

EE6322

Jitter generation in CDR

13/2/2018

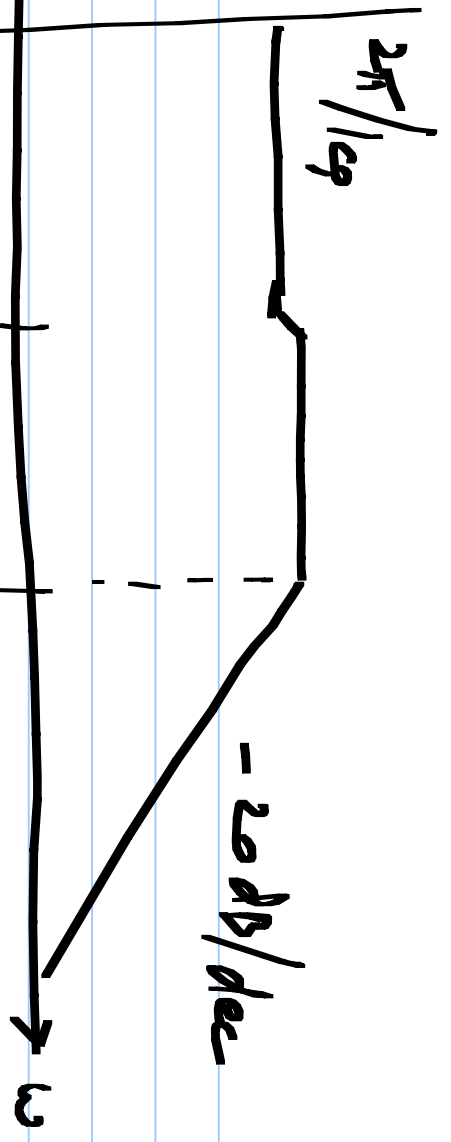
$$\phi_{out} = \frac{1}{1 + sCR}$$

$$\frac{\dot{\phi}_{in,CP}}{s} = \frac{1}{g_p/2\pi} \cdot \frac{1}{1 + sCR + s^2C/g_pK_{VCO}}$$

$$\frac{\phi_{out}}{V_{n,R}} = \frac{2\pi}{g_p R} \cdot \frac{sCR}{1 + sCR + s^2C/g_p K_{VCO}}$$

$$\frac{\phi_{out}}{\phi_{n,RES}} = \frac{s^2C/g_p K_{VCO}}{1 + sCR + s^2C/g_p K_{VCO}}$$

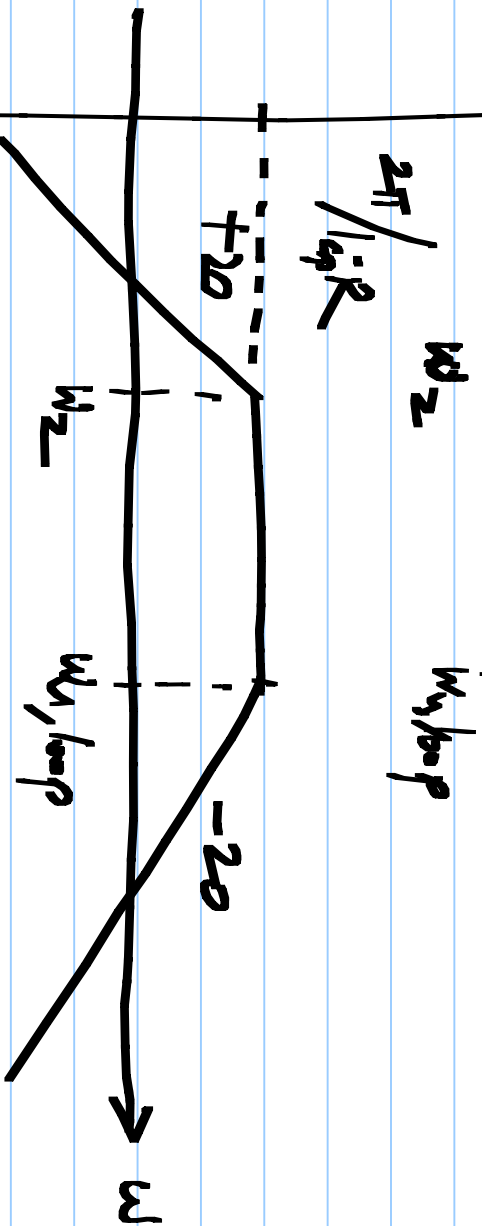
$$\left| \frac{\phi_{out}}{i_{in,q}} \right|$$



