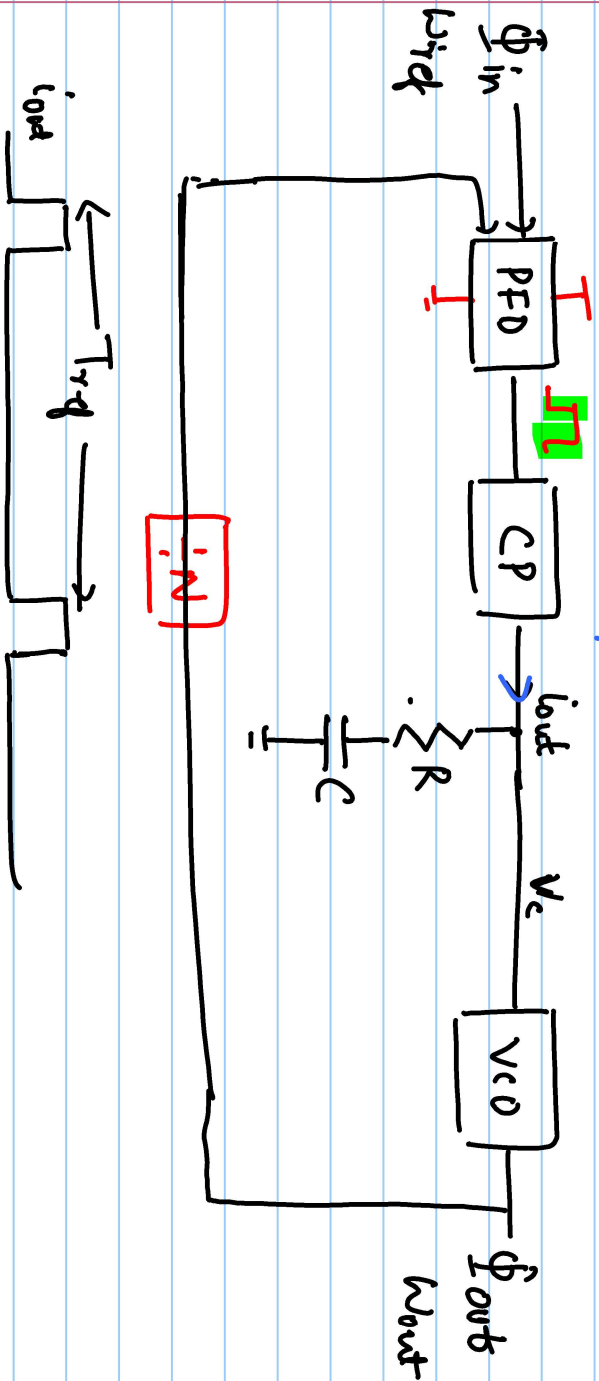
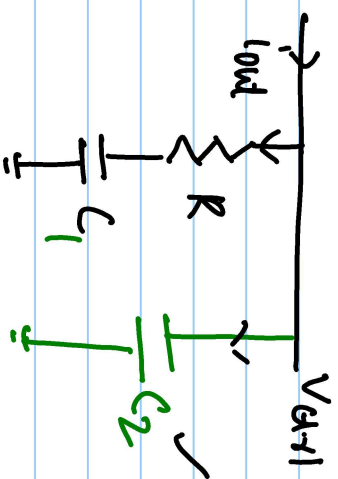


# Lecture # 15

$\Phi_{in}$



$\omega_{out} = N \omega_{vd}$   
 ( $\omega_{out} \pm \omega_{freq}$ )



$$Z_1 = \frac{1}{sC_2}$$

$$|Z_1| \parallel \omega = \omega_{vd} = \frac{1}{(\omega_{vd} C_2)}$$

$$Z_2 = R + \frac{1}{sC_1} \quad ; \quad |Z_2| = \left[ R + \frac{1}{j\omega C_1} \right] = \sqrt{R^2 + \frac{1}{\omega^2 C_1^2}}$$

$$\frac{V_c |_{C_2}}{V_c |_R} = \frac{i_{out} / \omega_{np} C_2}{i_{out} \cdot R} \ll 1 \Rightarrow \frac{1}{\omega_{np} C_2 R} \ll 1$$

