



Placement

Presented By:

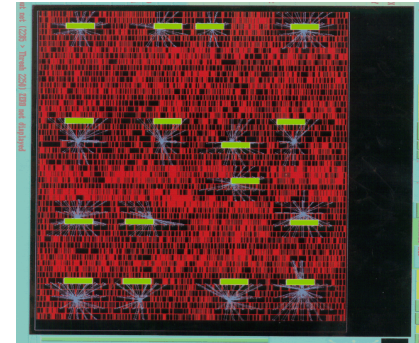
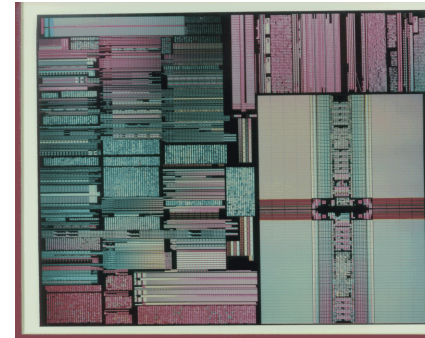
Sridhar H Rangarajan

**IBM Systems India Enterprise Systems
Development**

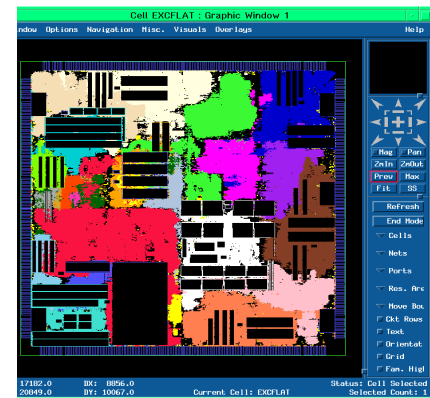
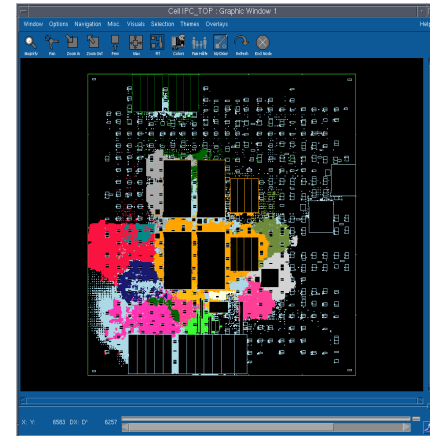
Agenda

- Introduction
- Placement Problem Footprints
- Placement Objective
- Algorithms
 - Min-Cut Placement
 - Analytic Placement
 - Quadratic placement
 - FDP
 - Simulated Annealing
 - Modern Placement Algorithms
- Summary

Trends in Placement

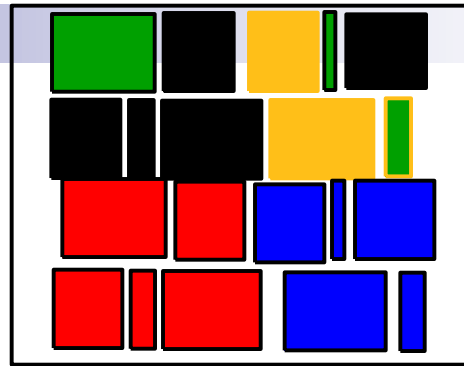


- Chips are larger
- Footprints are more diverse
- Empty Space % is growing
- Interconnect delays are larger percentage of chip cycle time
- Placement is no longer a point tool: It's part of a timing closure system.

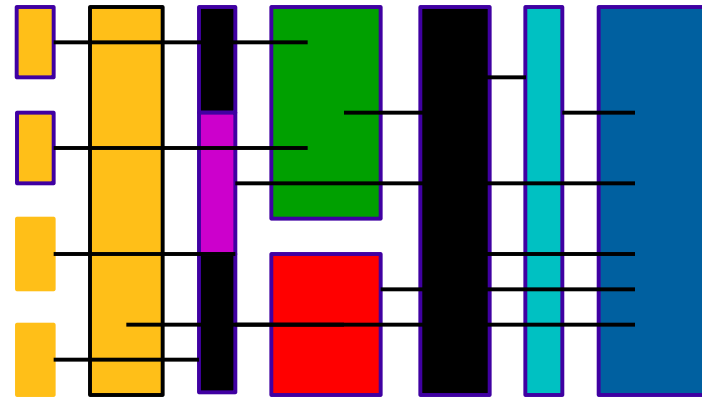


Placement Footprints:

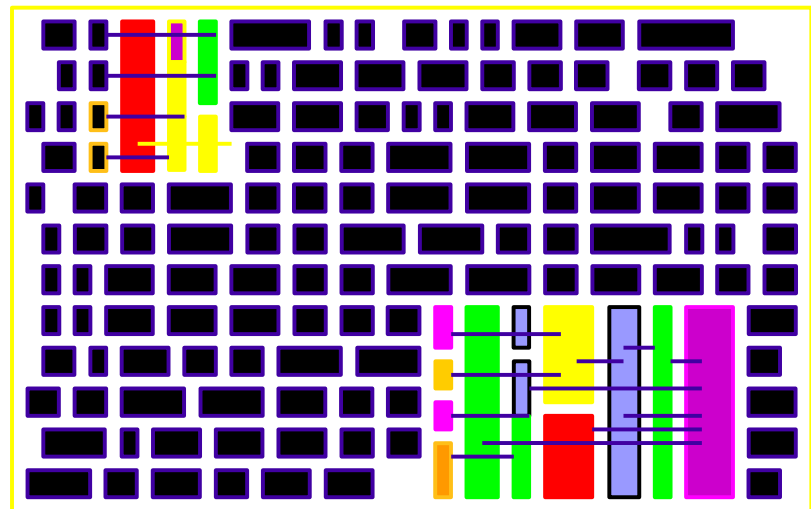
Standard Cell sea of gates:



Data Path:

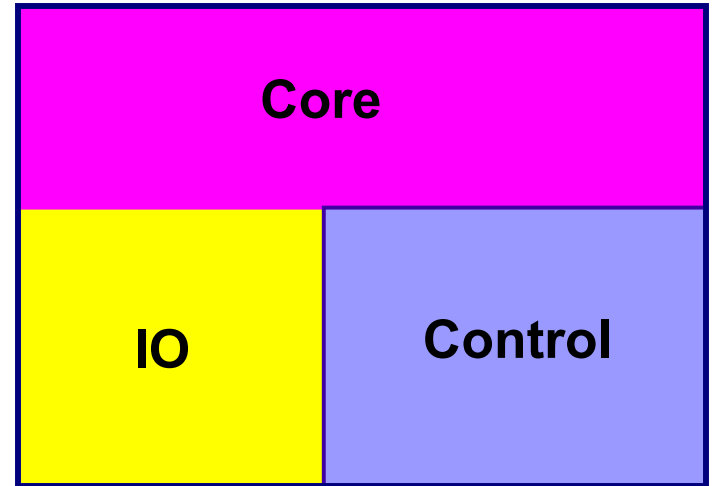


Mixed Data Path & sea of gates:



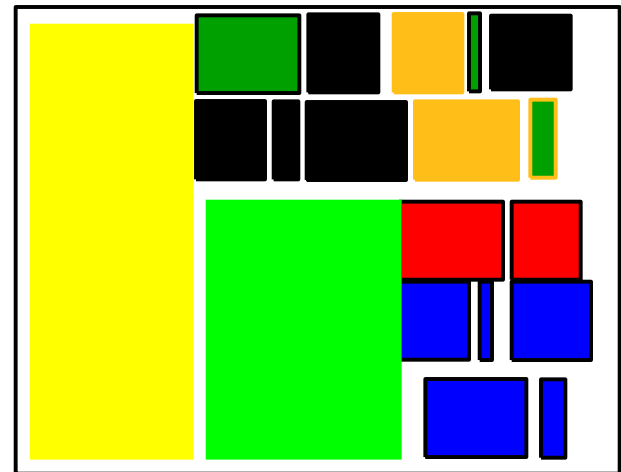
Placement Footprints:

Reserved areas



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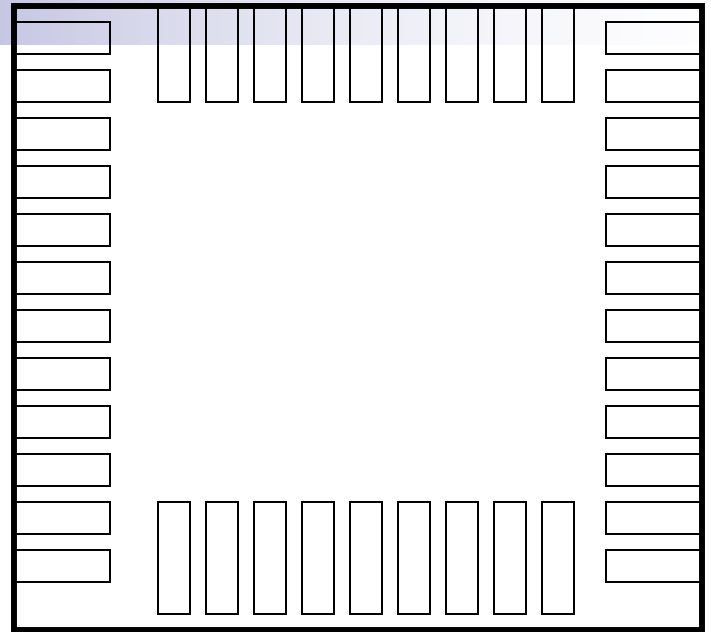
IP - Floorplanning



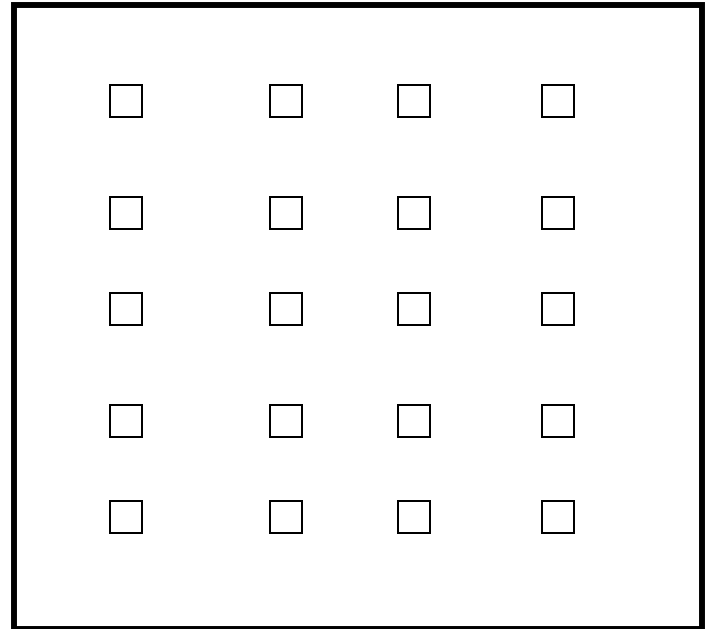
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Placement Footprints:

Perimeter IO



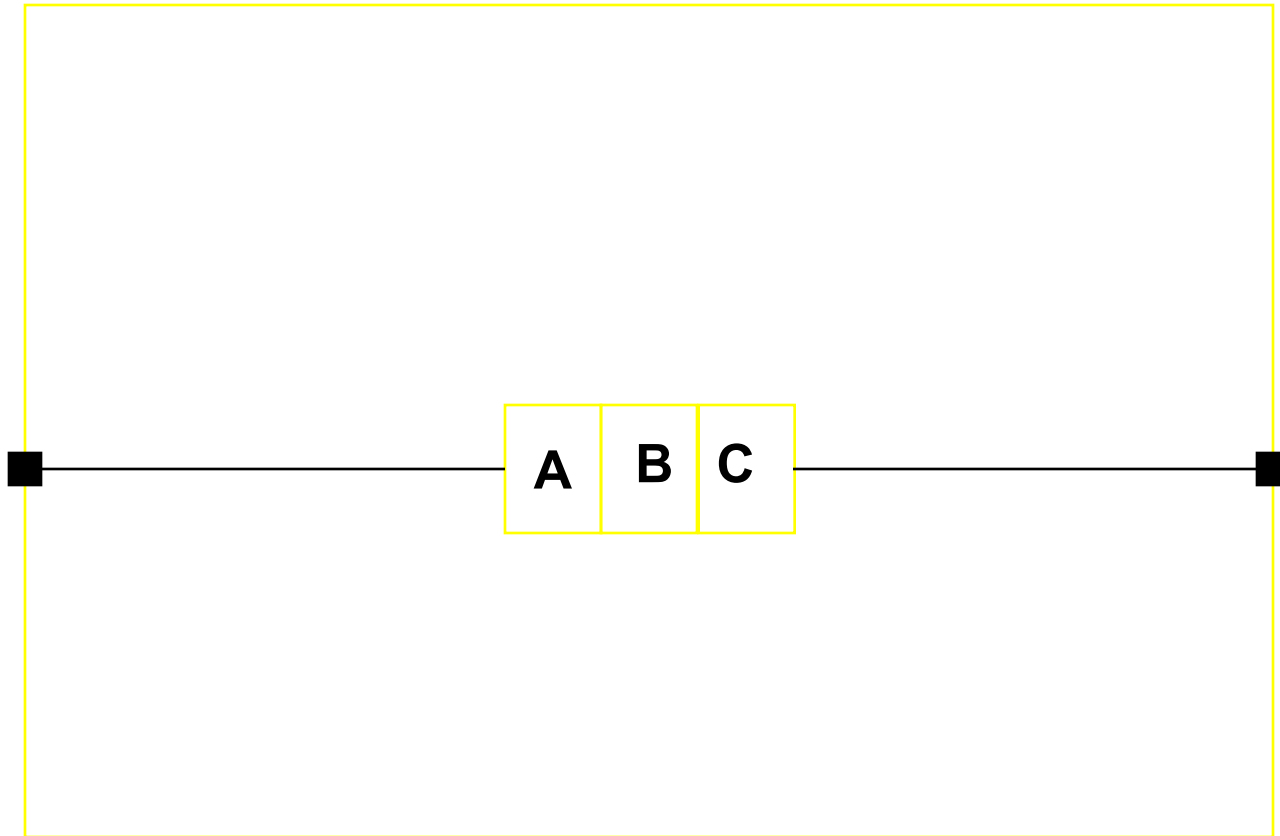
Area IO



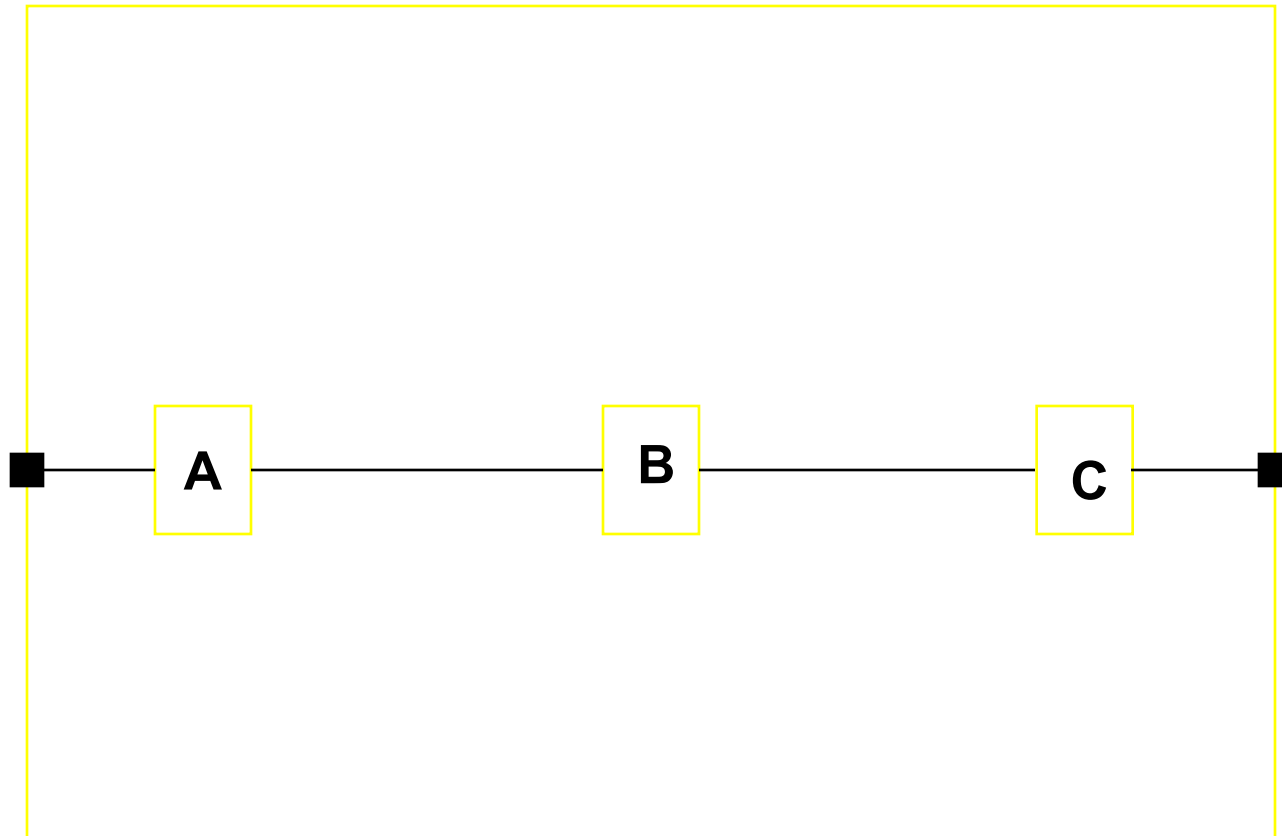
Placement Objective

- Find optimal relative ordering of cells
 - minimize wire length and congestion
 - maximize timing slack
- Find optimal spacing of cells
 - eliminate wiring congestion problems
 - provide space for post placement synthesis
 - clock trees
 - buffer insertion
 - timing correction
- Find optimal Global Position

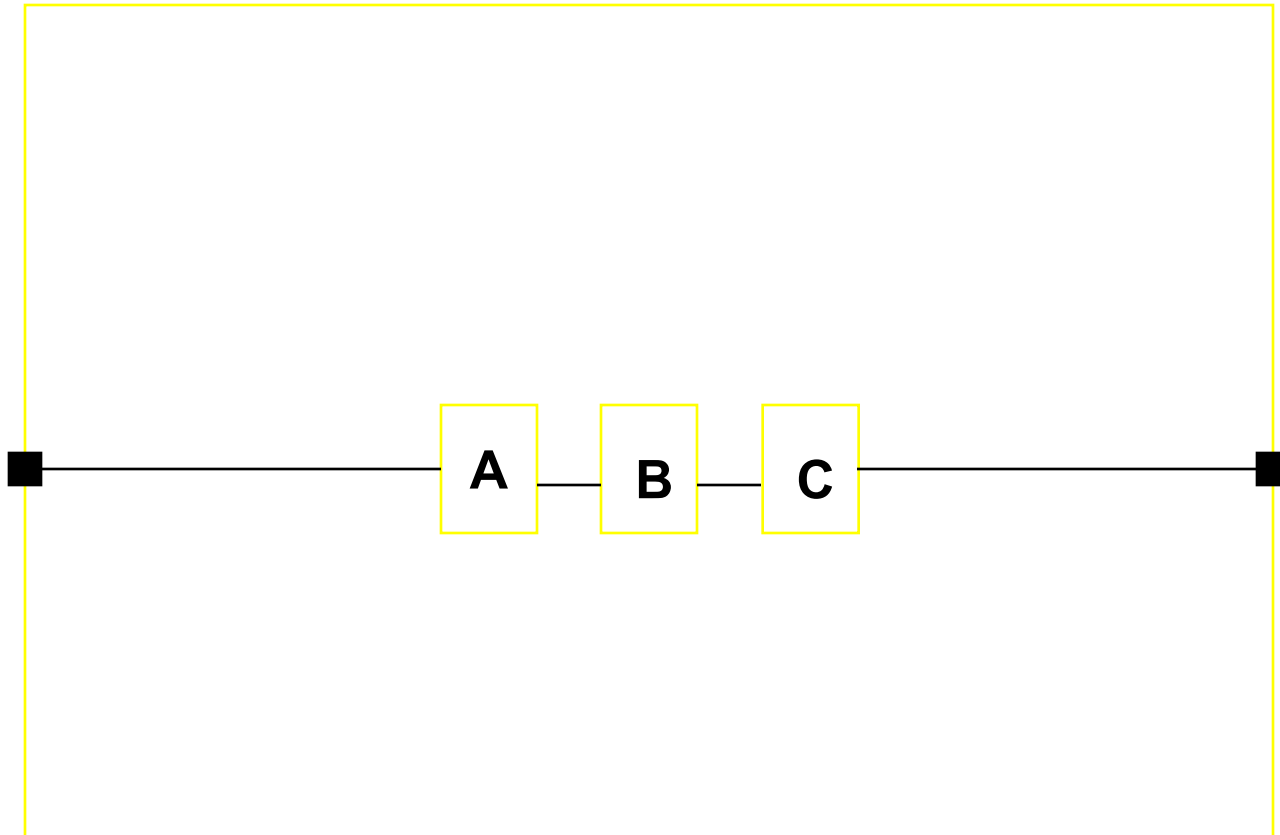
Optimal Relative Order:



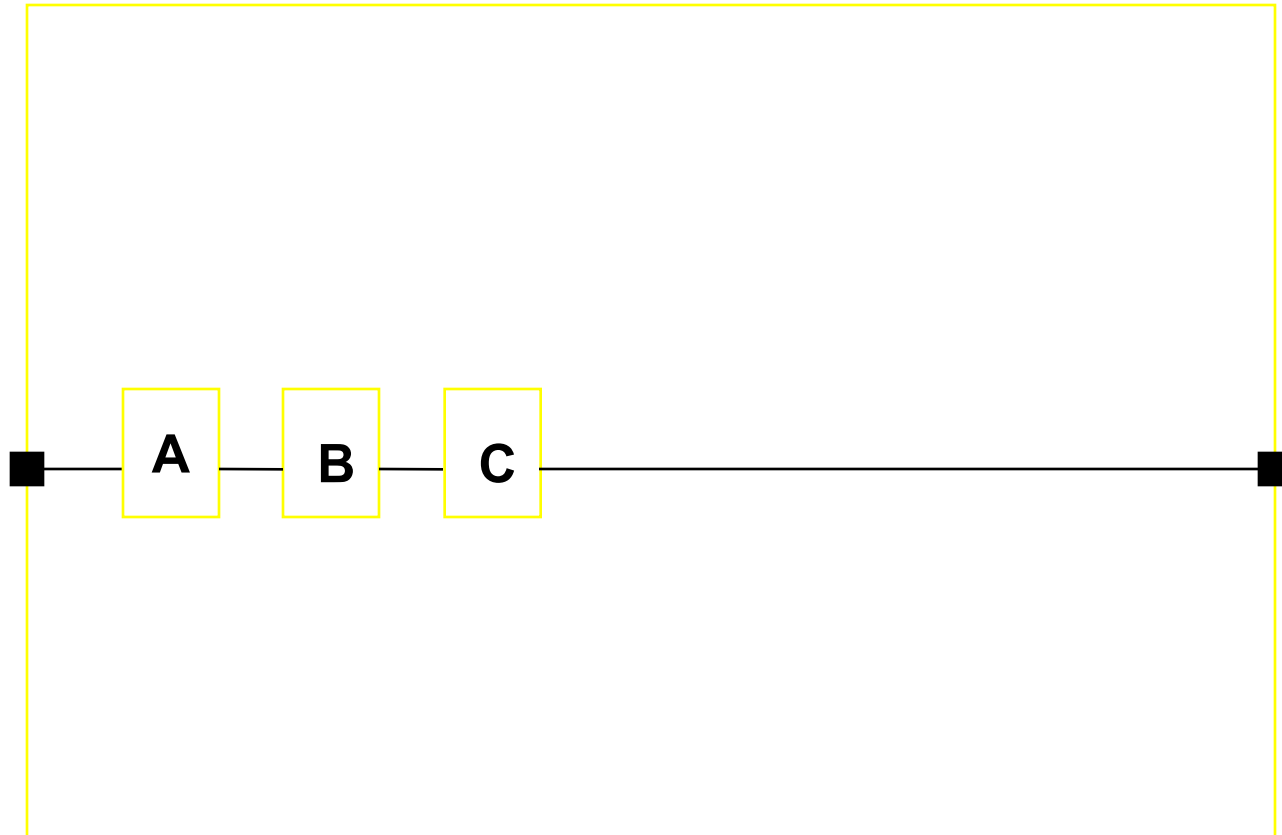
To spread ...