$$\omega_z = 1/R C$$

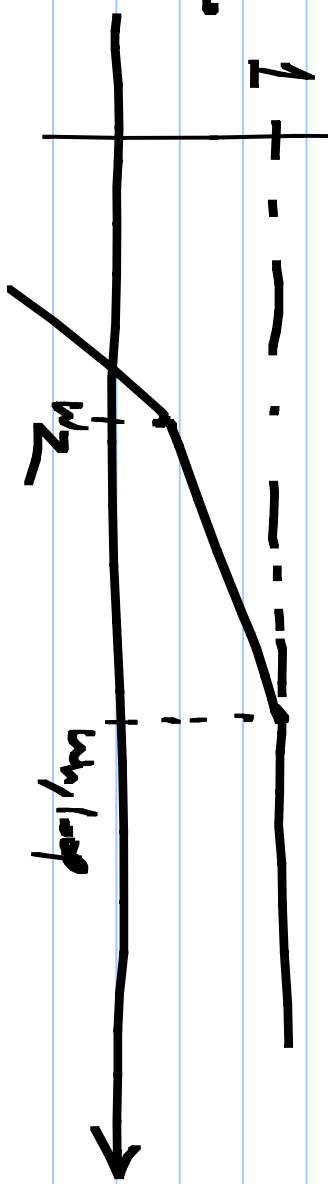
$$S_{i,q} \cdot \left| \frac{\phi_{out}}{i_{in,q}} \right|^2$$

$$\frac{\phi_{out}}{v_{in,R}}$$

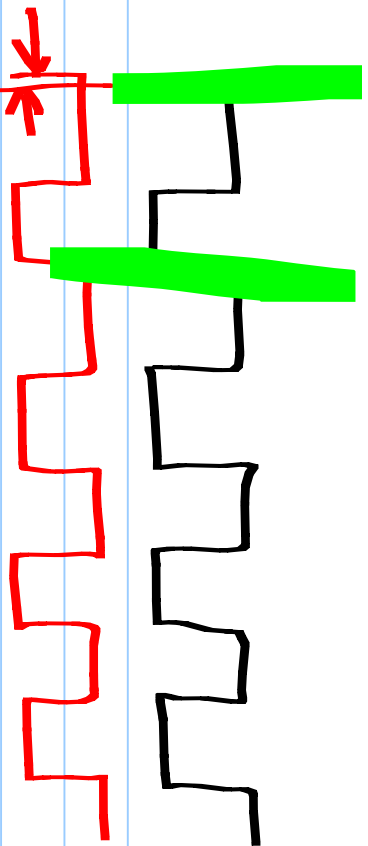


$$4kTR \left| \frac{\phi_{out}}{v_{in,R}} \right|^2$$

$$\frac{\phi_{out}}{\phi_{in}}$$

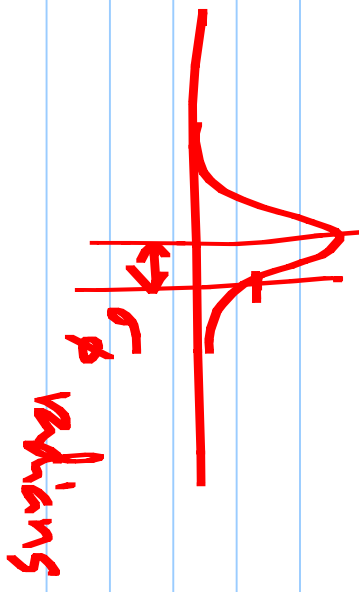


$$S_{p,v} \left| \frac{\phi_{out}}{\phi_{in}} \right|^2$$



absolute jitter

rms jitter:



