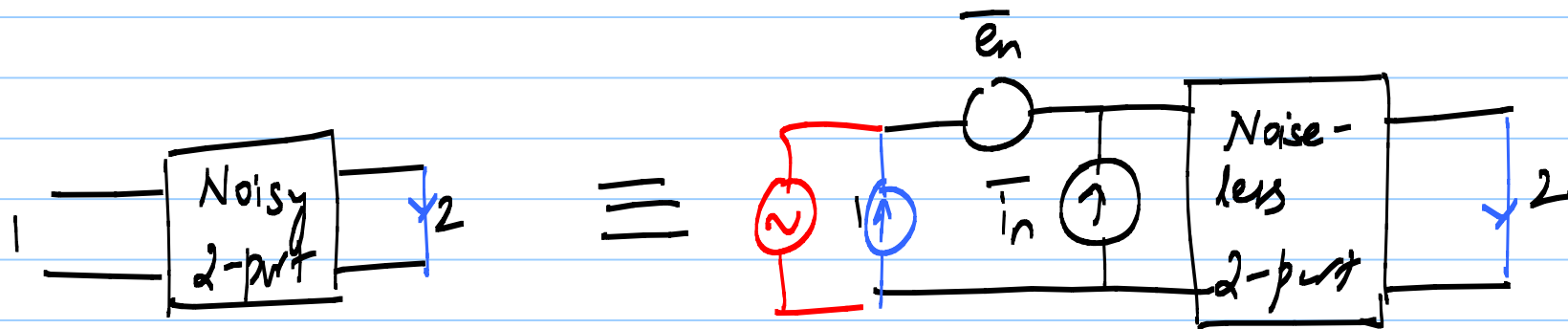


17/1/20

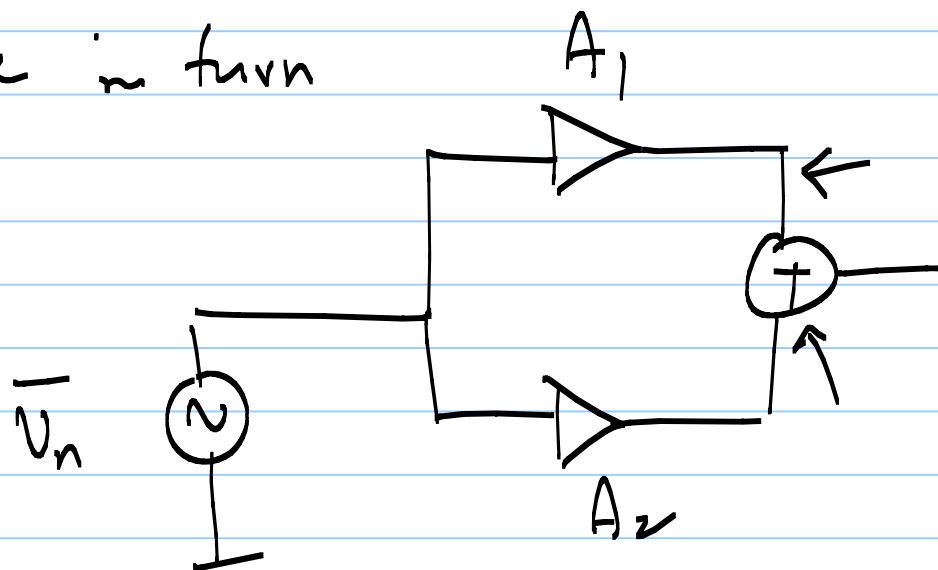
EE5320

Lec3

17-Jan-20



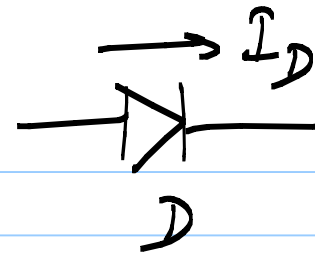
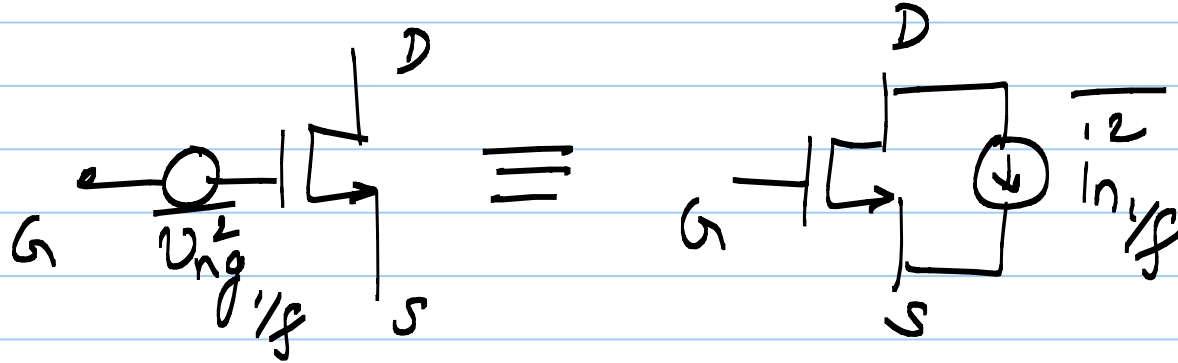
apply each noise source in turn



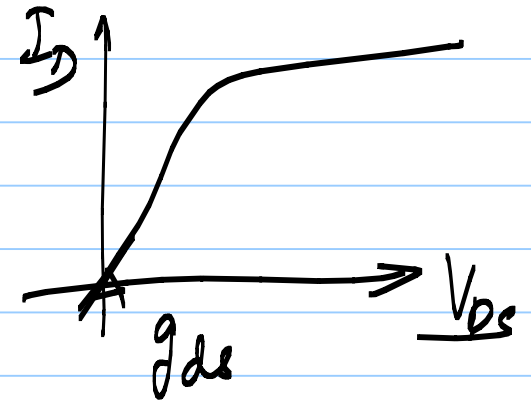
$$\bar{v}_{on} = (A_1 + A_2)^2 \cdot \bar{v}_n^2$$

MOSFET noise in saturation

1) Flicker noise ($1/f$ noise)



$$\overline{i_n^2} = 2qI_D \Delta f$$



$$\overline{v_{ng}^2}/f = \frac{K_{1/f}}{WL C_{ox}^2} \cdot \frac{1}{f}$$

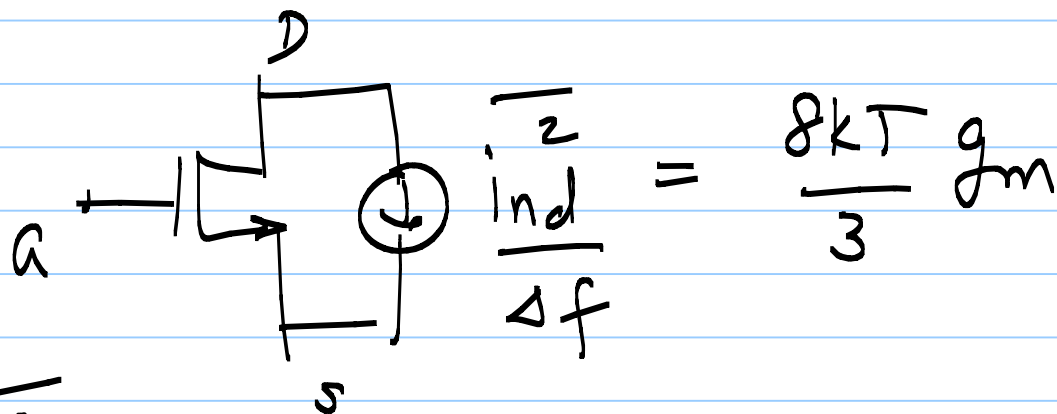
empirical parameter



$$\overline{i_n^2}/f = \frac{K_{1/f} \cdot g_m^2}{WL C_{ox}^2} \cdot \frac{1}{f}$$

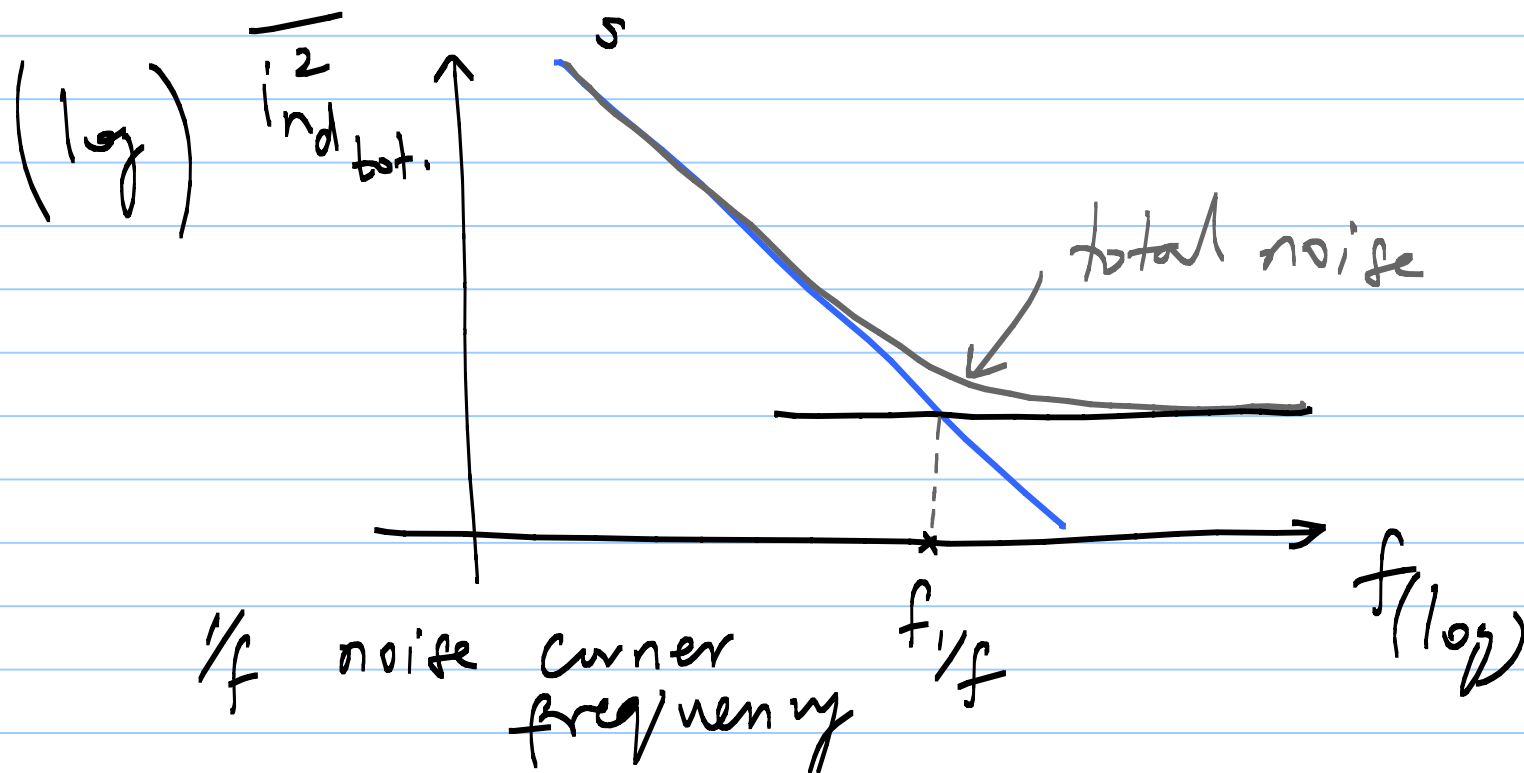
larger device $\leftrightarrow$ lower $1/f$ noise

2) Thermal noise:

