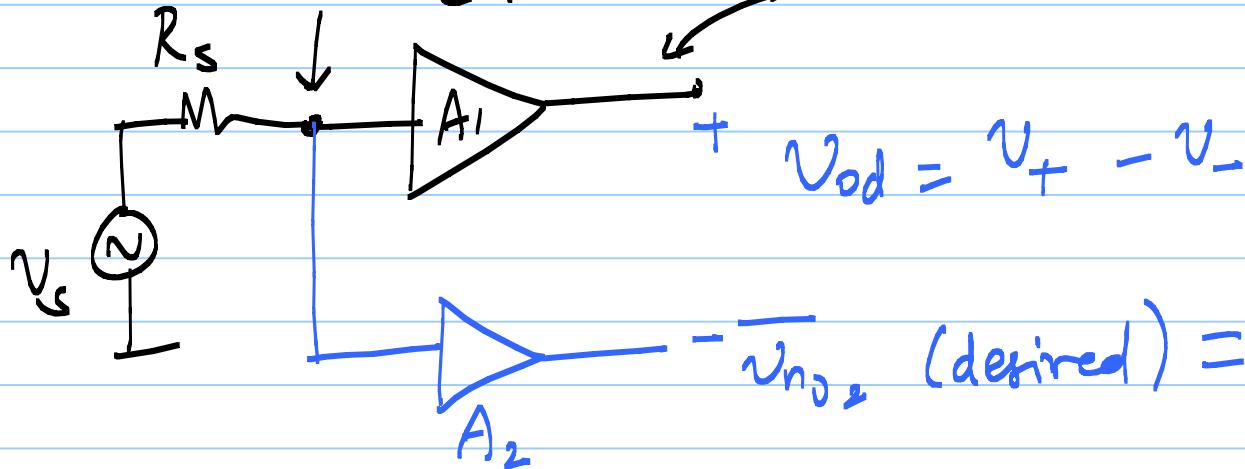


2/2/20

$$\bar{V}_{n,in} = \frac{\bar{i}_{in} R_s}{2} \text{ Lec 17}$$

CGLNA

$$\bar{V}_{n,out} = -\frac{\bar{i}_{in} R_d}{2}$$



We want $\bar{V}_{odn} = 0$

$$A_2 = -\frac{R_d}{R_s}$$

CG $\leftarrow X$ because Z_{in} is low

CD $\leftarrow X$ because no gain

CS ✓

* $Z_{in} \rightarrow \infty \Rightarrow$ small G_V , small $(\frac{W}{L})$

* gain = $-g_m R_L$ (correct sign)

$$\text{Set } g_m R_L = \frac{R_d}{R_s}$$

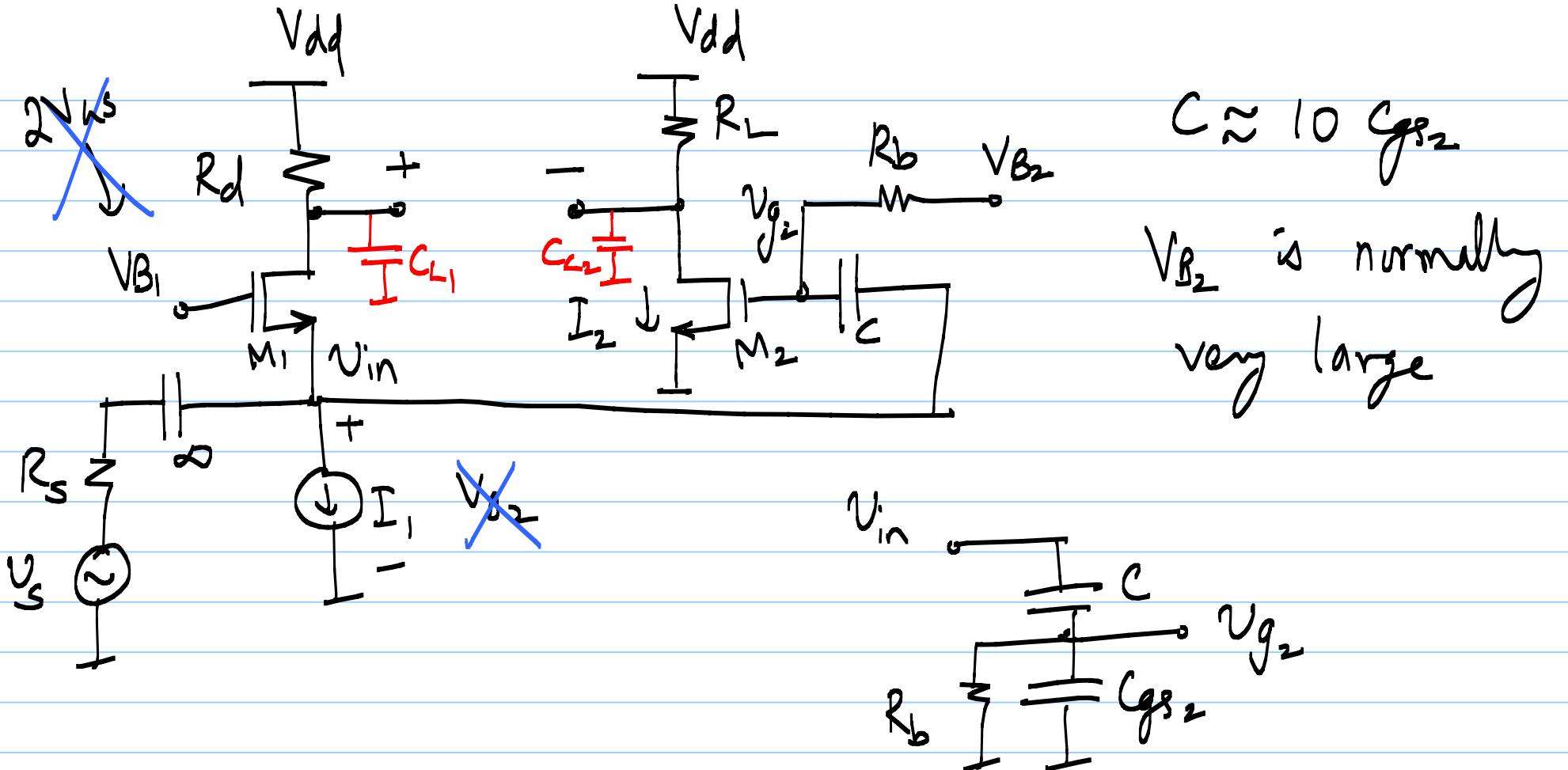
* Low noise : $\bar{e_n^2} = \frac{4kTg_m + \frac{4kT}{R_L}}{g_m^2}$