Standard deviation of phase
of clock edges, compared to
an ideal periodic clock

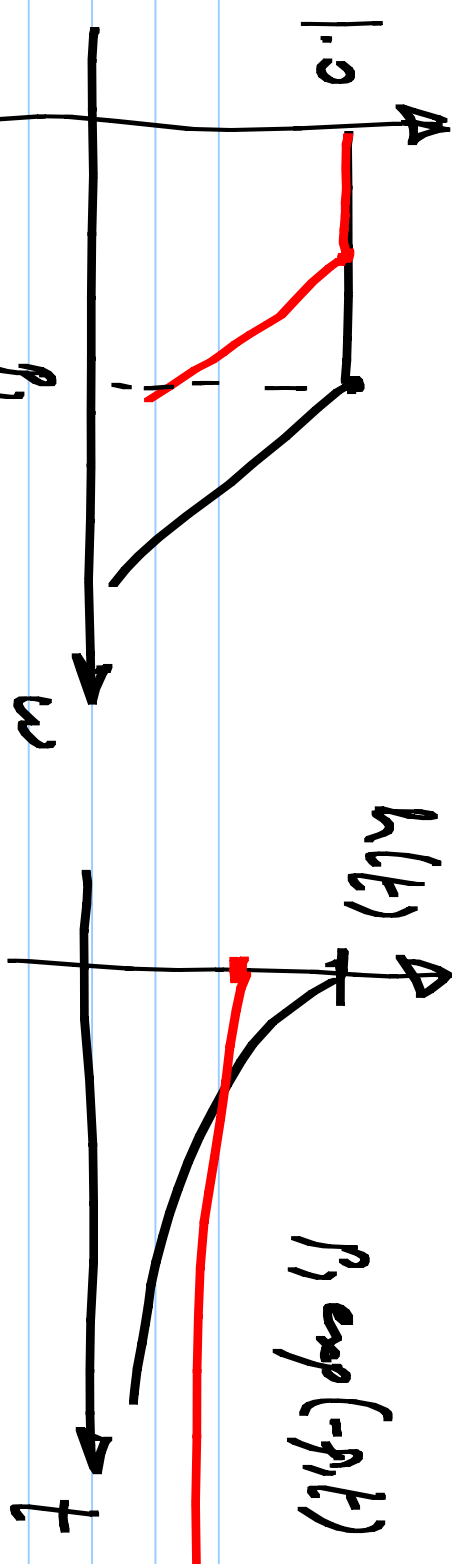
$$\phi \rightarrow \frac{\phi}{2\pi} \cdot T_s$$

$$\sigma_\phi \rightarrow \frac{\sigma_\phi}{2\pi} \cdot T_s$$

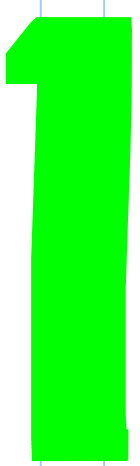
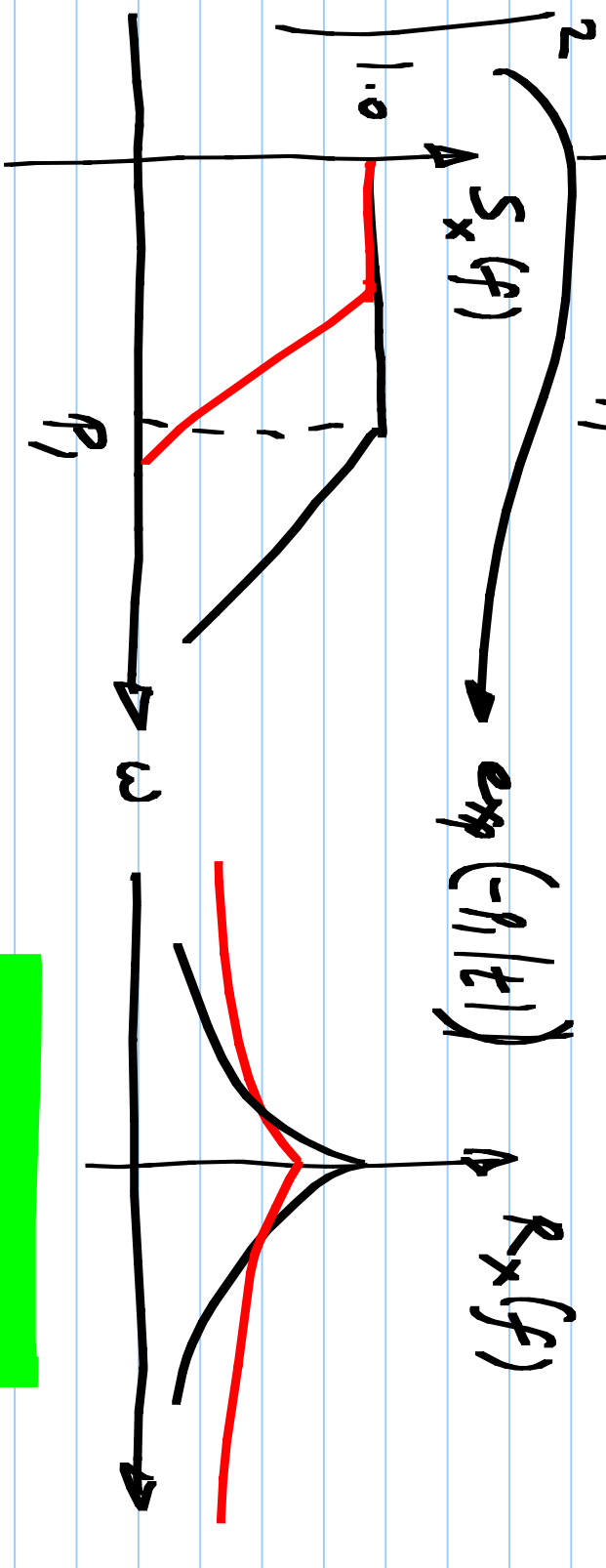
UI $\left[\frac{\sigma_\phi}{2\pi} \right]$