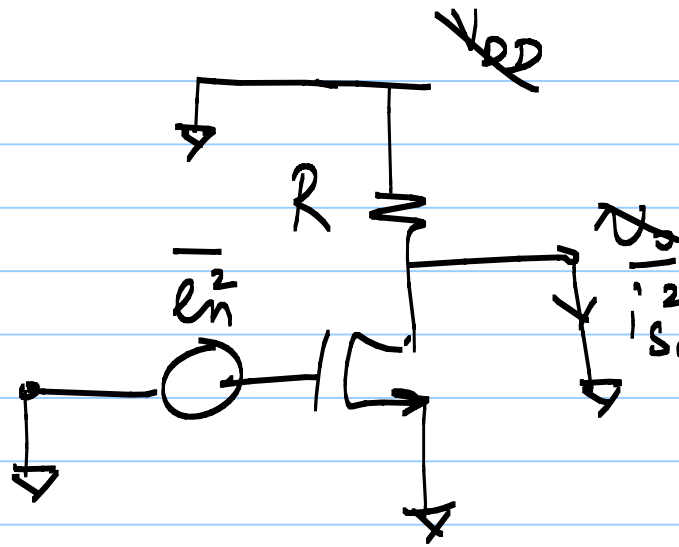


$$|i_d|^2 = g_m^2 \cdot |V_{gs}|^2$$

$$SNR_{\text{output}} = \frac{g_m^2 |V_{gs}|^2}{\frac{8kT}{3} g_m}$$



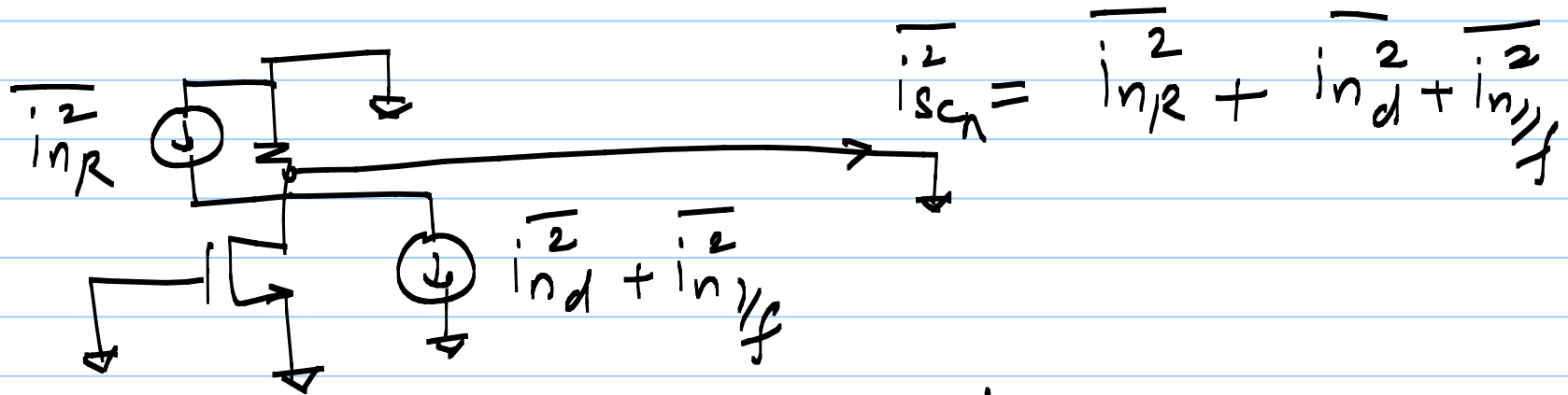
Σ.g.
1) CSA



$$i_{scn}^2 = g_m^2 \cdot e_n^2$$

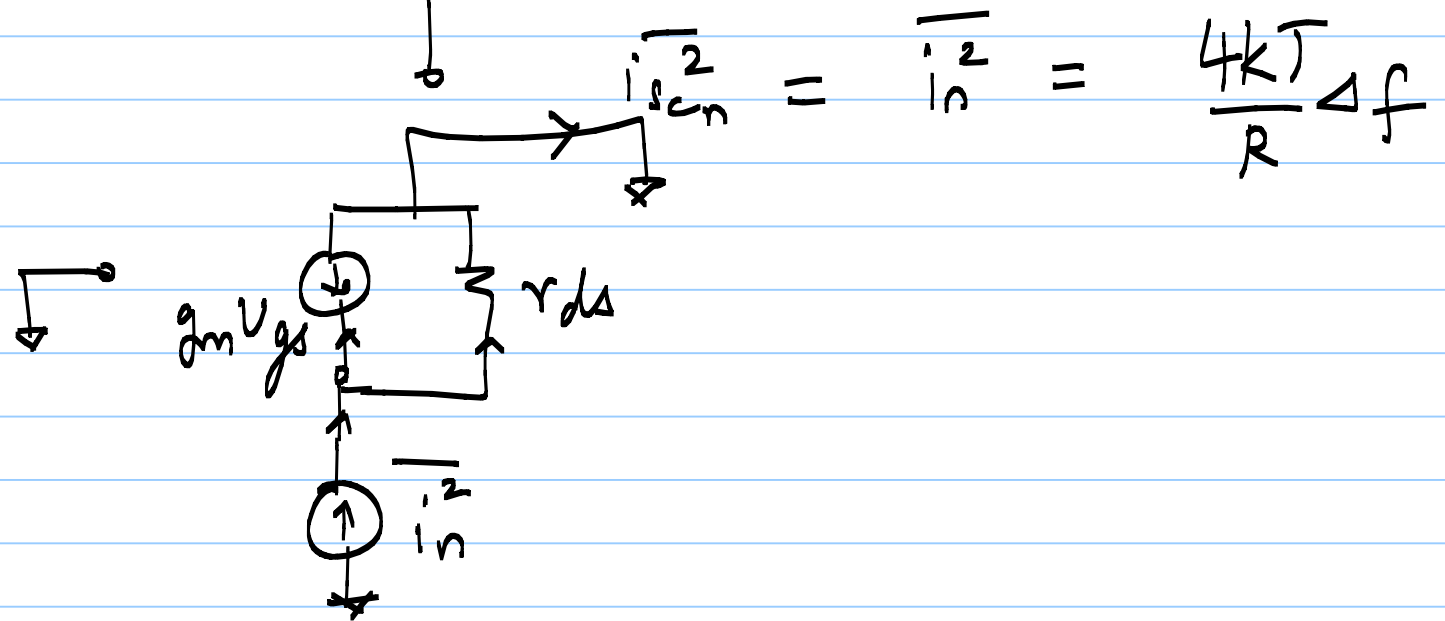
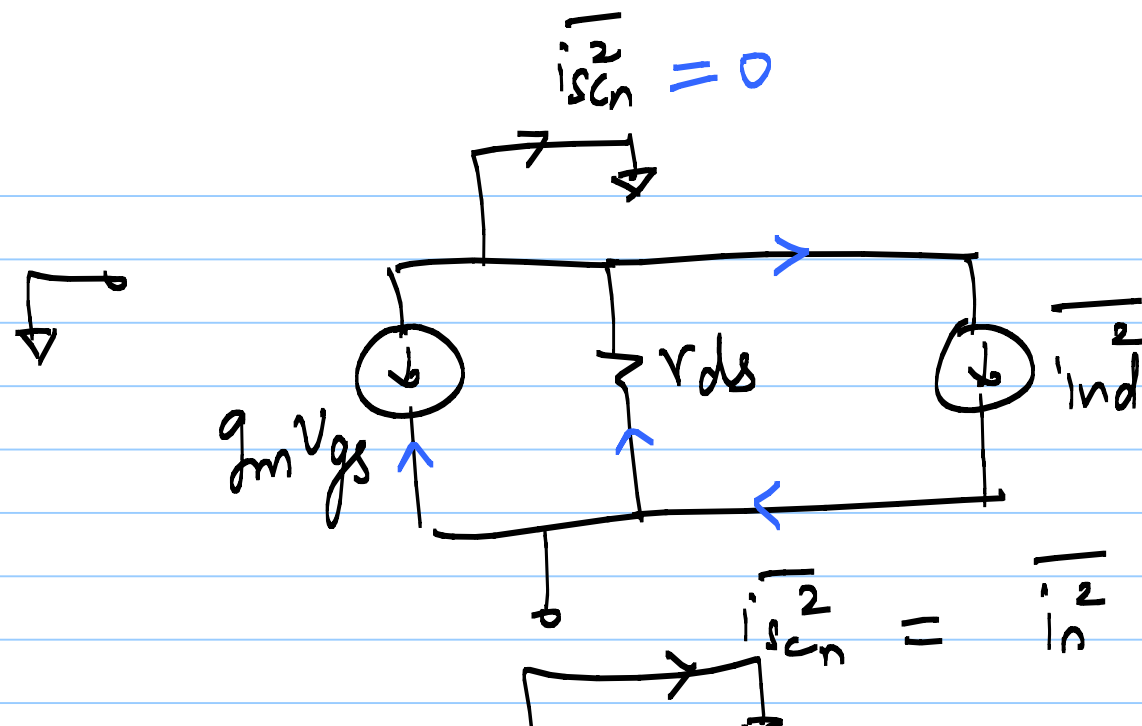
$$i_n = 0$$

$$e_n = ?$$



$$i_{scn}^2 = i_{nR}^2 + i_{nd}^2 + i_{nf}^2$$

$$\frac{e_n^2}{\Delta f} = \frac{4kT}{g_m^2 \cdot R} + \frac{8kT}{3g_m} + \frac{K_{1f}}{W \cdot L \cdot C_{ox}^2} \cdot \frac{1}{f}$$

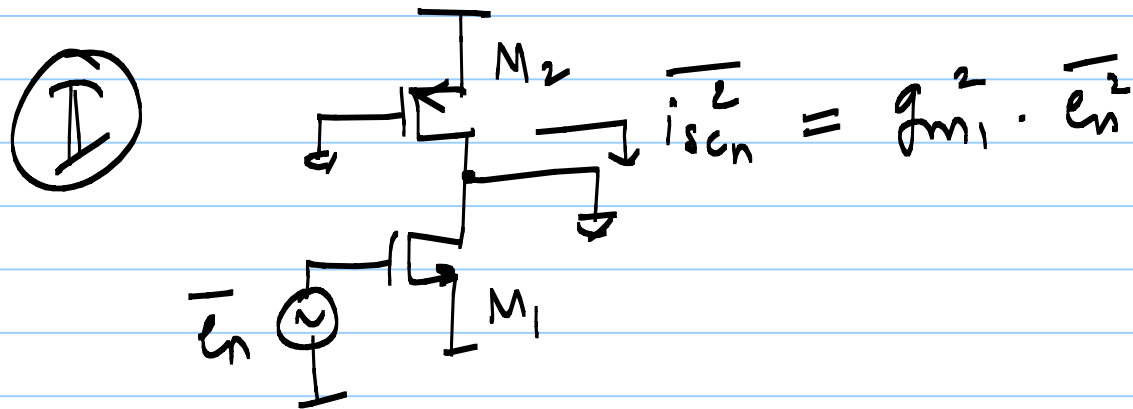
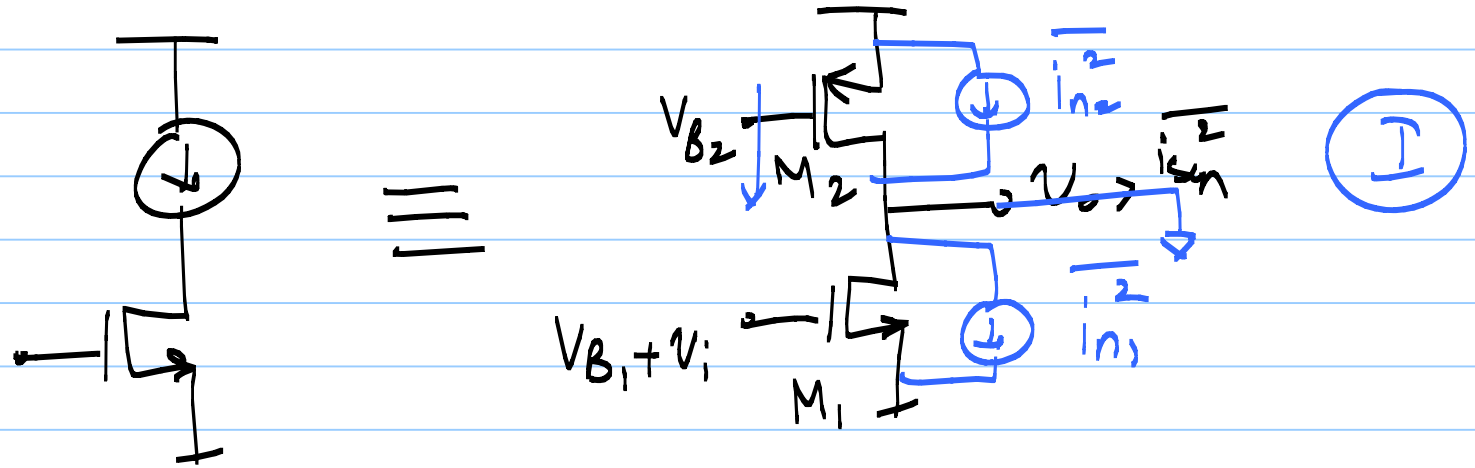


3) CDA — HW

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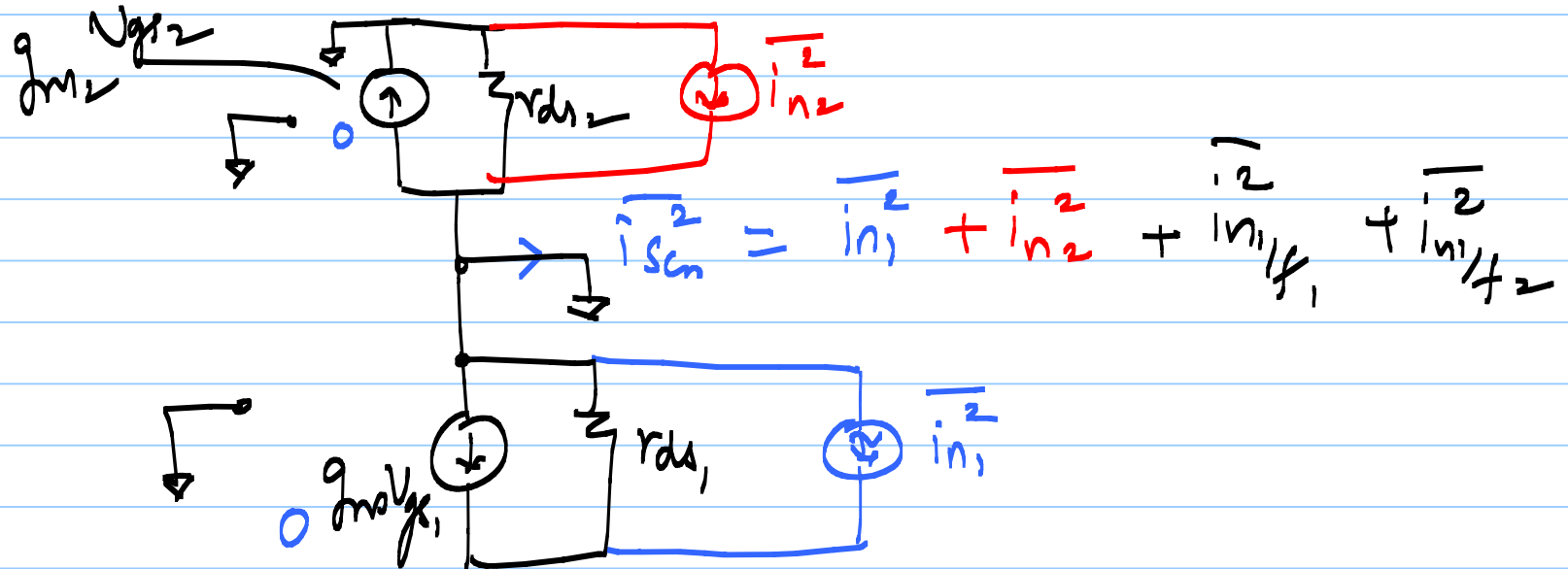
Lec 4

CSA w/ active load



$$i_{scn} = g_{m1}^2 \cdot e_{n2}$$

①



$$g_{m1}^2 \frac{\overline{e_n^2}}{\Delta f} = \frac{8kT}{3} (g_{m1} + g_{m2})$$

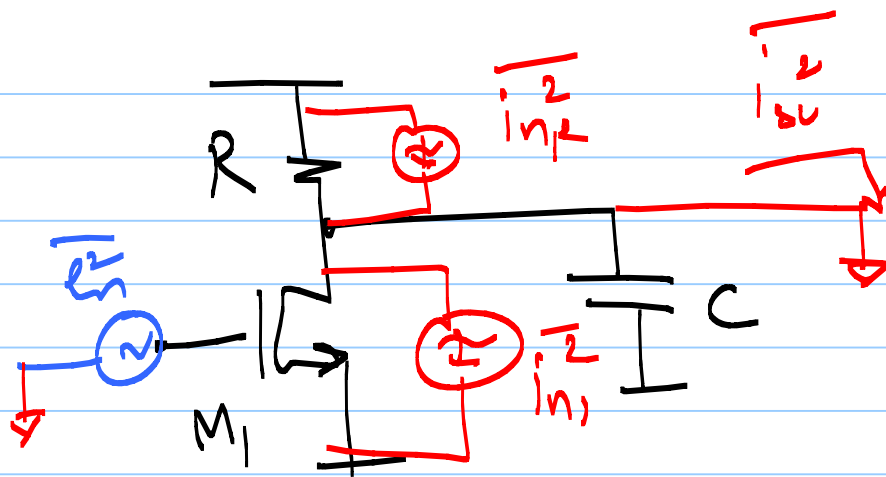
$$\frac{\overline{e_n^2}}{\Delta f} = \frac{8kT}{3g_{m1}} + \frac{8kT}{3} \frac{g_{m2}}{g_{m1}^2}$$

large g_{m1} ,
small g_{m2}
low noise

With flicker noise

$$\frac{\overline{e_n^2}}{\Delta f} = \frac{1}{g_{m1}^2} \left\{ \frac{8kT}{3} g_{m1} + \frac{8kT}{3} g_{m2} + \frac{K_{fn}}{W_n L_n C_{ox}^2} g_{m1}^2 \cdot \frac{1}{f} \right. \\ \left. + \frac{K_{fp}}{W_p L_p C_{ox}^2} g_{m2}^2 \cdot \frac{1}{f} \right\}$$

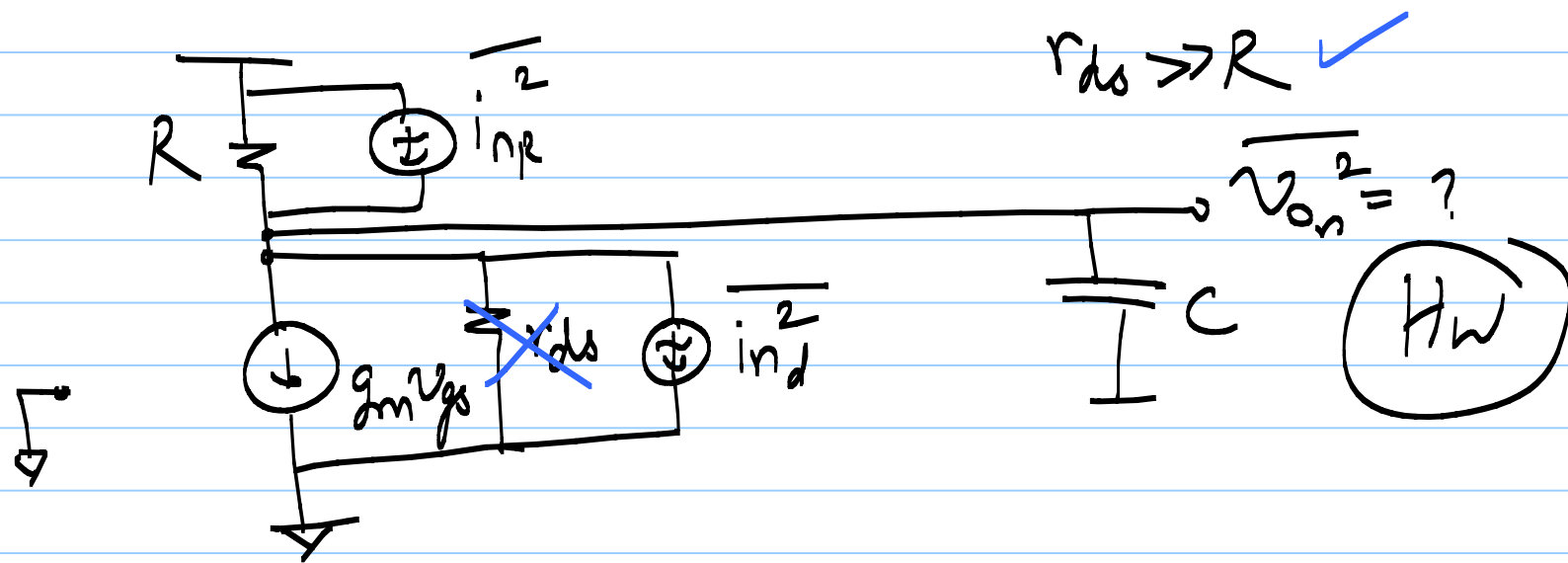
$$= \frac{8kT}{3 g_{m1}} + \frac{8kT}{3} \frac{g_{m2}}{g_{m1}^2} + \frac{K_{fn}}{W_n L_n C_{ox}^2} \cdot \frac{1}{f} \\ + \frac{K_{fp}}{W_p L_p C_{ox}^2} \cdot \frac{g_{m2}^2}{g_{m1}^2} \cdot \frac{1}{f}$$

