

Recapitulation

5/9/2014

Excess Carriers due to photo-generation

$$\frac{dp}{dt} = \frac{d(p_0 + \delta p)}{dt} = \frac{d\delta p}{dt} = \underline{G_{th}} - R + \underline{J_{op}}$$

$$\frac{d\delta p(t)}{dt} = \underline{G_{th}} - \underline{R} = \underbrace{(-\alpha_r(n_0 + p_0)\delta p)}_{\text{(low level generation)}} \quad || \quad 0$$

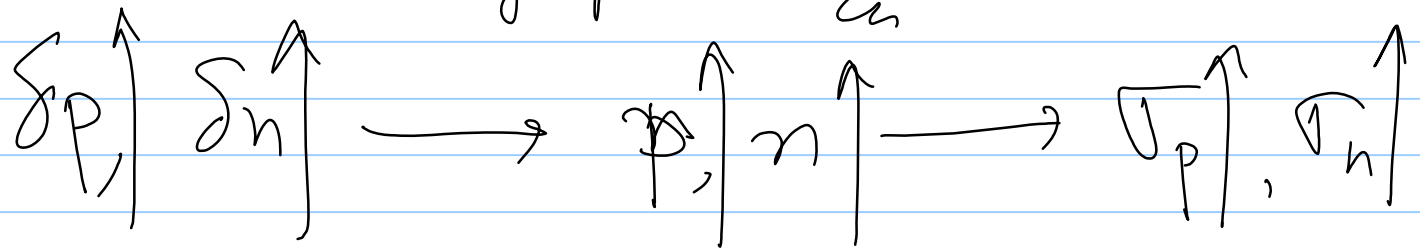
$$\delta p(t) = \delta p(t=0) e^{-t/\tau_p} \quad \tau_p = \frac{1}{\alpha_r(n_0 + p_0)}$$

$$\frac{d}{dt} f_p(t) = G_{th} - R + J_{sp} = 0$$

Steady State

$$J_{sp} = \frac{\delta p}{\tau_p}$$

$$J_{sp} = \frac{\delta n}{\tau_n}$$



ΔV

Continuity Eqn

$$\nabla \times H = J_c + \frac{dD}{dt}$$

$$D = \epsilon E$$

$$\nabla \cdot (\nabla \times H) = 0 = \nabla \cdot J_c + \frac{d(\nabla \cdot D)}{dt}$$

$$\nabla \cdot J_c + \frac{d\rho}{dt} = 0$$

$$\left[\frac{d\rho}{dt} = -\nabla \cdot J_c \right]$$

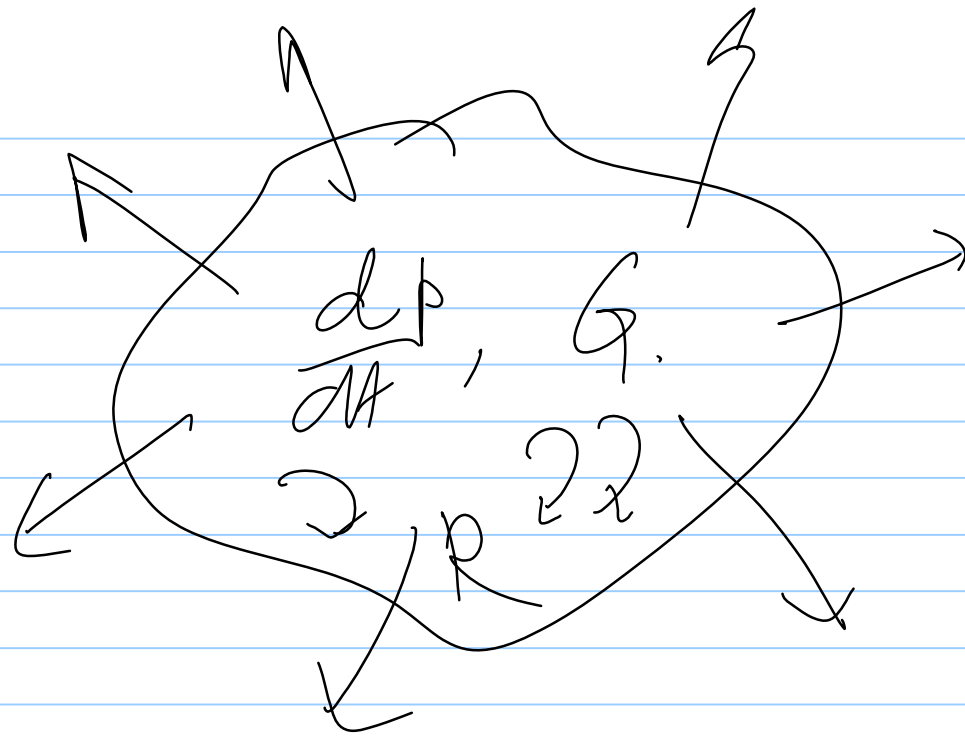
Continuity Eqn.

