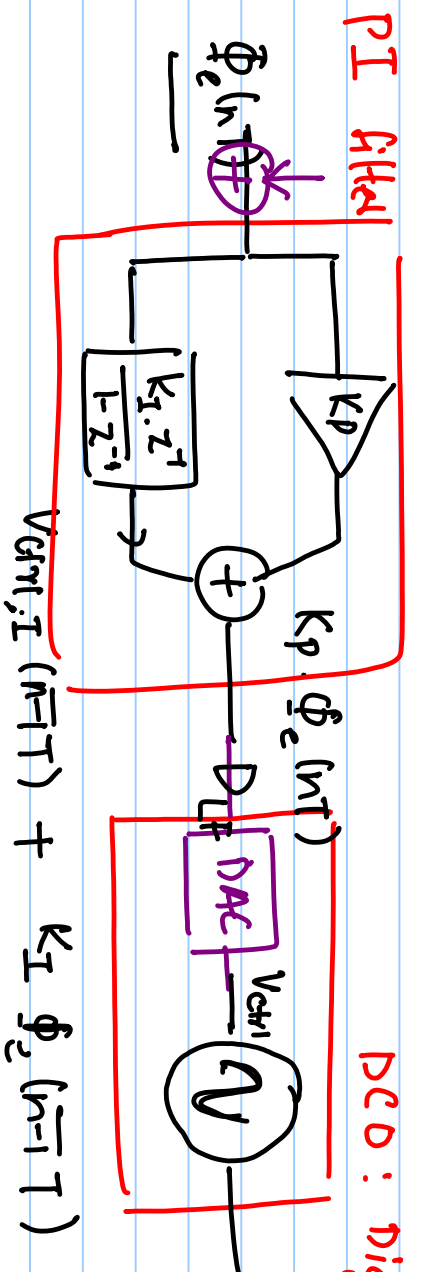
$-2\pi$  rad/s  $\rightarrow$  1111V

$K_p$ : 2 bits 00, 01, 10, 11

1111 x 10 = 1110

$K_I$ :

$$V_{err1}(nT) = \dots \quad 1. \quad K_p \cdot \Phi_e(nT) + K_I$$



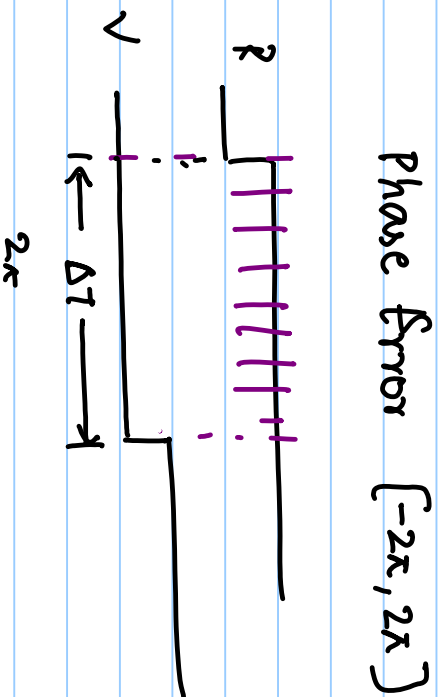
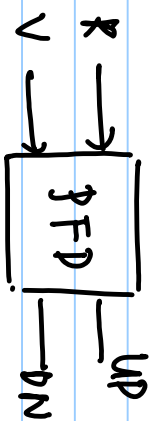
$$\frac{V_{err1}}{\Phi_e} = K_p + \frac{K_I \cdot z^{-1}}{1 - z^{-1}} = K_p + \frac{K_I}{z - 1} = K_p + \frac{K_I}{e^{sT} - 1} = K_p + \frac{K_I \cdot f_{rd}}{s}$$

$$= \frac{1}{s} [s K_p + K_I \cdot f_{rd}]$$

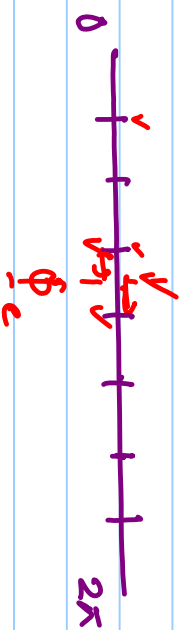
$$= \frac{K_I \cdot f_{rd}}{s} \left[ 1 + \frac{s K_p}{K_I \cdot f_{rd}} \right] \quad \omega_z = \frac{K_I \cdot f_{rd}}{K_p}$$

