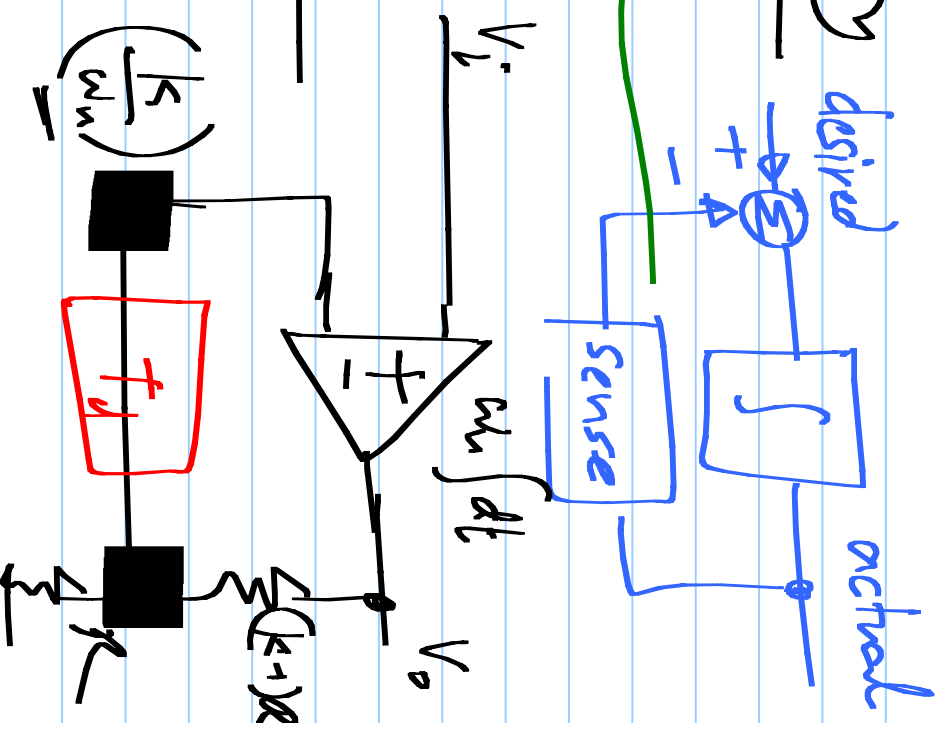
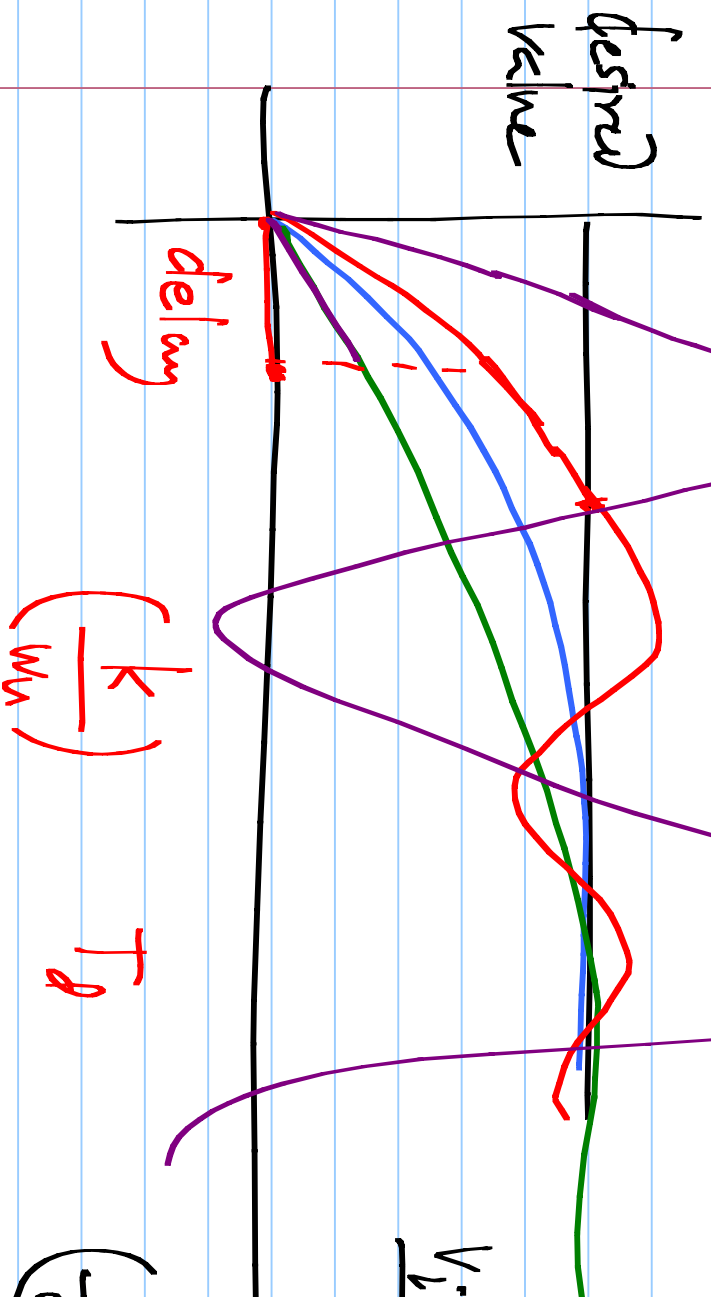