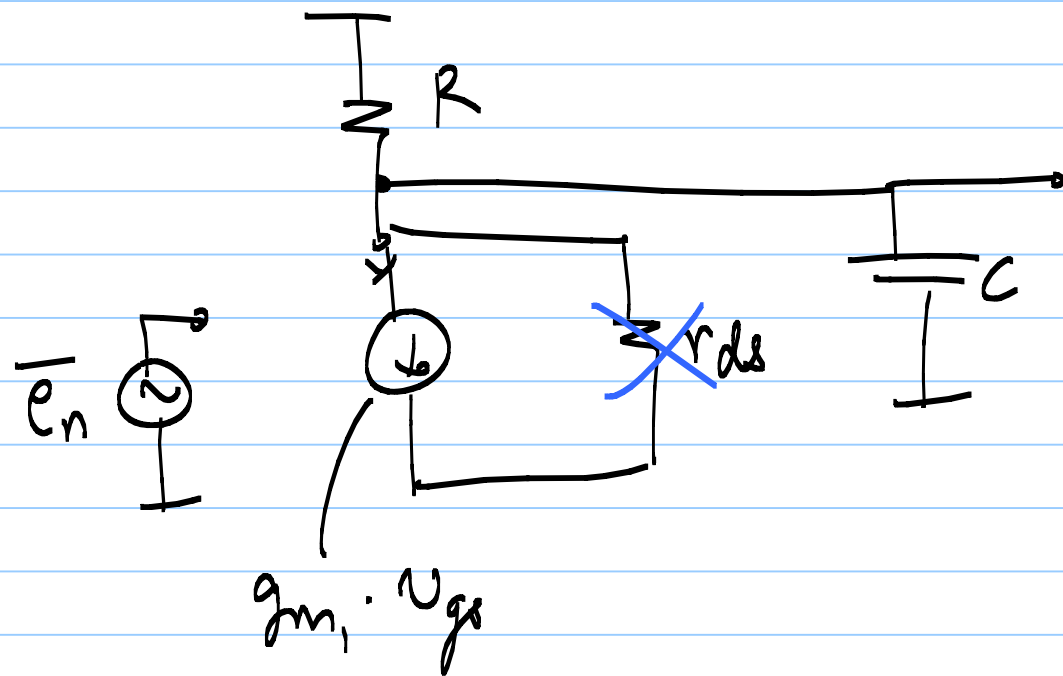


$$e_n = ?$$

same as
before?!

$$g_{m1}^2 e_n^2 = i_{n_R}^2 + i_{n_C}^2 + i_{n/f}^2$$





$$\overline{v_{on}^2} = g_{m1}^2 \cdot \overline{e_n^2} \cdot |Z|^2$$

$$Z = R \parallel \frac{1}{j\omega C}$$

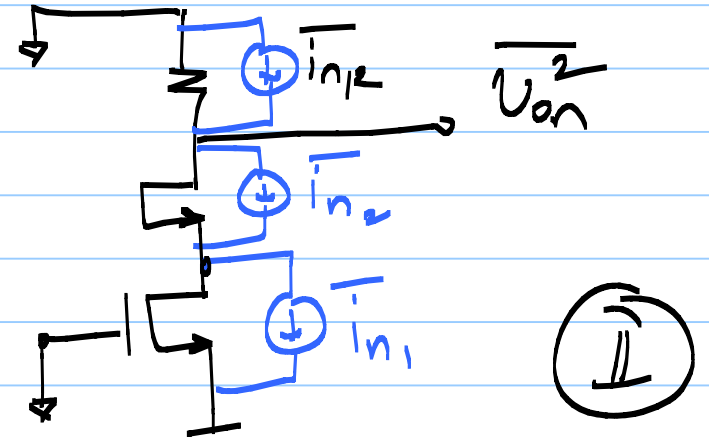
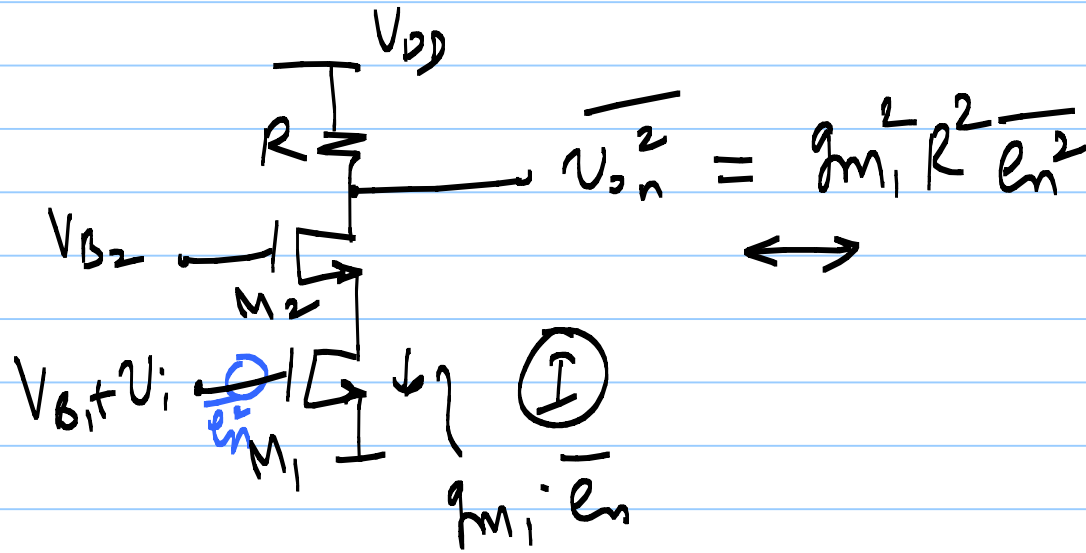
$$= \frac{R}{1 + j\omega RC}$$

$$\overline{v_{on}^2} = g_{m1}^2 \cdot \overline{e_n^2} \cdot \frac{R^2}{1 + \omega^2 R^2 C^2}$$

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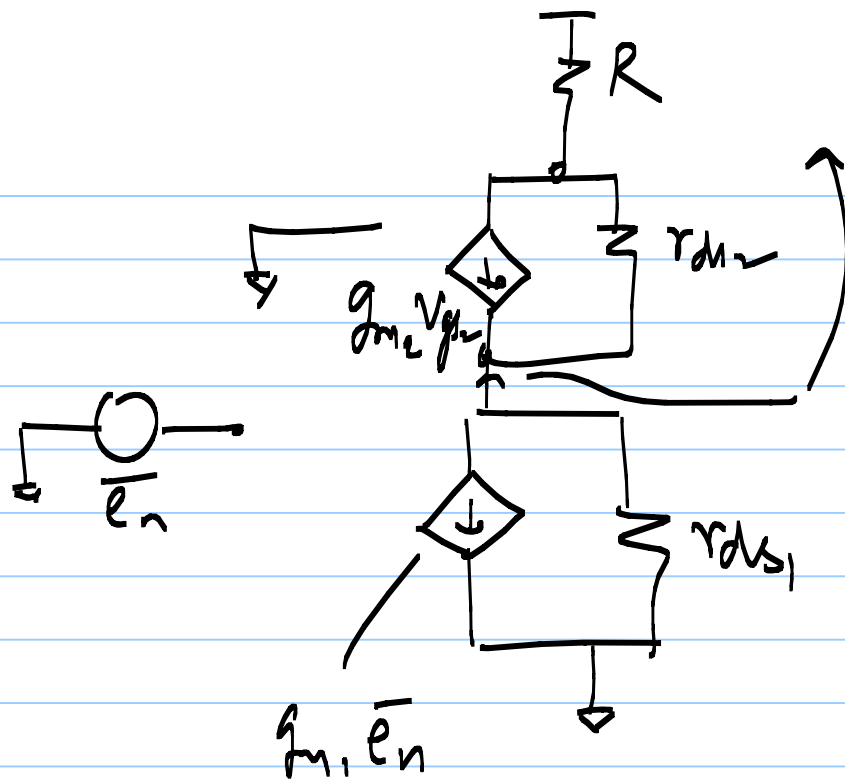
Lec 5

Cascode amplifier



$\textcircled{II} : \overline{v_{on,R}^2} = \overline{i_{n2}^2} \cdot R^2 ; \overline{v_{on,I}^2} = R^2 \cdot \overline{i_{n1}^2} \quad \left\{ \text{assuming } g_{m2} r_{ds2} \gg 1 \right\}$

$\overline{i_{n2}} = ?$



$$\frac{1}{g_{m2}} \sim r_{ds1}$$

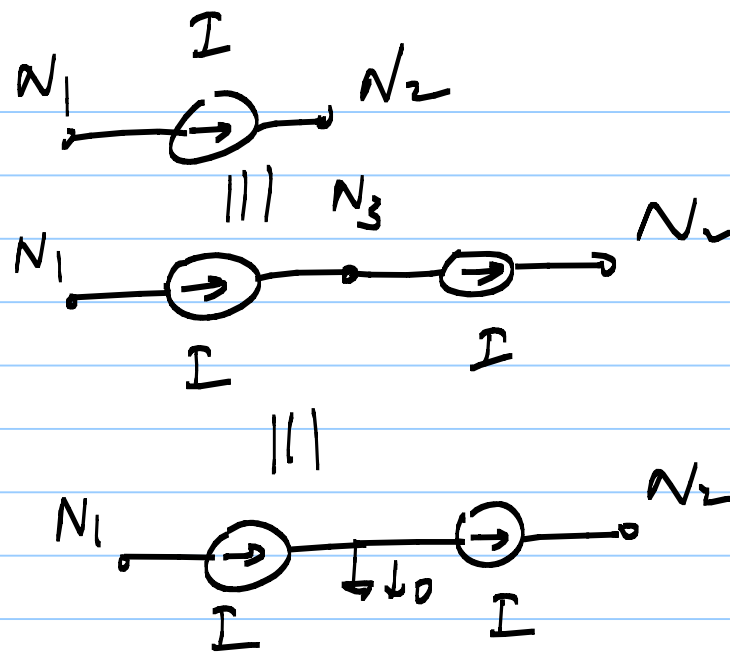
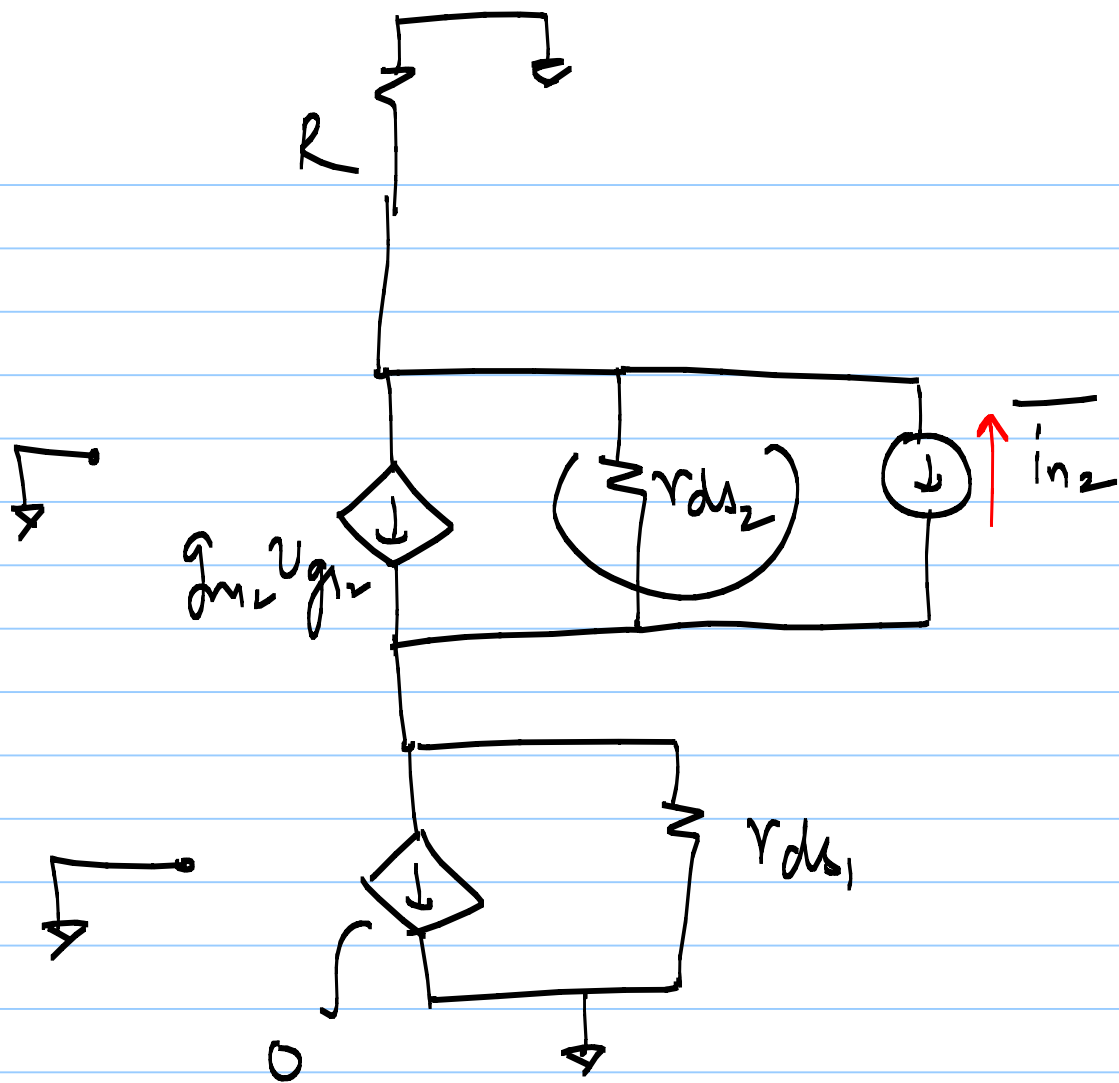
then