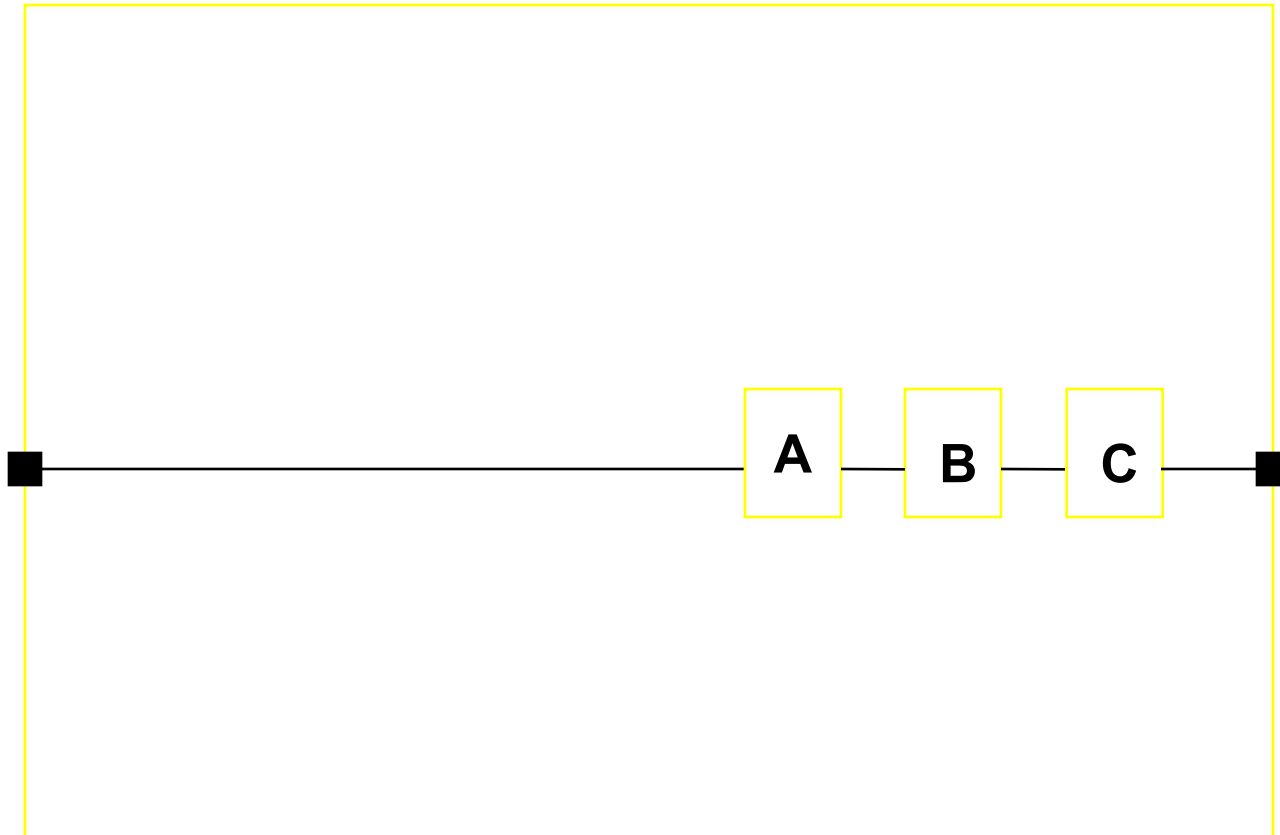
.. or not to spread



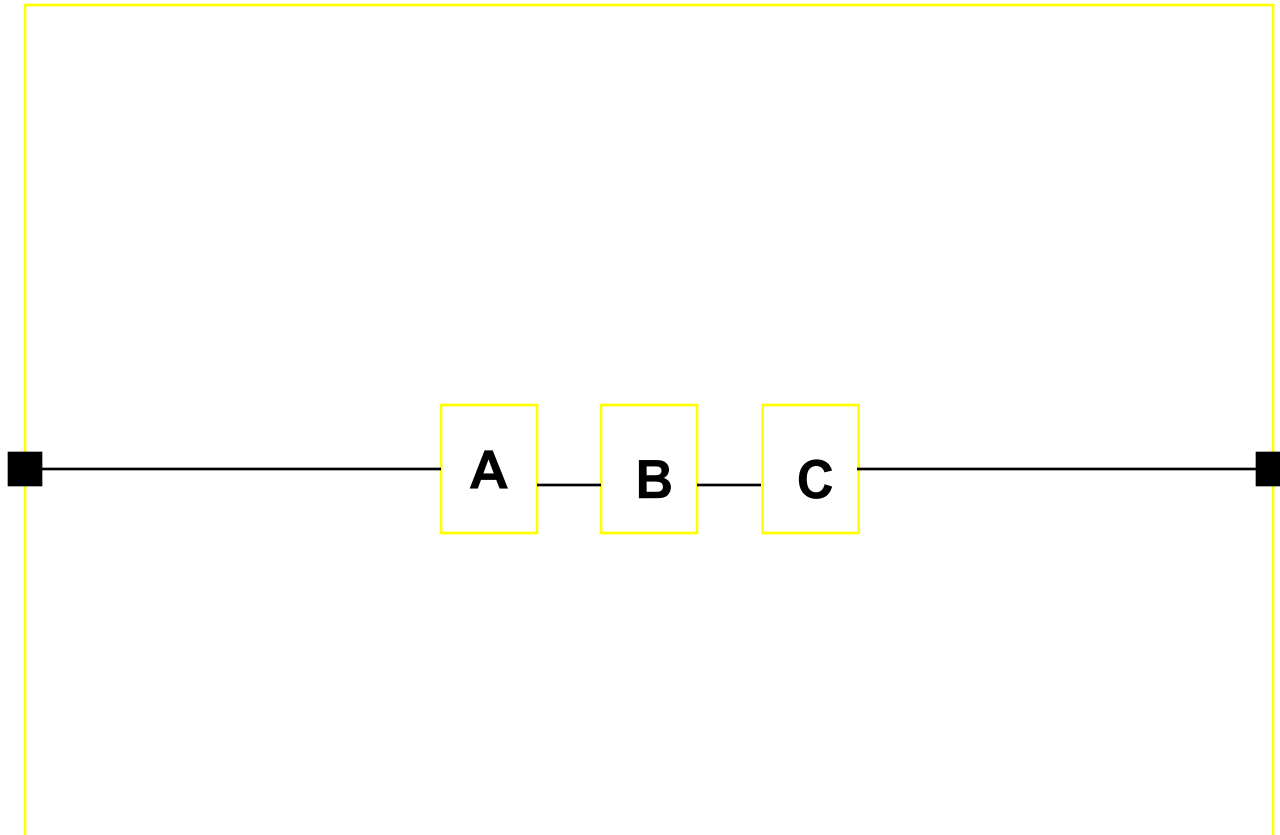
Place to the left



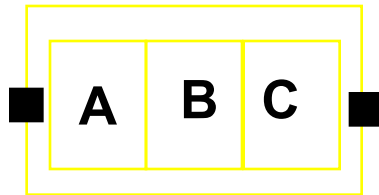
... or to the right



.. or near center

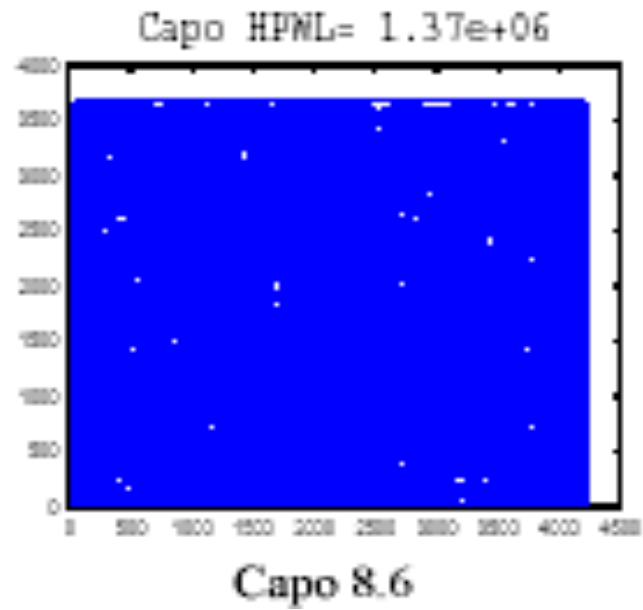


Optimal Relative Order:



Without “free” space the problem is degenerate: Relative order dominates the solution space.

Problems limited to Relative Order:

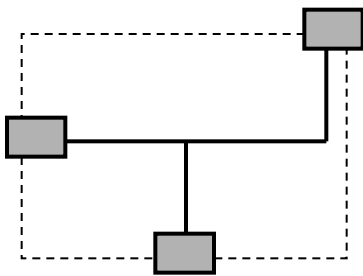


Problem w/spacing / global position components

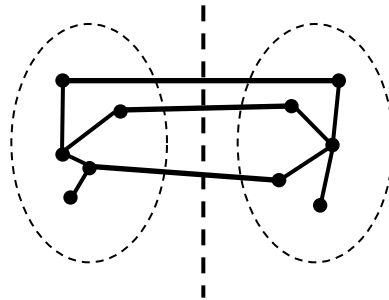


Optimization Objectives

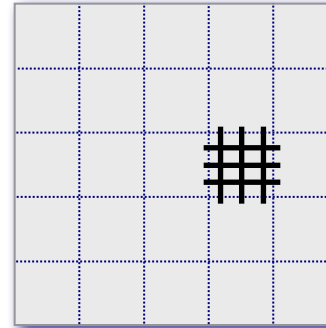
Total
Wirelength



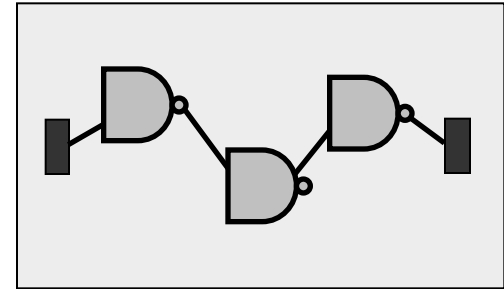
Number of
Cut Nets



Wire
Congestion



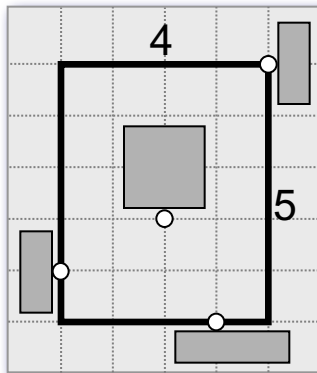
Signal
Delay



Optimization Objectives – Total Wirelength

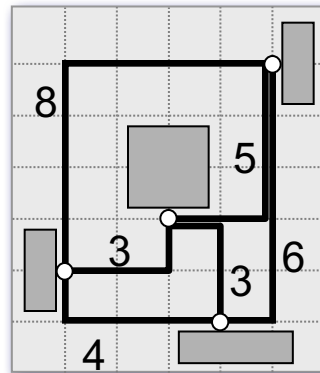
Wirelength estimation for a given placement

Half-perimeter
wirelength
(HPWL)



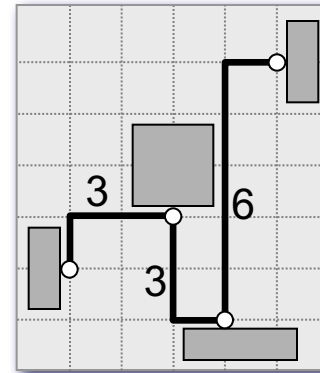
HPWL = 9

Complete
graph
(clique)



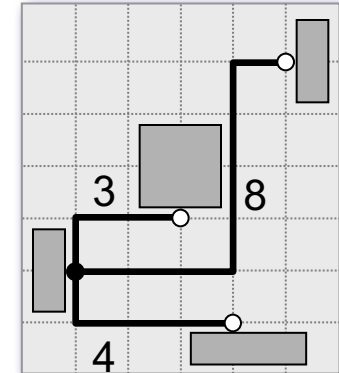
Clique Length =
 $(2/p)\sum_{e \in \text{clique}} d_M(e) = 14.5$

Monotone
chain



Chain Length = 12

Star model

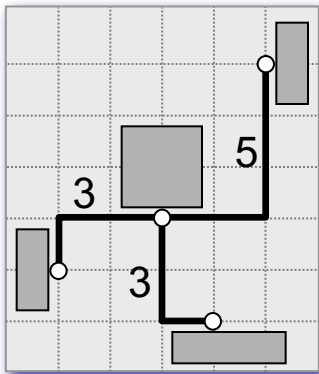


Star Length = 15

Optimization Objectives – Total Wirelength

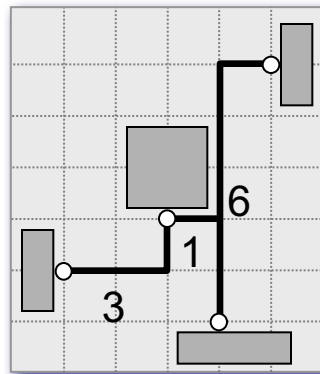
Wirelength estimation for a given placement (cont'd.)

Rectilinear
minimum
spanning
tree (RMST)



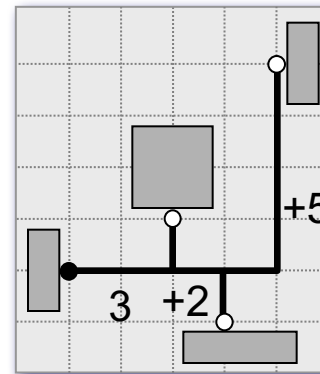
RMST Length = 11

Rectilinear
Steiner
minimum
tree (RSMT)



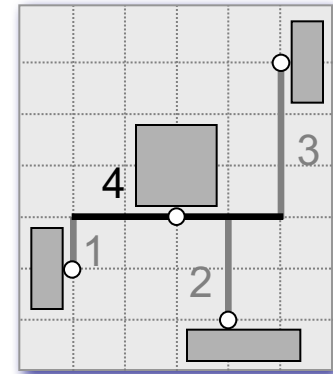
RSMT Length = 10

Rectilinear
Steiner
arborescence
model (RSA)



RSA Length = 10

Single-trunk
Steiner
tree (STST)



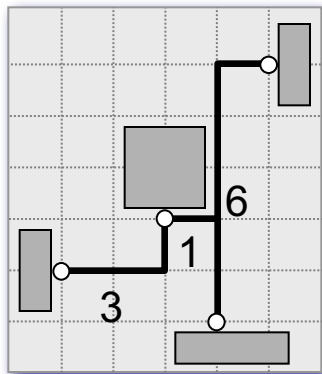
STST Length = 10

Optimization Objectives – Total Wirelength

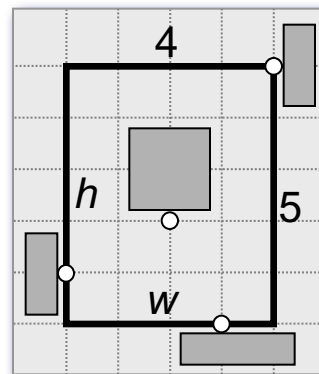
Wirelength estimation for a given placement (cont'd.)

Preferred method: Half-perimeter wirelength (HPWL)

- Fast (order of magnitude faster than RSMT)
- Equal to length of RSMT for 2- and 3-pin nets
- Margin of error for real circuits approx. 8% [Chu, ICCAD 04]



RSMT Length = 10



HPWL = 9

$$L_{\text{HPWL}} = w + h$$

Optimization Objectives – Total Wirelength

Total wirelength with net weights (weighted wirelength)

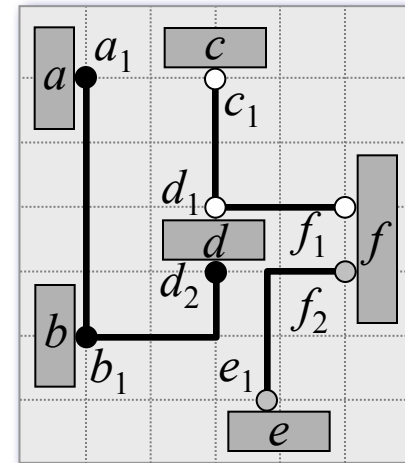
- For a placement P , an estimate of total weighted wirelength is

$$L(P) = \sum_{net \in P} w(net) \cdot L(net)$$

where $w(net)$ is the weight of net , and $L(net)$ is the estimated wirelength of net .

- Example:

Nets	Weights
$N_1 = (a_1, b_1, d_2)$	$w(N_1) = 2$
$N_2 = (c_1, d_1, f_1)$	$w(N_2) = 4$
$N_3 = (e_1, f_2)$	$w(N_3) = 1$



$$L(P) = \sum_{net \in P} w(net) \cdot L(net) = 2 \cdot 7 + 4 \cdot 4 + 1 \cdot 3 = 33$$

Optimization Objectives – Number of Cut Nets

Cut sizes of a placement

- To improve total wirelength of a placement P , separately calculate the number of crossings of global vertical and horizontal cutlines, and minimize

$$L(P) = \sum_{v \in V_P} \Psi_P(v) + \sum_{h \in H_P} \Psi_P(h)$$

where $\Psi_P(cut)$ be the set of nets cut by a cutline cut

Optimization Objectives – Number of Cut Nets

Cut sizes of a placement

■ Example:

Nets

$$N_1 = (a_1, b_1, d_2)$$

$$N_2 = (c_1, d_1, f_1)$$

$$N_3 = (e_1, f_2)$$

■ Cut values for each global cutline

$$\psi_P(v_1) = 1 \quad \psi_P(v_2) = 2$$

$$\psi_P(h_1) = 3 \quad \psi_P(h_2) = 2$$

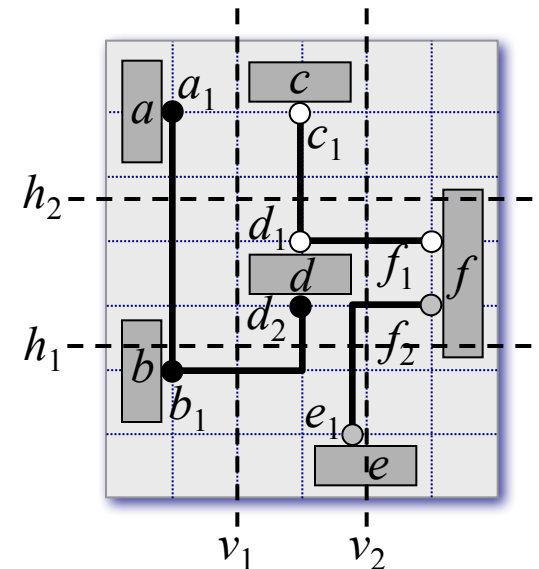
■ Total number of crossings in P

$$\psi_P(v_1) + \psi_P(v_2) + \psi_P(h_1) + \psi_P(h_2) = 1 + 2 + 3 + 2 = 8$$

■ Cut sizes

$$X(P) = \max(\psi_P(v_1), \psi_P(v_2)) = \max(1, 2) = 2$$

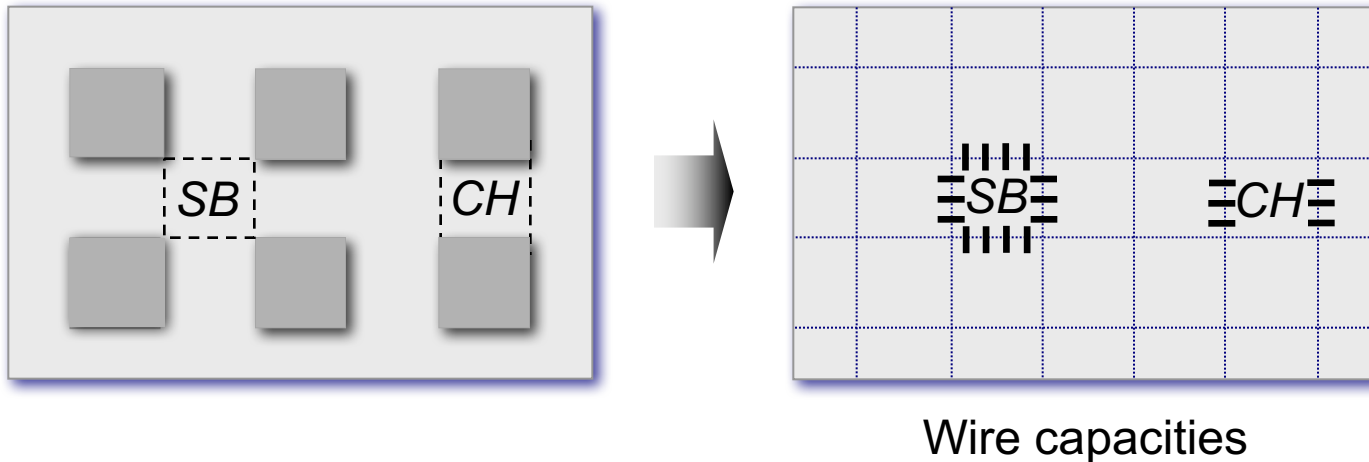
$$Y(P) = \max(\psi_P(h_1), \psi_P(h_2)) = \max(3, 2) = 3$$



Optimization Objectives – Wire Congestion

Routing congestion of a placement

- Ratio of demand for routing tracks to the supply of available routing tracks
- Estimated by the number of nets that pass through the boundaries of individual routing regions



Optimization Objectives – Wire Congestion

Routing congestion of a placement

- Formally, the local wire density $\varphi_P(e)$ of an edge e between two neighboring grid cells is

$$\varphi_P(e) = \frac{\eta_P(e)}{\sigma_P(e)}$$

where $\eta_P(e)$ is the estimated number of nets that cross e and $\sigma_P(e)$ is the maximum number of nets that can cross e

- If $\varphi_P(e) > 1$, then too many nets are estimated to cross e , making P more likely to be unroutable.
- The wire density of P is $\Phi(P) = \max_{e \in E}(\varphi_P(e))$

where E is the set of all edges

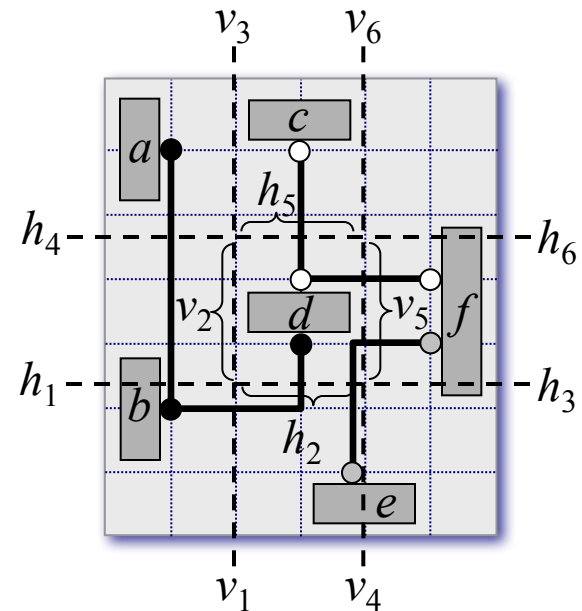
- If $\Phi(P) \leq 1$, then the design is estimated to be fully routable, otherwise routing will need to detour some nets through less-congested edges

Optimization Objectives – Wire Congestion

Wire Density of a placement

$\eta_P(h_1) = 1$	$\eta_P(v_1) = 1$
$\eta_P(h_2) = 2$	$\eta_P(v_2) = 0$
$\eta_P(h_3) = 0$	$\eta_P(v_3) = 0$
$\eta_P(h_4) = 1$	$\eta_P(v_4) = 0$
$\eta_P(h_5) = 1$	$\eta_P(v_5) = 2$
$\eta_P(h_6) = 0$	$\eta_P(v_6) = 0$

Maximum: $\eta_P(e) = 2$



$$\Phi(P) = \frac{\eta_P(e)}{\sigma_P(e)} = \frac{2}{3}$$



Routable

Optimization Objectives – Signal Delay

Circuit timing of a placement

- Static timing analysis using actual arrival time (AAT) and required arrival time (RAT)
 - $AAT(v)$ represents the latest transition time at a given node v measured from the beginning of the clock cycle
 - $RAT(v)$ represents the time by which the latest transition at v must complete in order for the circuit to operate correctly within a given clock cycle.
- For correct operation of the chip with respect to setup (maximum path delay) constraints, it is required that $AAT(v) \leq RAT(v)$.