$$\frac{dp}{dt} = - \frac{1}{\epsilon} \nabla \cdot J_p \quad \text{--- (1)}$$

$$\frac{dp}{dt} = G - R \quad \text{--- (2)}$$

$$\frac{dp}{dt} = - \frac{1}{\epsilon} \nabla \cdot J_p + G - R$$

Continuity Eqn. A hole in semiconductor.



$$\frac{dn}{dt} = - \underbrace{\int \nabla \cdot \bar{J}_n}_{(-2)} + \underline{\underline{G - R}}$$

$$n = n_0 + \delta n$$

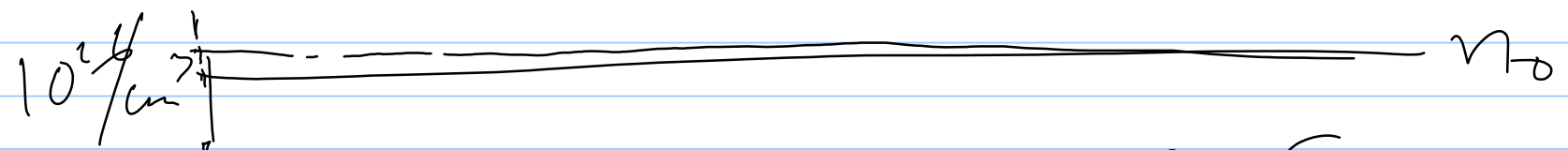
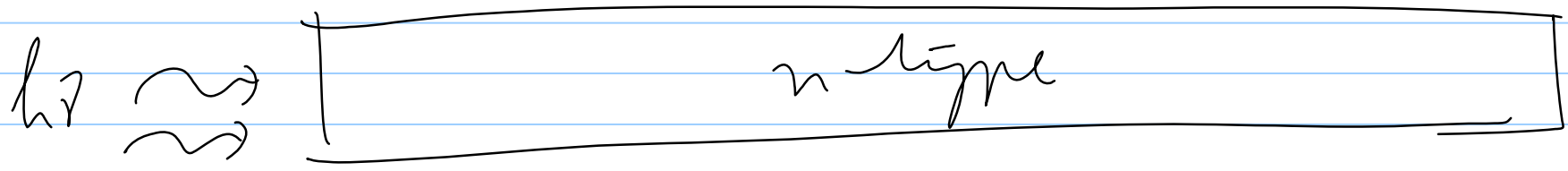
$$\frac{d\delta n}{dt} = \frac{1}{q} \nabla \cdot \mathbf{J}_n - \frac{\delta n}{\tau_n}$$

