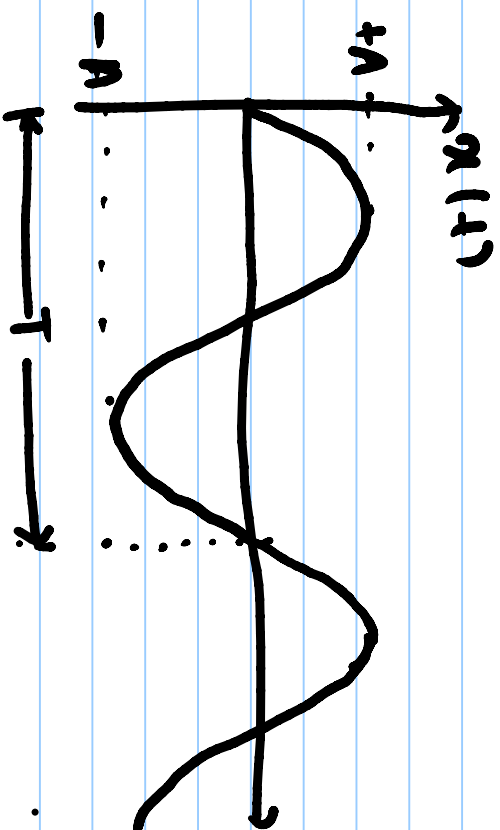


## Lecture # 2

### Phase-locked loops.



Amplitude =  $A$

Time period =  $T$

Frequency,  $f = \frac{1}{T}$

$$\omega = \frac{2\pi}{T}$$

$$x(t) = A \sin(\omega t)$$

$$= A \sin(\underbrace{2\pi f t}_\phi)$$

$$\text{Phase} = 2\pi f t = \int 2\pi f dt$$

# Ref. clock source

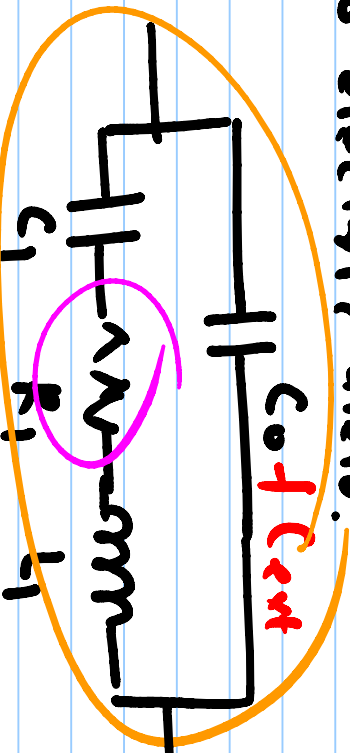
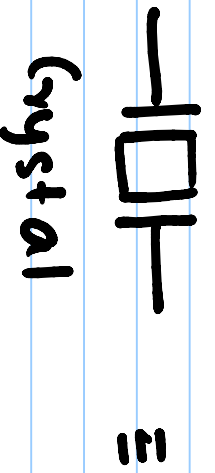
ppm = parts per million

$f = 100 \text{ MHz}$ ,  $T = 10 \text{ ns}$

Crystal device — Periodic outputs  $100 \text{ ppm} \rightarrow 100 \times 10^{-6} \times 100 \text{ MHz}$

Anti-piezo electric field.

\* Accuracy of clock < 100 ppm



\*  $f_{ow} < 100 \text{ MHz}$

$$Z(s) = \left( s^2 + s \left( \frac{R_1}{L_1} \right) + \omega_s^2 \right)$$

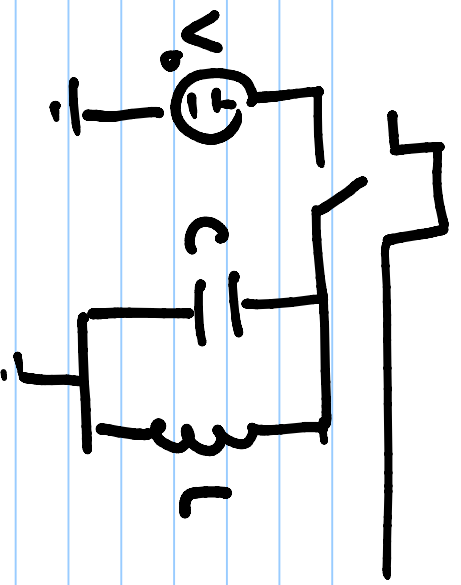
\* PVT: Very less susceptible.