Placement Algorithms

- Min-Cut Placement
- Analytic Placement
- Simulated Annealing
- Modern Placement Algorithms

Global Placement

■ Partitioning-based algorithms:

- The netlist and the layout are divided into smaller sub-netlists and sub-regions, respectively
- Process is repeated until each sub-netlist and sub-region is small enough to be handled optimally
- Detailed placement often performed by optimal solvers, facilitating a natural transition from global placement to detailed placement
- Example: min-cut placement

■ Analytic techniques:

- Model the placement problem using an objective (cost) function, which can be optimized via numerical analysis
- Examples: quadratic placement and force-directed placement

■ Stochastic algorithms:

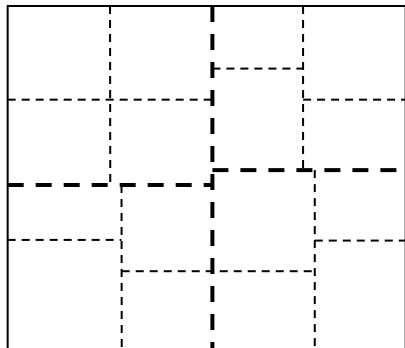
- Randomized moves that allow hill-climbing are used to optimize the cost function
- Example: simulated annealing

Global Placement

Partitioning-based



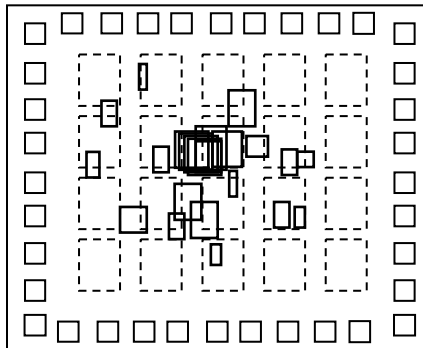
Min-cut
placement



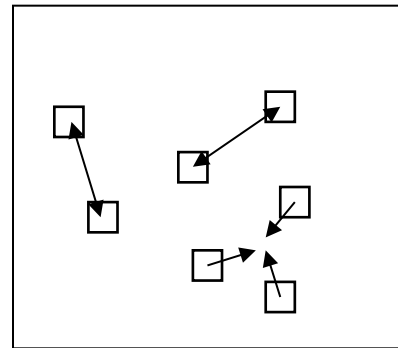
Analytic



Quadratic
placement



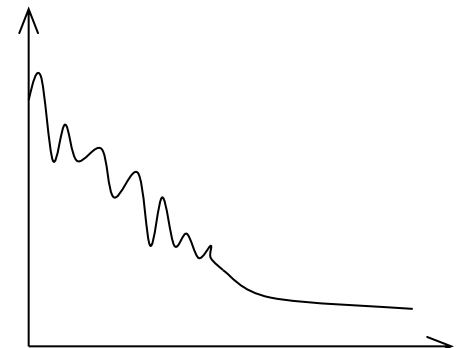
Force-directed
placement



Stochastic



Simulated annealing

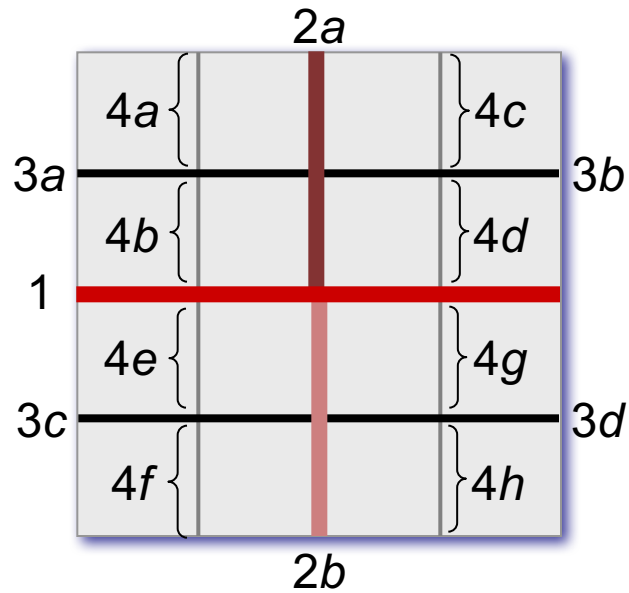


Min-Cut Placement

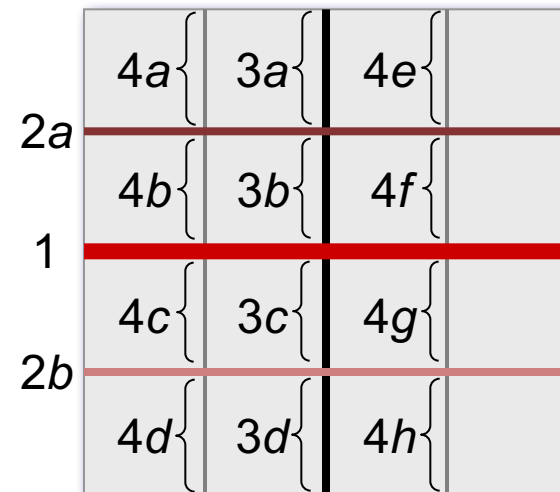
- Uses partitioning algorithms to divide the netlist and the layout region into smaller sub-netlists and sub-regions
- Conceptually, each sub-region is assigned a portion of the original netlist
- Each cut heuristically minimizes the number of cut nets using, for example,
 - Kernighan-Lin (KL) algorithm
 - Fiduccia-Mattheyses (FM) algorithm

Min-Cut Placement

Alternating cutline directions



Repeating cutline directions



Min-Cut Placement

Input: netlist *Netlist*, layout area *LA*, minimum number of cells per region *cells_min*

Output: placement *P*

$P = \emptyset$

regions = ASSIGN(*Netlist*,*LA*)

// assign netlist to layout area

while (*regions* != \emptyset)

// while regions still not placed

region = FIRST_ELEMENT(*regions*)

// first element in *regions*

 REMOVE(*regions*, *region*)

// remove first element of *regions*

if (*region* contains more than *cell_min* cells)

 (*sr1*,*sr2*) = BISECT(*region*)

// divide *region* into two subregions

// *sr1* and *sr2*, obtaining the sub-

// netlists and sub-areas

 ADD_TO_END(*regions*,*sr1*)

// add *sr1* to the end of *regions*

 ADD_TO_END(*regions*,*sr2*)

// add *sr2* to the end of *regions*

else

 PLACE(*region*)

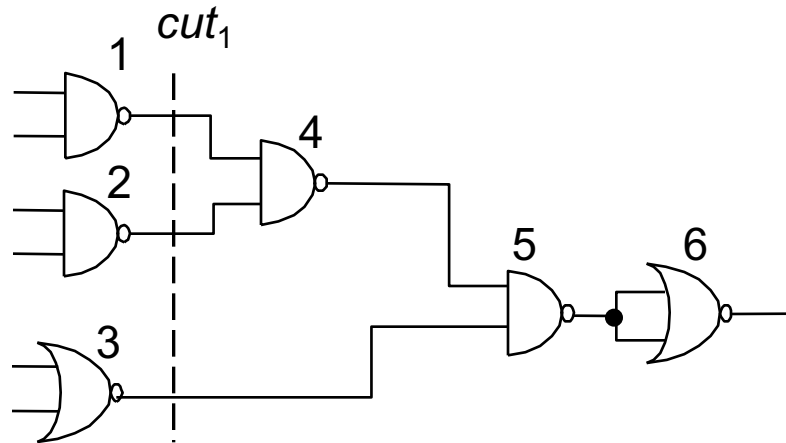
// place *region*

 ADD(*P*,*region*)

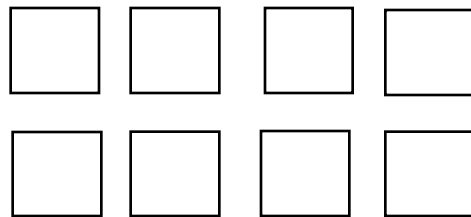
// add *region* to *P*

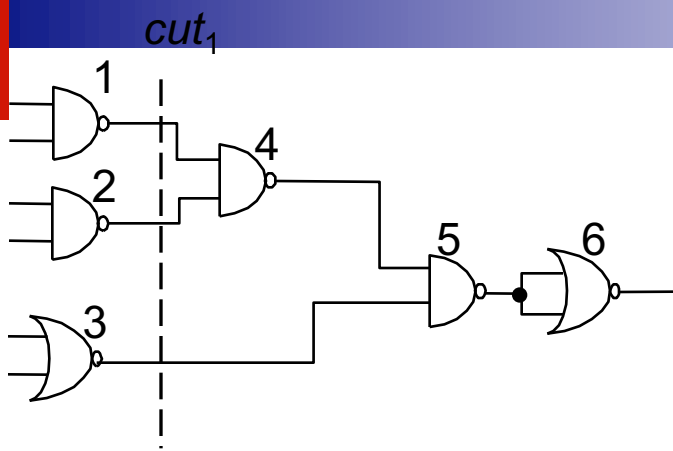
Min-Cut Placement – Example

Given:

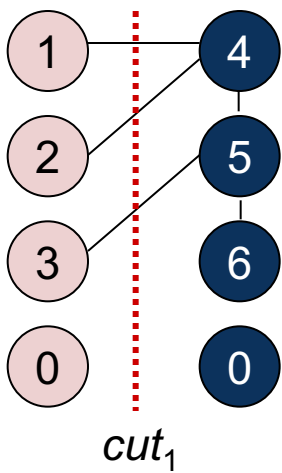


Task: 4 x 2 placement with minimum wirelength using alternative cutline directions and the KL algorithm

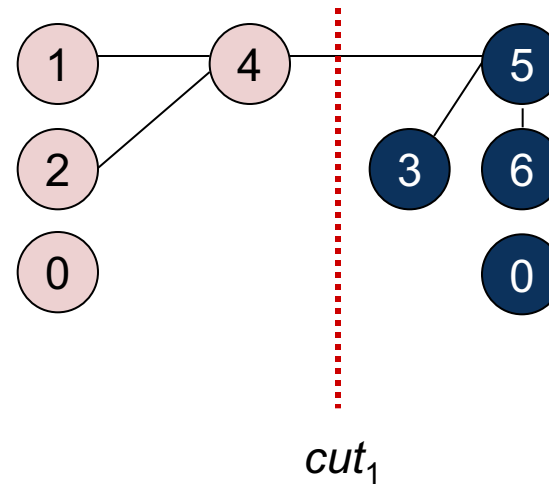


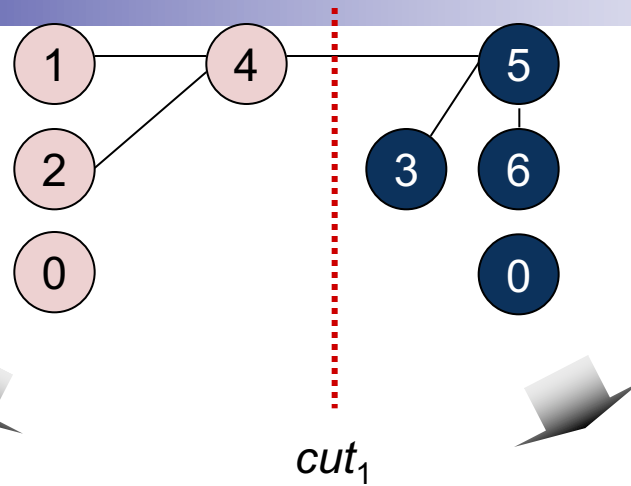


Vertical cut cut_1 : $L=\{1,2,3\}$, $R=\{4,5,6\}$



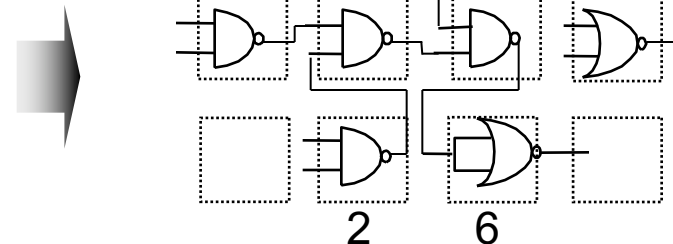
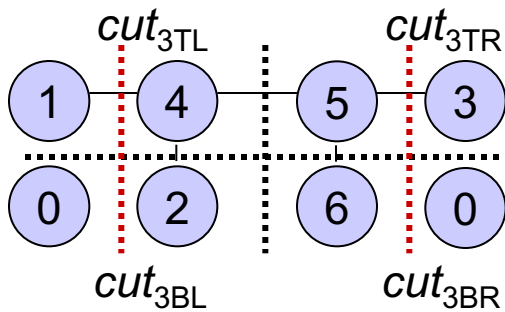
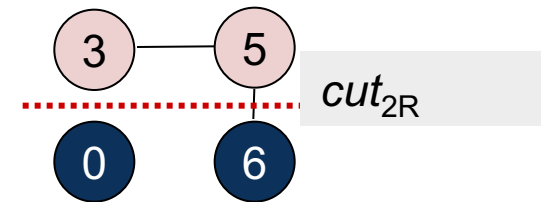
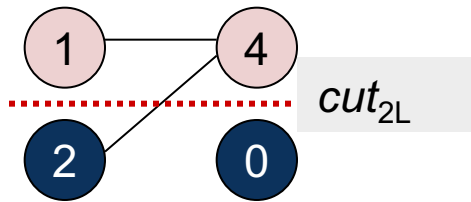
KL Algorithmus





Horizontal cut cut_{2L} : $T=\{1,4\}$, $B=\{2,0\}$

Horizontal cut cut_{2R} : $T=\{3,5\}$, $B=\{6,0\}$



Min-Cut Placement

- Advantages:
 - Reasonably fast
 - Objective function can be adjusted, e.g., to perform timing-driven placement
 - Hierarchical strategy applicable to large circuits
- Disadvantages:
 - Randomized, chaotic algorithms – small changes in input lead to large changes in output (**Stability is poor**)
 - Optimizing one cutline at a time may result in routing congestion elsewhere

Analytic Placement – Quadratic Placement

- Objective function is quadratic; sum of (weighted) **squared Euclidean distance** represents placement objective function

$$L(P) = \frac{1}{2} \sum_{i,j=1}^n c_{ij} \left((x_i - x_j)^2 + (y_i - y_j)^2 \right)$$

where n is the total number of cells, and $c(i,j)$ is the connection cost between cells i and j .

- Minimize objective function by equating its derivative to zero which reduces to solving a system of linear equations

Analytic Placement – Quadratic Placement

$$L(P) = \frac{1}{2} \sum_{i,j=1}^n c_{ij} \left((x_i - x_j)^2 + (y_i - y_j)^2 \right)$$

where n is the total number of cells, and $c(i,j)$ is the connection cost between cells i and j .

- Each dimension can be considered independently:

$$L_x(P) = \sum_{i=1,j=1}^n c(i,j)(x_i - x_j)^2 \quad L_y(P) = \sum_{i=1,j=1}^n c(i,j)(y_i - y_j)^2$$

- Convex quadratic optimization problem: any local minimum solution is also a global minimum
- Optimal x - and y -coordinates can be found by setting the partial derivatives of $L_x(P)$ and $L_y(P)$ to zero

Analytic Placement – Quadratic Placement

$$L(P) = \frac{1}{2} \sum_{i,j=1}^n c_{ij} \left((x_i - x_j)^2 + (y_i - y_j)^2 \right)$$

where n is the total number of cells, and $c(i,j)$ is the connection cost between cells i and j .

$$L_x(P) = \sum_{i=1,j=1}^n c(i,j)(x_i - x_j)^2 \quad L_y(P) = \sum_{i=1,j=1}^n c(i,j)(y_i - y_j)^2$$

- Each dimension can be considered independently:

$$\frac{\partial L_x(P)}{\partial X} = AX - b_x = 0$$

$$\frac{\partial L_y(P)}{\partial Y} = AY - b_y = 0$$


- where A is a matrix with $A[i][j] = c(i,j)$ when $i \neq j$, and $A[i][i] =$ the sum of incident connection weights of cell i .
- X is a vector of all the x -coordinates of the non-fixed cells, and b_x is a vector with $b_x[i] =$ the sum of x -coordinates of all fixed cells attached to i .
- Y is a vector of all the y -coordinates of the non-fixed cells, and b_y is a vector with $b_y[i] =$ the sum of y -coordinates of all fixed cells attached to i .


Analytic Placement – Quadratic Placement

$$L(P) = \frac{1}{2} \sum_{i,j=1}^n c_{ij} \left((x_i - x_j)^2 + (y_i - y_j)^2 \right)$$

where n is the total number of cells, and $c(i,j)$ is the connection cost between cells i and j .

- Each dimension can be considered independently:
 $L_x(P) = \sum_{i,j=1}^n c(i,j)(x_i - x_j)^2$ $L_y(P) = \sum_{i,j=1}^n c(i,j)(y_i - y_j)^2$


$$\frac{\partial L_x(P)}{\partial X} = AX - b_x = 0$$


$$\frac{\partial L_y(P)}{\partial Y} = AY - b_y = 0$$

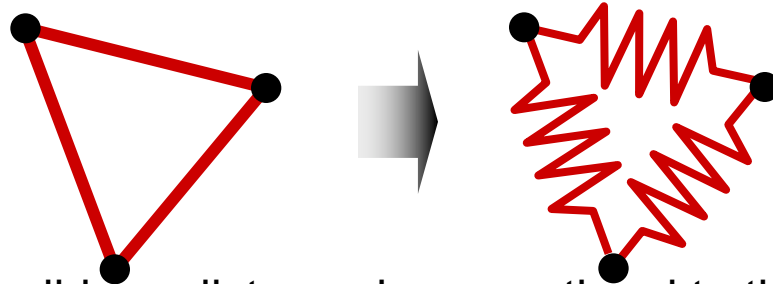
- System of linear equations for which iterative numerical methods can be used to find a solution

Why formulate the problem this way?

- Known techniques make solution easy to find
- There is only one solution
- The solution is a global optimum
- The solution conveys “relative order” information
- The solution conveys “global position” information

Analytic Placement – Quadratic Placement

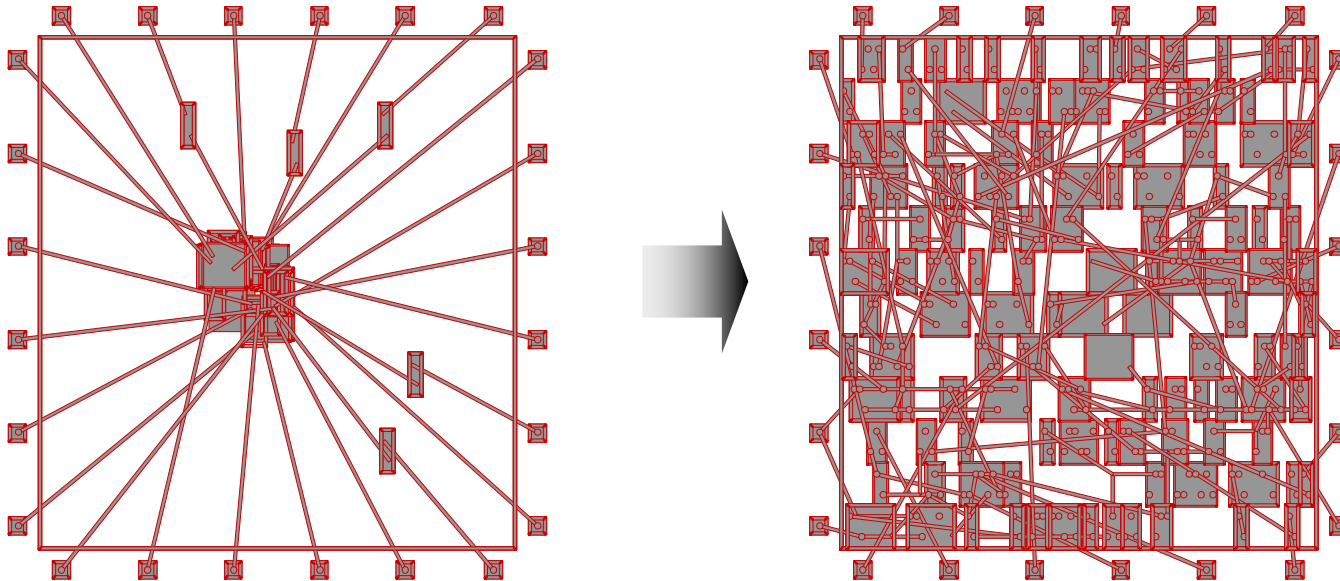
- Mechanical analogy: mass-spring system



- Squared Euclidean distance is proportional to the energy of a spring between these points
 - Quadratic objective function represents total energy of the spring system; for each movable object, the x (y) partial derivative represents the total force acting on that object
 - Setting the forces of the nets to zero, an equilibrium state is mathematically modeled that is characterized by zero forces acting on each movable object
 - At the end, all springs are in a force equilibrium with a minimal total spring energy; this equilibrium represents the minimal sum of squared wirelength
- Result: many cell overlaps

Analytic Placement – Quadratic Placement

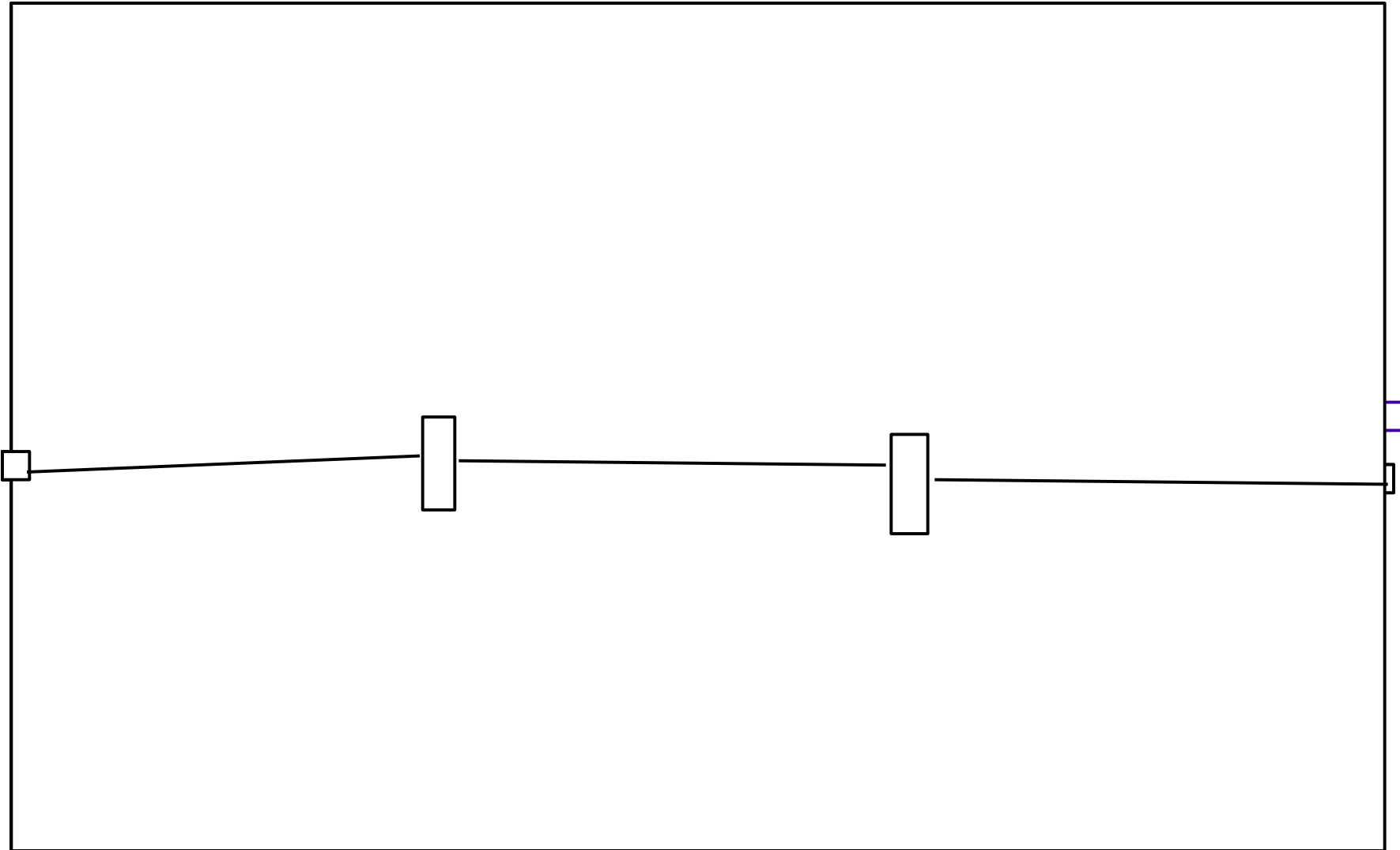
- Second stage of quadratic placers: cells are spread out to remove overlaps
- Methods:
 - Adding fake nets that pull cells away from dense regions toward anchors
 - Geometric sorting and scaling
 - Repulsion forces, etc.



What does the solution look like?

- To get an intuitive feel for the solution, examine the relaxation method for solving $Ax + B = 0$
- Actual program implementation may use other solution methods (that are generally less intuitive).

Solution of Quadratic using Relaxation:



Analytic Placement – Quadratic Placement

■ Advantages:

- Captures the placement problem concisely in mathematical terms
- Leverages efficient algorithms from numerical analysis and available software
- Can be applied to large circuits without netlist clustering (flat)
- Stability: small changes in the input do not lead to large changes in the output

■ Disadvantages:

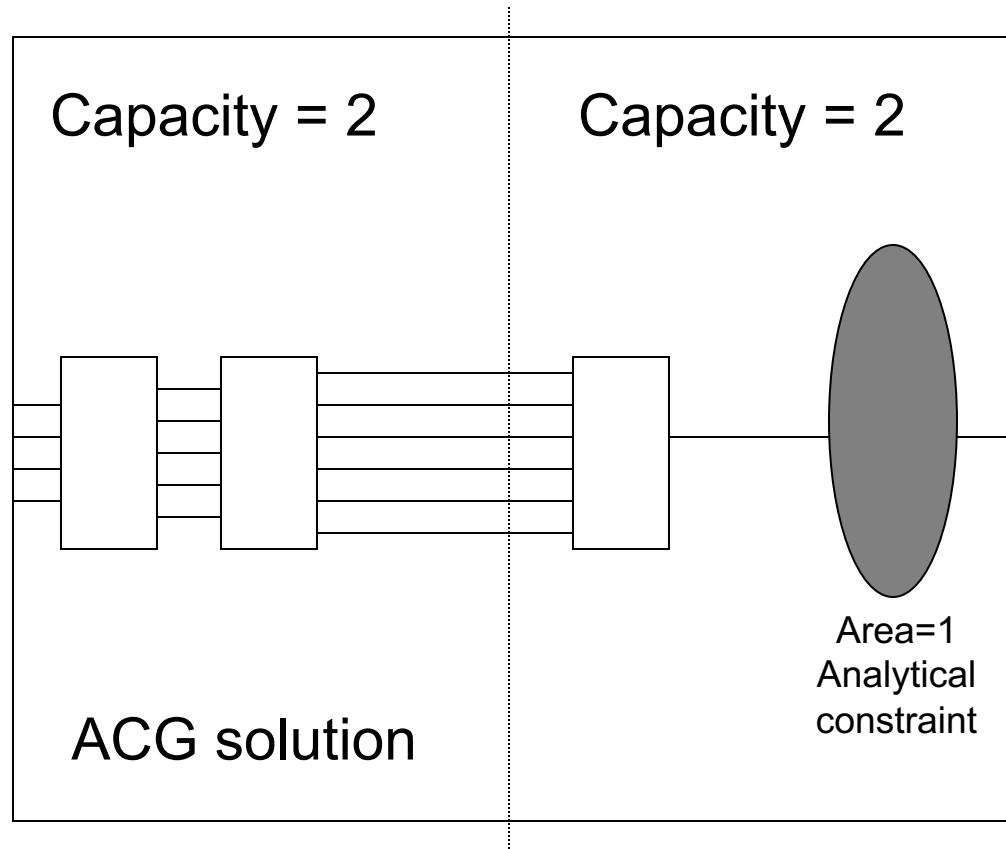
- Connections to fixed objects are necessary: I/O pads, pins of fixed macros, etc.