Continuity Eqn.
for electron

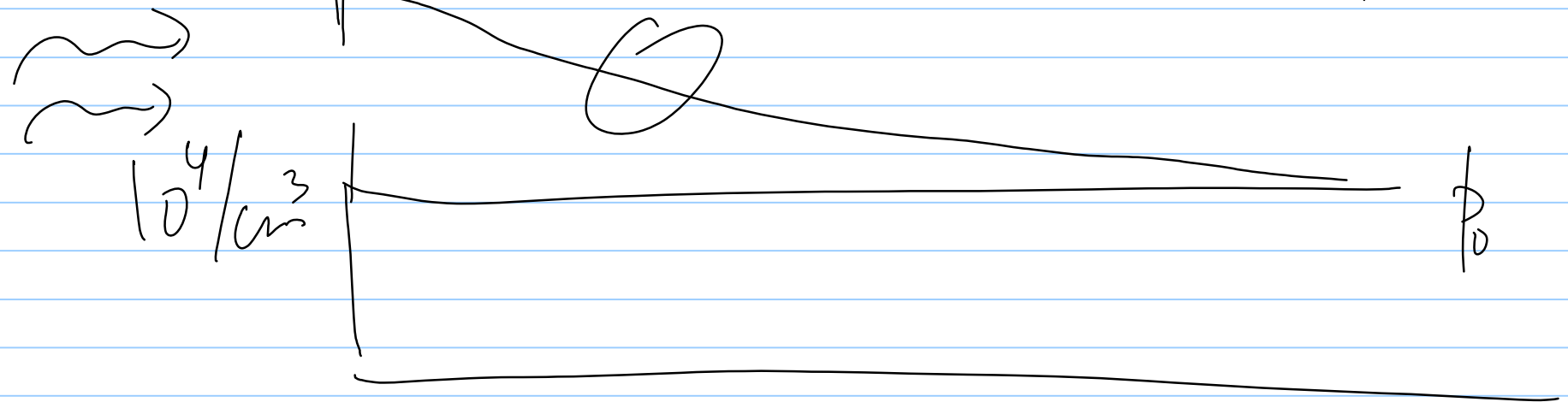
$$\begin{aligned} G_n - R &= \alpha_r n_0 p_0 - \alpha_r (n_0 + \delta n) (p_0 + \delta p) \\ &= -\alpha_r (n_0 + p_0) \delta n - \alpha_r \delta n^2 \\ &= -\frac{\delta n}{\tau_n} \end{aligned}$$

$$\frac{d\delta p}{dt} = -\frac{1}{q} \nabla \cdot \mathbf{J}_p - \frac{\delta p}{\tau_p}$$

Continuity
Eqn for hole



$$\delta n = \delta p$$



$$0 = \frac{dS_p}{dt} = -\frac{1}{\tau} \frac{dJ_p}{dx} - \frac{S_p}{\tau_p}$$

steady state

$$\frac{d(J_p/\tau)}{dx} = -\frac{S_p}{\tau_p}$$

$$J_p = -2D_p \frac{dJ_p}{dx}$$

$$\frac{d^2(S_p)}{dx^2} = \frac{S_p}{\tau_p}$$

$$\frac{d^2 \delta \phi(x)}{dx^2} = \frac{\delta \phi(x)}{L_p^2} = \frac{\delta \phi}{L_p^2}$$