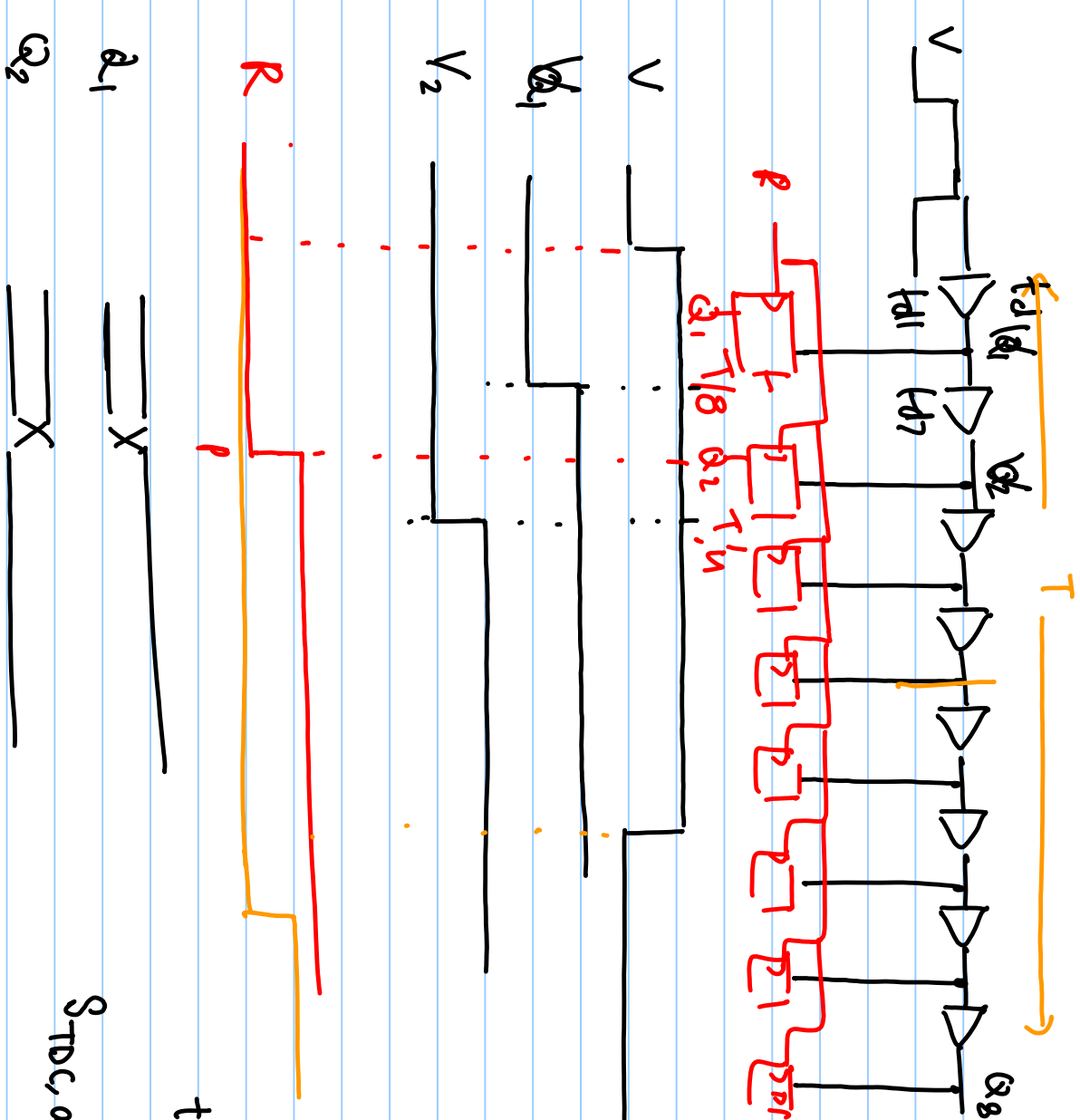
$\Phi_e \rightarrow$  fast

$$L_u = \left[ K_p + \frac{K \cdot z^{-1}}{1-z^{-1}} \right] \frac{2\pi K_{pdc0}}{s} \times \frac{1}{N}$$



Digital  
 $4'b_{xxxx}$   $\rightarrow$   $-2\pi \leftarrow 0 \rightarrow 2\pi$   
 1111      0000      0111





$$t_d = \frac{T}{8}$$

$Q_1 - Q_8$  | 3 bit

TDC: Time-to-Digital Conv

Quantization Error

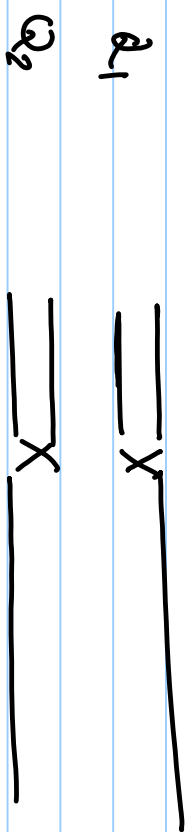
$$-\frac{t_d}{2} < \Delta < \frac{t_d}{2}$$

$t_d \downarrow \rightarrow$  # of delay cells.

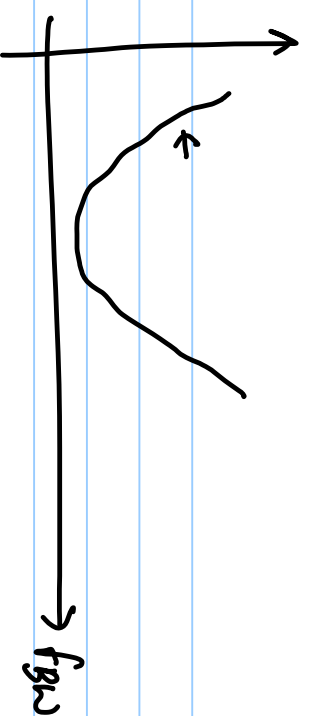
$t_d \uparrow \rightarrow$  large quantization.

$$t_d \rightarrow 2\pi \cdot \frac{t_d}{T}$$

$$S_{TDC, \sigma} = \frac{(2\pi \cdot t_d / T)^2}{12 \cdot f_{clk}} = \frac{(2\pi t_d)^2}{12 \cdot T}$$



TDC Quantization Noise  $\rightarrow$   $\downarrow$  BW  
 VCO Noise  $\rightarrow$   $\uparrow$  BW



Analog

Digital

$$V_{ctrl} = i_{cp} \cdot R + \dots$$