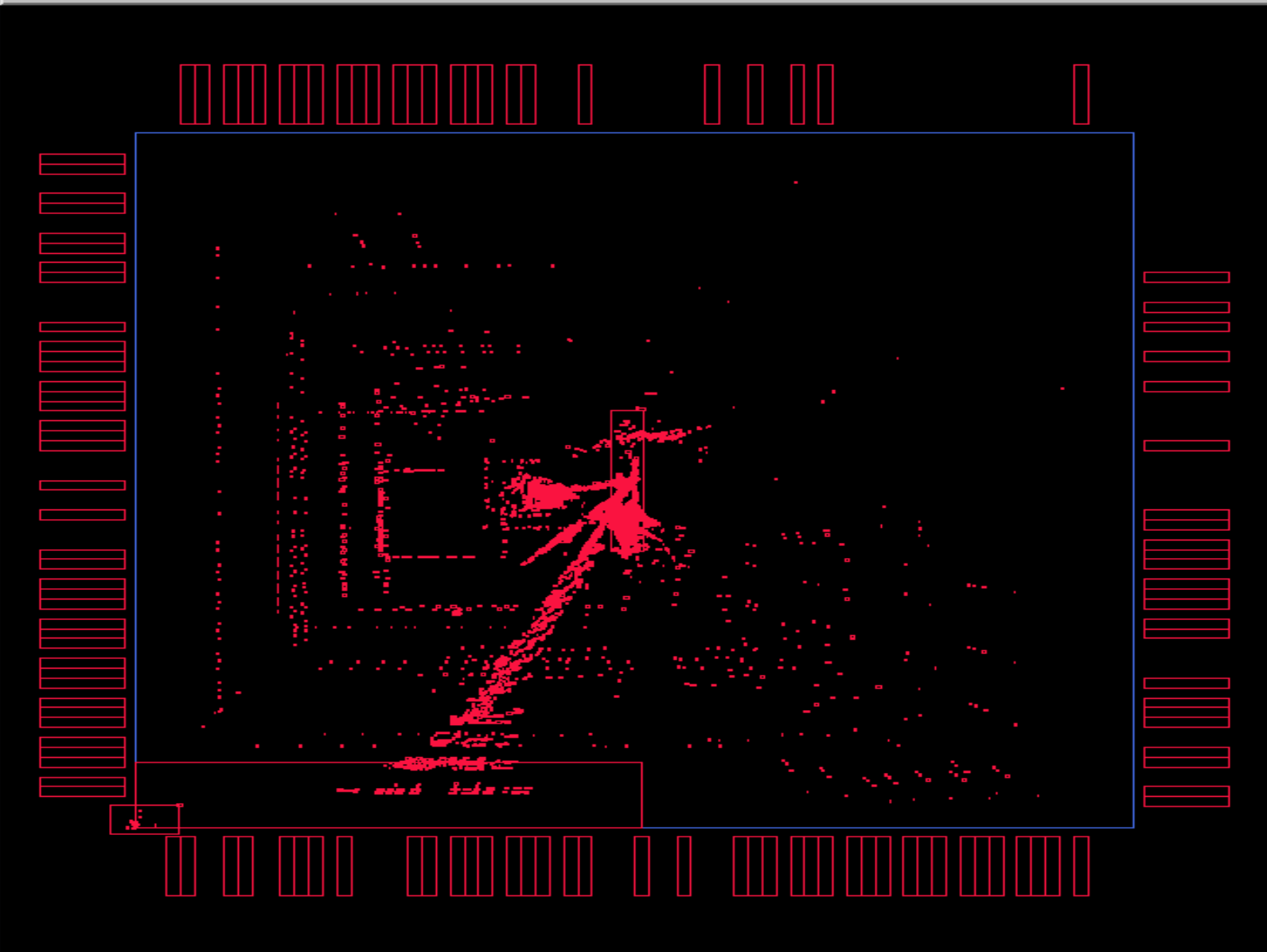
Analytical Constraint Generation: A Hybrid Approach

- Combine Quadratic techniques with MLP
- Use Quadratic solution to determine global position (ie balance)
- Use MLP to determine relative ordering of cells

[9] C. J. Alpert, G.-J. Nam, and P. G. Villarrubia,
"Free Space Management for Cut-Based Placement"
Proc. IEEE Intl. Conf. on Computer-Aided Design}, November, 2002.

Analytical Constraint Generation





Help



Mag Pan

ZmIn ZmOut

Prev Max

Fit SS

x= 2758.0
y= 6203.6
rx= 2091.8
ry= 1803.6
dx= 666.2
dy= 4400.0

Repaint

EndCommand

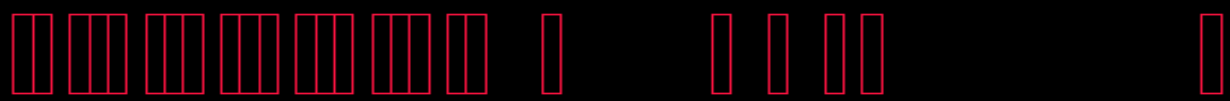
Grid
 Tic

Measure

Query

Select a command
Level PBLK: Visibility altered
Visibility has been altered for more than 1 level, only one modification is listed

Command> |



x= 442.0
y= 5932.9
rx= 2091.8
ry= 1803.6
dx= -1649.8
dy= 4129.3

Repaint

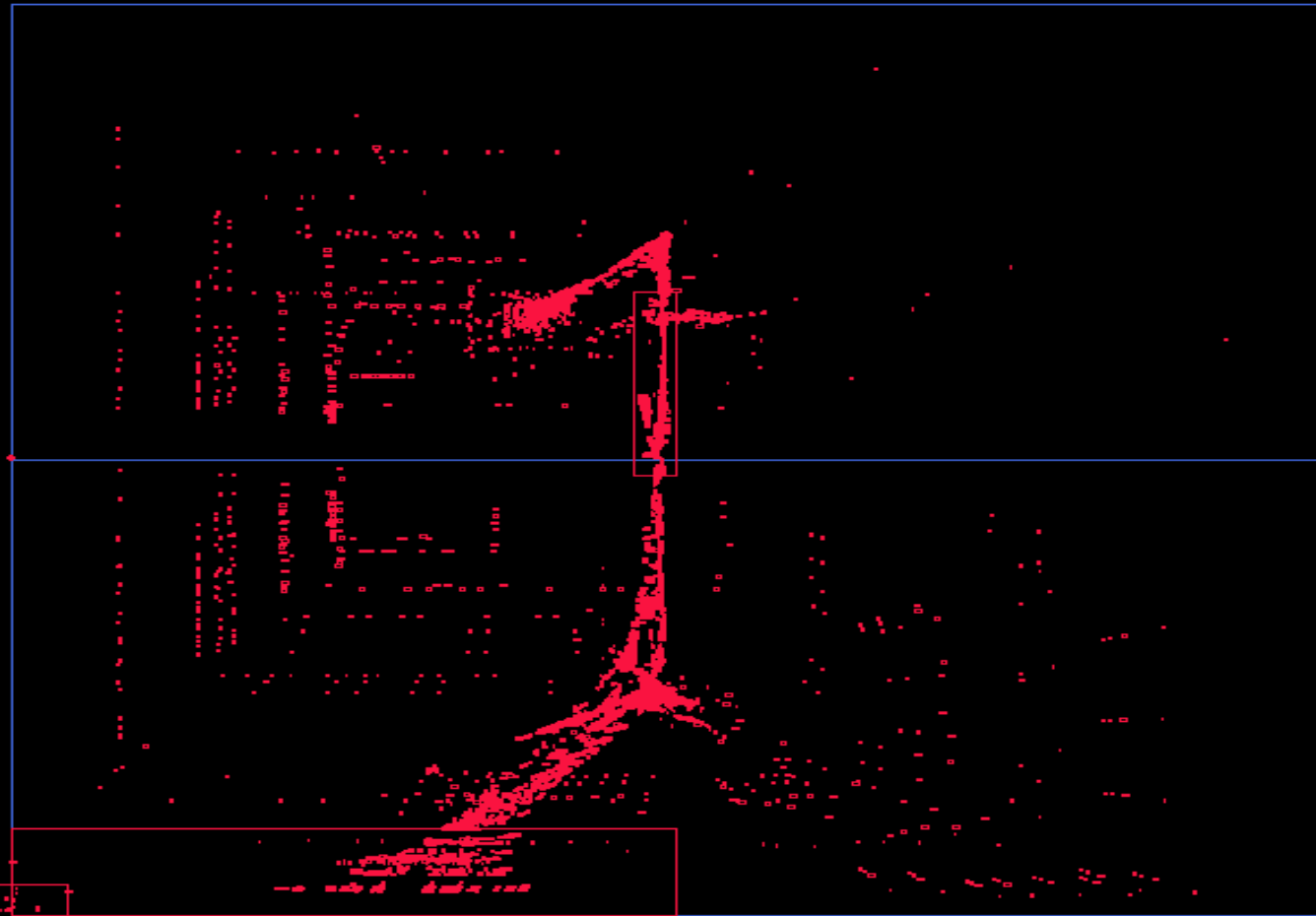
EndCommand

Grid

Tic

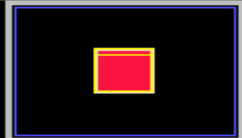
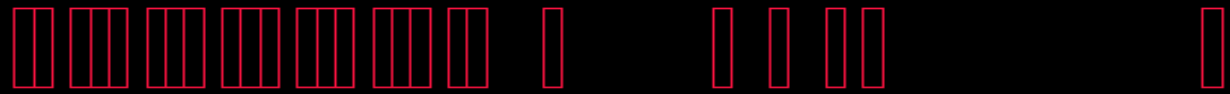
Measure

Query



Select a command
Level PBLK: Visibility altered
Visibility has been altered for more than 1 level, only one modification is listed

Command>



Mag Pan
 ZmIn ZmOut
 Prev Max
 Fit SS

x= 390.2
 y= 5708.2
 rx= 2091.8
 ry= 1803.6
 dx= -1701.6
 dy= 3904.6

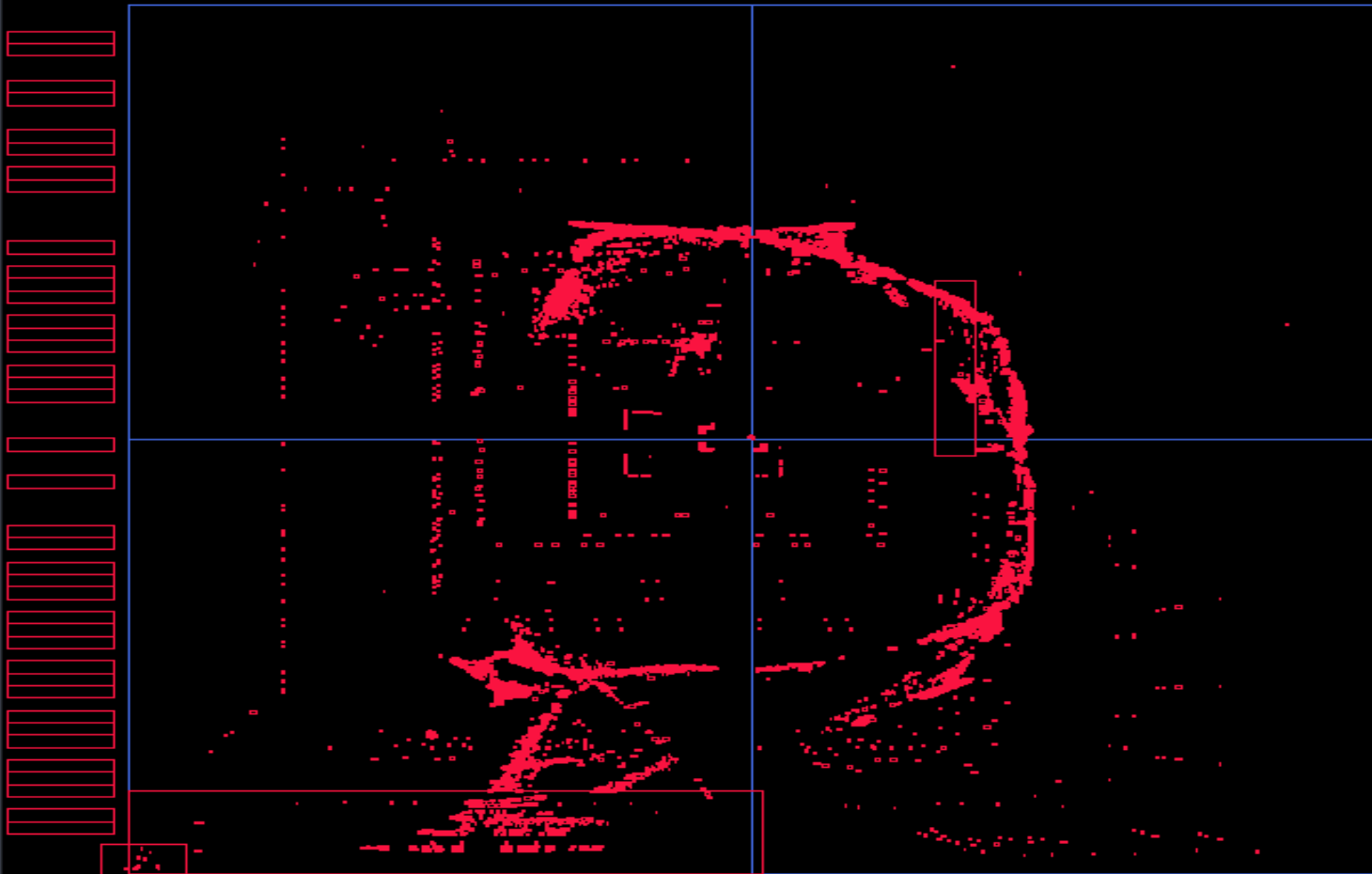
Repaint

EndCommand

Grid
 Tic

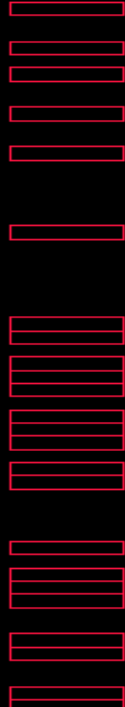
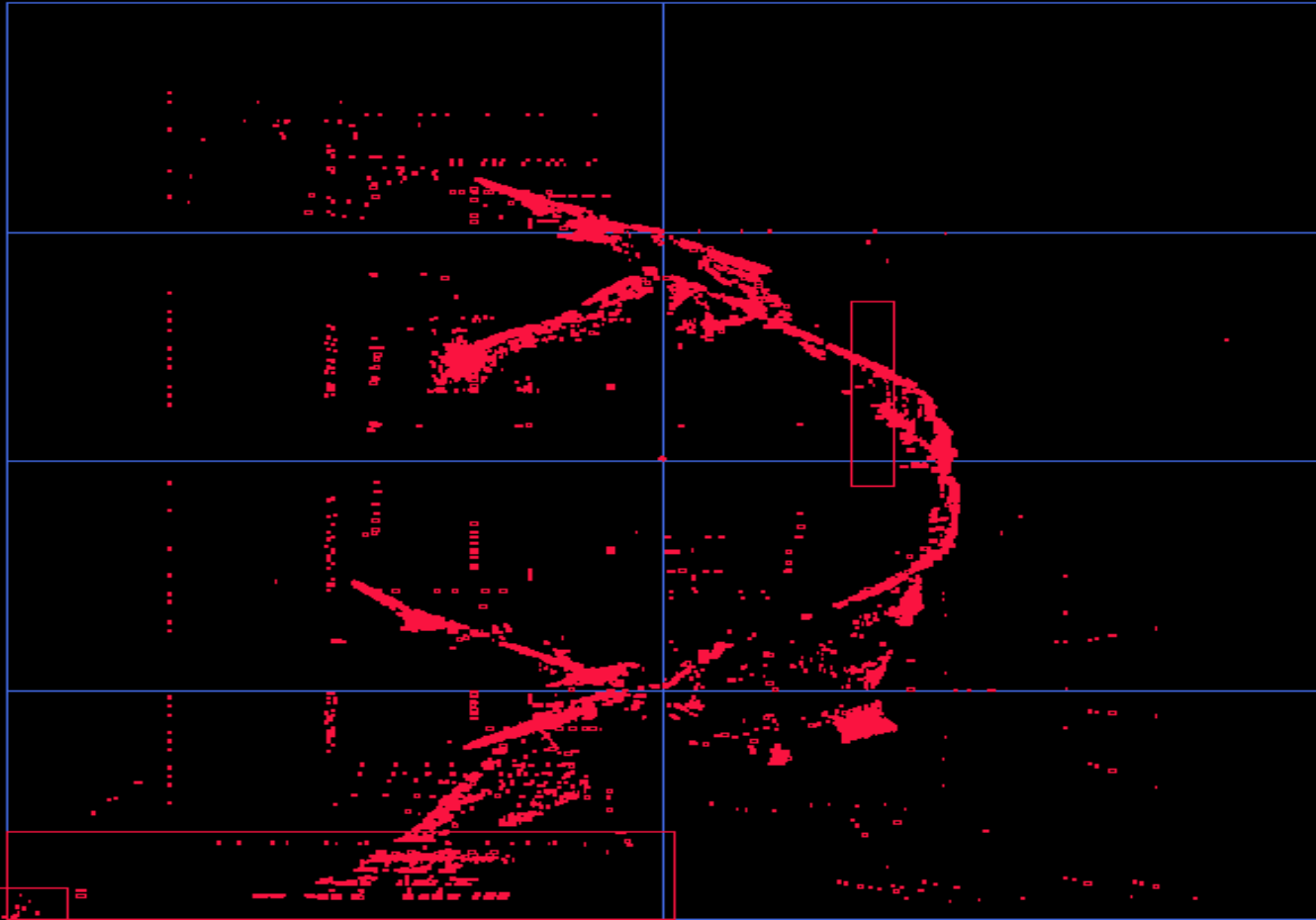
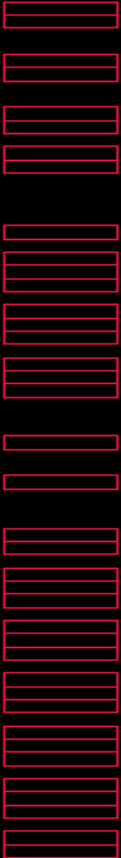
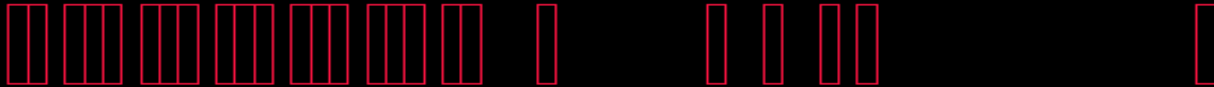
Measure

Query



Select a command
 Level PBLK: Visibility altered
 Visibility has been altered for more than 1 level, only one modification is listed

Command>



Mag Pan

ZmIn ZmOut

Prev Max

Fit SS

x= 27.3
 y= 4870.1
 rx= 2091.8
 ry= 1803.6
 dx= -2064.4
 dy= 3066.5

Repaint

EndCommand

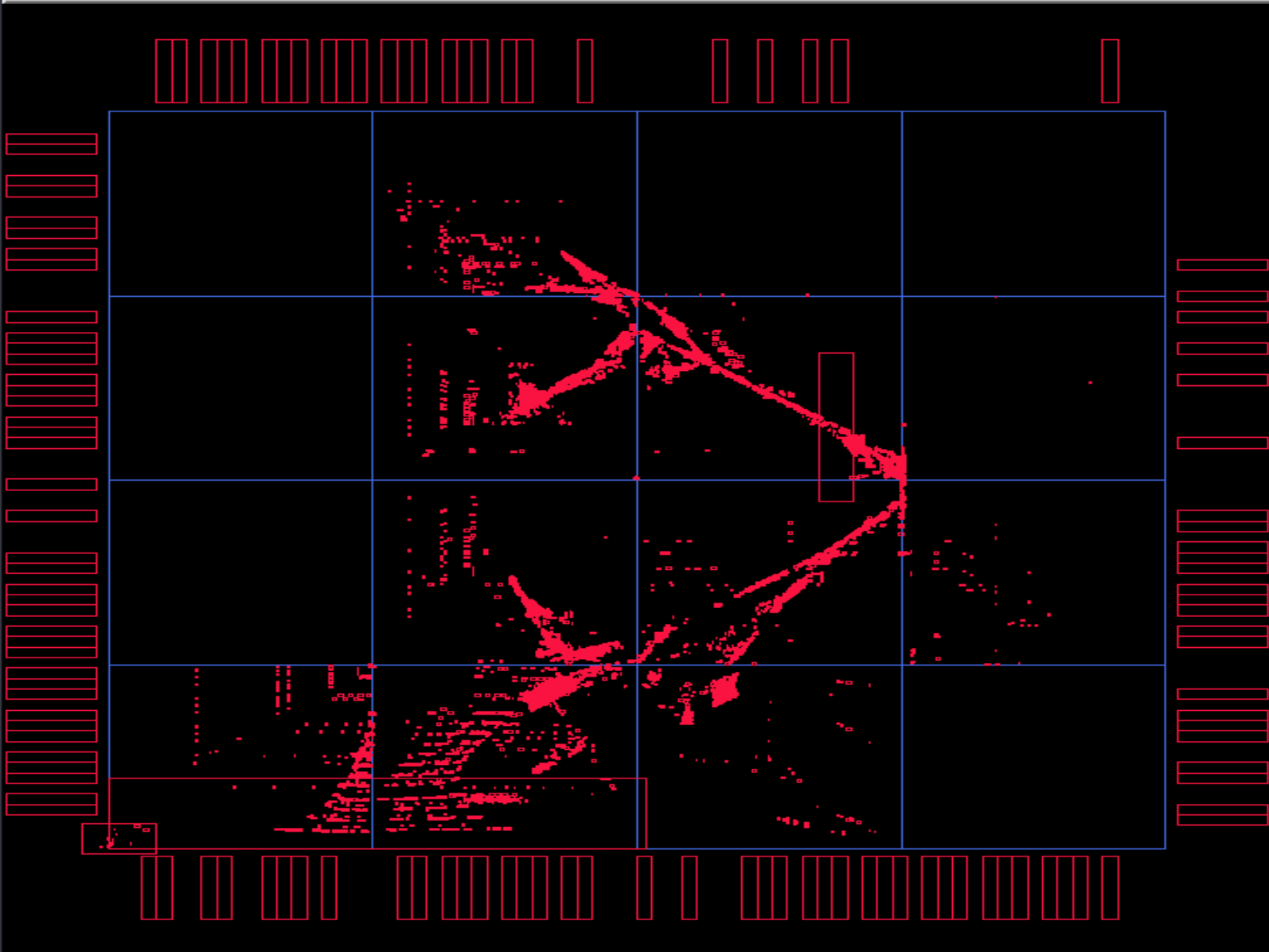
Grid
 Tic

Measure

Query

Select a command
 Level PBLK: Visibility altered
 Visibility has been altered for more than 1 level, only one modification is listed

Command>



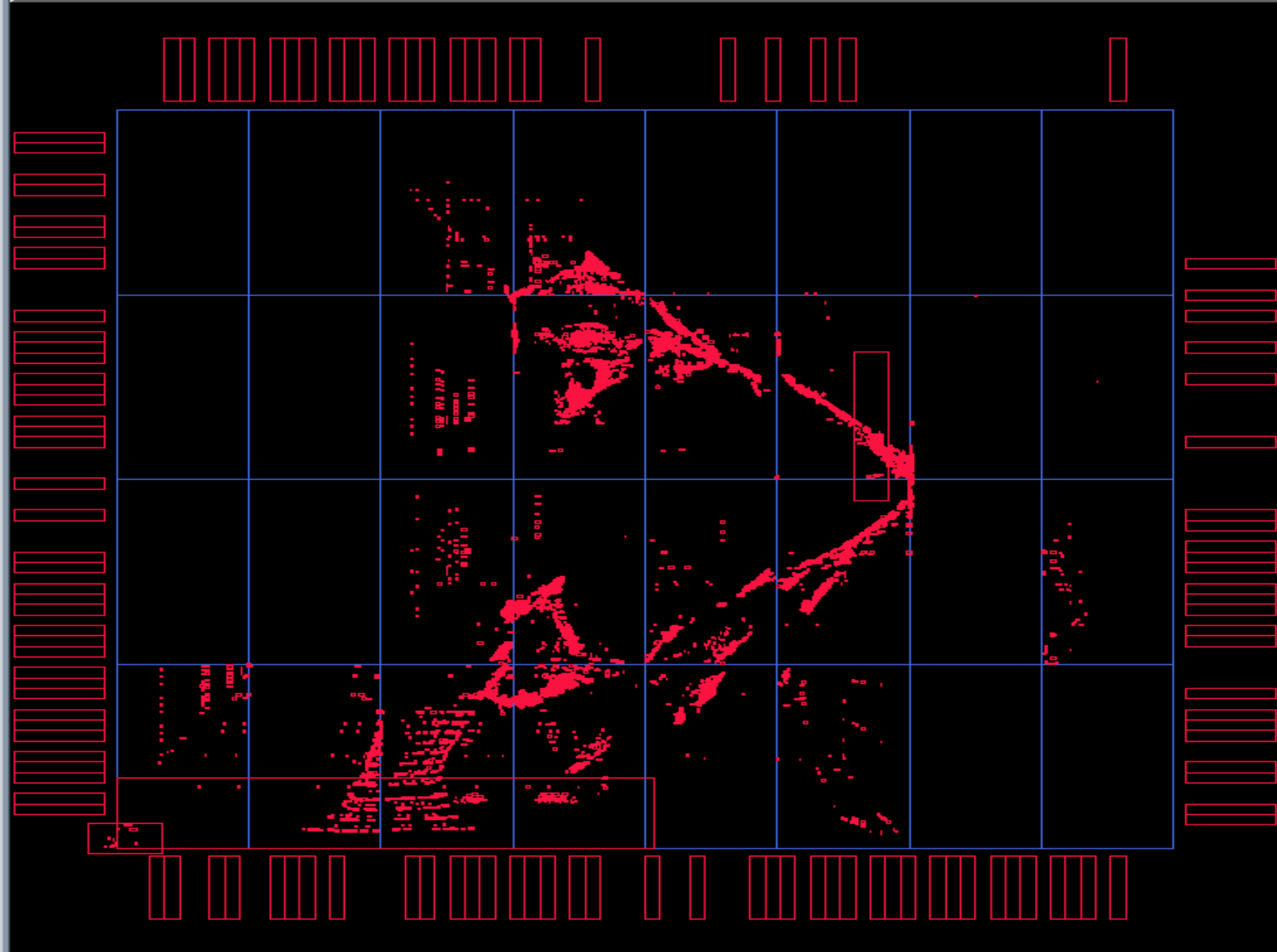
Mag Pan
 ZmIn ZmOut
 Prev Max
 Fit SS

x= 269.2
 y= 5708.2
 rx= 2091.8
 ry= 1803.6
 dx= -1822.6
 dy= 3904.6

Repaint
 EndCommand
 Grid
 Tic
 Measure
 Query

Select a command
 Level PBLK: Visibility altered
 Visibility has been altered for more than 1 level, only one modification is listed