$$H(s) = \frac{1}{1 + s/\rho_1}$$

$$\frac{1}{1 + s/\rho_1}$$

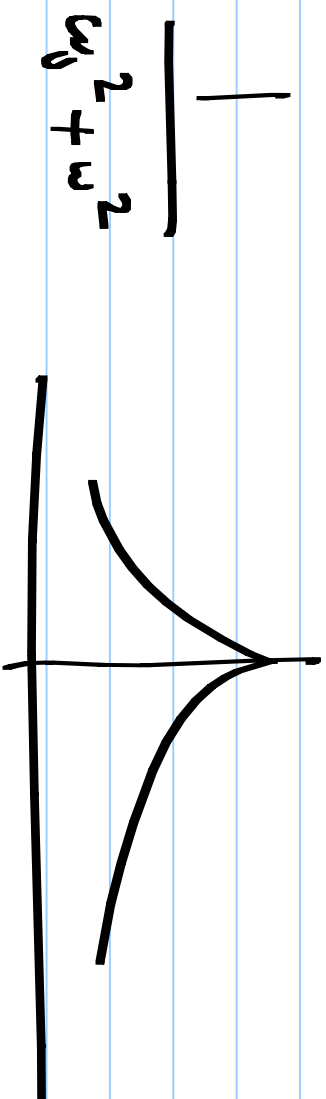


$$\frac{1}{1 + \gamma \omega / \rho_1}$$



$$\cos(\omega_0 t) : \quad \frac{s}{s^2 + \omega_0^2} \quad s = j\omega \quad \frac{j\omega}{\omega_0^2 - \omega^2} + \dots$$

$$\sin(\omega_0 t) : \quad \frac{\omega_0}{s^2 + \omega_0^2} \quad \frac{\omega_0}{\omega_0^2 - \omega^2}$$