Lecture 37

4/4/2016

$$\frac{w_u}{s}$$

Negative feedback and stability



Excess delay can cause instability.

Causes instability if $T_d \gg \frac{1}{\omega_{u,loop}}$

for stability,

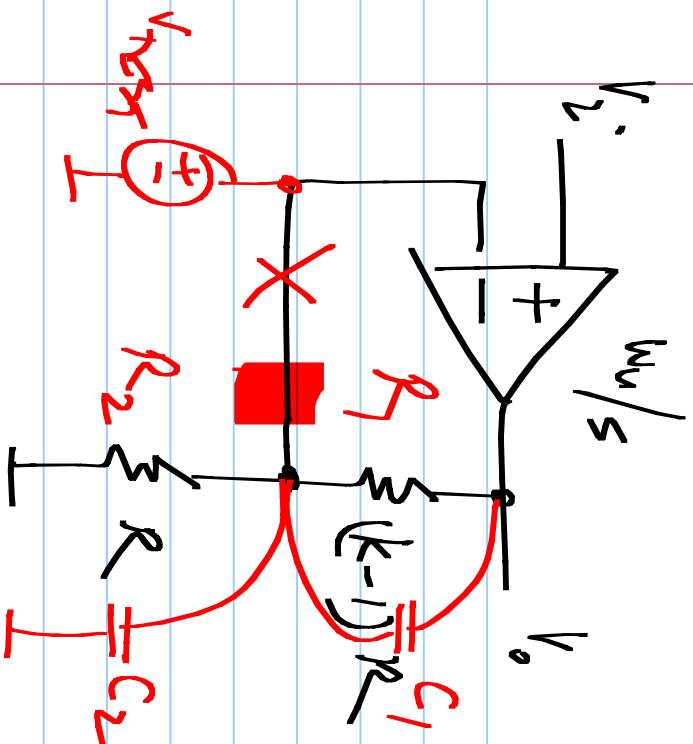
$$T_d < \frac{1}{\omega_{u,loop}}$$

Better
circuit
design,
improved
technology

reduce T_d