Command>

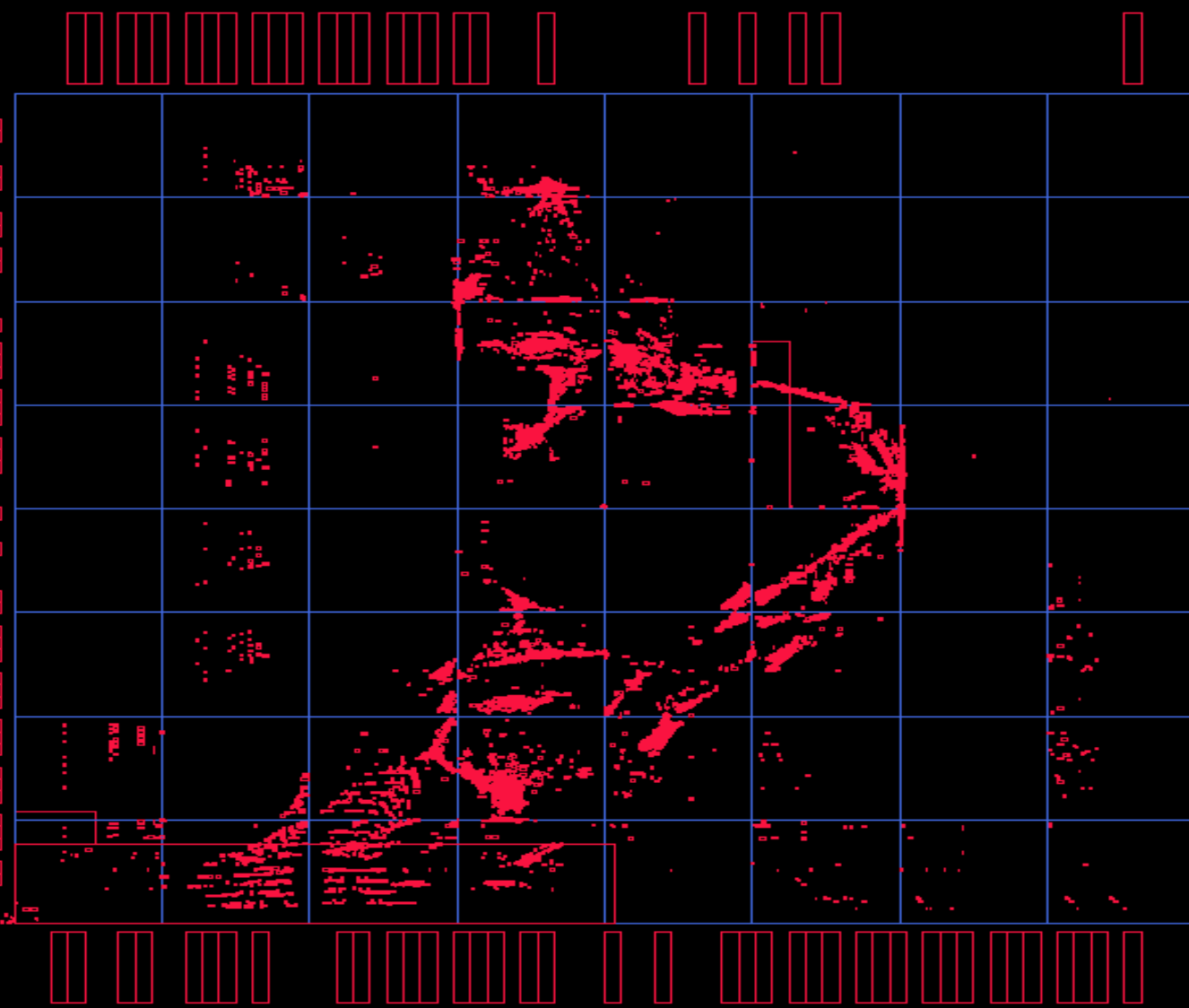


Navigation and control panel:

- Directional arrows (up, down, left, right, and combinations)
- Buttons: Mag, Pan, ZmIn, ZmOut, Prev, Max, Fit, SS
- Coordinate display:
x= 27.3
y= 3513.6
rx= 2091.8
ry= 1803.6
dx= -2064.4
dy= 1710.0
- Buttons: Repaint, EndCommand
- Checkboxes: Grid, Tic
- Buttons: Measure, Query

Select a command
Level PBLK: Visibility altered
Visibility has been altered for more than 1 level, only one modification is listed

Command>



<input type="checkbox"/> Mag	<input type="checkbox"/> Pan
ZmIn	ZmOut
Prev	Max
Fit	SS

x= 27.3
y= 4369.0
rx= 2091.8
ry= 1803.6
dx= -2064.4
dy= 2565.4

Repaint

EndCommand

Grid

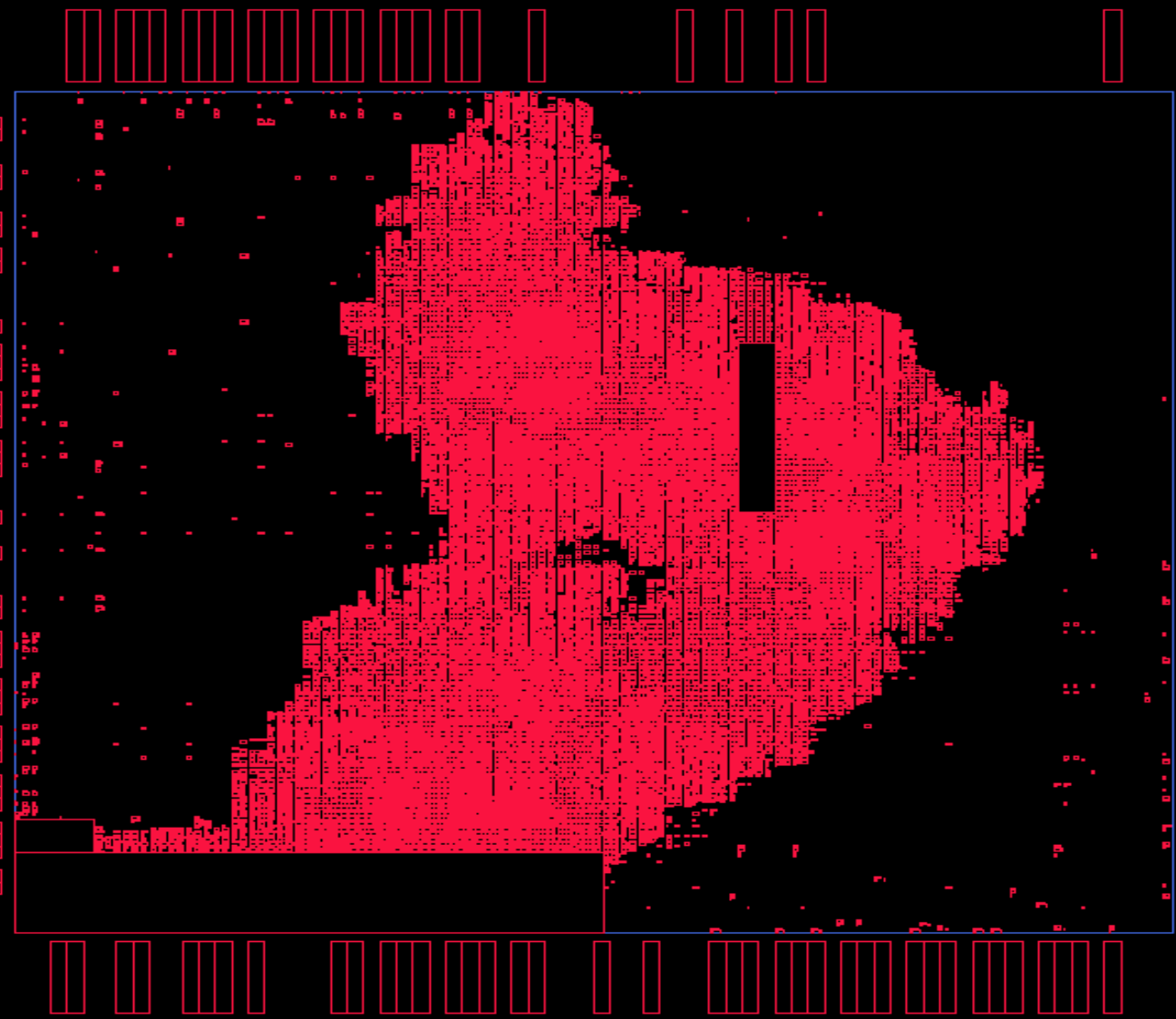
Tic

Measure

Query

Visibility has been altered for more than 1 level, only one modification is listed
Select a command
Level FX: Visibility altered

Command> |



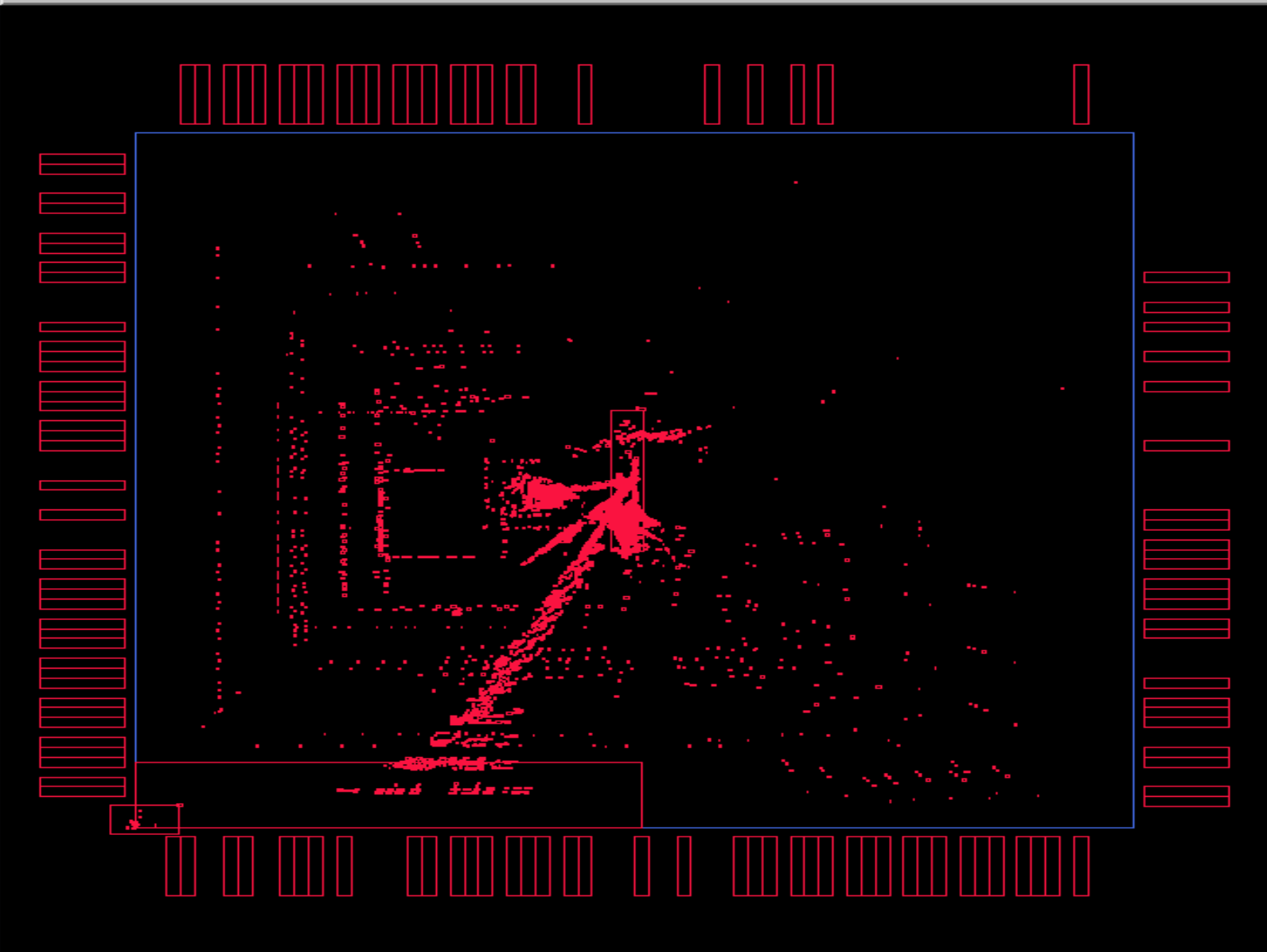
Mag Pan
 ZmIn ZmOut
 Prev Max
 Fit SS

x= 70.5
 y= 4783.7
 rx= 2091.8
 ry= 1803.6
 dx= -2021.2
 dy= 2980.1

Repaint
 EndCommand
 Grid
 Tic
 Measure
 Query

Select a command
 Level PBLK: Visibility altered
 Visibility has been altered for more than 1 level, only one modification is listed

Command>



Help

Navigation icons: a central cross with four arrows pointing outwards, and four corner arrows.

Mag Pan

ZmIn ZmOut

Prev Max

Fit SS

x= 2758.0
y= 6203.6
rx= 2091.8
ry= 1803.6
dx= 666.2
dy= 4400.0

Repaint

EndCommand

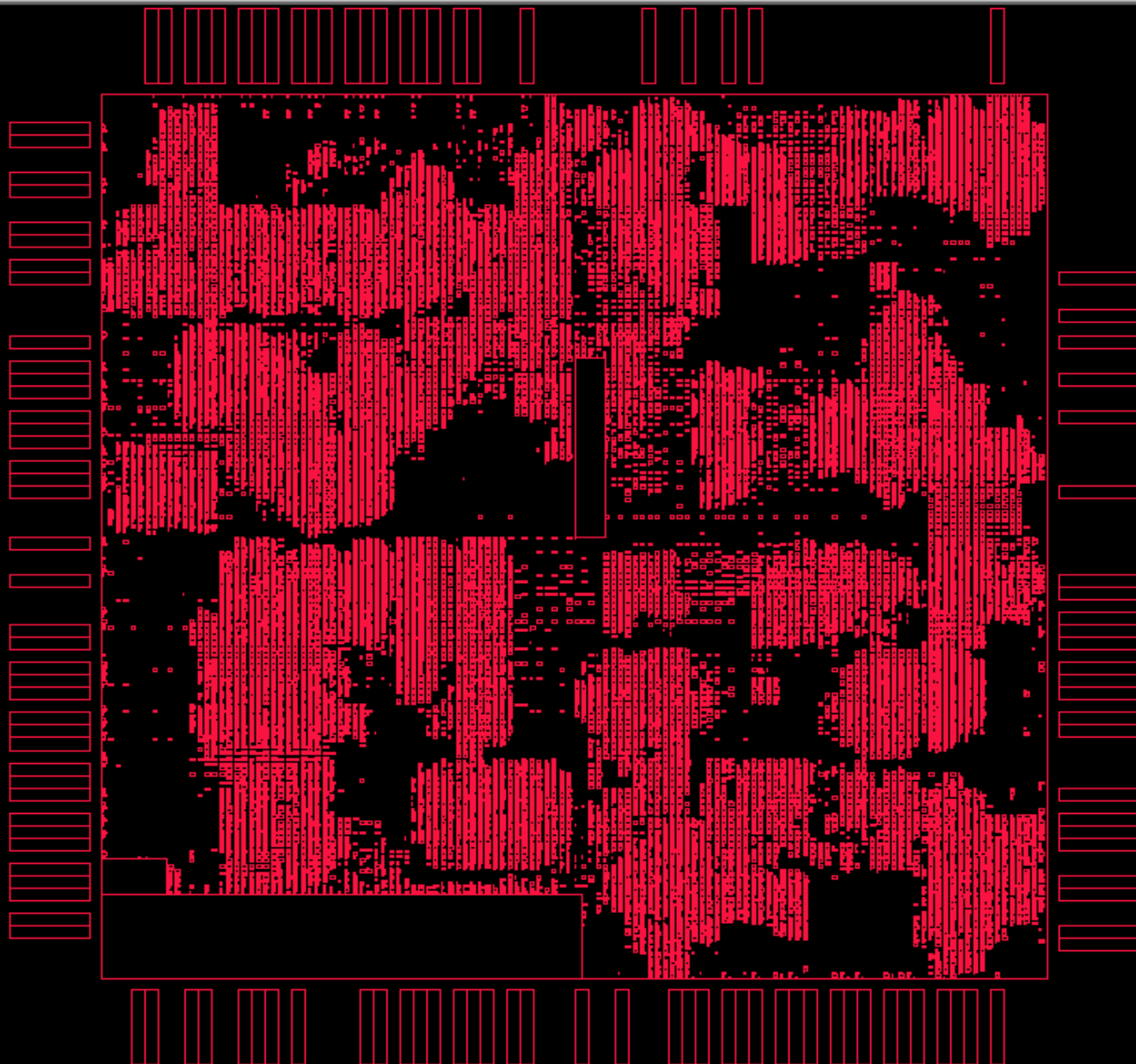
Grid
 Tic

Measure

Query

Select a command
Level PBLK: Visibility altered
Visibility has been altered for more than 1 level, only one modification is listed

Command> |



Navigation and control panel:

- Red square icon
- Navigation arrows (up, down, left, right, center)
- Maq, Pan buttons
- ZmIn, ZmOut buttons
- Prev, Max buttons
- Fit, SS buttons
- Coordinate display: x=-384.0, y=5297.9, rx=0.0, ry=0.0, dx=-384.0, dy=5297.9
- Repaint button
- EndCommand button
- Grid, Tic checkboxes
- Measure button
- Query button

Select a command
Level PBLK: Visibility altered
Visibility has been altered for more than 1 level, only one modification is listed

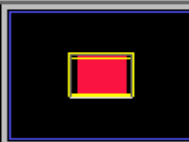
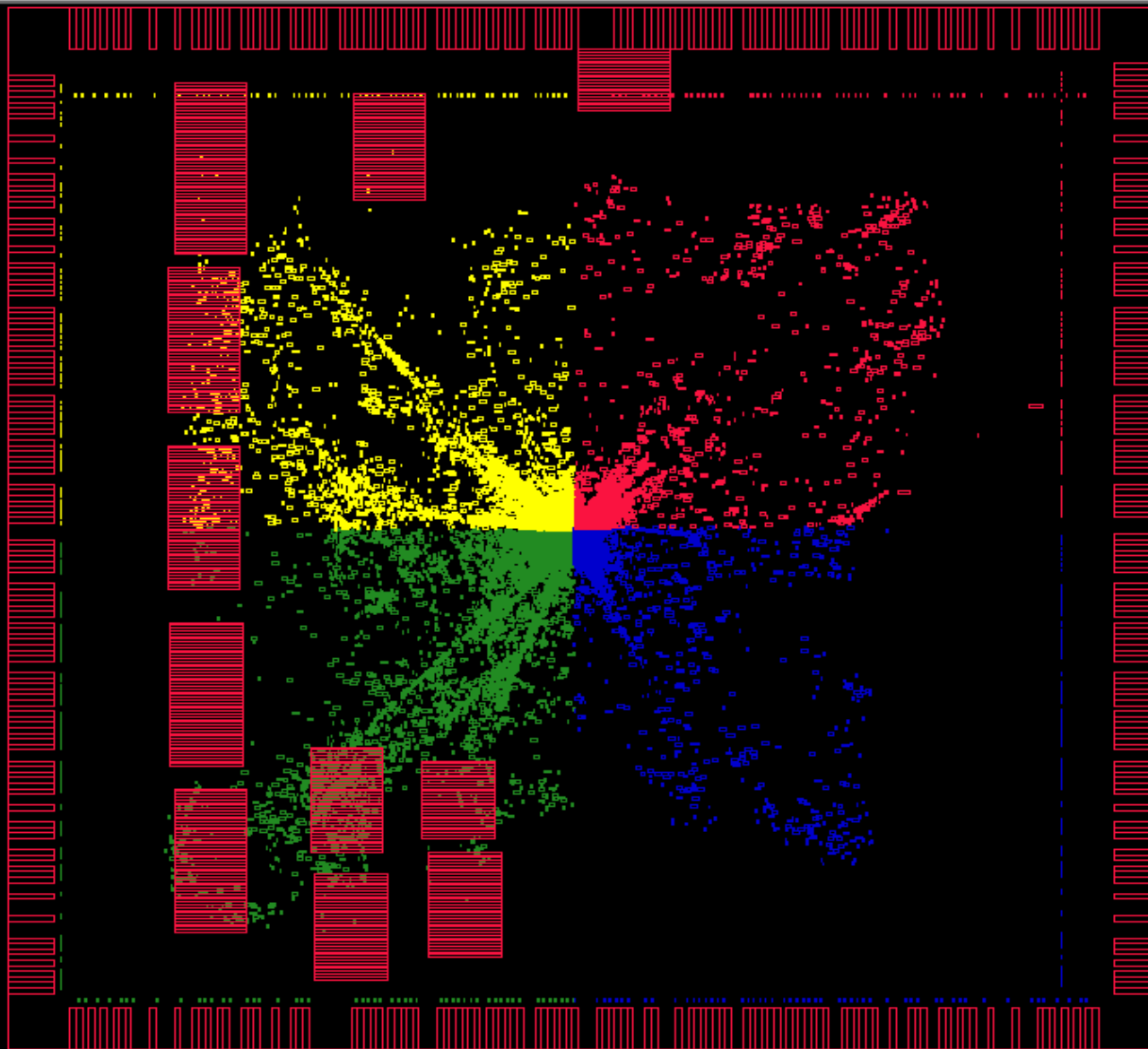
Command>

Geometric Partitioning

J. Vygen, "Algorithms for Large-Scale Flat Placement",
Proc. 34th IEEE/ACM Design Automation Conference, 1988, pp 746-751

File Model Highlight Options Check

Help

 Mag Pan

ZmIn

ZmOut

Prev

Max

Fit

SS

x= 480.5

y= 6032.9

rx= 0.0

ry= 0.0

dx= 480.5

dy= 6032.9

Repaint

EndCommand

 Grid Tic

Measure

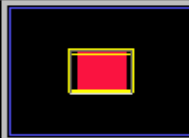
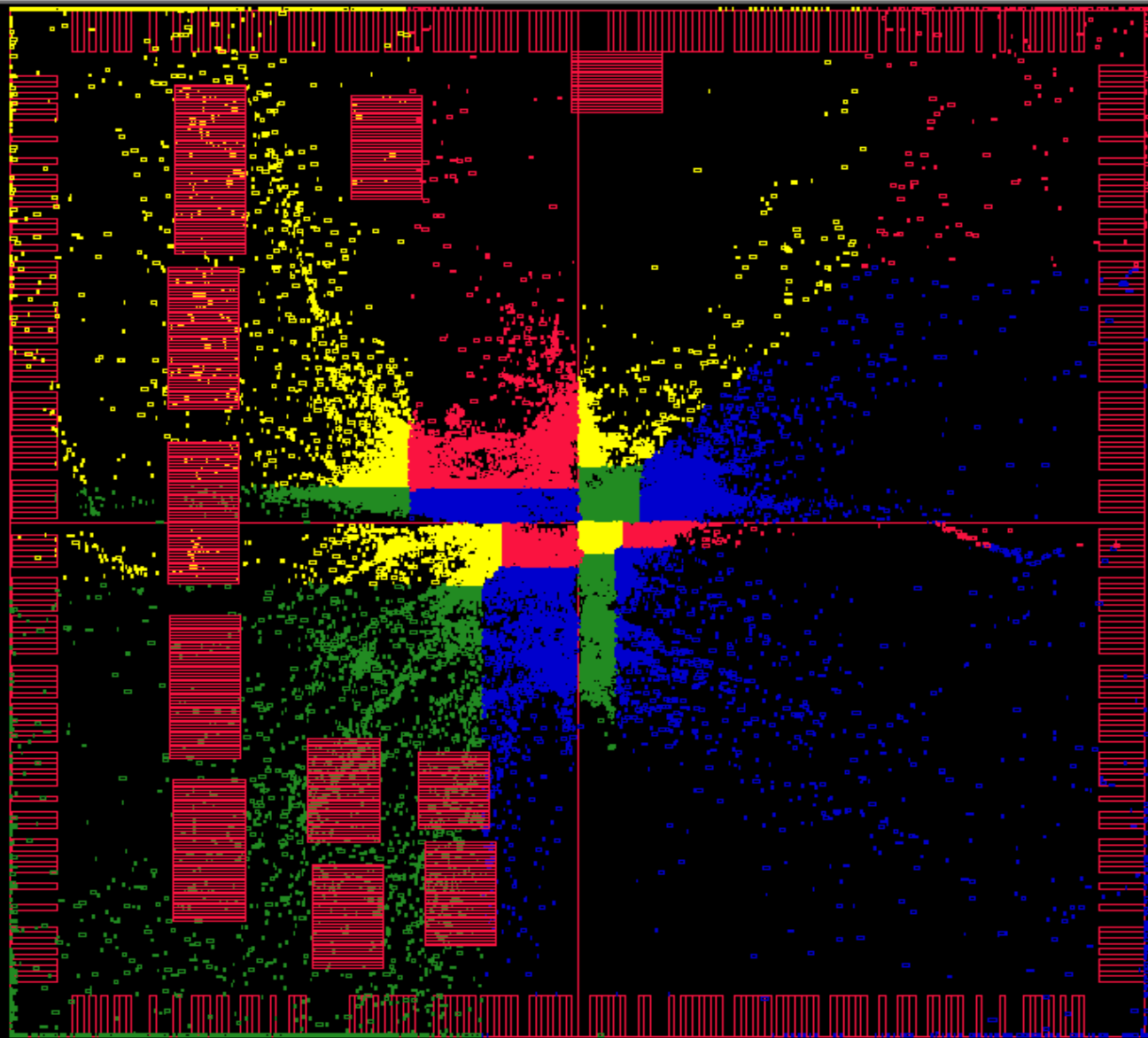
Query

