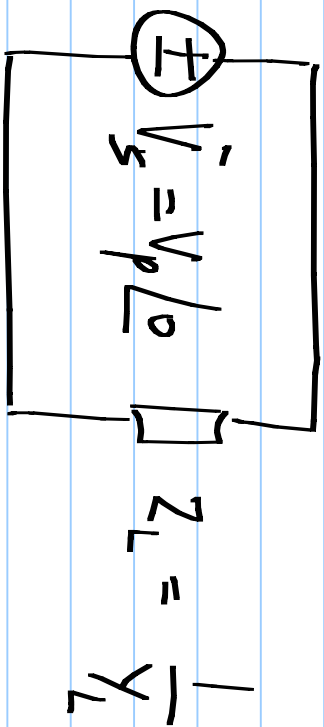


# Lecture 35



Real power, } instantaneous values

Reactive power

$$\text{Complex power} = \underline{P} = \frac{\underline{V} \underline{I}^*}{2} = \frac{\underline{V}_s \cdot \underline{V}_s^* \underline{Y}_L^*}{2}$$

$$= \frac{|V_s|^2 |Y_L| [\cos \phi - j \sin \phi]}{2} \quad \phi = \angle Z_L$$

$$Y_L = |Y_L| \cdot \angle \phi$$

$$p(t) = v(t) \cdot i(t)$$

$$= V_p \cos \omega t - \left[ V_p \cdot |Y_L| \cdot \cos(\omega t + \phi) \right] \cos \omega t \cos \phi$$

$$= V_p^2 |Y_L| \cos^2 \omega t - \cos \phi$$

- \sin \omega t \sin \phi

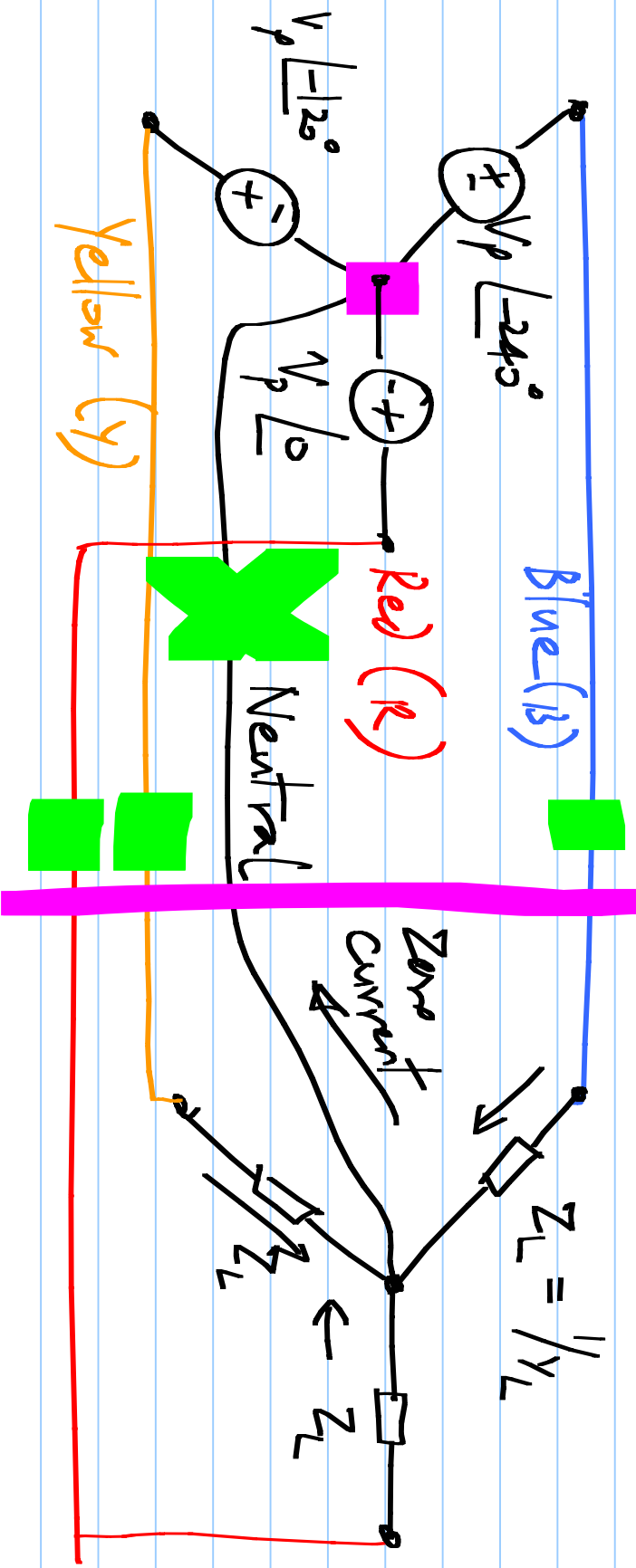
$$= V_p^2 |Y_L| \sin \omega t \cos \omega t - \sin \phi$$

$$= \frac{V_p^2 |Y_L|}{2} \left[ \cos \phi (1 + \cos 2\omega t) - \sin \phi \sin(2\omega t) \right]$$