$$\frac{1}{sC_0 \left( s^2 + s \left( \frac{R_1}{L_1} \right) + \omega_p^2 \right)}$$

\* Tunable range is very less

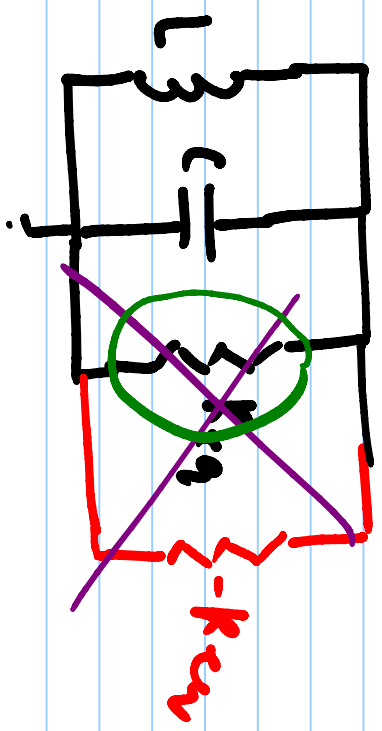
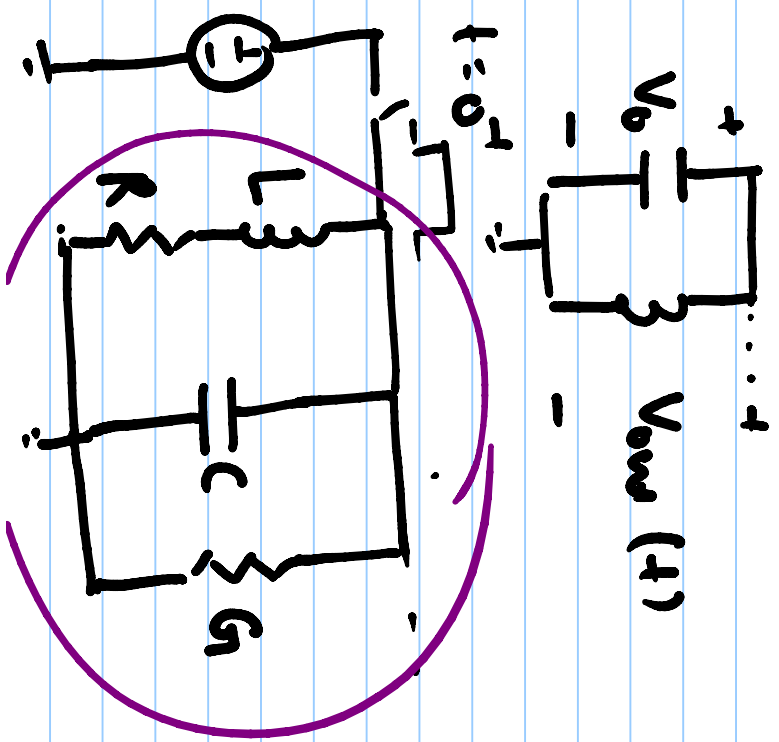
$$\omega_s = \frac{1}{\sqrt{L_1 C_1}}$$

$$\omega_p = \frac{1}{\sqrt{L_1 C_1 C_0}} \approx \omega_s \left( 1 + \frac{C_0}{2C_1} \right)$$