Color has been altered for more than 1 level, only one modification is listed
 Fill has been altered for more than 1 level, only one modification is listed
 Level CKTROW: Visibility altered

Command>

File Model Highlight Options Check

Help

 Mag Pan

ZmIn

ZmOut

Prev

Max

Fit

SS

x= -590.6

y= 6048.9

rx= 0.0

ry= 25.0

dx= -590.6

dy= 6023.9

Repaint

EndCommand

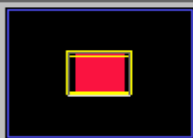
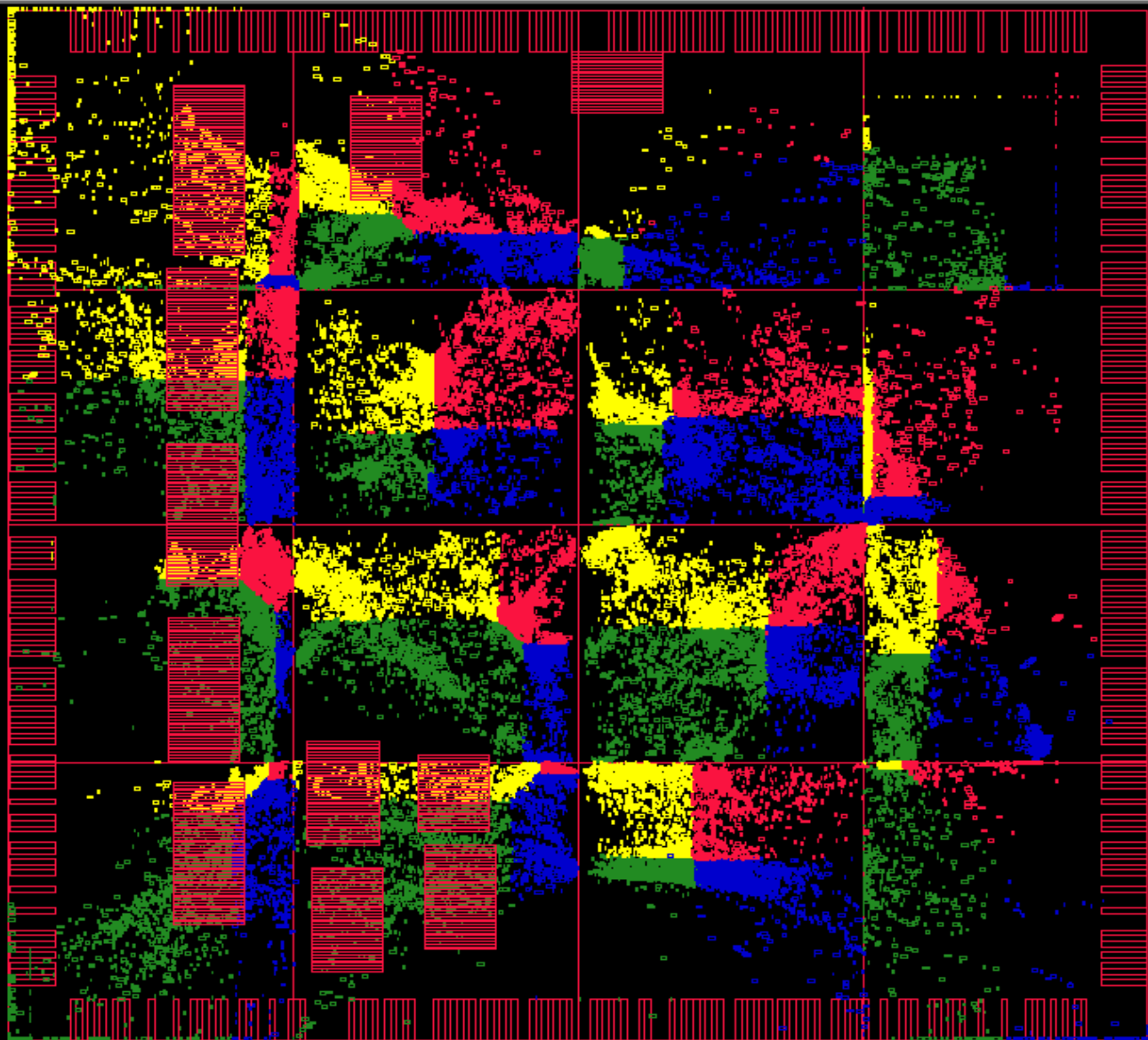
 Grid Tic

Measure

Query

Select a command
Select a command
Level CKTROW: Visibility altered

Command>



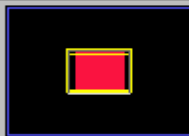
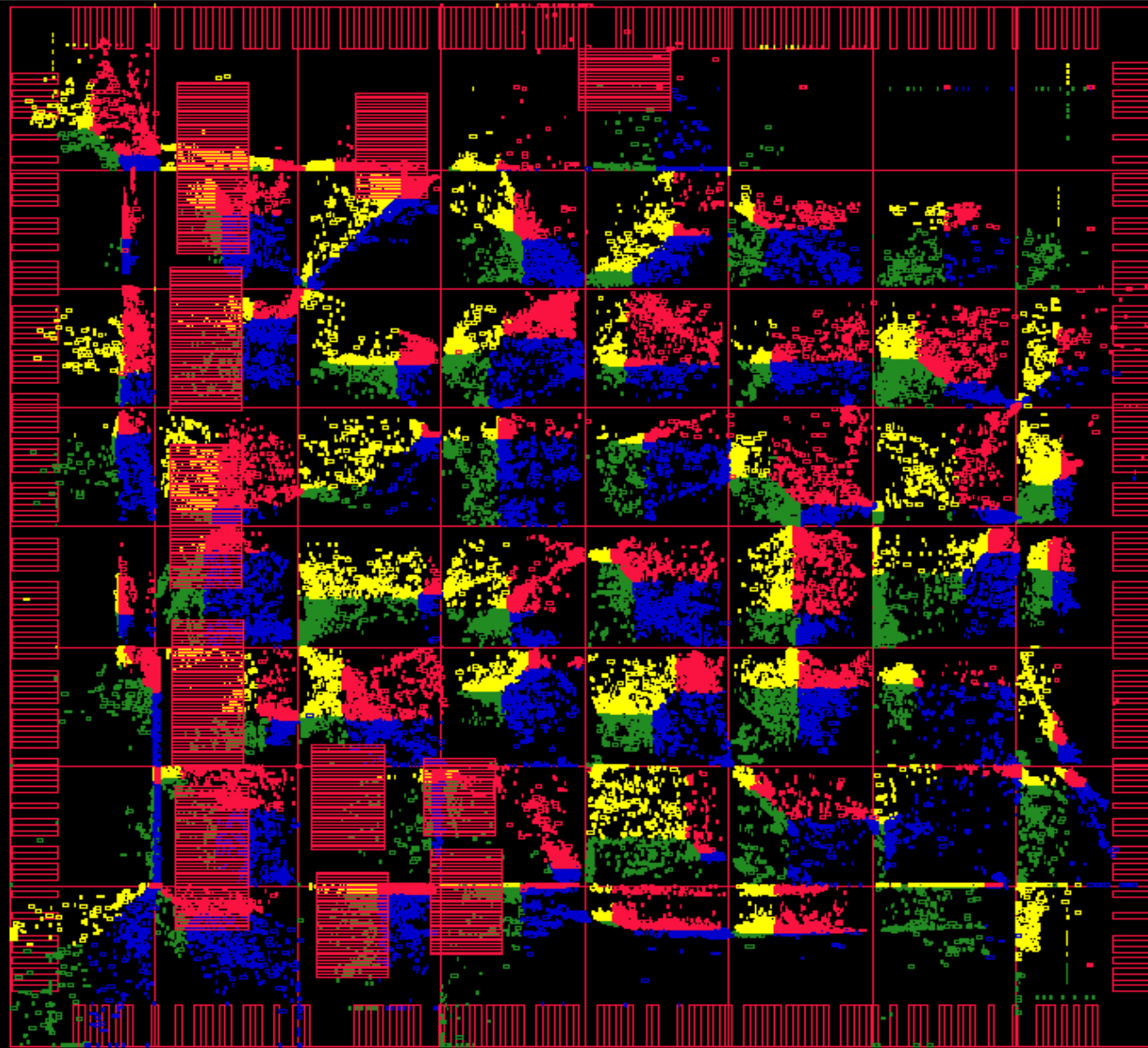
- Mag
- Pan
- ZmIn
- ZmOut
- Prev
- Max
- Fit
- SS

x= -760.2
y= 5816.9
rx= 0.0
ry= 25.0
dx= -760.2
dy= 5791.9

- Repaint
- EndCommand
- Grid
- Tic
- Measure
- Query

Select a command
Select a command
Level CKTROW: Visibility altered

Command>



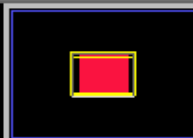
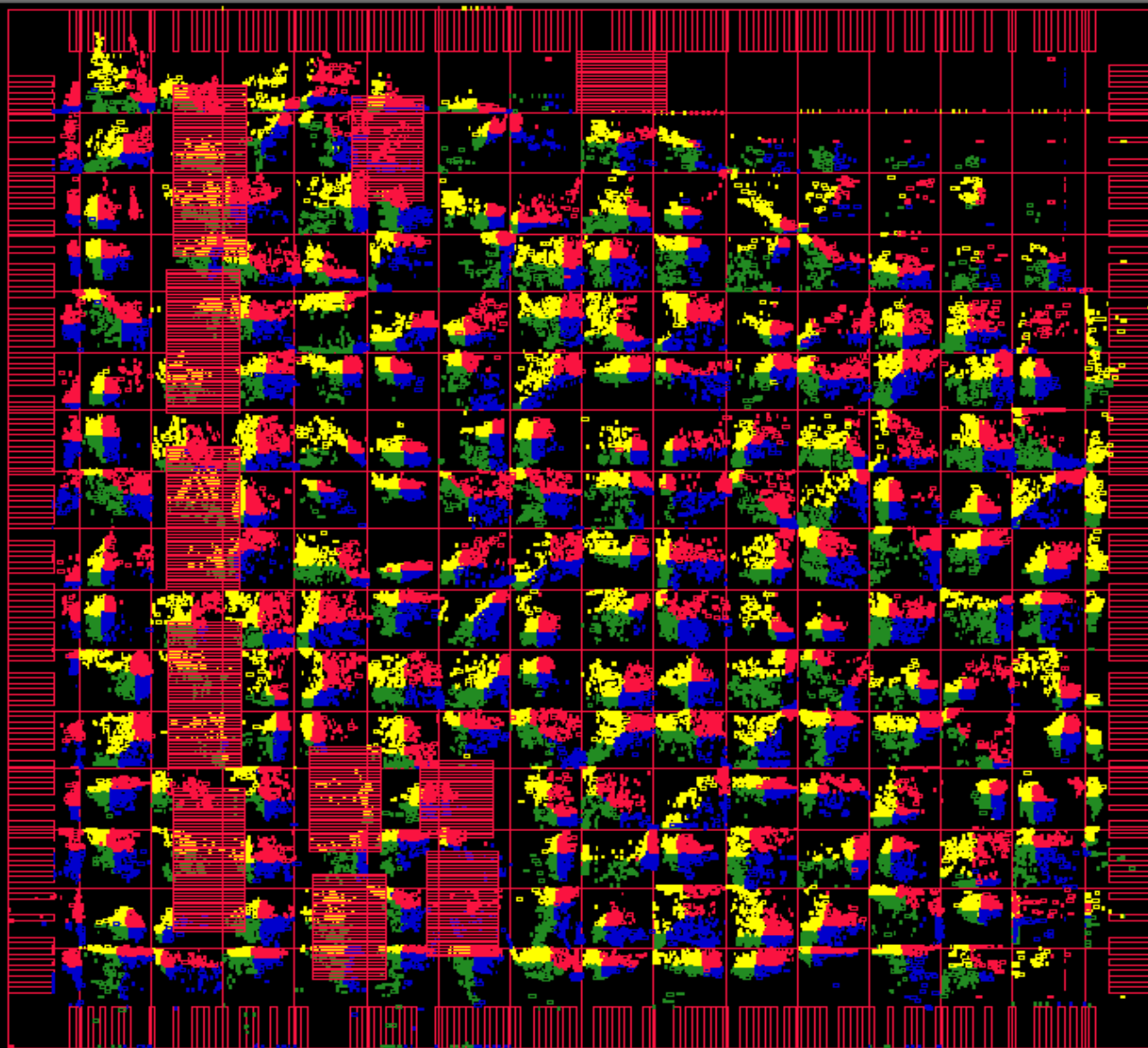
Mag Pan
 ZmIn ZmOut
 Prev Max
 Fit SS

x= -331.8
y= 6048.9
rx= 0.0
ry= 25.0
dx= -331.8
dy= 6023.9

Repaint
EndCommand
 Grid
 Tic
Measure
Query

Select a command
Select a command
Level CKTROW: Visibility altered

Command>



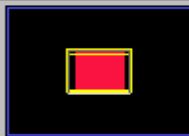
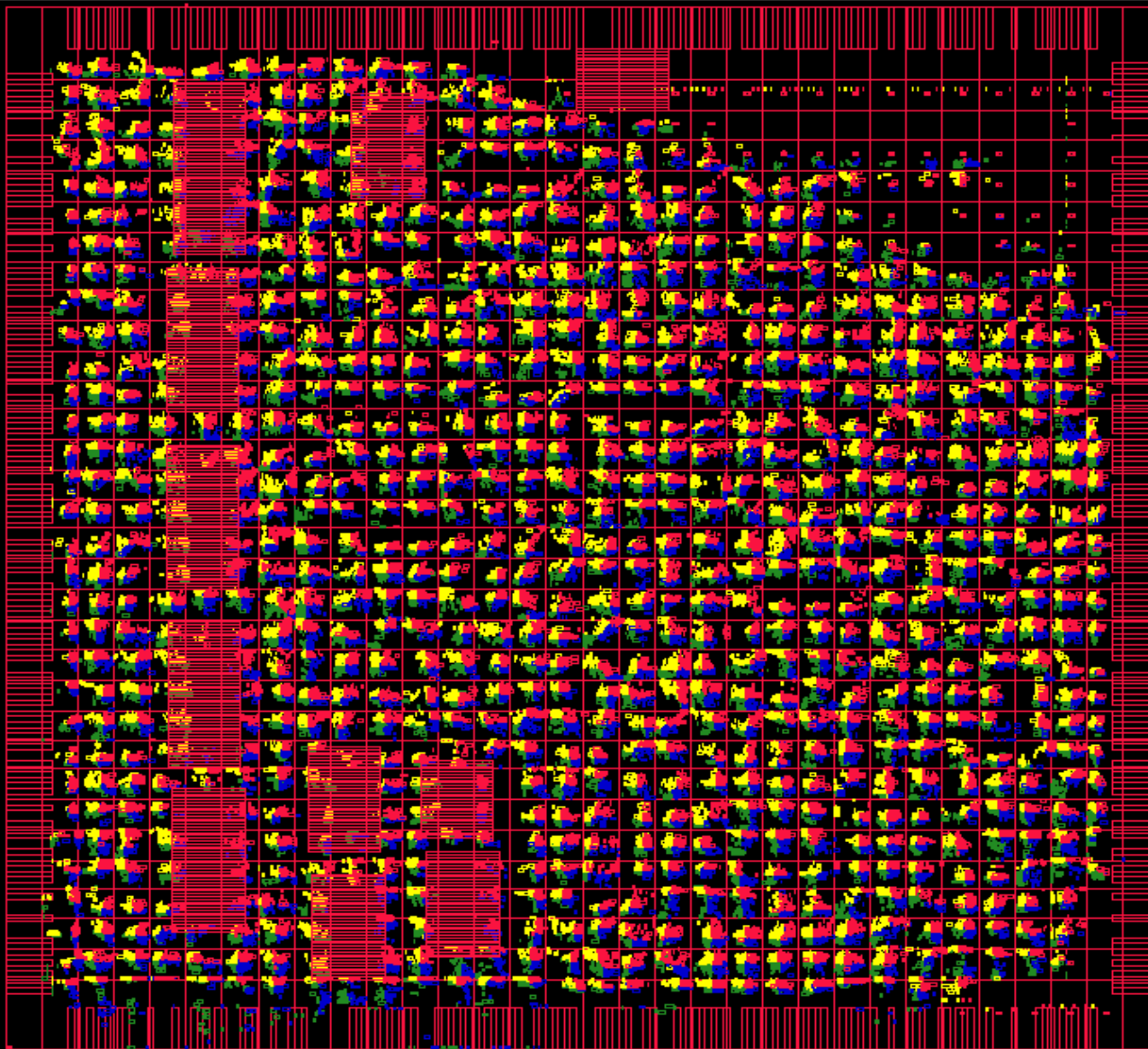
- Mag
- Pan
- ZmIn
- ZmOut
- Prev
- Max
- Fit
- SS

x= -478.2
y= 5906.2
rx= 0.0
ry= 25.0
dx= -478.2
dy= 5881.2

- Repaint
- EndCommand
- Grid
- Tic
- Measure
- Query

Select a command
Select a command
Level CKTROW: Visibility altered

Command>



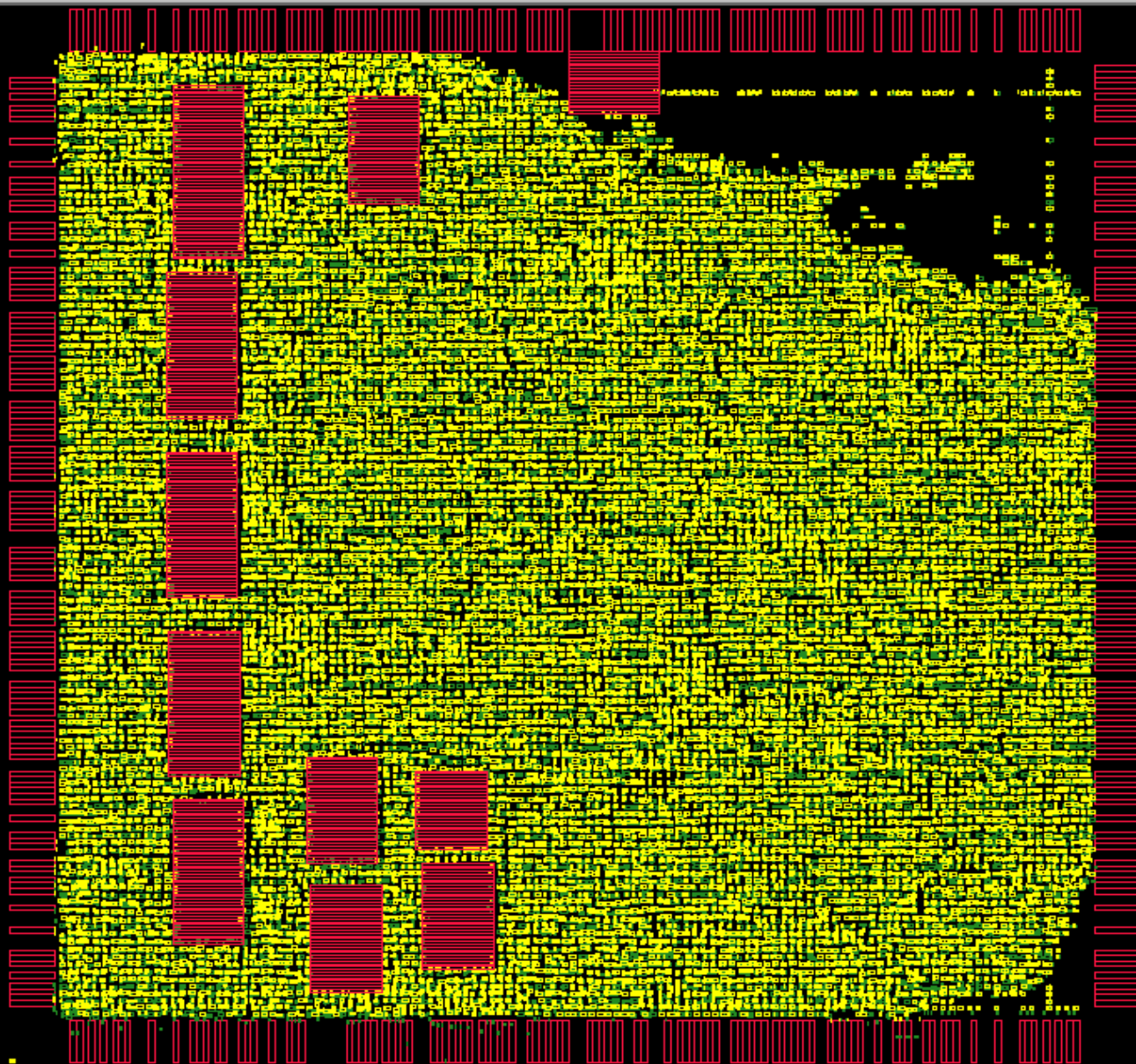
Mag Pan
 ZmIn ZmOut
 Prev Max
 Fit SS

x= -614.7
y= 5950.8
rx= 0.0
ry= 25.0
dx= -614.7
dy= 5925.8

Grid
 Tic

Select a command
Select a command
Level CKTROW: Visibility altered

Command>



<input type="checkbox"/> Mag	<input type="checkbox"/> Pan
ZmIn	ZmOut
Prev	Max
Fit	SS

x= -275.8
 y= 6032.9
 rx= 0.0
 ry= 25.0
 dx= -275.8
 dy= 6007.9

Repaint

EndCommand

Grid
 Tic

Measure

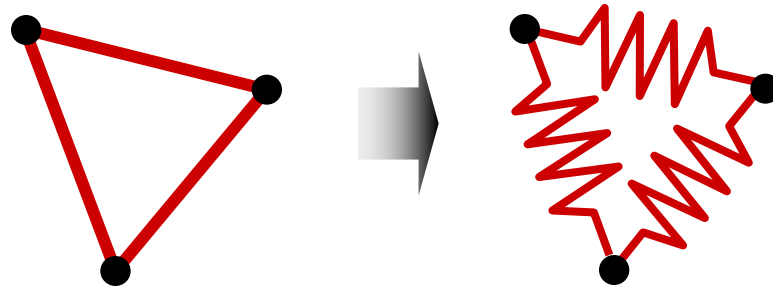
Query

Select a command
 Level BOUNDARY: Visibility altered
 Visibility has been altered for more than 1 level, only one modification is listed

Command>

Analytic Placement – Force-directed Placement

- Cells and wires are modeled using the mechanical analogy of a mass-spring system, i.e., masses connected to Hooke's-Law springs



- Attraction force between cells is directly proportional to their distance
- Cells will eventually settle in a **force equilibrium**
 - minimized wirelength

Analytic Placement – Force-directed Placement

- Given two connected cells a and b , the attraction force \vec{F}_{ab} exerted on a by b is

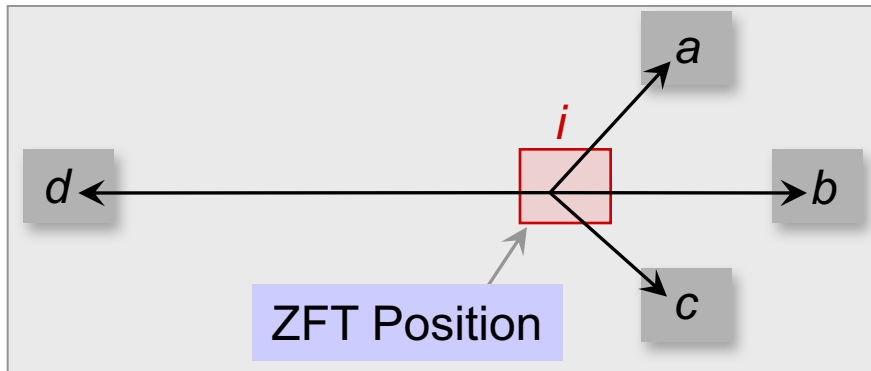
$$\vec{F}_{ab} = c(a, b) \cdot (\vec{b} - \vec{a})$$

where

- $c(a, b)$ is the connection weight (priority) between cells a and b , and
 - $(\vec{b} - \vec{a})$ is the vector difference of the positions of a and b in the Euclidean plane
-
- The sum of forces exerted on a cell i connected to other cells $1 \dots j$ is
$$\vec{F}_i = \sum_{c(i, j) \neq 0} \vec{F}_{ij}$$
 - **Zero-force target (ZFT):** position that minimizes this sum of forces

Analytic Placement – Force-directed Placement

Zero-Force-Target (ZFT) position of cell i



$$\min \vec{F}_i = c(i,a) \cdot (\vec{a} - \vec{i}) + c(i,b) \cdot (\vec{b} - \vec{i}) + c(i,c) \cdot (\vec{c} - \vec{i}) + c(i,d) \cdot (\vec{d} - \vec{i})$$

Analytic Placement – Force-directed Placement

Basic force-directed placement

- Iteratively moves all cells to their respective ZFT positions

- x- and y-direction forces are set to zero:

$$\sum_{c(i,j) \neq 0} c(i,j) \cdot (x_j^0 - x_i^0) = 0 \quad \sum_{c(i,j) \neq 0} c(i,j) \cdot (y_j^0 - y_i^0) = 0$$