$L_p \rightarrow$ Diffusion length $L_p = \sqrt{D_p \tau_p}$

~~$\mu_p = 500 \text{ cm}^2/\text{V}\cdot\text{s}$~~

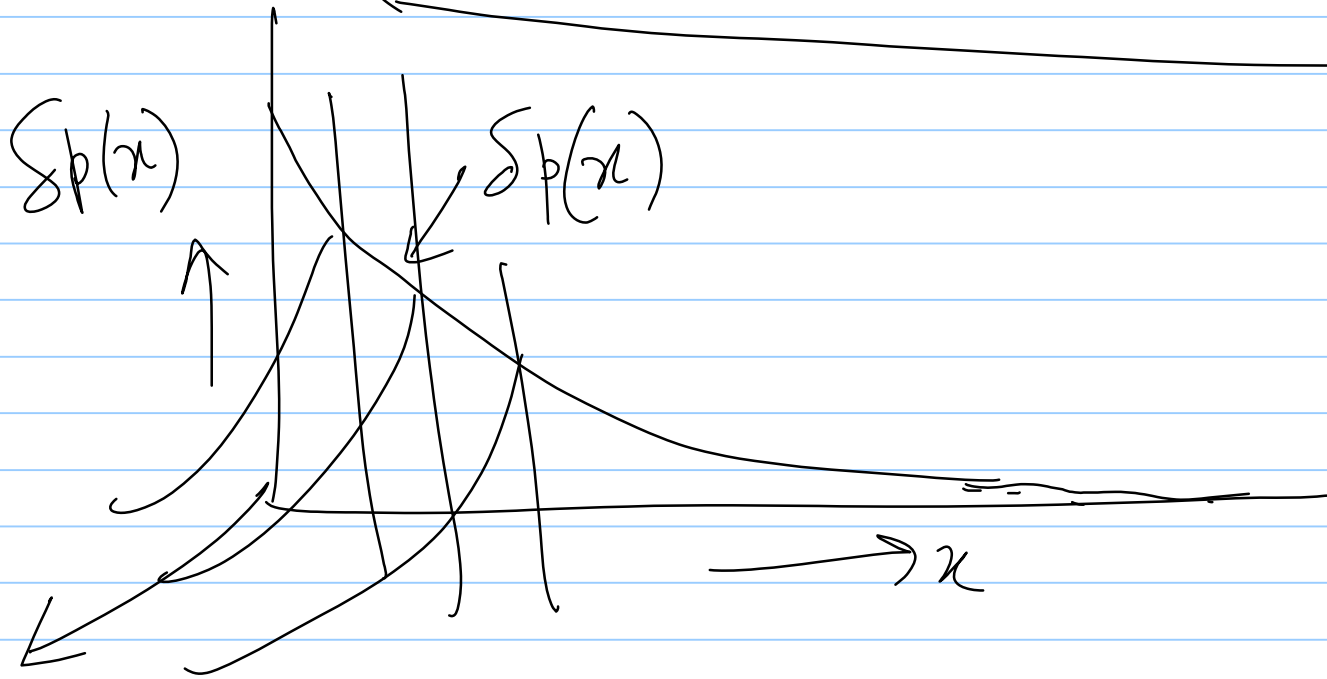
$$D_p = V_T \cdot \mu_p = 0.0259 \times 500$$