$$\omega_0 = \frac{1}{\sqrt{LC}} \text{ rad/s}$$

$$V_{out} = A \sin(\omega_0 t)$$



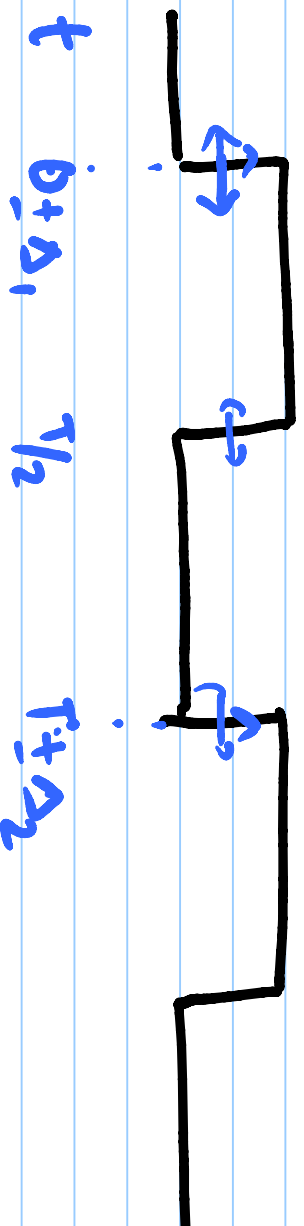
\* Wide tunable range

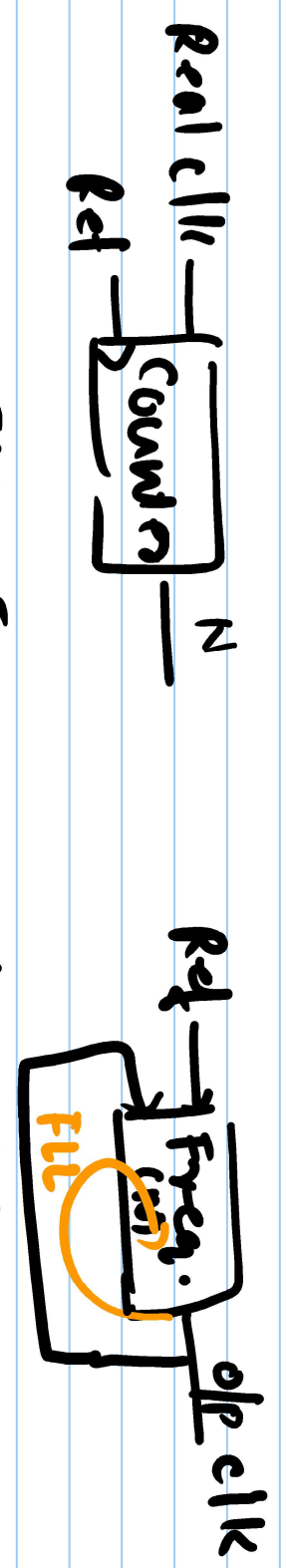
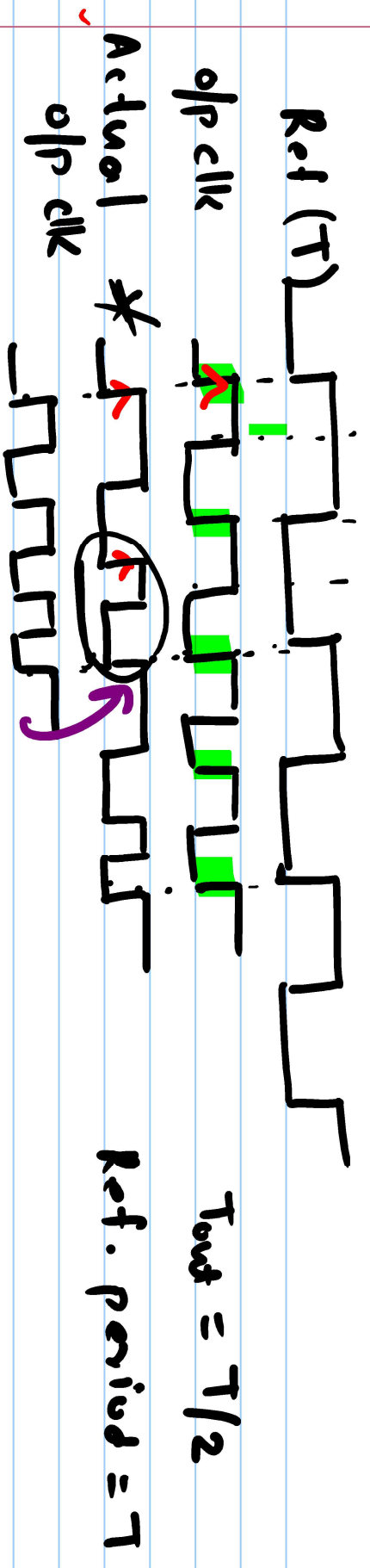
\* No limit on frequency

\* More susceptible to PVT variations

✓ 1. Ref. clock source: highly accurate but limited freq.