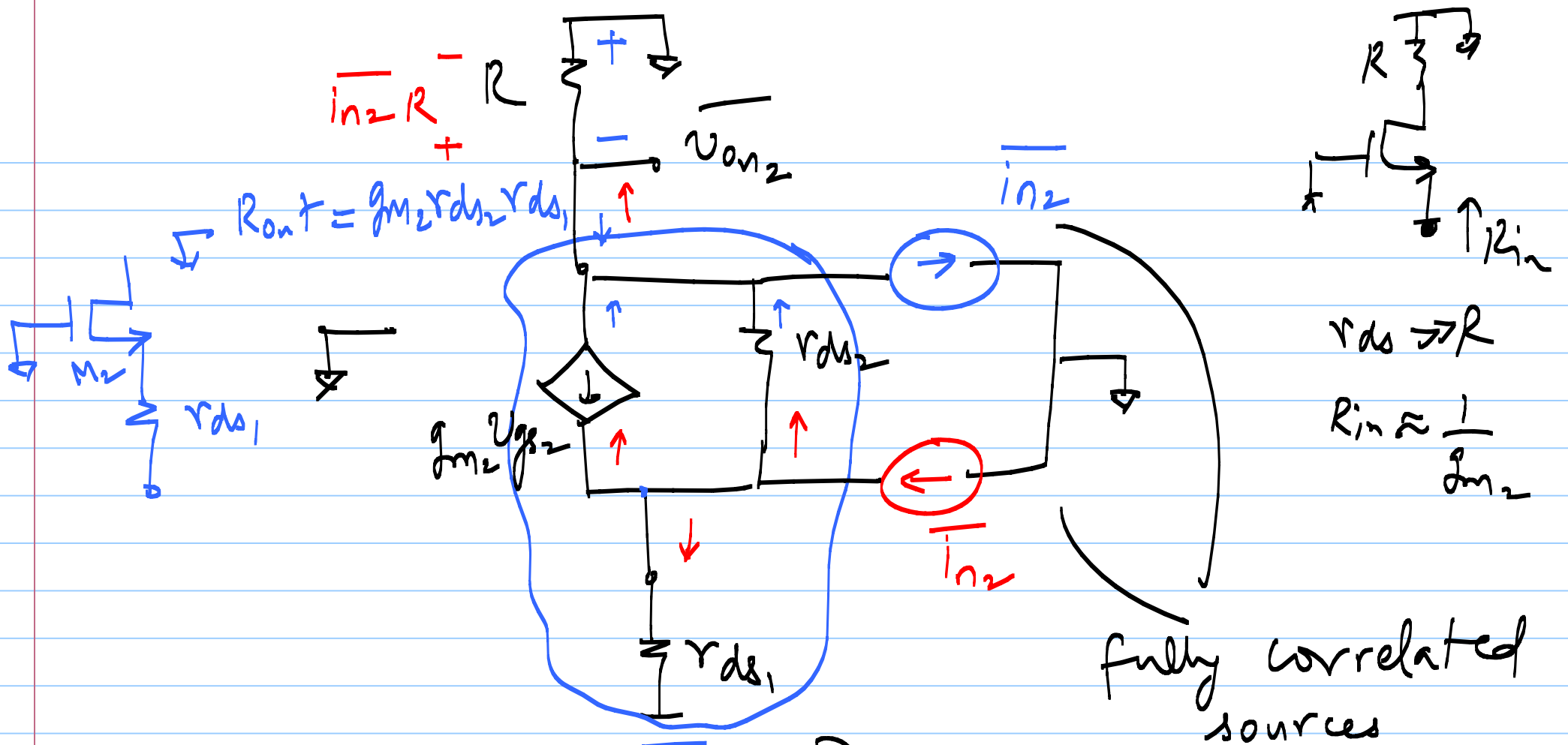
$$\bar{i}_{scn} = \frac{r_{ds1}}{\frac{1}{g_{m2}} + r_{ds1}} \cdot g_{m1} \bar{e}_n$$

$$\frac{1}{g_{m2}} \gg \frac{1}{r_{ds1}}$$

$$\bar{i}_{scn} \approx g_{m1} \bar{e}_n$$

$$\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$



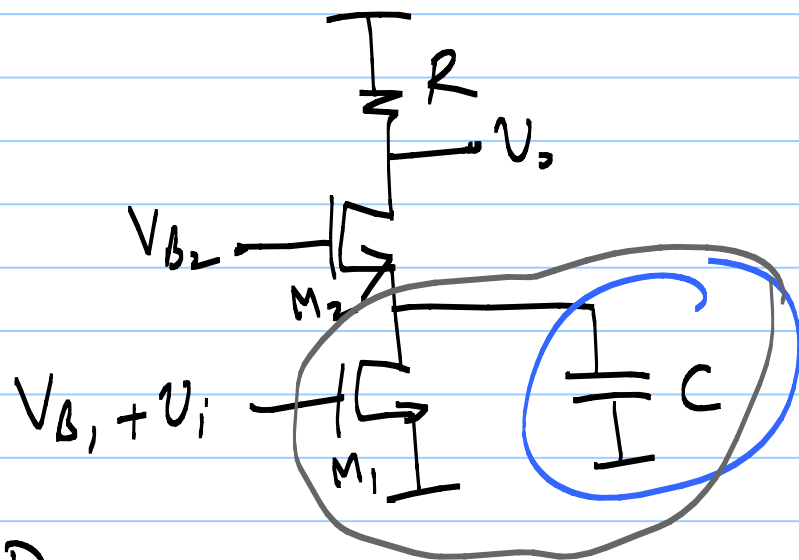


$$\left. \begin{aligned} \overline{v_{on2}} &= -\overline{i_{n2}} R \\ \overline{v_{on2}} &= +\overline{i_{n2}} R \end{aligned} \right\} \overline{v_{on2}} = 0$$

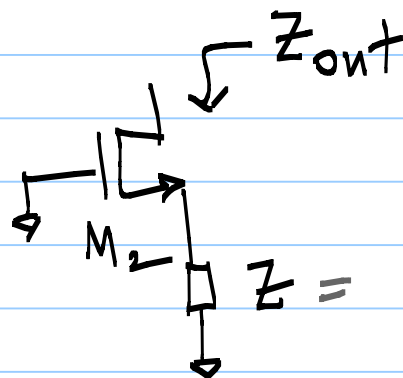
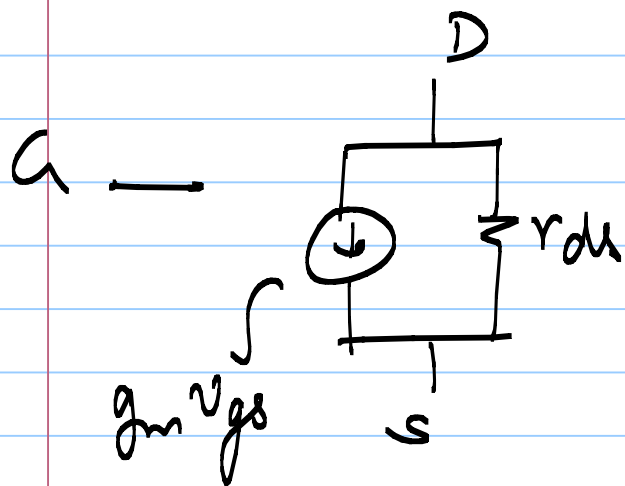
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Lec 6

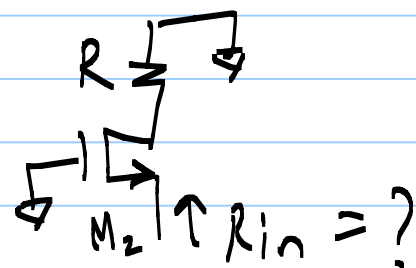
$$\overline{i_n} = 0, \quad \overline{e_n} = ?$$



$$Z = \frac{r_{ds1}}{1 + j\omega C r_{ds1}}$$

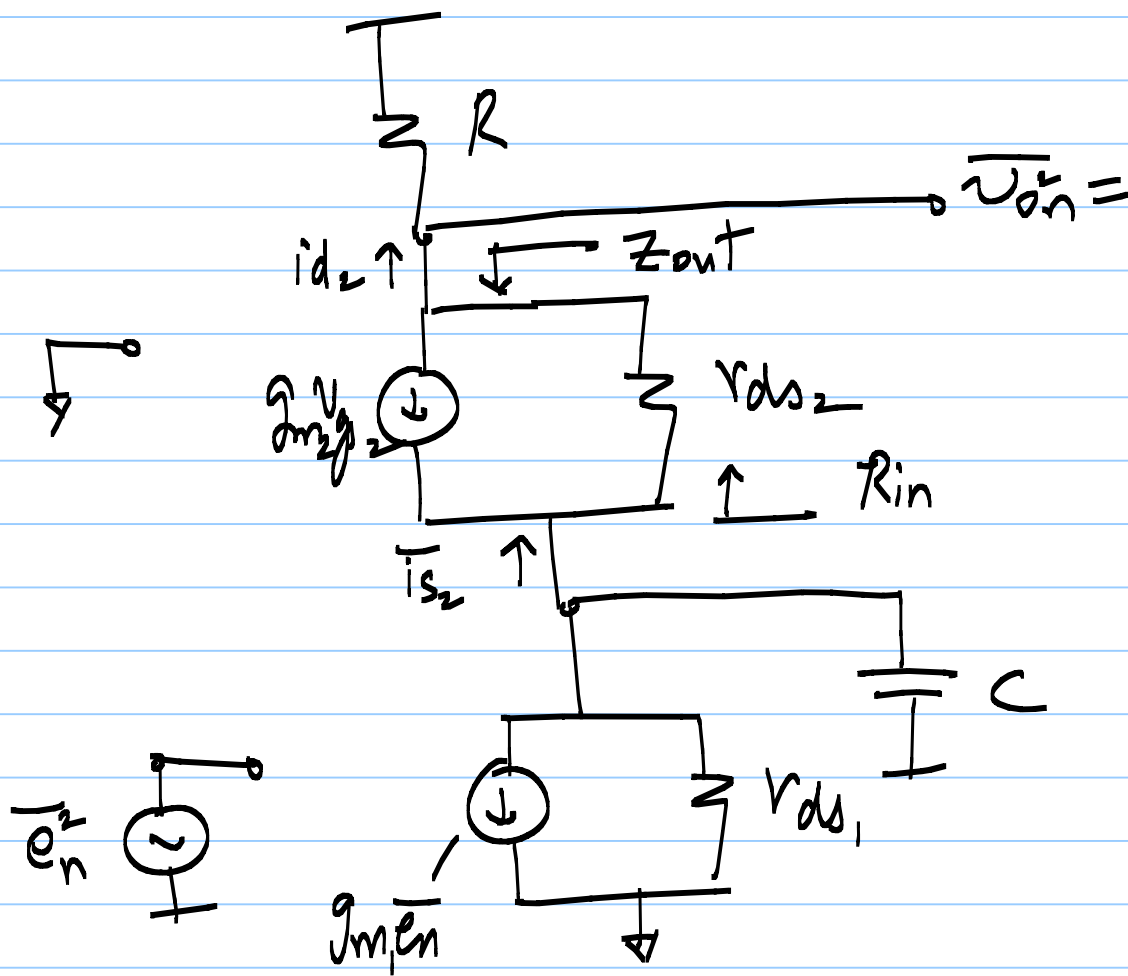


$$Z = r_{ds1} \parallel \frac{1}{j\omega C}$$



$$R_{in} = \frac{r_{ds1} + R}{1 + g_{m2} r_{ds2}}$$

$$Z_{out} = g_{m2} r_{ds2} Z + Z + \underline{r_{ds2}}$$



$$R_{in} \approx \frac{1}{g_{m2}} \text{ if } g_{m2} r_{ds2} \gg 1 \text{ and } r_{ds2} \gg R$$

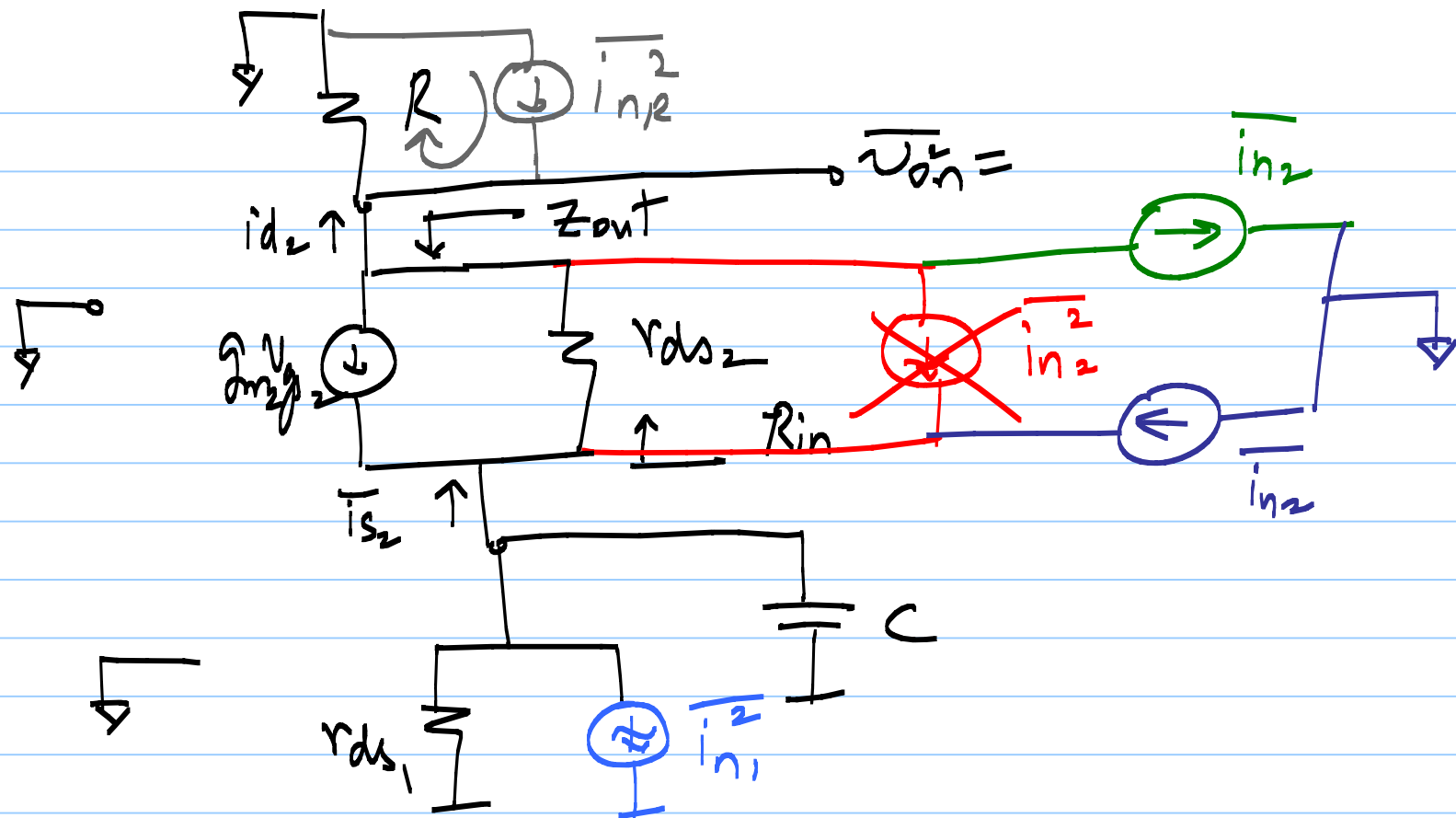
Assume $\frac{1}{g_{m2}} \ll r_{ds1}$

$$\overline{i_{s2}} = \frac{\frac{1}{j\omega C}}{\frac{1}{g_{m2}} + \frac{1}{j\omega C}} \cdot g_{m1} \overline{e_n}$$

$$= \frac{g_{m2}}{g_{m2} + j\omega C} \cdot g_{m1} \overline{e_n} = \overline{i_{d2}}$$

$$\overline{v_{on}} = \overline{i_{d2}} \cdot R$$

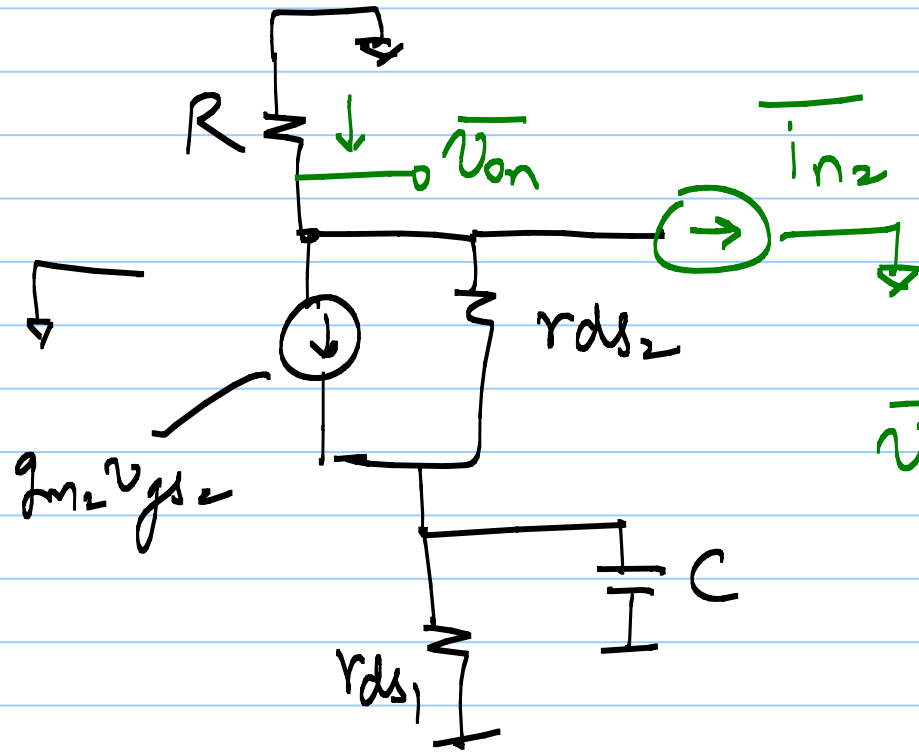
$$\overline{v_{on}^2} = R^2 \cdot \overline{i_{d2}^2} = \frac{g_{m1}^2 g_{m2}^2 R^2}{g_{m2}^2 + \omega^2 C^2} \cdot \overline{e_n^2}$$