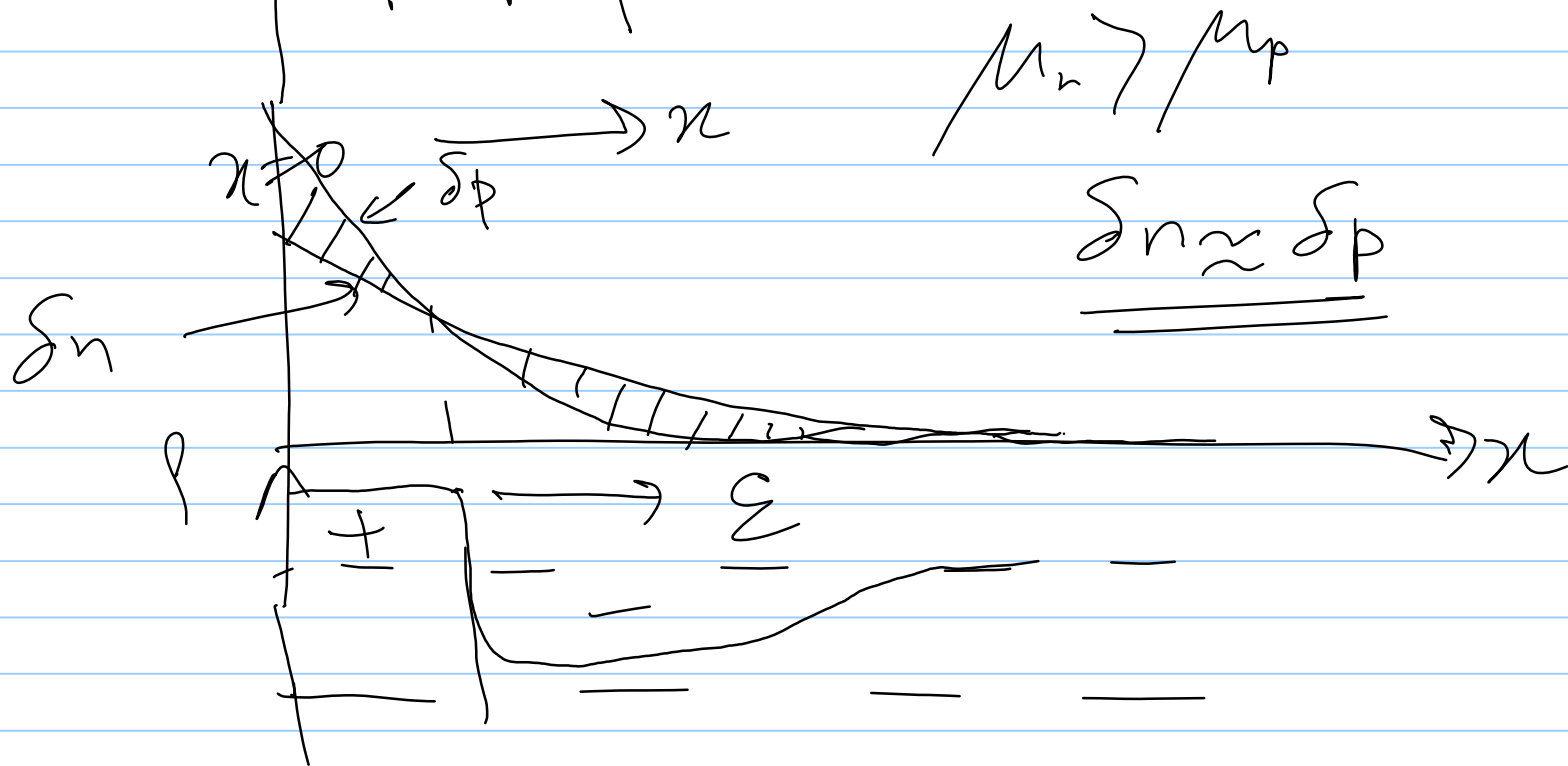
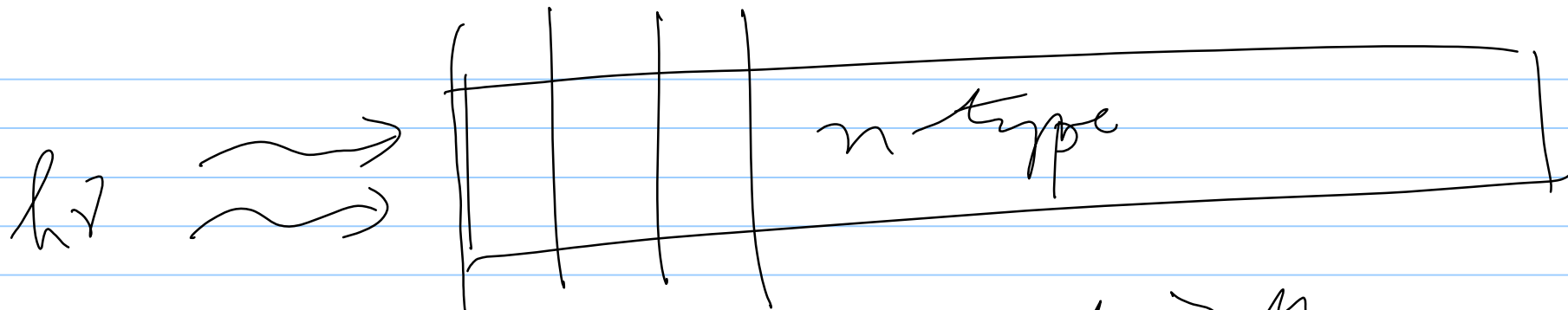
$$\approx 10 \text{ cm}^2/\text{s}$$