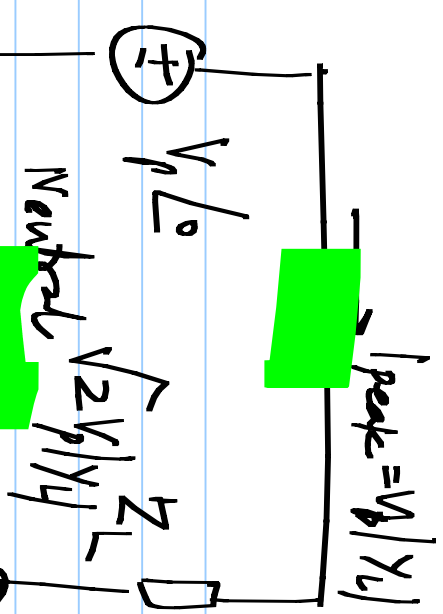
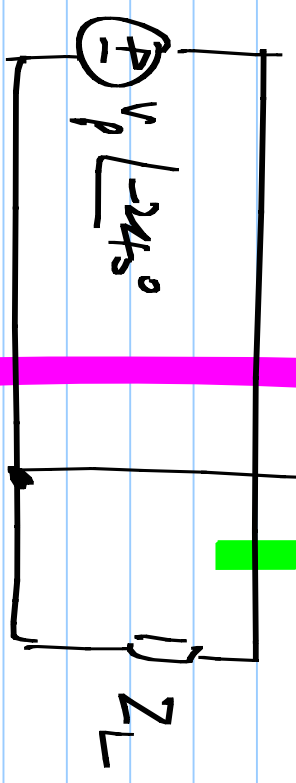
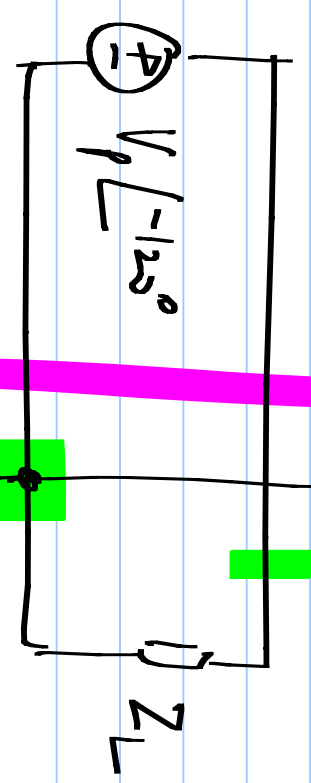
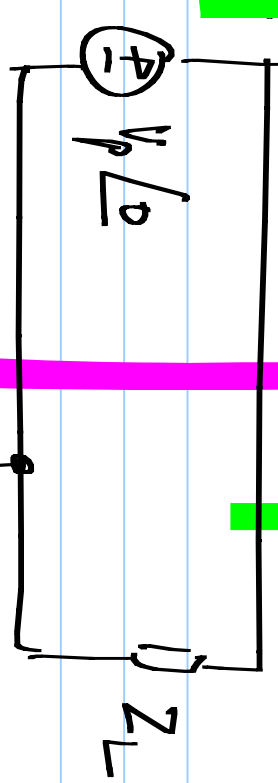
average = 0

Real & reactive powers: oscillating at  $2\omega$  } single plane

average value =  $\frac{|V_p^2 Y_L| \cos \phi}{2}$



3.  $\left(\frac{V_p^2 |Y_L|}{2}\right) \cos \phi$  peak current:  $V_p |Y_L|$



$2 \cdot \frac{V_p^2 |Y_L|}{2} \cdot \cos \phi$



$$P_R(t) = \frac{V_p^2 |Y_L|}{2} \left[ \cos \phi (1 + \cos 2\omega t) - \sin \phi \sin(2\omega t) \right]$$

$$P_Y(t) = \frac{V_p^2 |Y_L|}{2} \left[ \cos \phi (1 + \cos(2\omega t - 240^\circ)) - \sin \phi \sin(2\omega t - 240^\circ) \right]$$

$$P_B(t) = \frac{V_p^2 |Y_L|}{2} \left[ \cos \phi (1 + \cos(2\omega t - 480^\circ)) - \sin \phi \sin(2\omega t - 480^\circ) \right]$$

Balanced 3 phase load driven from a (balanced)

3 phase source :

$k$  Constant (total) real power } instantaneous  
\* Zero (total) reactive power } values