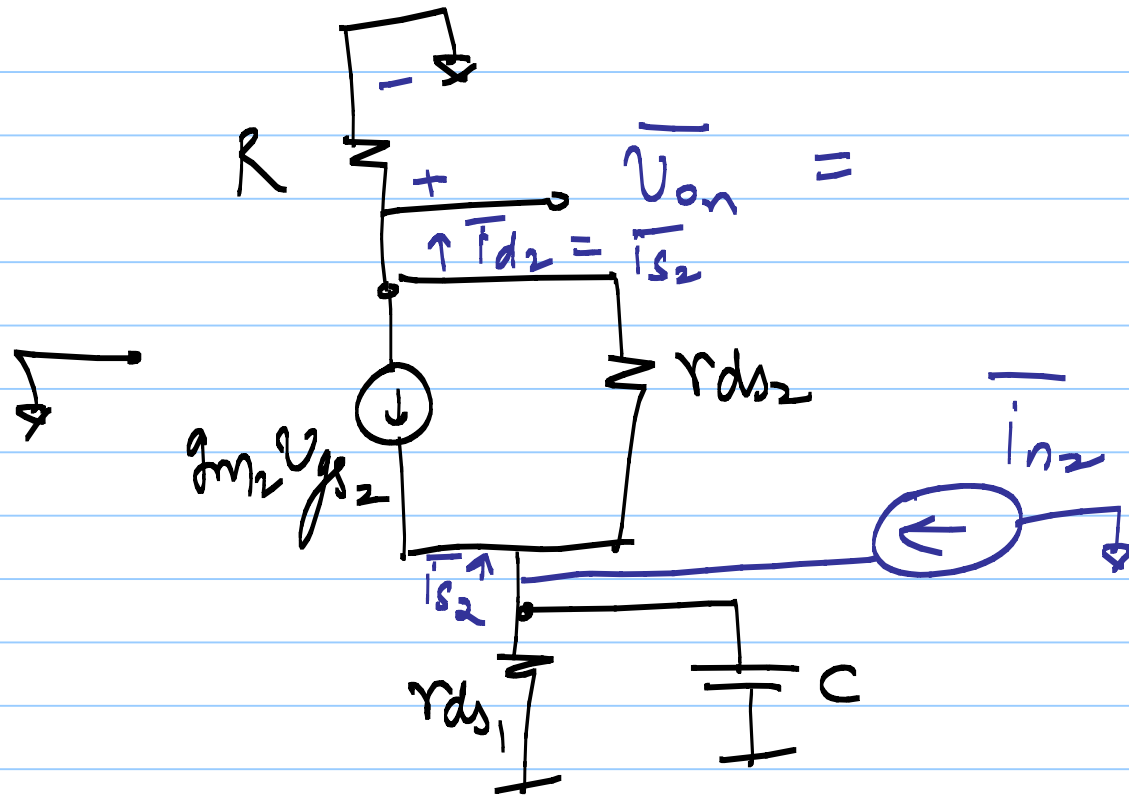
$$v_{o1} = \frac{g_{m2}^2 R^2}{g_{m2}^2 + \omega^2 C^2} \cdot i_{n1} \leftarrow$$

$$\overline{v_{on}^2} = \overline{i_{n2}^2} \cdot R^2$$

assuming $r_{ds2} \rightarrow R \leftarrow$



$$\overline{v_{on}} = -\overline{i_{n2}} R$$



$$\bar{i}_{s2} = \frac{1/j\omega C}{1/j\omega C + 1/g_{m2}} \cdot \bar{i}_{n2} = \frac{g_{m2}}{g_{m2} + j\omega C} \cdot \bar{i}_{n2}$$

$$\bar{v}_{on} = + \frac{g_{m2} R}{g_{m2} + j\omega C} \cdot \bar{i}_{n2}$$

$$\overline{v_{on}} = \overline{v_{on}} + \overline{v_{on}}$$

$$= -\overline{i_{n2}} R + \frac{g_{m2} R}{g_{m2} + j\omega C} \cdot \overline{i_{n2}}$$

$$= \overline{i_{n2}} R \cdot \frac{-j\omega C}{g_{m2} + j\omega C}$$

$$\overline{v_{on2}^2} = \frac{\omega^2 C^2 R^2}{g_{m2}^2 + \omega^2 C^2} \cdot \overline{i_{n2}^2}$$

$$\text{Total } \overline{v_{on}^2} = \overline{v_{on1}^2} + \overline{v_{on2}^2} + \overline{v_{onr}^2}$$

$$= \frac{g_{m2}^2 R^2}{g_{m2}^2 + \omega^2 C^2} \cdot \overline{i_{n1}^2} + \frac{\omega^2 C^2 R^2}{g_{m2}^2 + \omega^2 C^2} \cdot \overline{i_{n2}^2} + \overline{i_{nr}^2} \cdot R^2$$

$$\frac{g_{m1}^2 g_{m2}^2 \cancel{R^2}}{\cancel{g_{m2}^2 + \omega^2 C^2}} \cdot \overline{e_n^2}$$

$$= \frac{g_{m2}^2 \cancel{R^2}}{\cancel{g_{m2}^2 + \omega^2 C^2}} \cdot \overline{i_{n1}^2} + \frac{\omega^2 C^2 \cancel{R^2}}{\cancel{g_{m2}^2 + \omega^2 C^2}} \cdot \overline{i_{n2}^2} + \overline{i_{nR}^2} \cdot \cancel{R^2} (g_{m2}^2 + \omega^2 C^2)$$

$$\overline{e_n^2} = \frac{\overline{i_{n1}^2}}{g_{m1}^2} + \frac{\omega^2 C^2}{g_{m1}^2 g_{m2}^2} \cdot \overline{i_{n2}^2} + \frac{g_{m2}^2 + \omega^2 C^2}{g_{m1}^2 g_{m2}^2} \cdot \overline{i_{nR}^2}$$

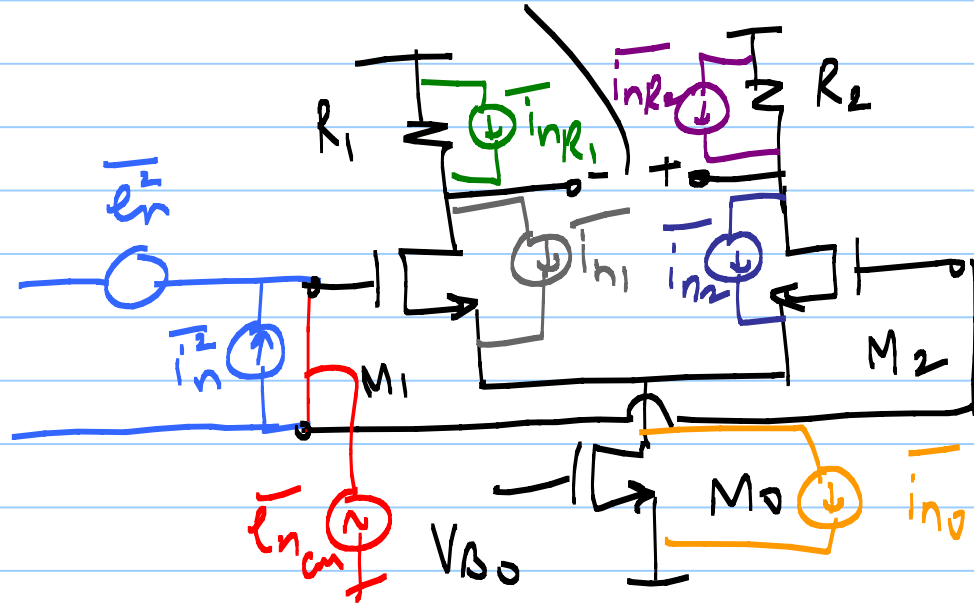
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$\overline{V_{on}}^2$ Lec 7

Noise of Diff. Amplifier

$$\overline{i_n} = 0 \quad R_1 = R_2 = R$$

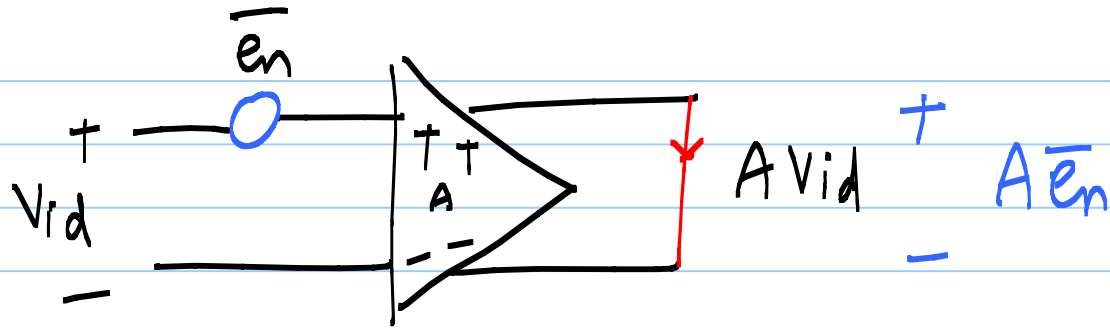
$$\overline{e_n} = ? \quad g_{m1} = g_{m2} = g_m$$



* Noise analysis
— cannot use "half-circuit" analysis

* Noise sources are applied asymmetrically in the diff. circuit

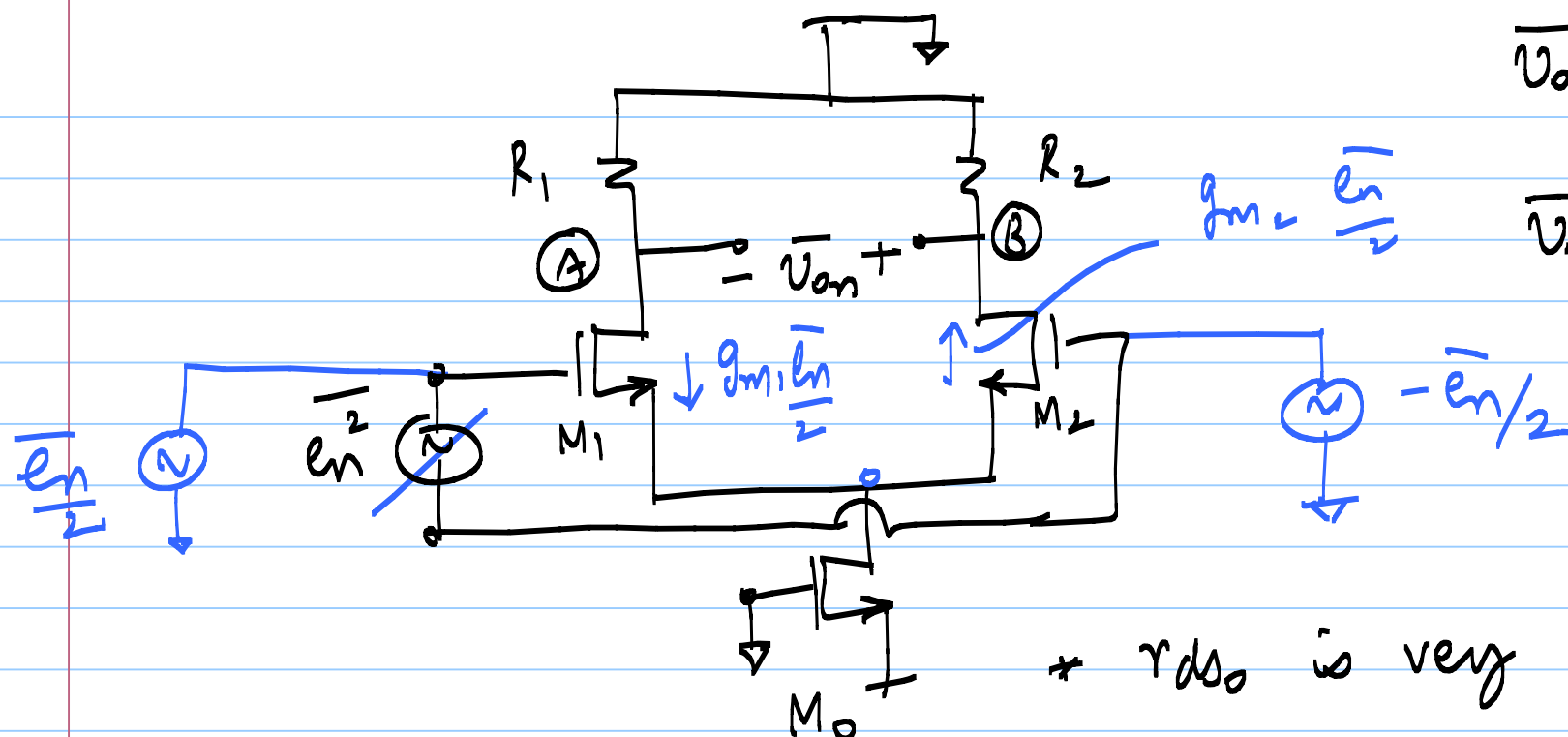
* Can use H.C. concepts when calculating output noise due to $\overline{e_n}/\overline{i_n}$



set $V_{id} = 0$ for noise analysis

case I: apply $\bar{e}_n$ only

case II: apply $\bar{i}_{n1}$, $\bar{i}_{n2}$, $\bar{i}_{no}$, $\bar{i}_{n1}$, $\bar{i}_{n2}$ in turn
and find $\bar{V}_{on}^2$ as mean
square sum