$$D_p \tau_p = 10 \text{ cm}^2 \cdot 10^{-6} = 10 \times 10^{-6} \text{ cm}^2$$

$$\delta p(x) = \delta p(x=0) \exp\left(-\frac{x}{L_p}\right)$$

$$\delta p(x) = \delta(t=0) \exp\left(-x/L_p\right)$$





J_{drift}

\textcircled{n}

p

J_{diff}

$\frac{dn}{dx}$

$\frac{dp}{dx}$

$\implies \underline{J_{p, \text{diff}}}$

$\longleftarrow \underline{J_{n, \text{diff}}}$

$\implies J_{p, \text{drift}} \times$

$\implies \underline{\underline{J_{n, \text{drift}}}}$

$$|J_{p, \text{diff}}| = |J_{n, \text{diff}}| - \underline{\underline{|J_{n, \text{drift}}|}}$$

$$J(x) = 0$$

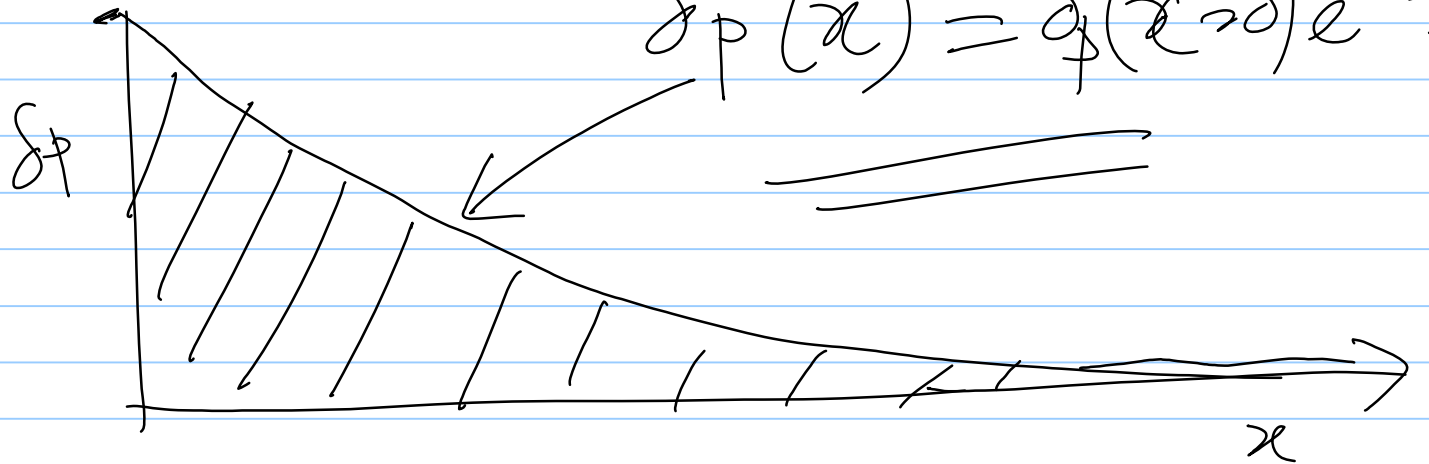
$$x = 0 \quad \delta p(x=0) = 10^{16} / \text{cm}^3$$