- Rearranging the variables to solve for x_i^0 and y_i^0 yields

$$x_i^0 = \frac{\sum_{c(i,j) \neq 0} c(i,j) \cdot x_j^0}{\sum_{c(i,j) \neq 0} c(i,j)}$$

$$y_i^0 = \frac{\sum_{c(i,j) \neq 0} c(i,j) \cdot y_j^0}{\sum_{c(i,j) \neq 0} c(i,j)}$$

Computation of ZFT position of cell i connected with cells 1 ... j

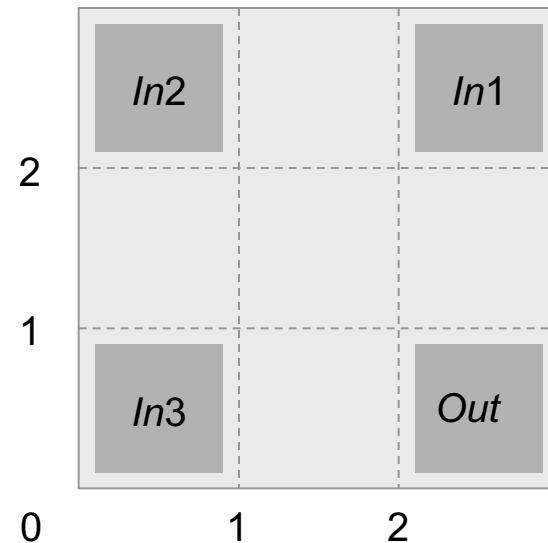
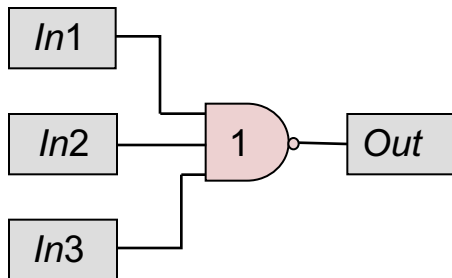
Analytic Placement – Force-directed Placement

Example: ZFT position

Given:

- Circuit with NAND gate 1 and four I/O pads on a 3 x 3 grid
- Pad positions: $In1$ (2,2), $In2$ (0,2), $In3$ (0,0), Out (2,0)
- Weighted connections: $c(a, In1) = 8$, $c(a, In2) = 10$, $c(a, In3) = 2$, $c(a, Out) = 2$

Task: find the ZFT position of cell a



Analytic Placement – Force-directed Placement

Example: ZFT position

Given:

- Circuit with NAND gate 1 and four I/O pads on a 3 x 3 grid
- Pad positions: $In1$ (2,2), $In2$ (0,2), $In3$ (0,0), Out (2,0)

Solution:

$$x_a^0 = \frac{\sum_{c(i,j) \neq 0} c(a,j) \cdot x_j^0}{\sum_{c(i,j) \neq 0} c(a,j)} = \frac{c(a, In1) \cdot x_{In1} + c(a, In2) \cdot x_{In2} + c(a, In3) \cdot x_{In3} + c(a, Out) \cdot x_{Out}}{c(a, In1) + c(a, In2) + c(a, In3) + c(a, Out)} = \frac{8 \cdot 2 + 10 \cdot 0 + 2 \cdot 0 + 2 \cdot 2}{8 + 10 + 2 + 2} = \frac{20}{22} \approx 0.9$$

$$y_a^0 = \frac{\sum_{c(i,j) \neq 0} c(a,j) \cdot y_j^0}{\sum_{c(i,j) \neq 0} c(a,j)} = \frac{c(a, In1) \cdot y_{In1} + c(a, In2) \cdot y_{In2} + c(a, In3) \cdot y_{In3} + c(a, Out) \cdot y_{Out}}{c(a, In1) + c(a, In2) + c(a, In3) + c(a, Out)} = \frac{8 \cdot 2 + 10 \cdot 2 + 2 \cdot 0 + 2 \cdot 0}{8 + 10 + 2 + 2} = \frac{36}{22} \approx 1.6$$

ZFT position of cell a is (1,2)

Analytic Placement – Force-directed Placement

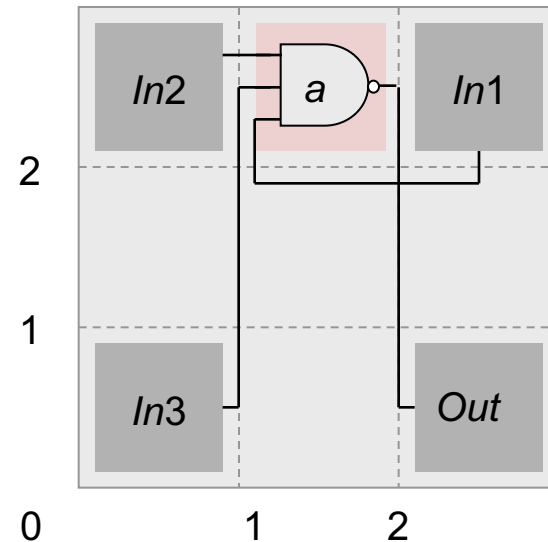
Example: ZFT position

Given:

- Circuit with NAND gate 1 and four I/O pads on a 3 x 3 grid
- Pad positions: $In1$ (2,2), $In2$ (0,2), $In3$ (0,0), Out (2,0)

Solution:

ZFT position of cell a is (1,2)



Analytic Placement – Force-directed Placement

Input: set of all cells V

Output: placement P

```
P = PLACE(V)
loc = LOCATIONS(P)
foreach (cell c ∈ V)
    status[c] = UNMOVED
while (ALL_MOVED(V) || !STOP())

    c = MAX_DEGREE(V,status)

    ZFT_pos = ZFT_POSITION(c)
    if (loc[ZFT_pos] == ∅)
        loc[ZFT_pos] = c
    else
        RELOCATE(c,loc)
    status[c] = MOVED
```

// arbitrary initial placement
// set coordinates for each cell in P

// continue until all cells have been
// moved or some stopping
// criterion is reached
// unmoved cell that has largest
// number of connections
// ZFT position of c
// if position is unoccupied,
// move c to its ZFT position

// use methods discussed next
// mark c as moved

Analytic Placement – Force-directed Placement

- Finding a valid location for a cell with an occupied ZFT position (p : incoming cell, q : cell in p 's ZFT position)
- If possible, move p to a cell position close to q .
- Chain move: cell p is moved to cells q 's location.
 - Cell q , in turn, is shifted to the next position. If a cell r is occupying this space, cell r is shifted to the next position.
 - This continues until all affected cells are placed.
- Compute the cost difference if p and q were to be swapped. If the total cost reduces, i.e., the weighted connection length $L(P)$ is smaller, then swap p and q .

Analytic Placement – Force-directed Placement (Example)

Given:

Nets

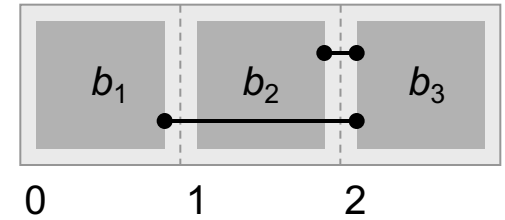
$$N_1 = (b_1, b_3)$$

$$N_2 = (b_2, b_3)$$

Weight

$$c(N_1) = 2$$

$$c(N_2) = 1$$



Analytic Placement – Force-directed Placement (Example)

Given:

Nets

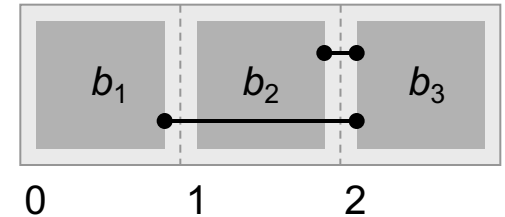
$$N_1 = (b_1, b_3)$$

$$N_2 = (b_2, b_3)$$

Weight

$$c(N_1) = 2$$

$$c(N_2) = 1$$



Incoming cell p

ZFT position of cell p

Cell q

$L(P)$ before move

$L(P)$ / placement after move

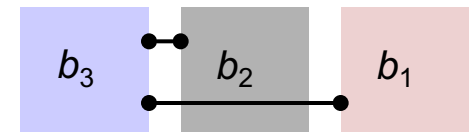
b_3

$$x_{b_3}^0 = \frac{\sum_{c(b_3,j) \neq 0} c(b_3,j) \cdot x_j^0}{\sum_{c(b_3,j) \neq 0} c(b_3,j)} = \frac{2 \cdot 0 + 1 \cdot 1}{2 + 1} \approx 0$$

b_1

$$L(P) = 5$$

$$L(P) = 5$$



\Rightarrow No swapping of b_3 and b_1

Analytic Placement – Force-directed Placement (Example)

Given:

Nets

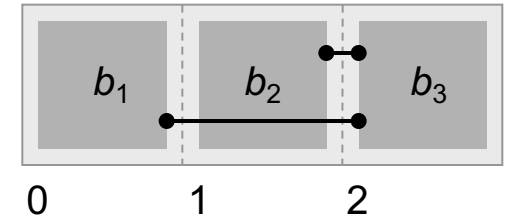
$$N_1 = (b_1, b_3)$$

$$N_2 = (b_2, b_3)$$

Weight

$$c(N_1) = 2$$

$$c(N_2) = 1$$

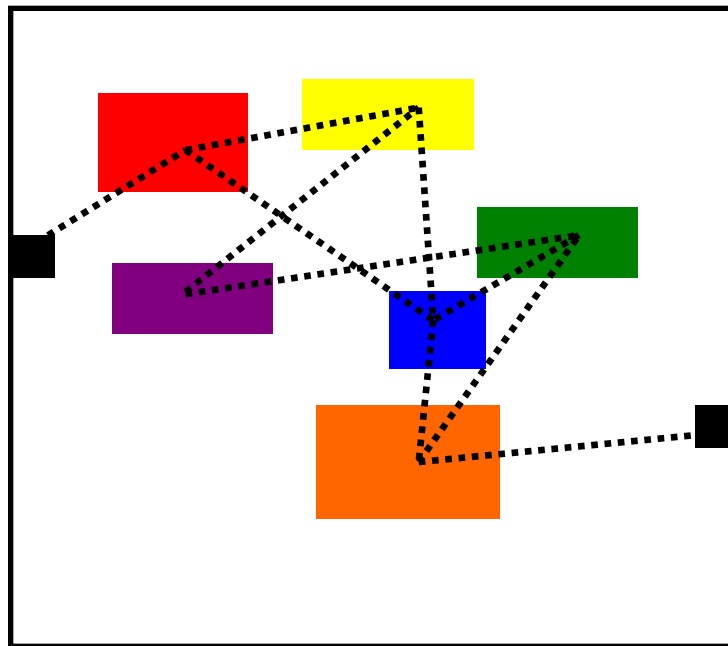


Incoming cell p	ZFT position of cell p	Cell q	$L(P)$ before move	$L(P)$ / placement after move
b_3	$x_{b_3}^0 = \frac{\sum_{c(b_3,j) \neq 0} c(b_3,j) \cdot x_j^0}{\sum_{c(b_3,j) \neq 0} c(b_3,j)} = \frac{2 \cdot 0 + 1 \cdot 1}{2 + 1} \approx 0$	b_1	$L(P) = 5$	$L(P) = 5$ <p>→ No swapping of b_3 and b_1</p>
b_2	$x_{b_2}^0 = \frac{\sum_{c(b_2,j) \neq 0} c(b_2,j) \cdot x_j^0}{\sum_{c(b_2,j) \neq 0} c(b_2,j)} = \frac{1 \cdot 2}{1} = 2$	b_3	$L(P) = 5$	$L(P) = 3$ <p>→ Swapping of b_2 and b_3</p>

FDP Flow

(1)

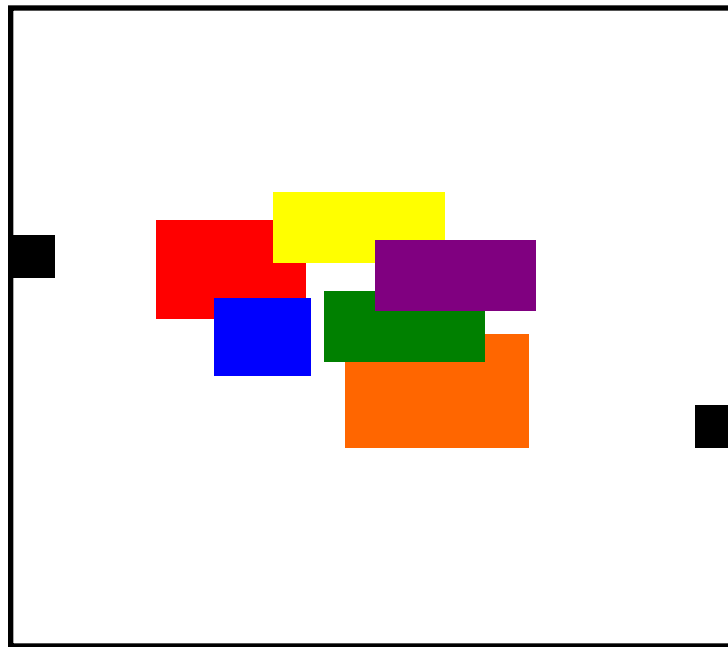
- 6 Movable Objects
- 2 PIOs
- Connections between objects (Nets)



FDP Flow

(2)

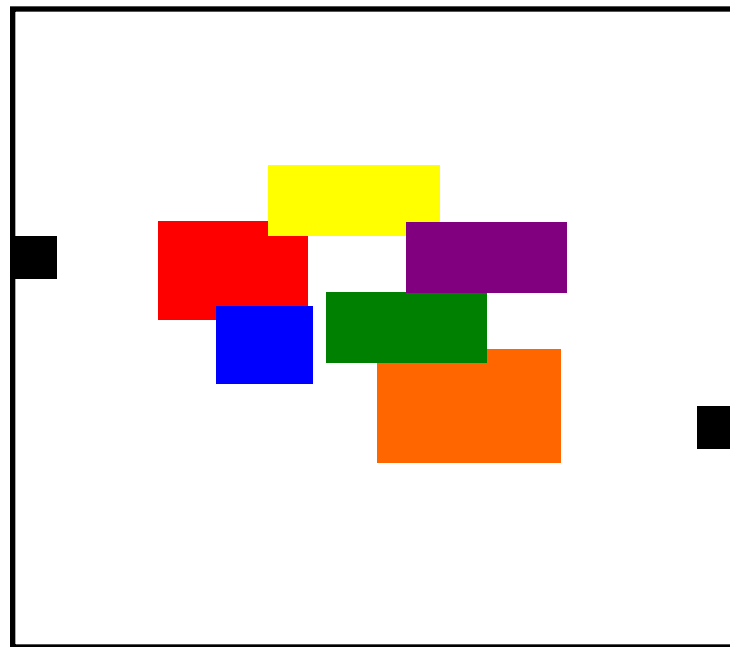
Step 1: Solve convex quadratic program



FDP Flow

(3)

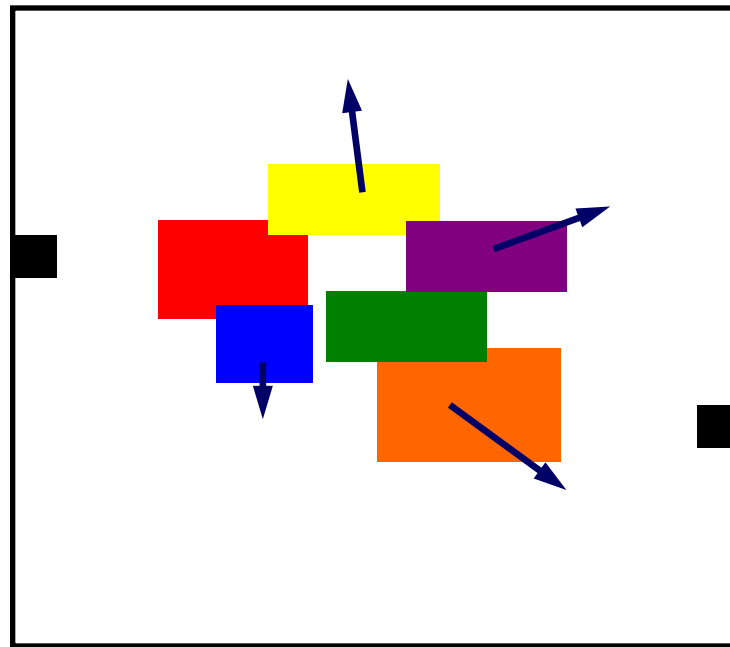
Step 2: Spread objects to reduce overlap



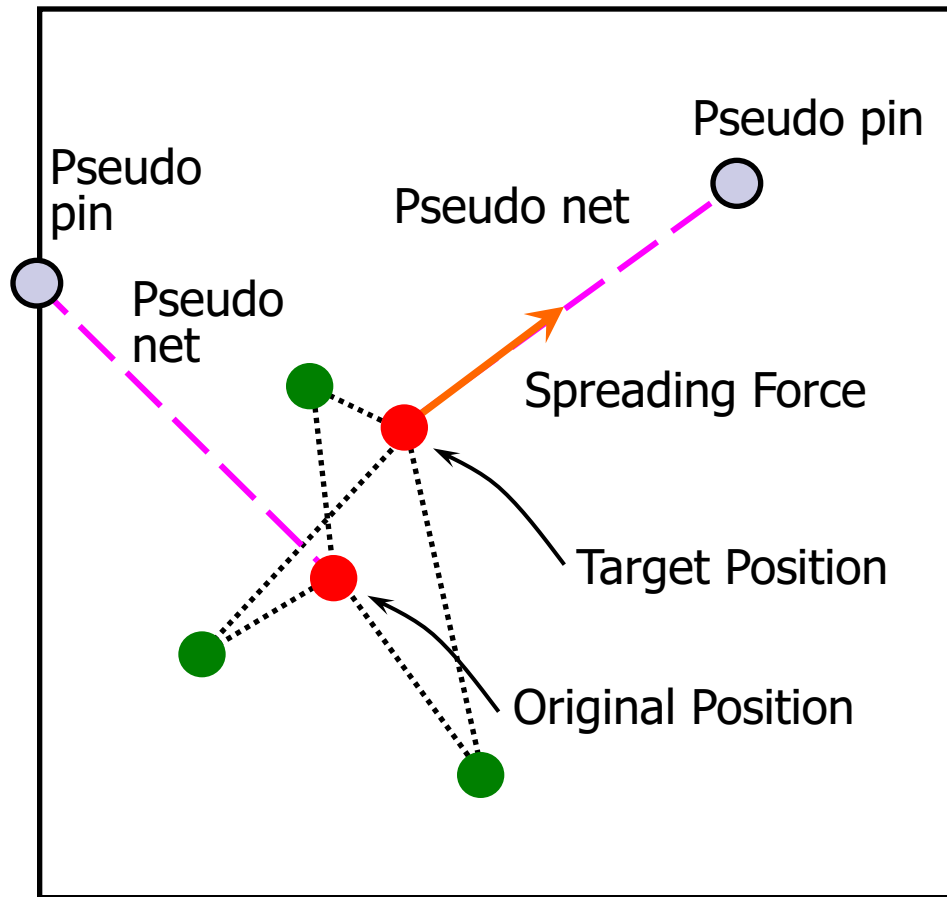
FDP Flow

(4)

Step 3: Add spreading forces to objects for next quadratic program



Addition of Spreading Forces



Importance of Spreading

Solve initial convex quadratic program (QP)

While target density is not met

Spread objects to reduce overlap

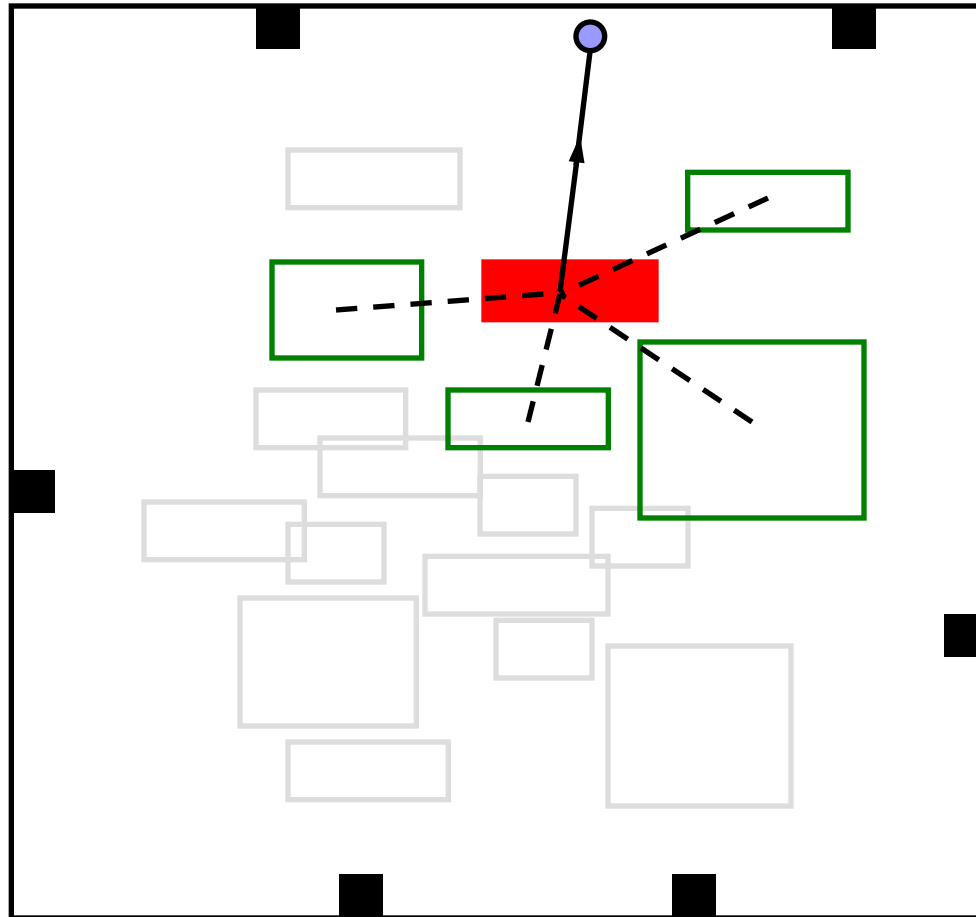
Add spreading forces to QP formulation

Solve the convex quadratic program

end while

- Need to carefully control the magnitude of the spreading forces
 - Fast spreading will severely degrade wirelength
 - Slow spreading affects turn-around-time

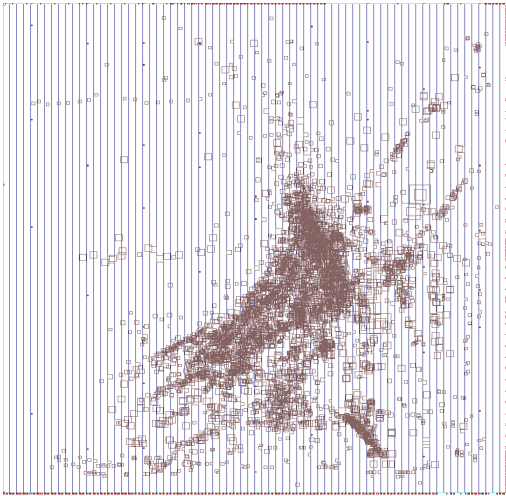
Force Directed Placement



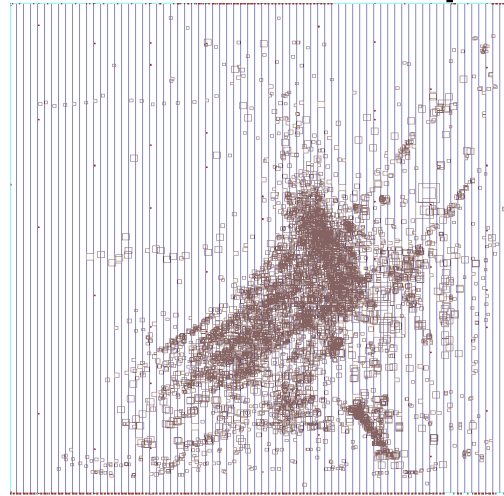
Analytic Placement – Force-directed Placement

- Advantages:
 - Conceptually simple, easy to implement
 - Primarily intended for global placement, but can also be adapted to detailed placement
- Disadvantages:
 - Does not scale to large placement instances
 - Is not very effective in spreading cells in densest regions
 - Poor trade-off between solution quality and runtime
- In practice, FDP is extended by specialized techniques for cell spreading
 - This facilitates scalability and makes FDP competitive