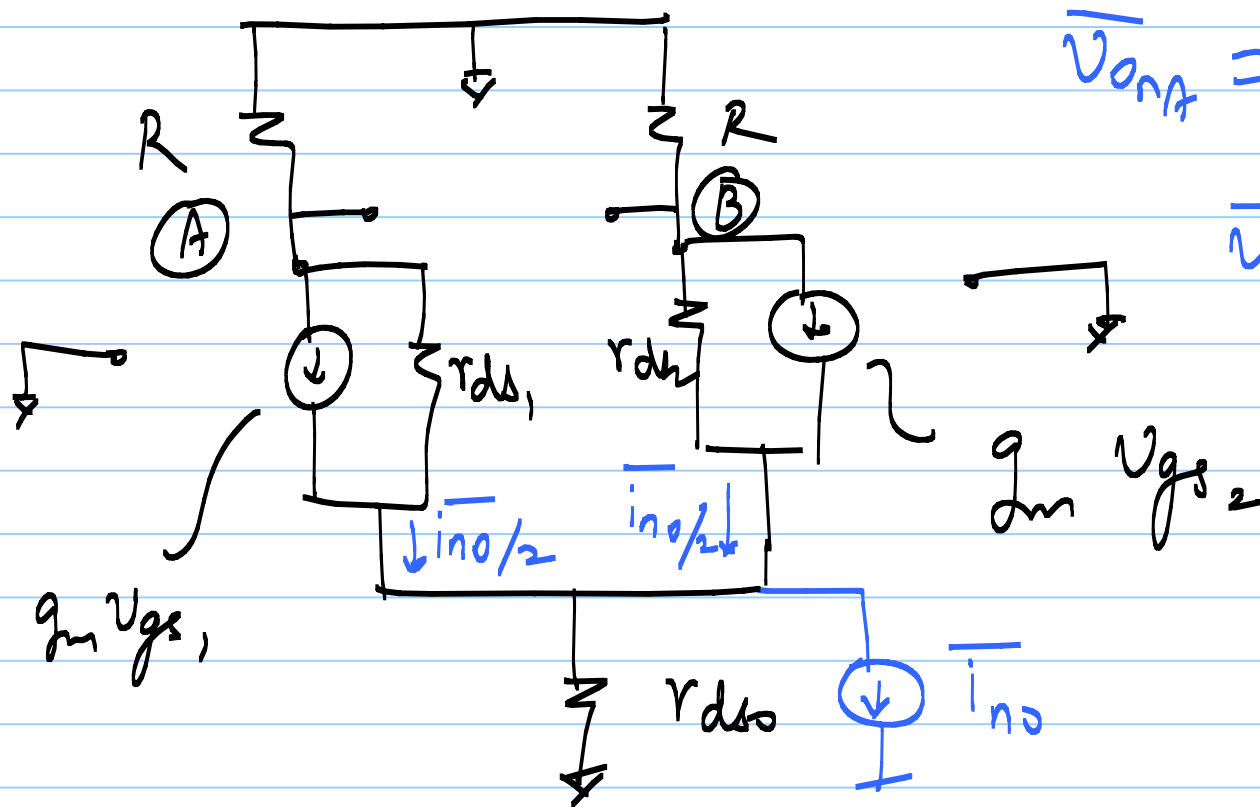
$$\overline{V_{onA}} = -g_{m1} R_1 \cdot \frac{e_n}{2}$$

$$\overline{V_{onB}} = g_{m2} R_2 \cdot \frac{e_n}{2}$$

* r_{ds0} is very high

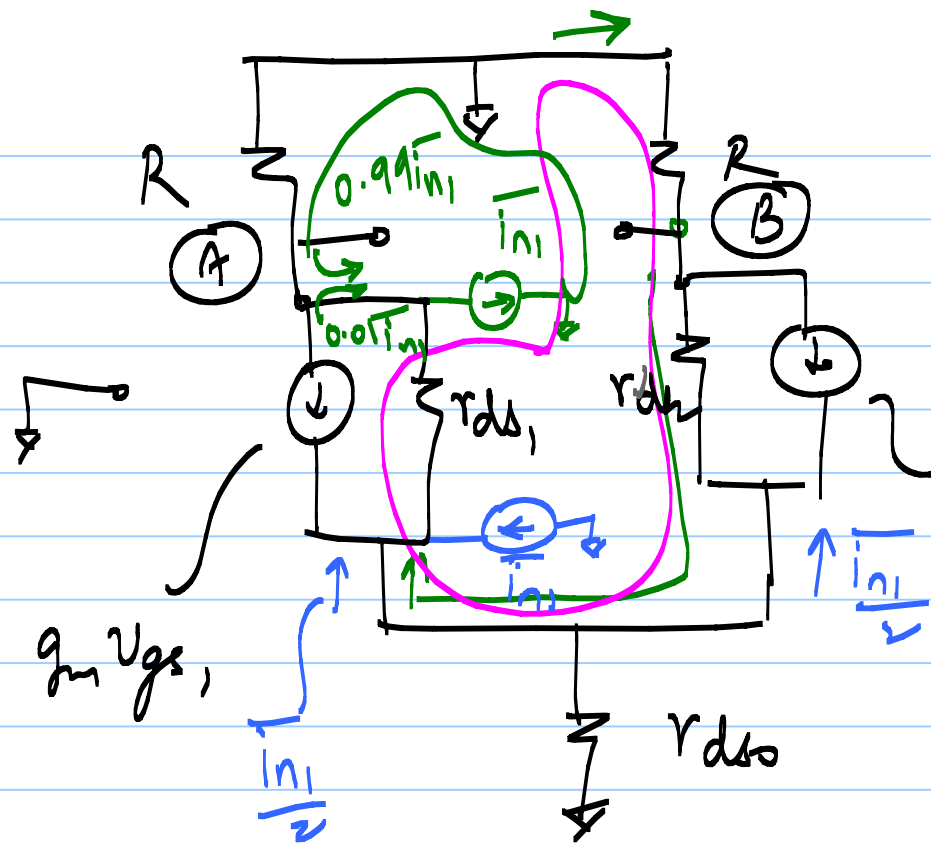
$$\overline{V_{on}} = \overline{V_{onB}} - \overline{V_{onA}} = g_m R e_n$$

$$\overline{V_{on}^2} = g_m^2 R^2 \overline{e_n^2}$$



$$\overline{V_{outA}} = -\frac{R \overline{i_{no}}}{2} = \overline{V_{outB}}$$

$$\overline{V_{on}} = 0$$



$$\overline{v_{onA}} = \overline{v_{onB}} = \frac{R \overline{i_{n1}}}{2}$$

$$\overline{v_{onA}} = -R \overline{i_{n1}}$$

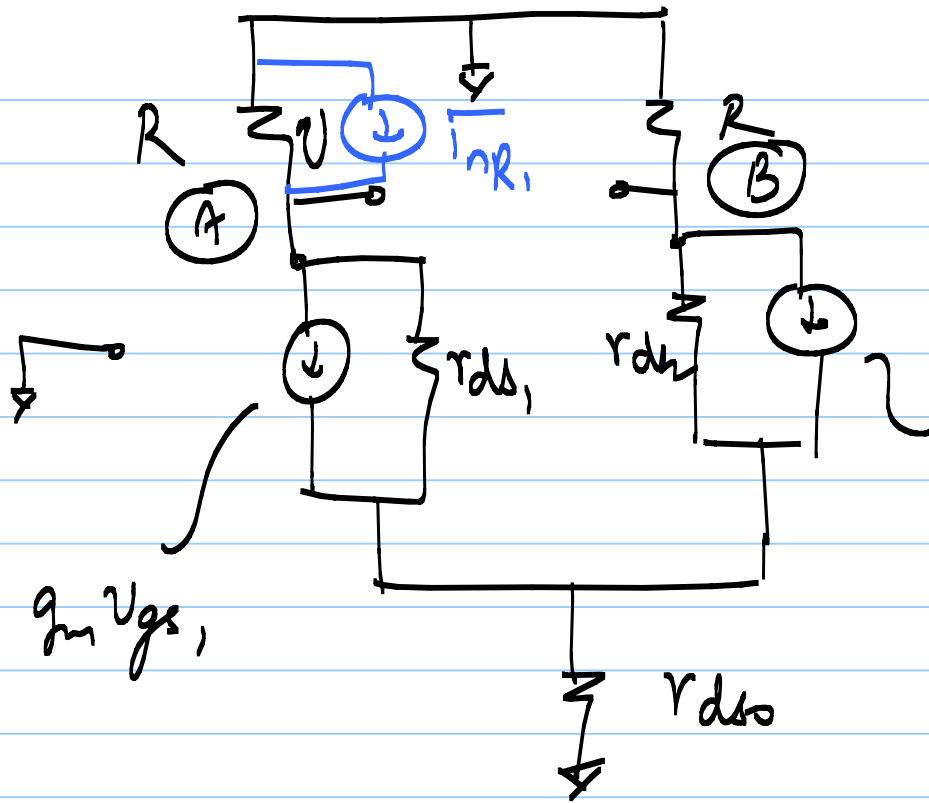
$$\overline{v_{onB}} = 0$$

$$g_m v_{gs2}$$

$$\overline{v_{on}} = R \overline{i_{n1}}$$

$$\overline{v_{on}^2} = R^2 \overline{i_{n1}^2}$$

$$\text{due to } M_2: \overline{v_{on}^2} = R^2 \cdot \overline{i_{n2}^2}$$



$$\overline{v_{out,A}} = R \overline{i_{nR,1}} ; \overline{v_{out,B}} = 0$$

$$\overline{v_{out}^2} = R^2 \cdot \overline{i_{nR,1}^2}$$

$$g_m v_{gs,2}$$

$$\text{for } \overline{i_{nR,2}^2} = 0 \quad \overline{v_{out,A}} = 0$$

$$\overline{v_{out,B}} = R \cdot \overline{i_{nR,2}}$$

$$\overline{v_{out}} = R^2 \cdot \overline{i_{nR,2}^2}$$

$$\text{Total } \overline{v_{on}^2} = R^2 \cdot [\overline{i_{n1}^2} + \overline{i_{n2}^2} + \overline{i_{nR1}^2} + \overline{i_{nR2}^2}]$$

$$= g_m^2 R^2 \cdot \overline{e_n^2}$$

$$\frac{\overline{e_n^2}}{\Delta f} = \frac{1}{g_m^2} \left[\frac{16kT}{3} g_m + \frac{8kT}{R} \right]$$

$$= \frac{16kT}{3g_m} + \frac{8kT}{g_m^2 R}$$

HW: determine $\overline{e_n}$ using $\overline{i_{scn}^2}$
 S.C. noise current

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Lec 8

* $\bar{e}_n$ & $\bar{i}_n$

* Apply v_s & i_s — separate effect of $\bar{e}_n$ & $\bar{i}_n$

* Apply s.c. ($\bar{i}_{sc}$) or o.c. ($\bar{v}_{oc}^2$) at o/p.

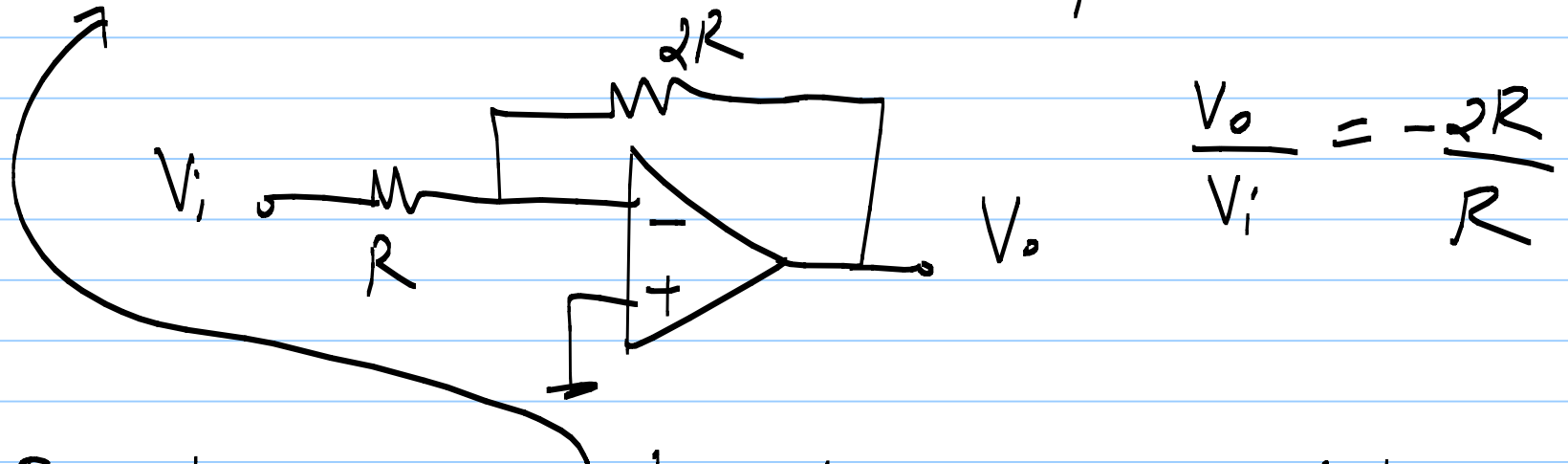
* Case I : $\bar{e}_n$ & $\bar{i}_n$ with ideal 2-port

Case II : apply noise sources in turn using superposition

* equate the two

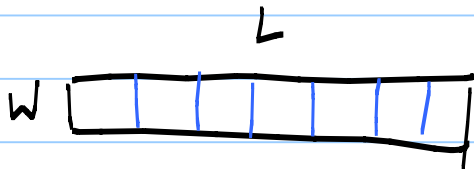
Mismatch

- * Expect 2 components / circuits etc to be identical or exact multiples



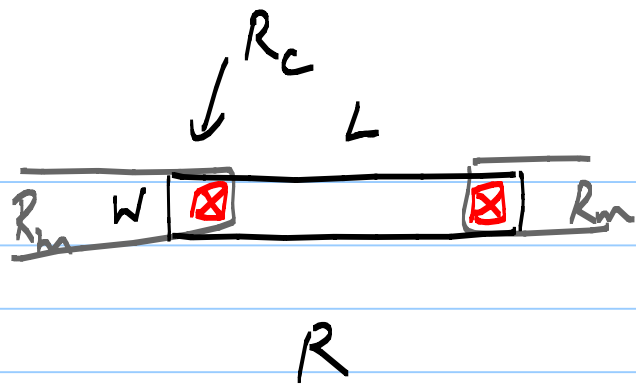
$$\frac{V_o}{V_i} = -\frac{2R}{R}$$

- * If they are not, they are said to be mismatched.

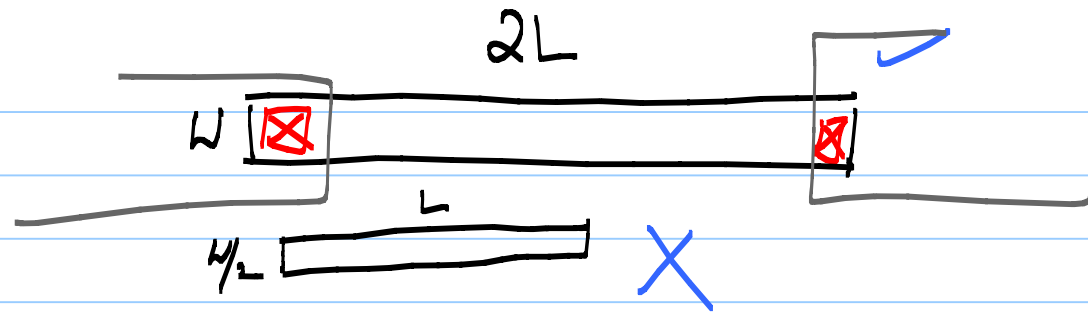


$$R_{\text{sheet}} = \frac{\Omega}{\square}$$

$$R = R_{\text{sheet}} \times \# \text{ of } \square$$



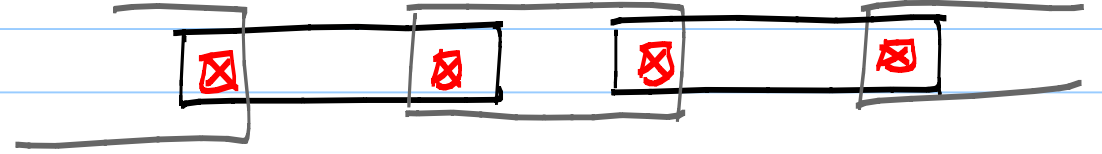
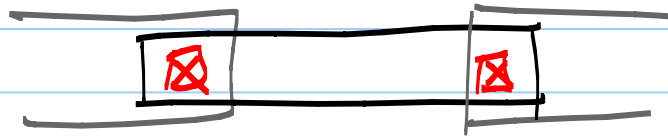
$$R_{actual} = R + 2R_c$$



$$R'_{actual} = 2R + 2R_c$$

$M_x - M_y$ connection $\hat{=}$ Via

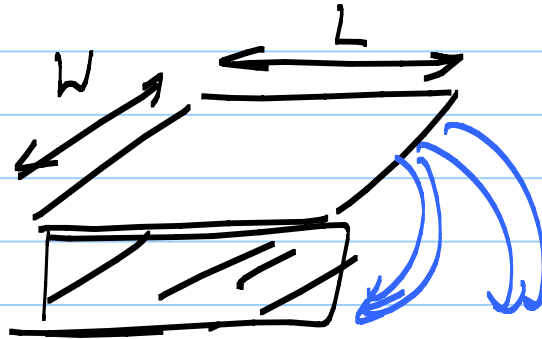
Diffusion - M_1 connection = 'contact'



