## EE539: Analog Integrated Circuit Design

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TWO STAGE OPAMP.



Figure 1: TWO STAGE



Figure 2: TWO STAGE

This circuit can be redrawn as DC gain of stage  $1=\frac{g_{m1}}{G_2}$ DC gain of stage  $2=\frac{g_{m5}}{G_L}$ Overall DC gain $=\frac{g_{m1}}{G_2}\frac{g_{m5}}{G_L}$ **Frequency response** No: of poles=2

 $\frac{V_o}{V_{in}} = \frac{g_{m1}(-sC_c + g_{m5})}{s^2(C_2C_c + C_2C_L + C_cC_L) + s(C_c(g_{m5} + G_L + G_2) + C_2G_L + C_LG_2) + G_2G_L}$ (1)

If  $C_c = 0$  then

$$\frac{V_o}{V_{in}} = \frac{g_{m1}g_{m5}}{s^2 C_2 C_L + s(C_2 G_L + C_L G_2) + G_2 G_L}$$
(2)

This is just a cascade of two transfer functions but when we introduce  ${\cal C}_c$  , the two gets coupled.

To find the poles of the transfer function, we assume that the two poles are far apart, then

$$ax^2 + bx + c = 0 \tag{3}$$

$$P_1 = \frac{-c}{b} \tag{4}$$

$$P_1 = \frac{-G_2 G_L}{C_c (g_{m5} + G_L + G_2) + C_2 G_L + C_L G_2}$$
(5)

$$P_1 = \frac{-G_2}{C_c(\frac{g_{m5}}{G_L} + 1 + \frac{G_2}{G_L}) + C_2 + C_L \frac{G_2}{G_L}}$$
(6)

The term  $C_c(\frac{g_{m5}}{G_L} + 1 + \frac{G_2}{G_L})$  shows the MILLER EFFECT , but it is not exact since this is not an ideal voltage amplifier.

$$P_2 = \frac{-b}{a} \tag{7}$$



Figure 3: THE POLE

$$P_2 = -\frac{C_c(g_{m5} + G_L + G_2) + C_2G_L + C_LG_2}{C_2C_c + C_2C_L + C_cC_L}$$
(8)

$$P_2 = -\frac{g_{m5} + G_2 + G_L + \frac{C_2}{C_c}G_L + \frac{C_L}{C_c}G_2}{C_2 + C_L + C_L \frac{C_2}{C_c}}$$
(9)

Since  $g_{m5}$  is large,  $P_2$  becomes the non dominant term. It has increased to high frequency due to pole splitting.

If  $g_{m5} >> G_L, G_2$  and  $C_c >> C_2, C_L$ , then  $P_2 = \frac{-g_{m5}}{C_2 + C_L}$ . This is true since at high frequency when  $C_c$  is shorted  $C_2$  and  $C_L$  is parallel. But since  $C_c$  is introduced for compensation so the assumption  $C_c >> C_2, C_L$  is not valid, So taking only that

$$g_{m5} >> G_L, G_2$$

then

$$P_2 = \frac{-g_{m5}}{C_2 C_c + C_2 C_L + C_c C_L}$$

i.e

$$P_2 = \frac{-g_{m5} \frac{C_c}{C_c + C_2}}{C_L + \frac{C_2 C_c}{C_c + C_2}}$$

This is correct since applying a  $V_{test}$  at the drain of  $M_5$ ,

$$I = \frac{g_{m5}V_{test}C_c}{C_2 + C_c}$$

So the effective conductance is  $\frac{g_{m5}C_c}{C_2+C_c}$  and the effective capacitance is  $C_L + \frac{C_cC_2}{C_c+C_2}$