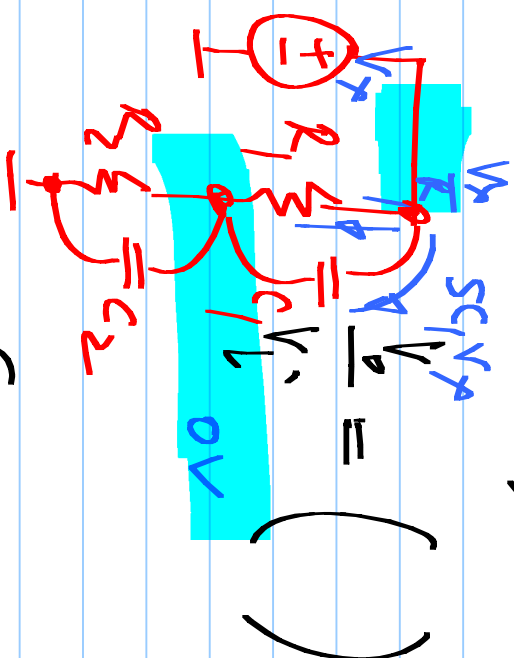
reduce $\omega_{u,loop}$

Slowing
down the
system

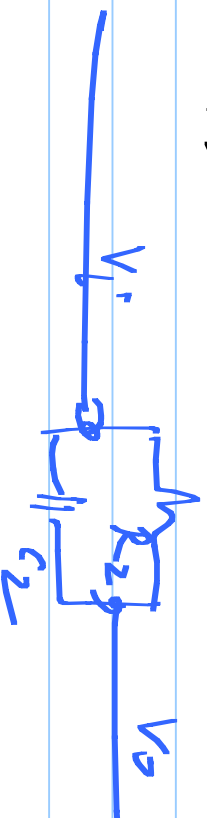


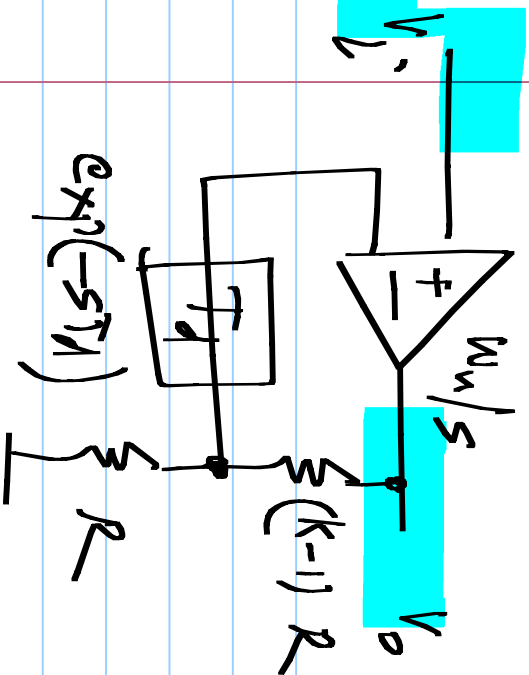
Loop gain: $\frac{w_n}{k s} = L(s)$

$$\frac{L(s)}{1 + L(s)}$$



$$L(s) = \frac{w_n}{k \cdot s} \left[\frac{1 + s C_1 R_1}{1 + s (C_1 + C_2) (R_1 \parallel R_2)} \right]$$