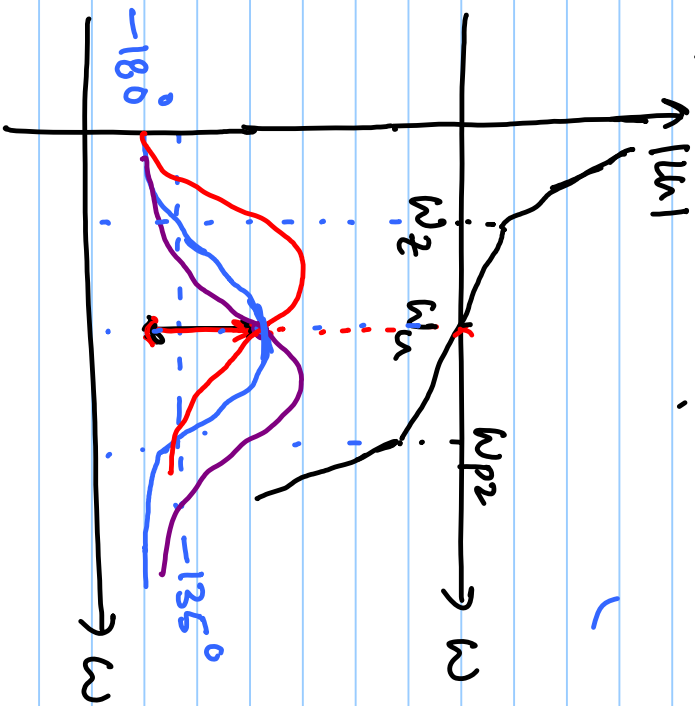
$$\begin{aligned} LF(s) &= \left( R + \frac{1}{sC_1} \right) \parallel \frac{1}{sC_2} = \frac{1 + sC_1 R}{sC_1} \times \frac{1}{sC_2} = \frac{1 + sC_1 R}{sC_1} \times \frac{1}{sC_2} = \frac{1 + sC_1 R}{s(C_2 + s^2 C_1 C_2 R + sC_1)} \end{aligned}$$

$$= \frac{1 + sC_1 R}{s(C_1 + C_2) \left[ 1 + \frac{sC_1 C_2}{C_1 + C_2} R \right]}$$

$$\omega_z = \frac{1}{C_1 R}, \quad \omega_{p1} = 0, \quad \omega_{p2} = \frac{1}{\frac{C_1 C_2}{C_1 + C_2} R}$$

$$L_G(s) = \frac{1}{2R} I_{cp} LF(s) \times \frac{2R K_{vco}}{s} \times \frac{1}{N} = \frac{I_{cp}}{s^2 (C_1 + C_2)} \frac{K_{vco}}{N} \frac{(1 + s/\omega_z)}{(1 + s/\omega_{p2})}$$

# Type-II, Order-3

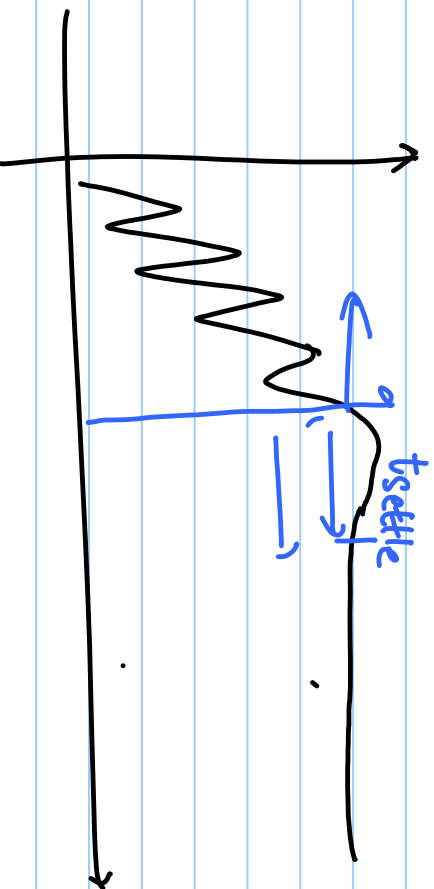


$$\angle G_u = -180^\circ + \tan^{-1} \left( \frac{\omega_n}{\omega_z} \right) - \tan^{-1} \left( \frac{\omega_n}{\omega_{p2}} \right)$$

$$|G_u(\omega_n)| \approx \frac{I_{cp}}{\omega_n^2 (1 + \zeta^2)} \frac{K_{uc0}}{N} \frac{\omega_n / \omega_z}{\omega_n / \omega_{p2}} = 1$$

$$\phi_m = -180^\circ - \angle G_u$$

$$= \tan^{-1} \left( \frac{\omega_n}{\omega_{p2}} \right) - \tan^{-1} \left( \frac{\omega_n}{\omega_z} \right)$$



$v_{L_{BW}}$  (kHz): Settling time, noise

(MHz)



$\Phi_m$

$K_{VCO}$