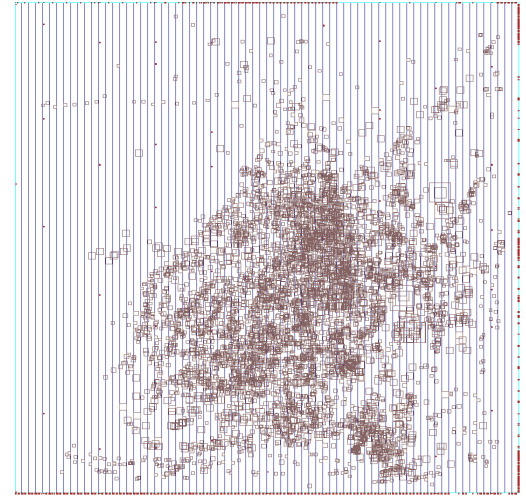
Force Directed Placement Example



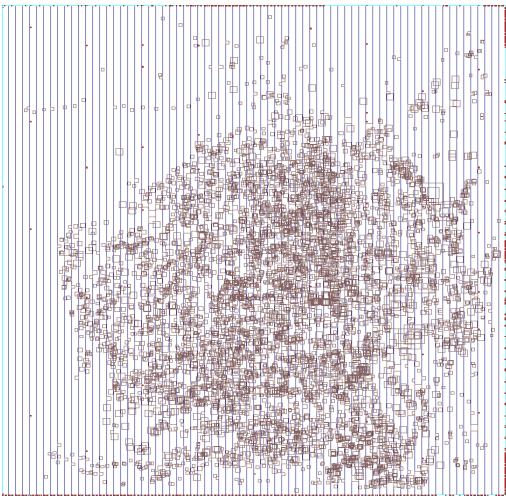
Initial



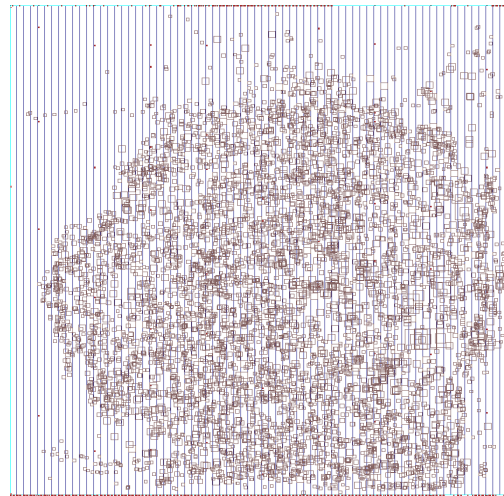
1 iteration



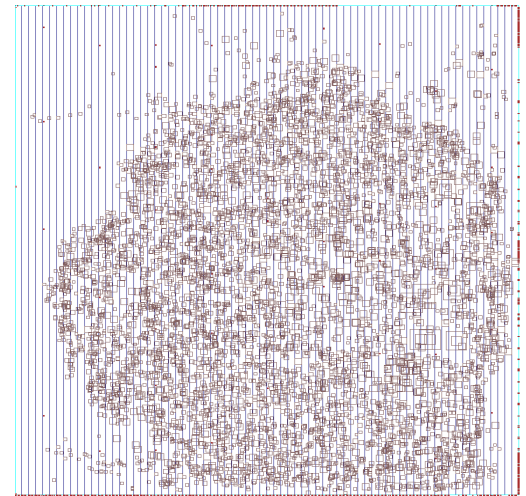
3 iterations



6 iterations



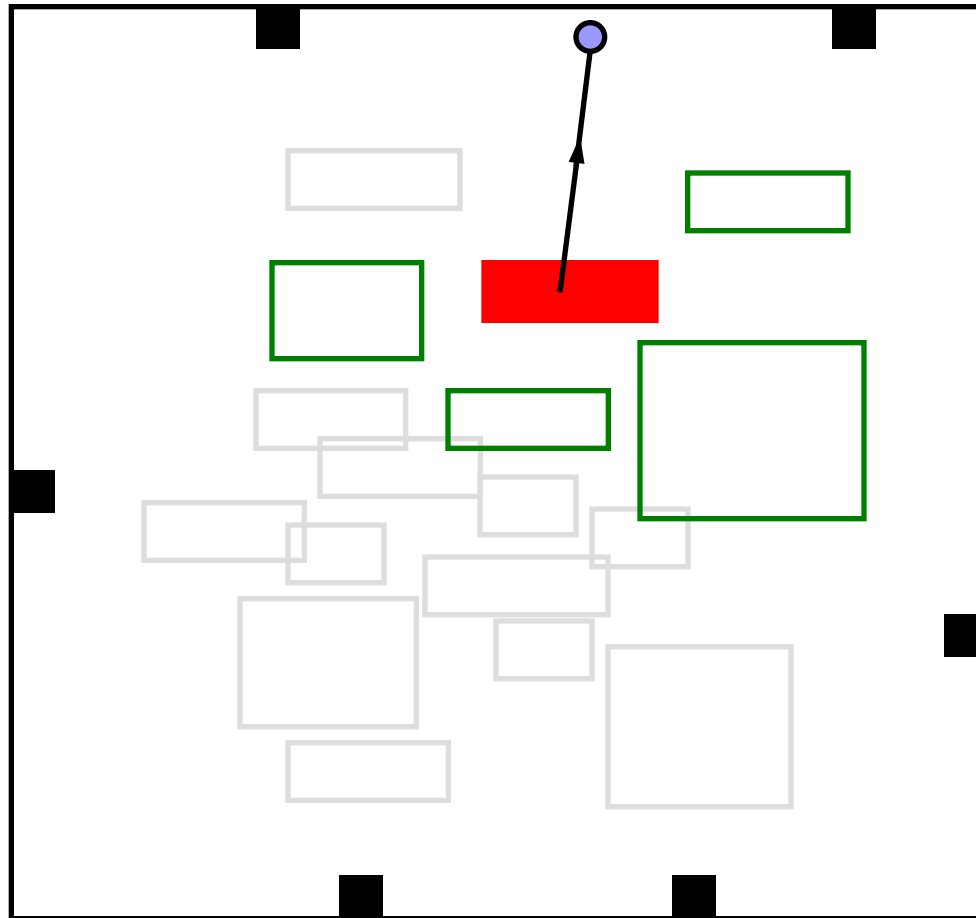
9 iterations



12 iterations

Force-vector modulation

Proposes to **modulate** the spreading force vectors within analytical placement



FDP Flow with Modulation

Solve initial convex quadratic program (QP)

While target density is not met

Spread objects to reduce overlap

Order objects based on spreading force magnitude

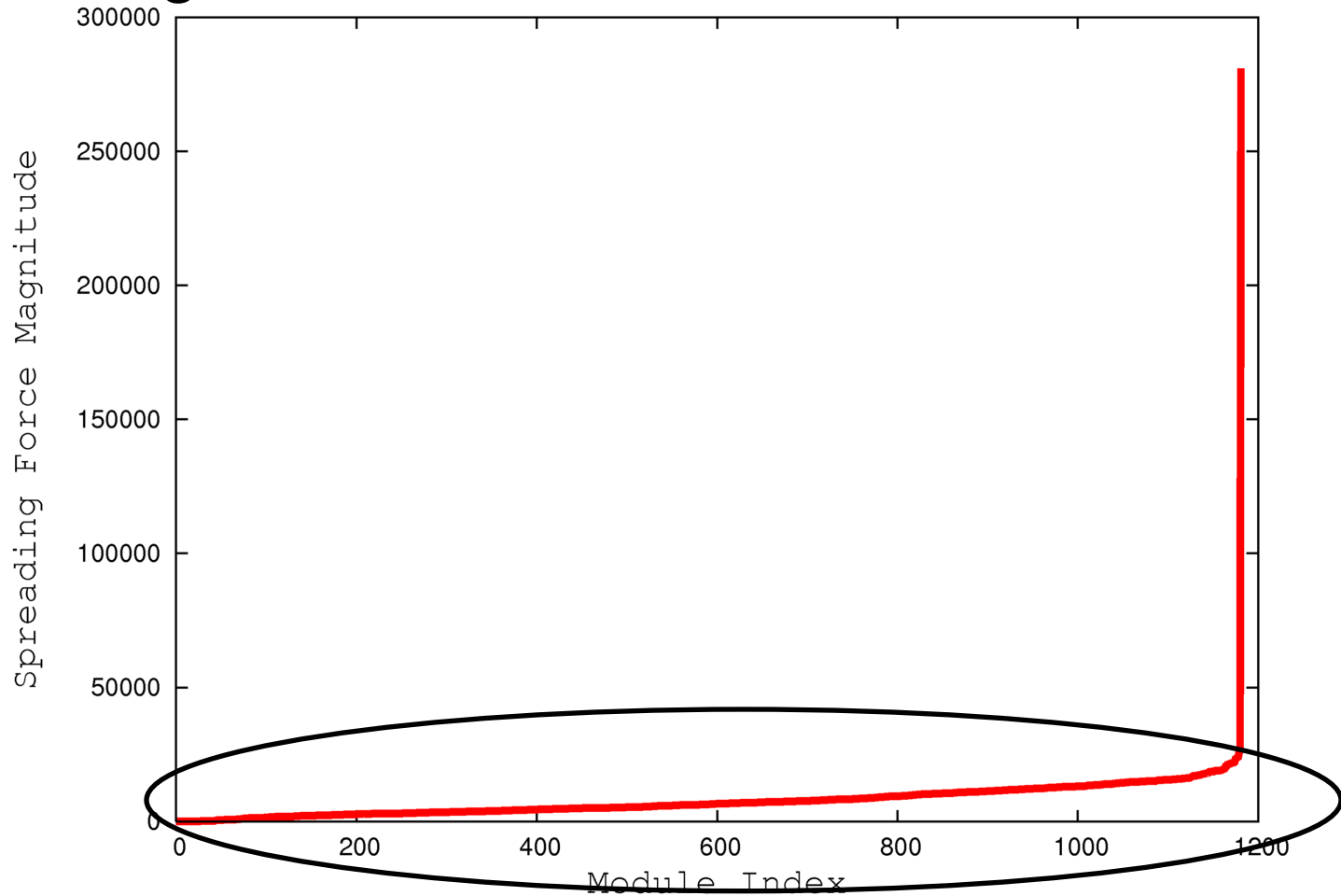
Modulate spreading forces for top x% of objects

Add spreading forces to QP formulation

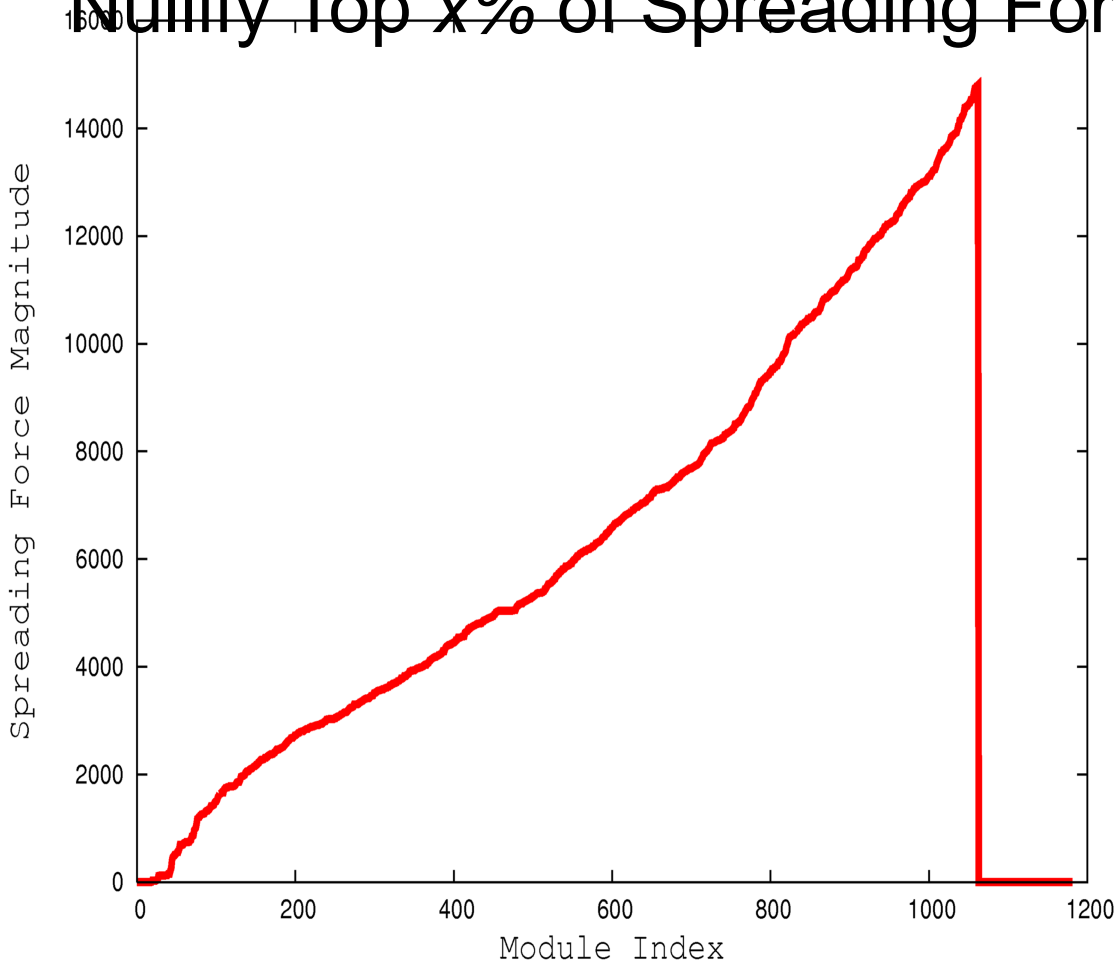
Solve the convex quadratic program

end while

Spreading forces



Nullify Top x% of Spreading Forces



Rank Modules based on the spreading force magnitude

Nullify the spreading force magnitude for top x% of modules

Typically $x = 5-10\%$ within RQL

Advantages of modulation

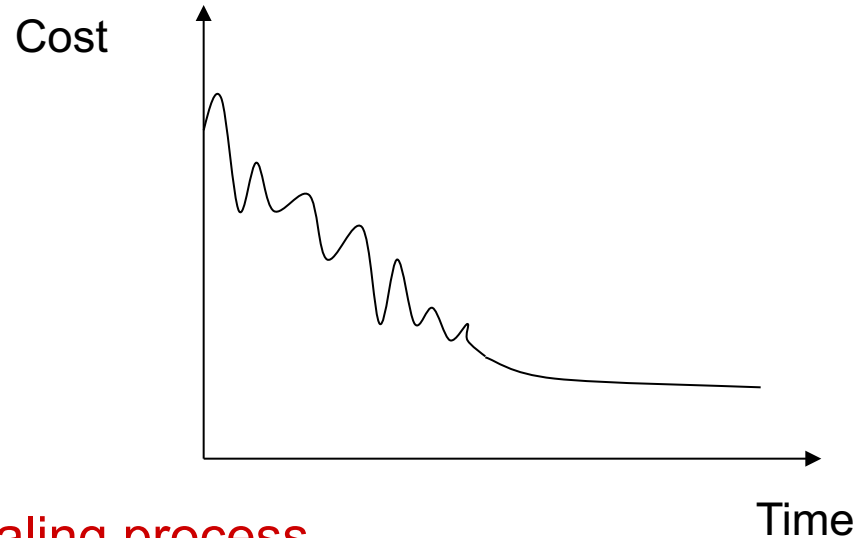
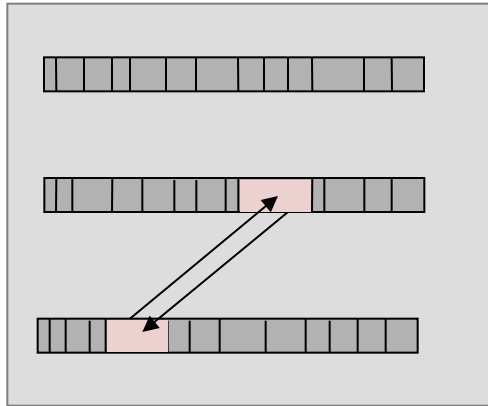
Improves Wirelength

Reorders modules at a global scale

No Impact on spreading

Can be incorporated within any analytical placer

Simulated Annealing



- Analogous to the physical **annealing process**
 - Melt metal and then slowly cool it
 - Result: energy-minimal crystal structure
- Modification of an initial configuration (placement) by moving/exchanging of randomly selected cells
 - Accept the new placement if it improves the objective function
 - If no improvement: Move/exchange is accepted with temperature-dependent (i.e., decreasing) probability

Simulated Annealing – Algorithm

Input: set of all cells V

Output: placement P

```
 $T = T_0$  // set initial temperature
 $P = \text{PLACE}(V)$  // arbitrary initial placement
while ( $T > T_{min}$ )
  while (!STOP()) // not yet in equilibrium at  $T$ 
     $new\_P = \text{PERTURB}(P)$ 
     $\Delta cost = \text{COST}(new\_P) - \text{COST}(P)$ 
    if ( $\Delta cost < 0$ ) // cost improvement
       $P = new\_P$  // accept new placement
    else // no cost improvement
       $r = \text{RANDOM}(0,1)$  // random number [0,1)
      if ( $r < e^{-\Delta cost/T}$ ) // probabilistically accept
         $P = new\_P$ 
   $T = \alpha \cdot T$  // reduce  $T$ ,  $0 < \alpha < 1$ 
```

Simulated Annealing

- Advantages:
 - Can find global optimum (given sufficient time)
 - Well-suited for detailed placement
- Disadvantages:
 - Very slow
 - To achieve high-quality implementation, laborious parameter tuning is necessary
 - Randomized, chaotic algorithms - small changes in the input lead to large changes in the output
- Practical applications of SA:
 - Very small placement instances with complicated constraints
 - Detailed placement, where SA can be applied in small windows (not common anymore)
 - FPGA layout, where complicated constraints are becoming a norm

Modern Placement Algorithms

- Predominantly analytic algorithms
- Solve two challenges: interconnect minimization and cell overlap removal (spreading)
- Two families:



Quadratic placers



Non-convex
optimization placers

Modern Placement Algorithms

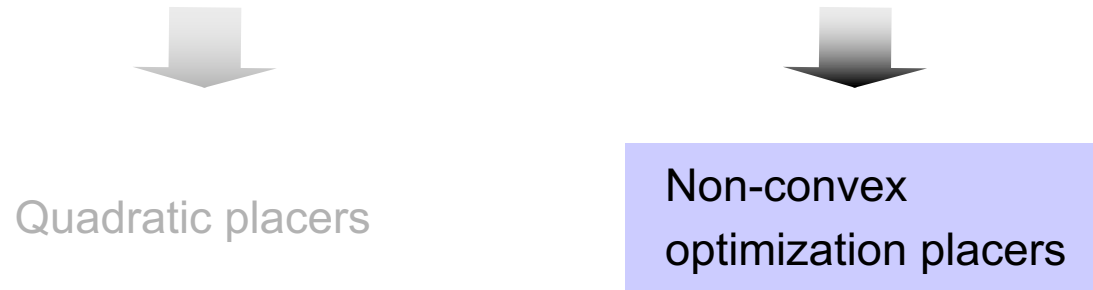


Quadratic placers

Non-convex
optimization placers

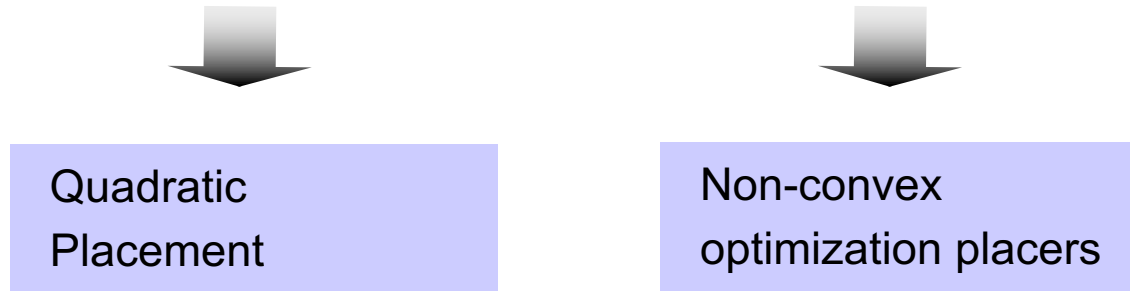
- Solve large, sparse systems of linear equations (formulated using force-directed placement) by the Conjugate Gradient algorithm
- Perform cell spreading by adding fake nets that pull cells away from dense regions toward carefully placed anchors

Modern Placement Algorithms



- Model interconnect by sophisticated differentiable functions, e.g., log-sum-exp is the popular choice
- Model cell overlap and fixed obstacles by additional (non-convex) functional terms
- Optimize interconnect by the non-linear Conjugate Gradient algorithm
- Sophisticated, slow algorithms
- All leading placers in this category use netlist clustering to improve computational scalability (this further complicates the implementation)

Modern Placement Algorithms



Pros and cons:

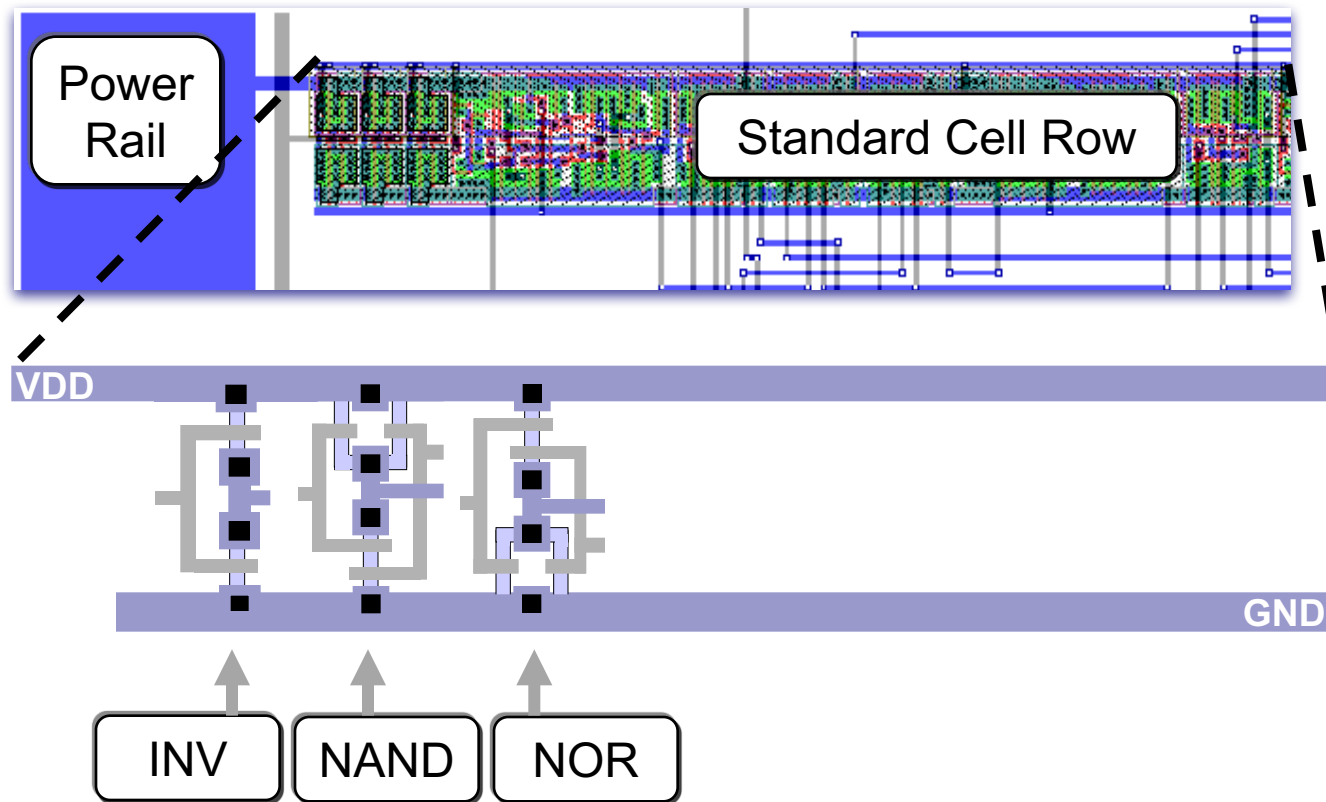
- Quadratic placers are simpler and faster, easier to parallelize
- Non-convex optimizers tend to produce better solutions
- As of 2011, quadratic placers are catching up in solution quality while running 5-6 times faster [1]

Legalization and Detailed Placement

- Global placement must be legalized
 - Cell locations typically do not align with power rails
 - Small cell overlaps due to incremental changes, such as cell resizing or buffer insertion
- **Legalization** seeks to find legal, non-overlapping placements for all placeable modules
- Legalization can be improved by **detailed placement** techniques, such as
 - Swapping neighboring cells to reduce wirelength
 - Sliding cells to unused space
- Software implementations of legalization and detailed placement are often bundled

Legalization and Detailed Placement

Legal positions of standard cells between VDD and GND rails



Summary

- Row-based standard-cell placement
 - Cell heights are typically fixed, to fit in rows (but some cells may have double and quadruple heights)
 - Legal cell sites facilitate the alignment of routing tracks, connection to power and ground rails
- Wirelength as a key metric of interconnect
 - Bounding box half-perimeter (HPWL)
 - Cliques and stars
 - RMSTs and RSMTs
- **Objectives:** wirelength, routing congestion, circuit delay
 - Algorithm development is usually driven by wirelength
 - The basic framework is implemented, evaluated and made competitive on standard benchmarks
 - Additional objectives are added to an operational framework

Summary

- Combinatorial optimization techniques: min-cut and simulated annealing
 - Can perform both global and detailed placement
 - Reasonably good at small to medium scales
 - SA is very slow, but can handle a greater variety of constraints
 - Randomized and chaotic algorithms – small changes at the input can lead to large changes at the output
- Analytic techniques: force-directed placement and non-convex optimization
 - Primarily used for global placement
 - Unrivaled for large netlists in speed and solution quality
 - Capture the placement problem by mathematical optimization
 - Use efficient numerical analysis algorithms
 - Ensure stability: small changes at the input can cause only small changes at the output
 - Example: a modern, competitive analytic global placer takes 20mins for global placement of a netlist with 2.1M cells (single thread, 3.2GHz Intel CPU) ^[1]

Legalization and Detailed Placement

- Legalization ensures that design rules & constraints are satisfied
 - All cells are in rows
 - Cells align with routing tracks
 - Cells connect to power & ground rails
 - Additional constraints are often considered, e.g., maximum cell density
- Detailed placement reduces interconnect, while preserving legality
 - Swapping neighboring cells, rotating groups of three
 - Optimal branch-and-bound on small groups of cells
 - Sliding cells along their rows
 - Other local changes
- Extensions to optimize routed wirelength, routing congestion and circuit timing
- Relatively straightforward algorithms, but high-quality, fast implementation is important
- Most relevant after analytic global placement, but are also used after min-cut placement
- Rule of thumb: 50% runtime is spent in global placement, 50% in detailed placement [1]

State-of-the-art Analytical Placers

	APlace	mPL6	NTUP3	FDP
Wirelength Model	Log-sum-exponential (Naylor patent)			Quadratic
Spreading	Density potential based			Fixed-point based
Objective Function	Non-linear objective			Quadratic wirelength

The mountain hike analogy