$$\begin{aligned}\frac{\bar{e_n^2}}{\Delta f} &= \frac{4kT\gamma}{g_m} + \frac{4kT}{g_m^2 R_L} \\ &= \frac{4kT}{g_m} \left[\gamma + \frac{R_s}{R_d} \right]\end{aligned}$$

\Rightarrow maximize g_m of CS stage

\Rightarrow burn more current

*



$$\frac{V_{g_2}}{V_{in}} = \frac{R_b \parallel \frac{1}{sC_{gs2}}}{R_b \parallel \frac{1}{sC_{gs2}} + \frac{1}{sC}}$$

@ RF e.g. $|R_b| \gg \left(\frac{1}{\omega C_{gs2}} \right)$

$$\left| \frac{v_{g_2}}{v_{in}} (\omega) \right| = \frac{c}{c + c_{gs_2}}$$

close to DC: $|R_b| \ll \left| \frac{1}{\omega c_{gs_2}} \right|, \left| \frac{1}{\omega c} \right|$

$$\left| \frac{v_{g_2}(\omega)}{v_{in}} \right| = \left| \frac{R_b}{R_b + \frac{1}{j\omega c}} \right| \text{ small}$$

* DC @ \oplus node = $V_{dd} - I_1 R_d$

DC @ \ominus node = $V_{dd} - I_2 R_L$

$$\text{BW @ } (+) \text{ node output} = \frac{1}{2\pi R_d (C_{db_1} + C_{L_1})}$$

$$\text{BW @ } (-) \text{ output node} = \frac{1}{2\pi R_L (C_{db_2} + C_{L_2})}$$

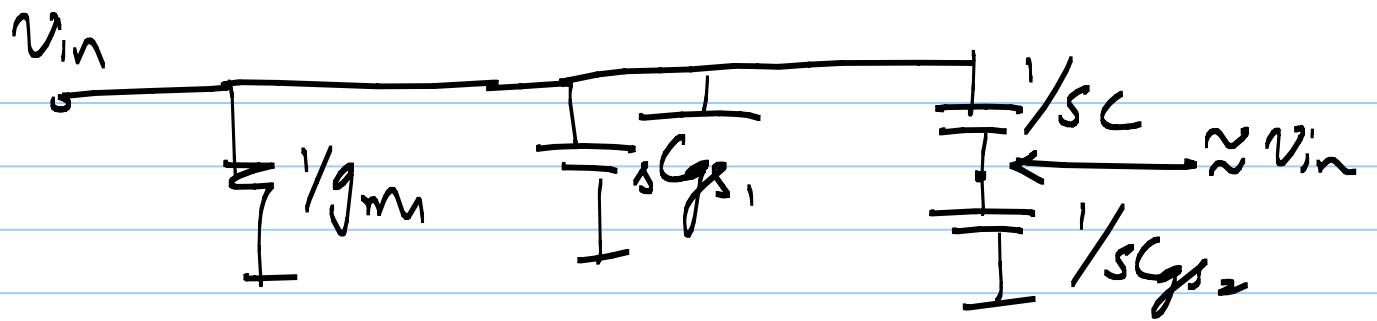
$$R_d \neq R_L ; C_{db_1} \neq C_{db_2}$$