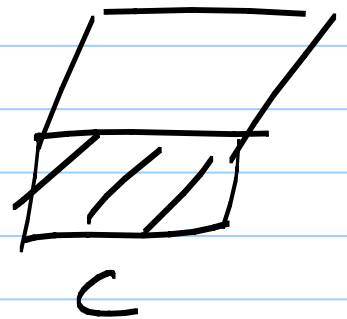
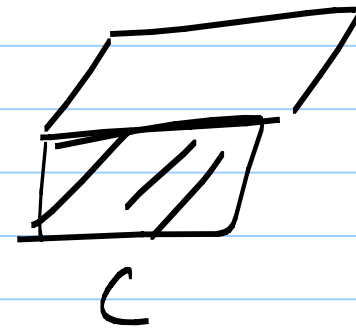
$$R_{ac} = R + 2R_c$$

$$R_{ac}' = 2R + 4R_c$$

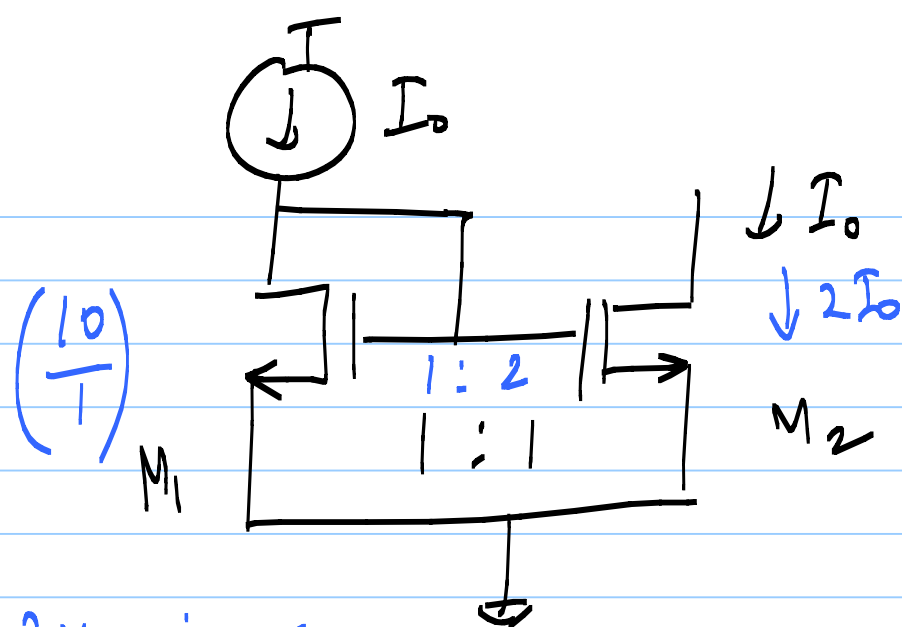
* We want C & $2C$ capacitors



$$C = \epsilon_0 \epsilon_r A / d$$



* Fringe cap. depends on perimeter; so, we use 2 identical pieces



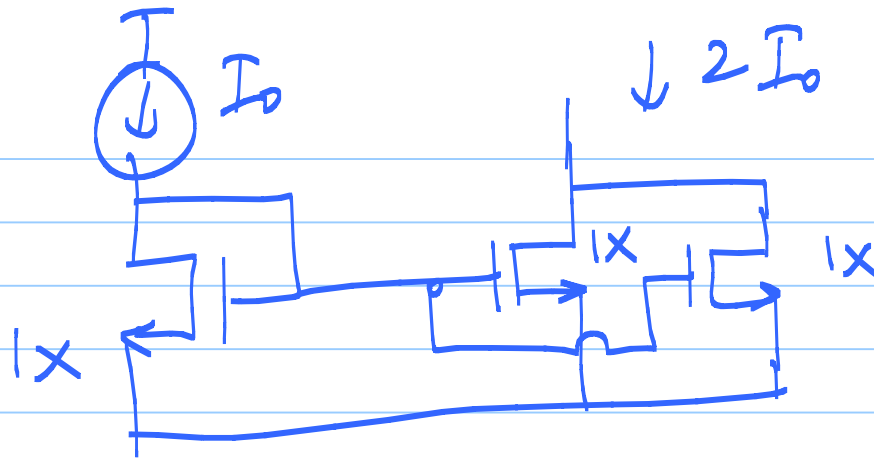
If $V_{DS2} = V_{AS1}$,
you need to ensure
 $I_2 = I_0$

$$L_1 = L_2; \text{ \& } W_1 = W_2$$

2x mirror

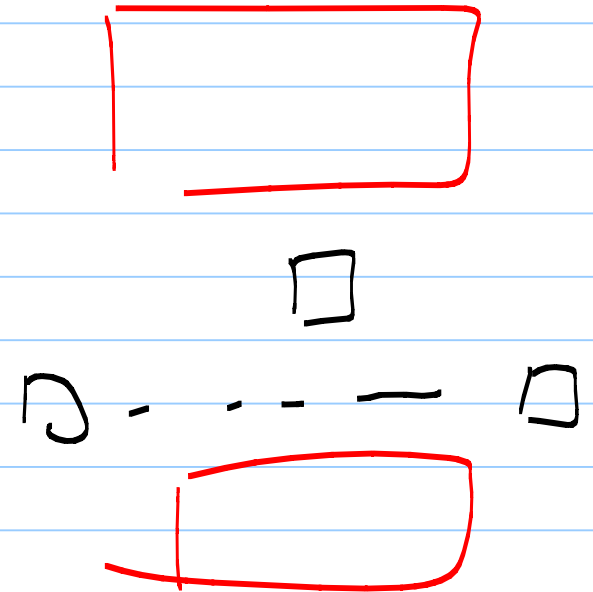
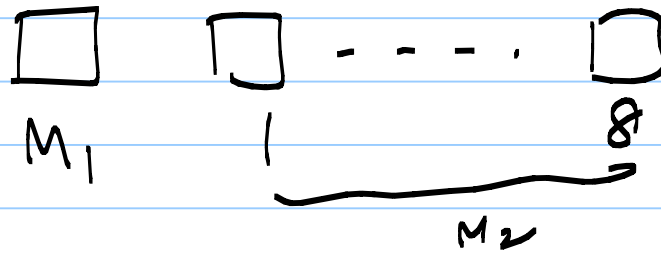
$$\textcircled{1} \quad \left(\frac{W}{L}\right)_2 = \left(\frac{20\mu\text{m}}{1\mu\text{m}}\right) \times$$

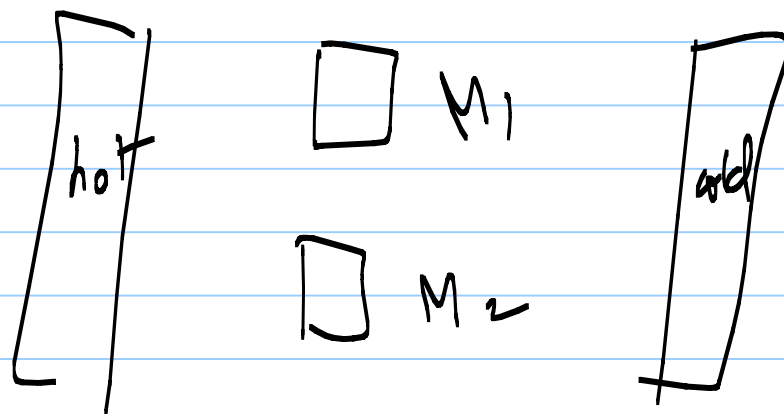
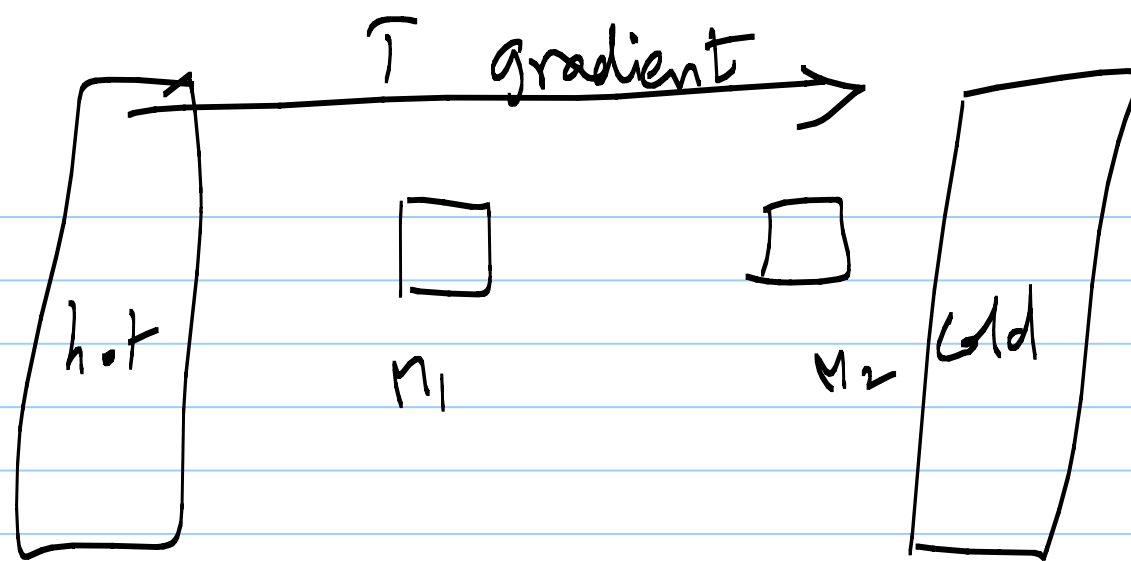
$$\textcircled{2} \quad \left(\frac{W}{L}\right)_2 = 2 \times \left(\frac{10\mu\text{m}}{1\mu\text{m}}\right) \checkmark$$

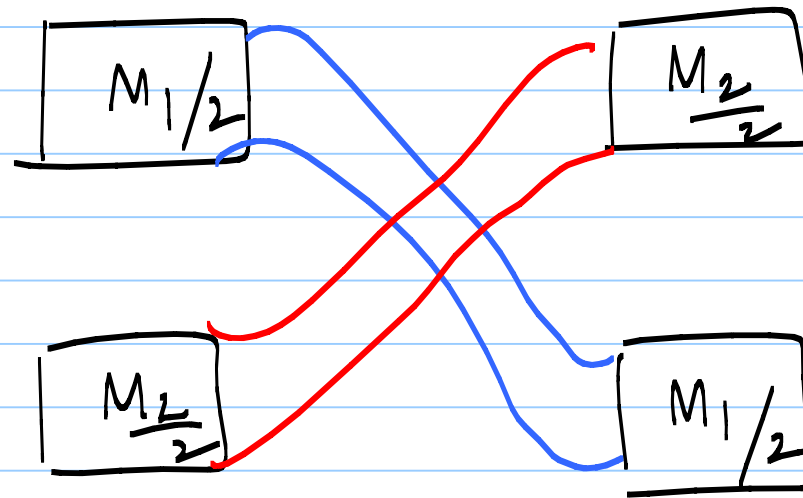


Layout :

e.g. 1:8 CM





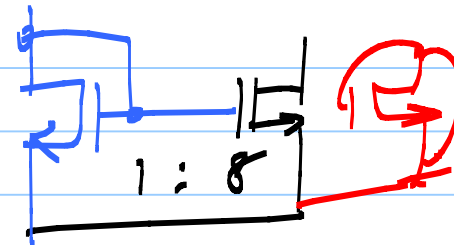
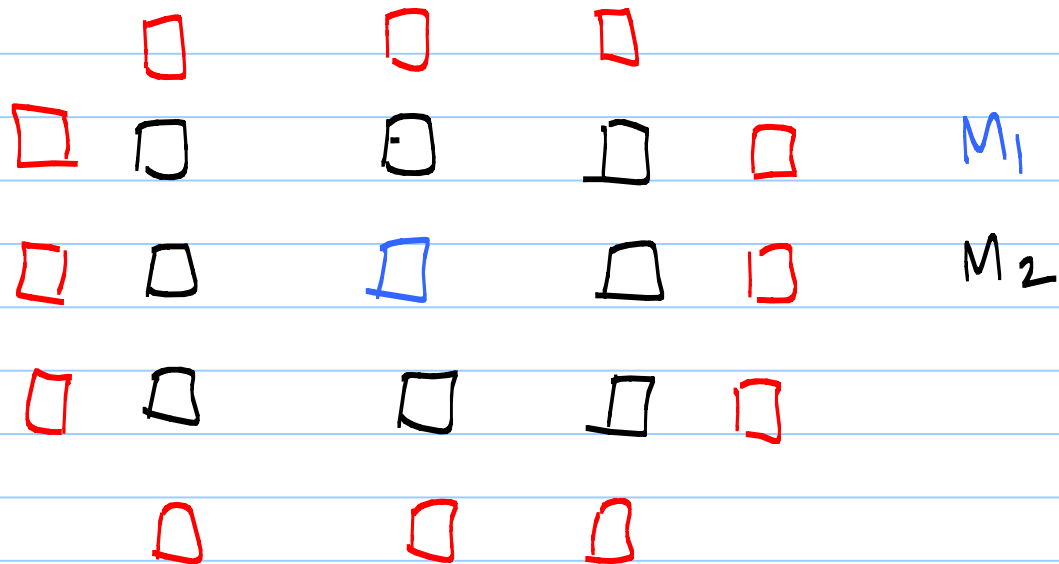


Common
centroid
layout

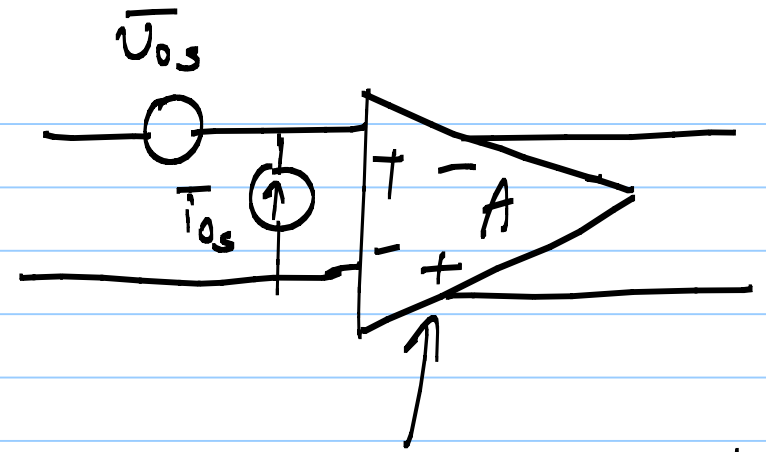
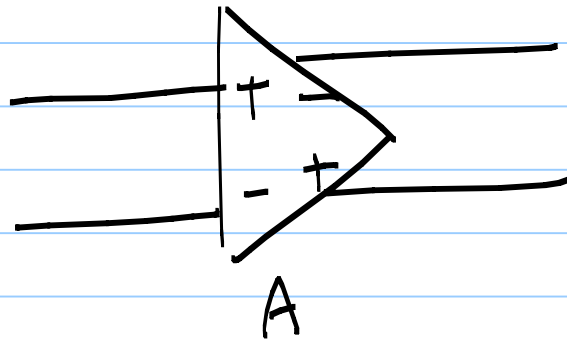
"Systematic Mismatch"

28/1/20

Lec 9

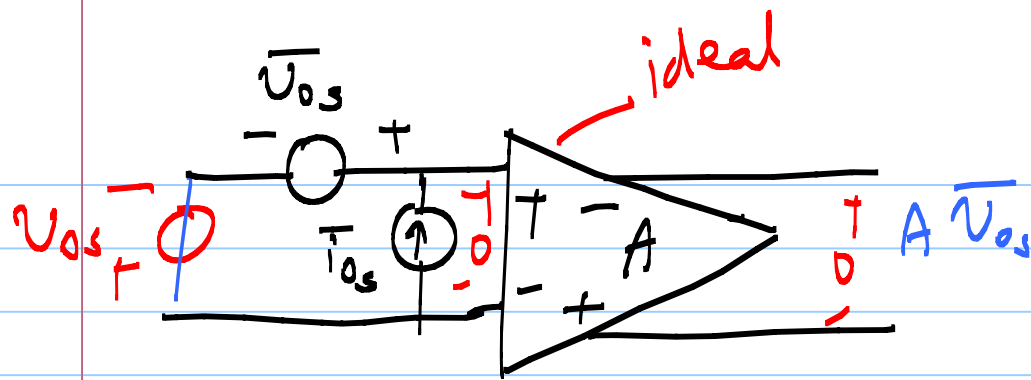


with mismatch



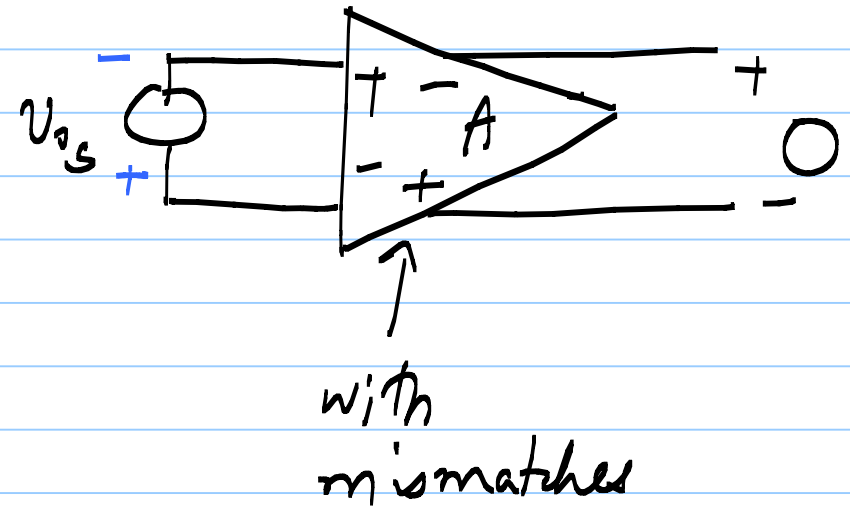
perfectly matched

- * $\bar{V}_{os}$ & $\bar{I}_{os} \rightarrow$ input-referred offset sources
- * $\bar{V}_{os}$ & $\bar{I}_{os} \rightarrow$ have a gaussian distribution
(due to random mismatches)
- * No systematic mismatch $\Rightarrow \bar{V}_{os}$ & $\bar{I}_{os}$ have 0 mean
- * V_{os} & i_{os} are constant (or slowly varying with time) for a particular IC.