$$R_x(\tau) = E[x(t) x(t + \tau)]$$

$T = 1\text{ms}$

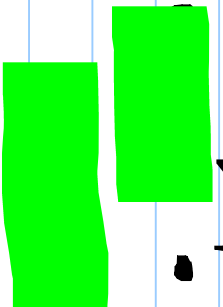
$x(t)$: zero mean

$$E[x(t)] \cdot E[x(t + \tau)]$$

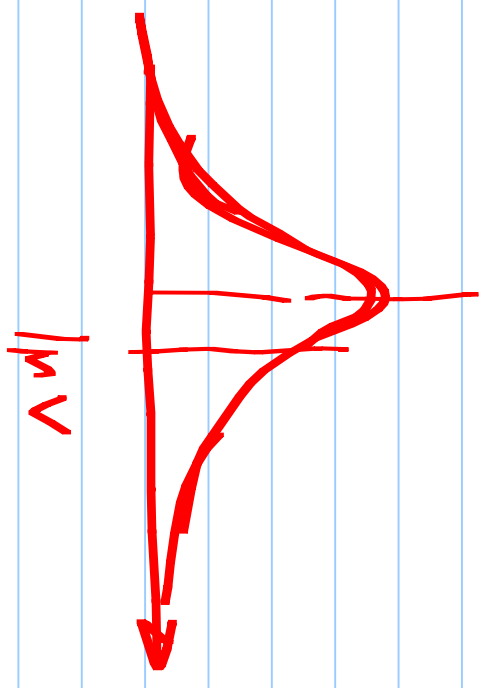
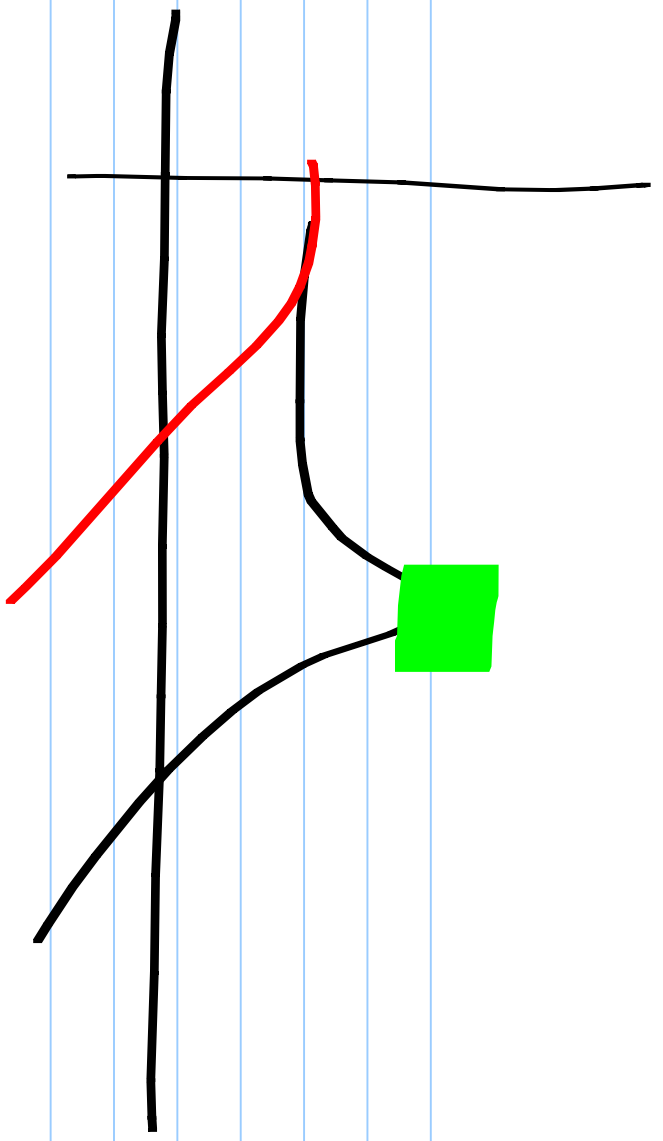
coin toss: $x[n]$

$$y[n] = x[n] + x[n-1] + x[n-2]$$

1 2 3 4 . . . 7 8 9 . . .



$\phi_{out} - \phi_{in}$



$$\int_{-\infty}^{\infty} \text{Spectral density: } df = \text{Variance}$$

$$S_x(f) \xleftrightarrow{f} R_x(\tau)$$

$$S_x(f) = \int_{-\infty}^{\infty} R_x(\tau) \exp(-j2\pi f\tau) d\tau$$

$$R_x(\tau) = \int_{-\infty}^{\infty} S_x(f) \exp(j2\pi f\tau) df$$

$$R_x(0) = \sigma_x^2 = \int_{-\infty}^{\infty} S_x(f) \cdot df$$

one-sided S.D

$$\int_0^{\infty} \sqrt{S_x(f)} df$$

one-sided