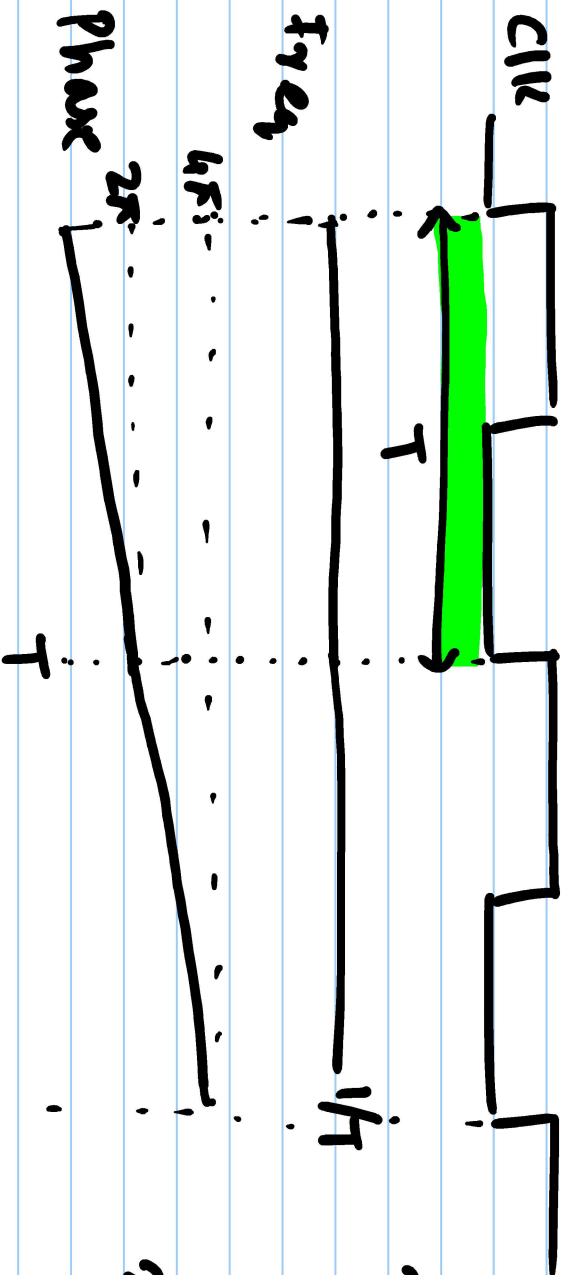
✓ 2. LC resonator: less accurate but no limit on freq.





FLL: Frequency locked loop.



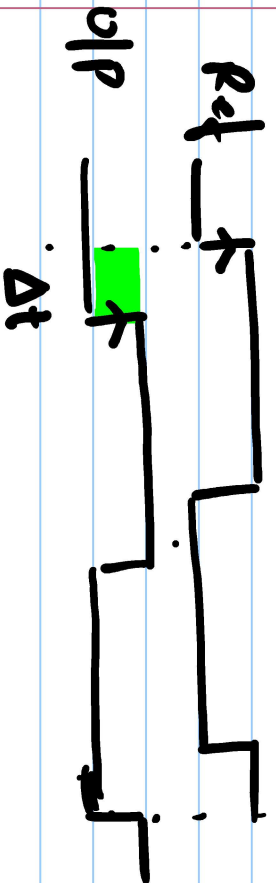


$$x(t) = \sum c_n \exp(j\omega_n t)$$

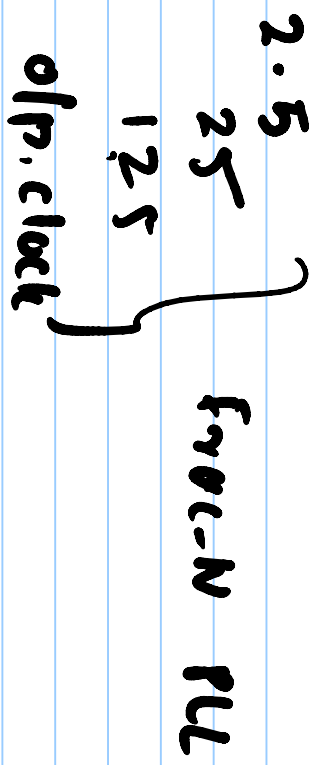
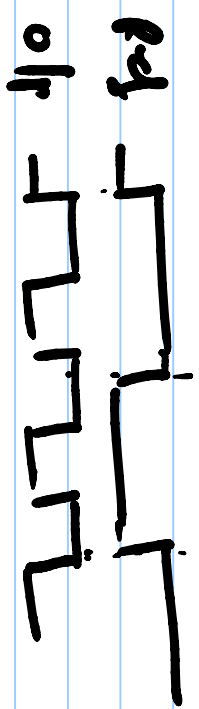
$$\omega_0 = \frac{2\pi}{T}$$

$$x_1(t) = A \sin\left(\frac{2\pi}{T} t\right)$$

$$\phi = \frac{2\pi}{T} t$$



$$\frac{\Delta\phi}{2\pi} = \frac{\Delta t}{T} \Rightarrow \Delta\phi = \frac{2\pi \Delta t}{T}$$



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