$$\text{Cross-sectional Area } A = 10^{-3} \text{ cm}^2$$

$$L_p = 10^{-3} \text{ cm}$$

$$\tau_p = 10^{-6} \text{ sec.}$$

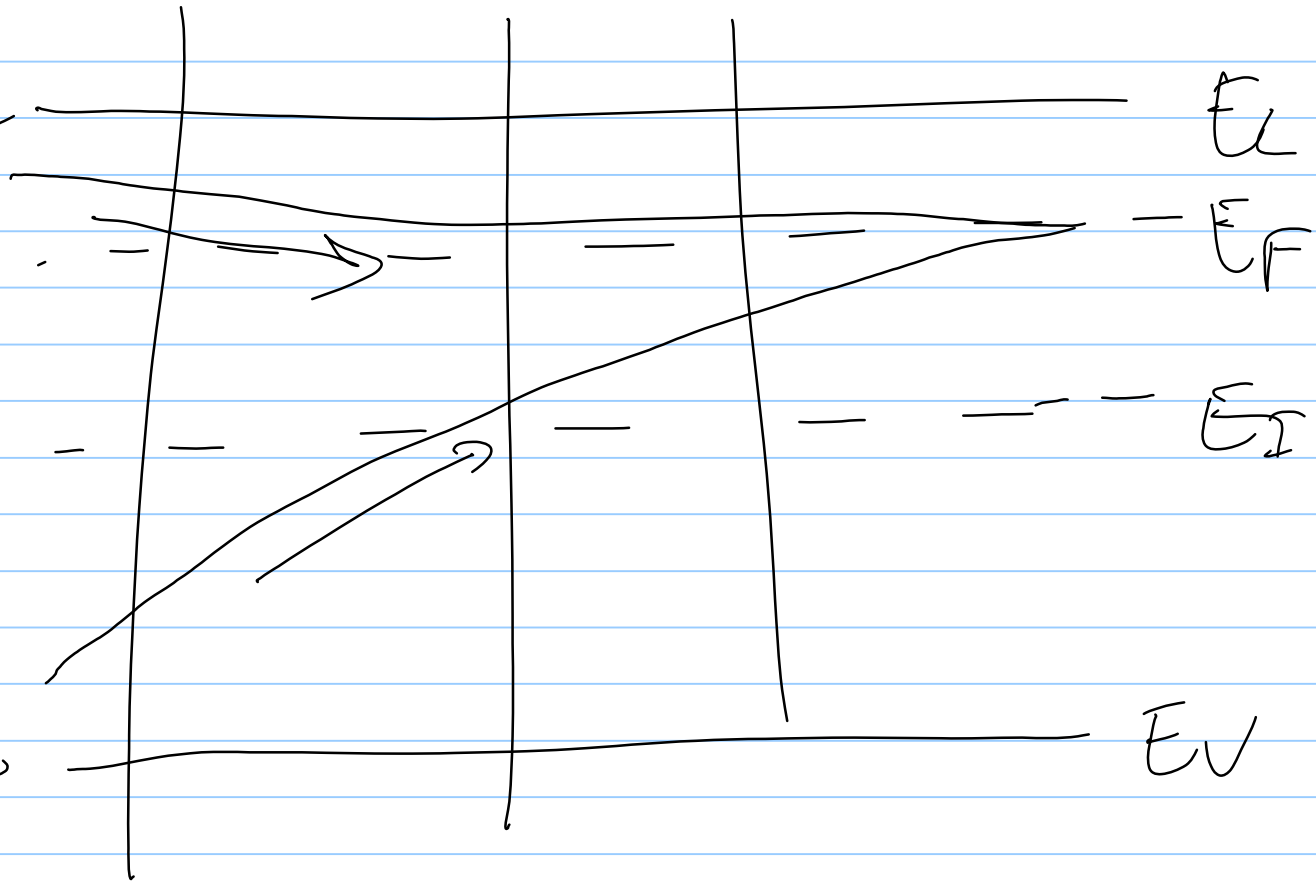
$$\delta Q_p = ?$$



$$J_t = J_{p\text{diff}} + J_{p\text{drift}}$$

$$J_p = -q \mu_p \left(\frac{dE_p}{dx} \right)$$

$$J_n = q \mu_n \left(\frac{dE_n}{dx} \right)$$



$$J_p = p z / \mu_p (\Sigma) - q D_p \left(\frac{dp}{dx} \right)$$

$$p = n_i \exp \left(\frac{E_i - E_{fp}}{kT} \right)$$

$$\Sigma = - \frac{dV}{dx} = + \frac{1}{z} \cdot \frac{d(\Sigma V)}{dx} = + \frac{1}{z} \frac{dE_i}{dx}$$

$$\begin{aligned} \hat{J}_p &= p z / \mu_p \left| \frac{dE_i}{dx} \right| - (\Sigma) D_p p \cdot \left(\frac{d}{dx} (E_i - E_{fp}) \right) \\ &= p / \mu_p \frac{dE_{fp}}{dx} \end{aligned}$$