In general, R_d is larger than R_L

The two outputs are asymmetric

What about $\frac{V_{od}}{V_s}$?

$$Z_{in} = 50\Omega \Rightarrow g_{m_1} = 20 \text{ mS} \xrightarrow{\left(\frac{W}{L}\right)_1} I_1$$



$$v_{in} = \frac{v_s}{2}$$

$$v_{o+} = + \frac{R_d}{2R_s} \cdot v_s$$

$$v_{o-} = - i d_2 \cdot R_L$$

$$\approx - g_{m_2} \cdot v_{in} \cdot R_L = - \frac{g_{m_2} R_L}{2} \cdot v_s$$

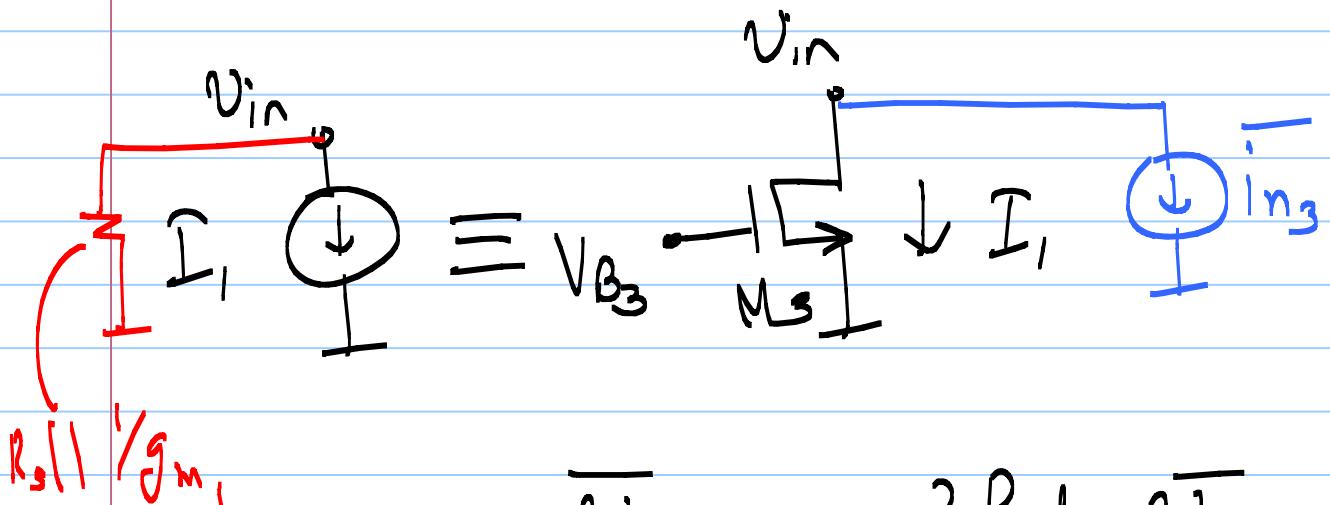
$$v_{od} = \left[\frac{R_d}{2R_s} + \frac{g_{m_2} R_L}{2} \right] v_s$$

Condition for noise cancellation: $\frac{R_d}{R_s} = g_{m_2} R_L$

$$\Rightarrow \frac{V_{od}}{V_s} = \frac{R_d}{R_s} = g_{m_2} R_L$$

$R_s || g_m$

* Noise of current source I_1 ?



$$\bar{V}_{inM_3} = -\frac{i_{n3} \cdot R_s}{2}$$

$$\bar{V}_{o+} = \frac{R_d}{R_s} \cdot \bar{V}_{inM_3}$$

$$\bar{V}_{o-} = -g_{m_2} R_L \bar{V}_{inM_3}$$

$$\bar{V}_{odn} = \frac{2 R_d}{R_s} \cdot \bar{V}_{inM_3}$$

$$\begin{aligned} \bar{V}_{odn}^2 &= \frac{4 R_d^2}{R_s^2} \cdot \bar{V}_{inM_3}^2 = \frac{4 R_d^2}{R_s^2} \cdot \bar{i}_{n3}^2 \frac{R_s^2}{4} \\ &= 4 k T \gamma g_{m_3} \cdot R_d^2 \end{aligned}$$