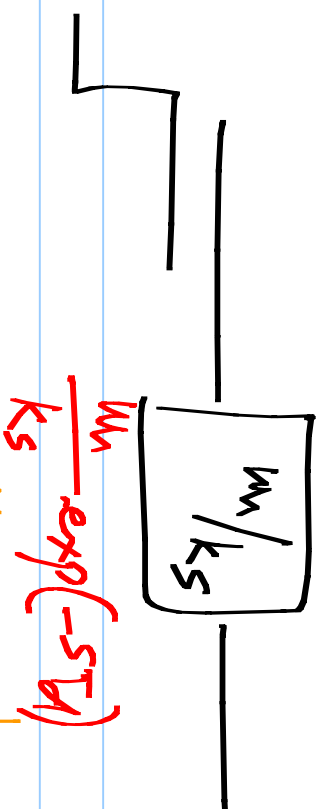
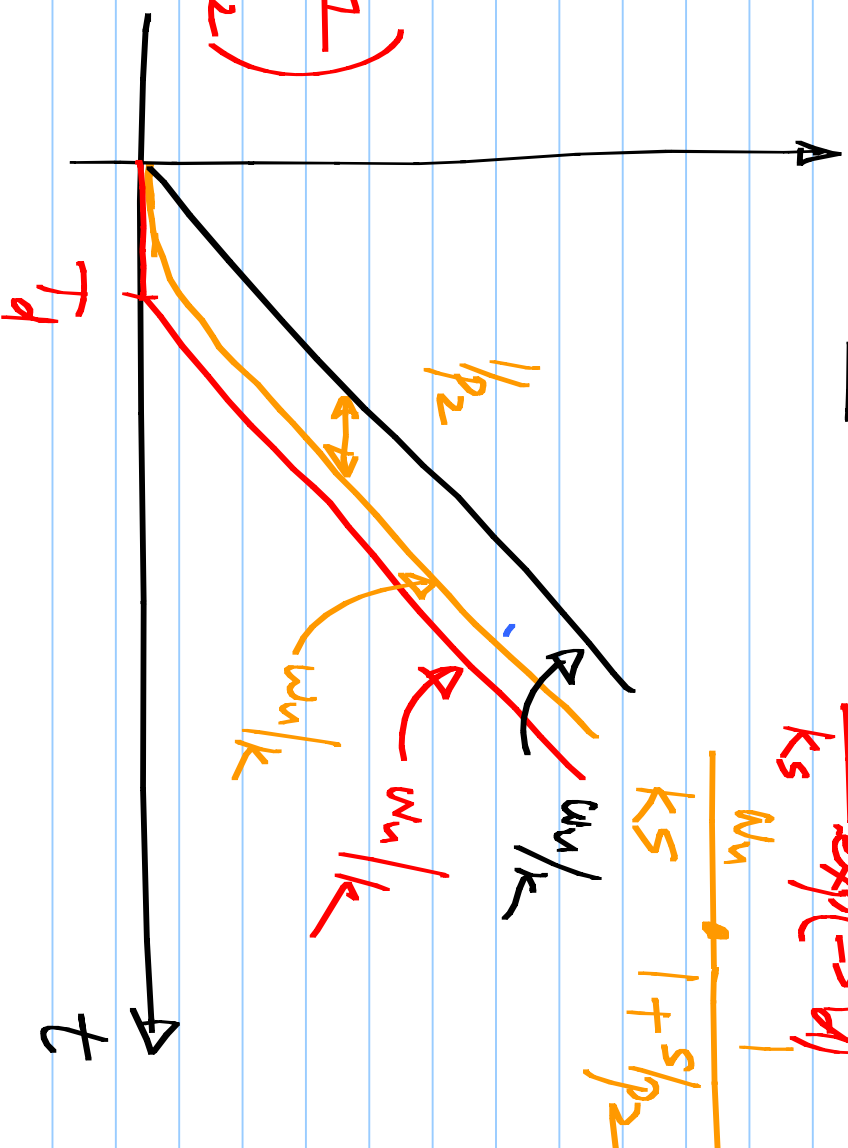




Loop gain: $\frac{u_n}{k s} = L(s)$

Step response $\frac{u_n}{k s} \left(\frac{1 + s/z_1}{1 + s/p_2} \right)$

$\frac{u_n}{k s} \left(1 + s/z_1 \right)$



$\frac{u_n}{k s} \exp(-sT_d)$

$\frac{u_n}{k s} \left(1 + s/p_2 \right)$

$$L(s) = \frac{w_n}{ks} \cdot \frac{1}{1 + s/p_2} = \frac{w_n}{k} \left[\frac{1}{s} \cdot \frac{1}{1 + s/p_2} \right]$$

$$= \frac{w_n}{k} \left[\frac{1}{s} - \frac{1/p_2}{1 + s/p_2} \right]$$

$$\frac{1}{s + p_2} = \frac{1/p_2}{1 + s/p_2}$$

$$(1 - \exp(-p_2 t)) \frac{1}{p_2}$$