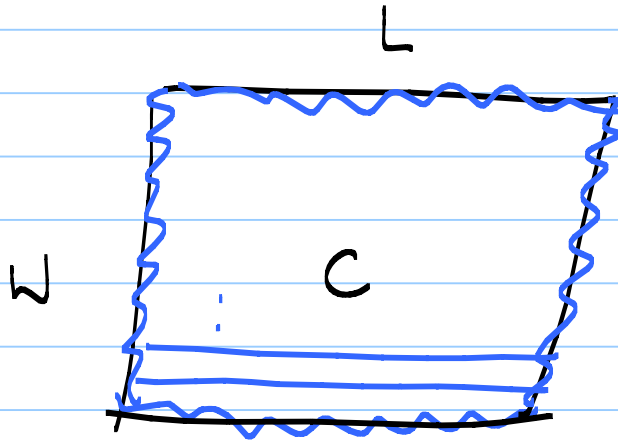


* $I_{in} = 0 \Rightarrow i_{os} = 0$

*



Random Mismatch



$$C_1 + \delta C_1$$

$$C_1 + \delta C_2$$

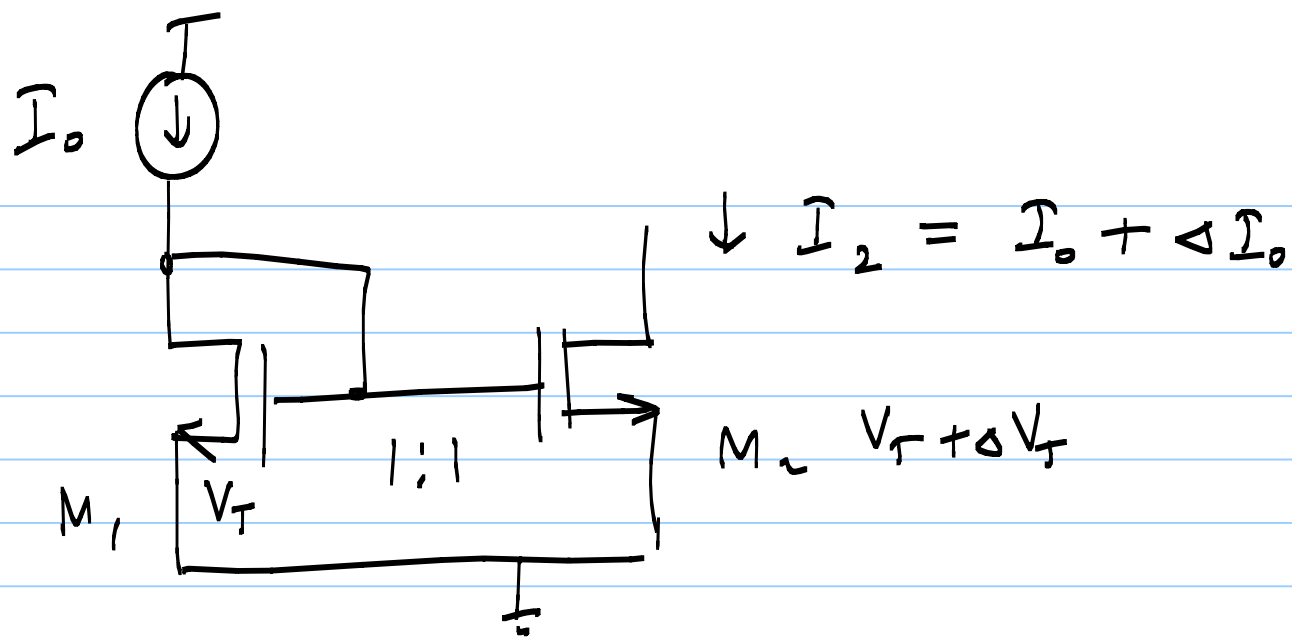
⋮

$$\sigma_{C/C} = \frac{A_{\Delta C/C}}{\sqrt{W \cdot L}}$$

$$\sigma_{\Delta c/c} = \frac{A_{\Delta c/c}}{\sqrt{W_c \cdot L_c}} ; \quad \sigma_{\frac{\Delta R}{R}} = \frac{A_{\Delta R/R}}{\sqrt{W_R \cdot L_R}}$$

$$\sigma_{V_T} = \frac{A_{V_T}}{\sqrt{W \cdot L}} ; \quad \sigma_{\mu_{\text{box}}} = \frac{A_{\mu_{\text{box}}}}{\sqrt{W \cdot L}}$$

$A_{\frac{\Delta c}{c}}$, A_{V_T} etc. are empirical parameters
specific to a process



* Assume ΔV_T is small

*
$$I_D = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L} \right) (V_{gs} - V_T)^2$$

$$\frac{\partial I_D}{\partial V_T} = - \frac{\partial I_D}{\partial V_{gs}} = -g_m$$

$$\Delta I_0 = -g_m \Delta V_T$$

$$\nabla_{\Delta I_0} = -g_m \nabla_{\Delta V_T}$$

$$\sigma_{\Delta I_0}^2 = g_m^2 \sigma_{\Delta V_T}^2$$

$$\sigma_{\Delta I_0/I_0}^2 = \frac{g_m^2}{I_0^2} \cdot \sigma_{\Delta V_T}^2$$

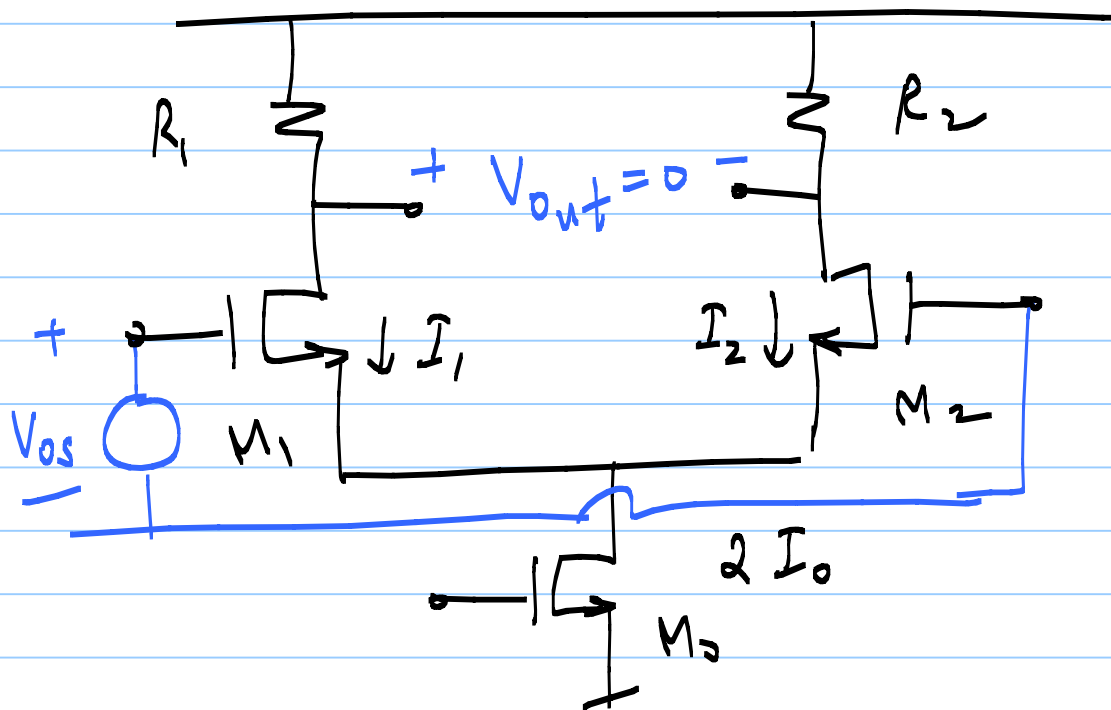
$$g_m = \frac{2 I_D}{V_{as} - V_T}$$

$$\frac{g_m^2}{I_0^2} = \frac{4}{V_{Dsat}^2}$$

$$\sigma_{\Delta I/I_0}^2 = \frac{4}{V_{Dsat}^2} \cdot \left[\frac{A_{V_T}^2}{W \cdot L} \right]$$

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Lec 10



$$R_1 \neq R_2$$

$$\left(\frac{W}{L}\right)_1 \neq \left(\frac{W}{L}\right)_2$$

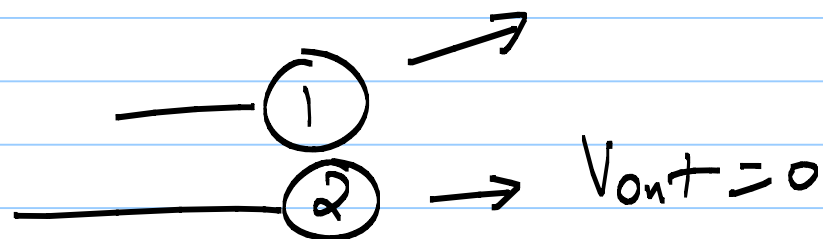
$$V_{T1} \neq V_T$$

$$\mu C_{ox} = \beta$$

$$V_{os} = V_{as1} - V_{as2}$$

$$I_1 R_1 = I_2 R_2$$

$$V_{os} = V_{T1} + \sqrt{\frac{2I_1}{\beta \left(\frac{W}{L}\right)_1}}$$



$$- \left(V_{T2} + \sqrt{\frac{2I_2}{\beta \left(\frac{W}{L}\right)_2}} \right)$$

$$R = \frac{R_1 + R_2}{2} ; \Delta R = \frac{R_1 - R_2}{2}$$

$$\Rightarrow R_1 = R + \Delta R ; R_2 = R - \Delta R$$

$$V_{T1} - V_{T2} = \Delta V_T$$

$$\left(\frac{W}{L}\right) = \frac{(W/L)_1 + (W/L)_2}{2} ; \Delta(W/L) = \frac{(W/L)_1 - (W/L)_2}{2}$$

$$\left(\frac{W}{L}\right)_1 = \left(\frac{W}{L}\right) + \Delta(W/L) ; (W/L)_2 = \left(\frac{W}{L}\right) - \Delta(W/L)$$

$$V_{os} = \Delta V_T + \sqrt{\frac{2 I_1}{\beta [(W/L) + \Delta(W/L)]}} - \sqrt{\frac{2 I_2}{\beta [(W/L) - \Delta(W/L)]}}$$

$$I_1 R_1 = I_2 R_2$$

$$I_1 = I_0 + \Delta I , I_2 = I_0 - \Delta I$$

$$(I_0 + \Delta I)(R + \Delta R) = (I_0 - \Delta I)(R - \Delta R)$$

$$\cancel{I_0 R} + I_0 \Delta R + \Delta I R + \cancel{\Delta I \Delta R}$$

$$= \cancel{I_0 R} - I_0 \Delta R - \Delta I R + \cancel{\Delta I \Delta R}$$

$$\frac{\Delta I}{I_0} = - \frac{\Delta R}{R}$$

$$V_{OS} = \Delta V_T + \sqrt{\frac{2(I_0 + \Delta I)}{\beta(W/L) + \Delta(W/L)}} - \sqrt{\frac{2(I_0 - \Delta I)}{\beta(W/L) - \Delta(W/L)}}$$

$$= \Delta V_T + \sqrt{\frac{2I_0}{\beta(W/L)}} \left[\sqrt{\frac{1 + \Delta I/I_0}{1 + \frac{\Delta W/L}{W/L}}} - \sqrt{\frac{1 - \Delta I/I_0}{1 - \frac{\Delta W/L}{W/L}}} \right]$$

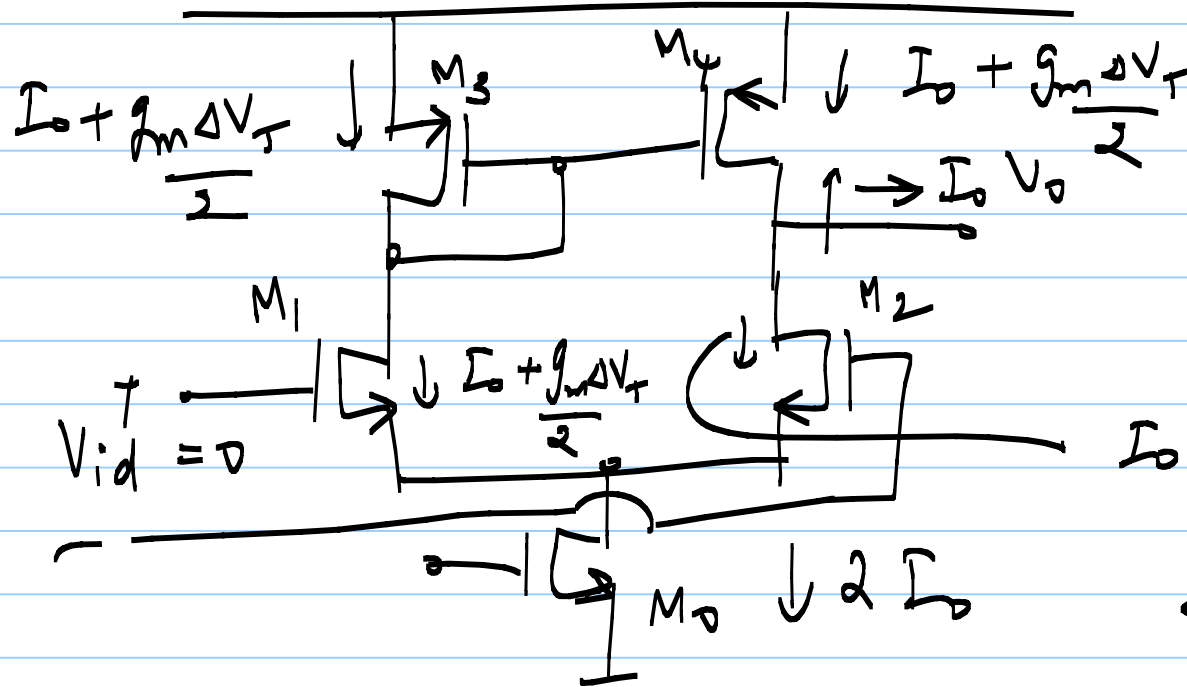
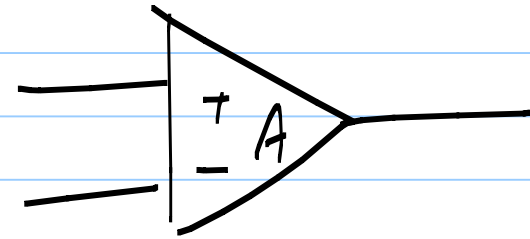
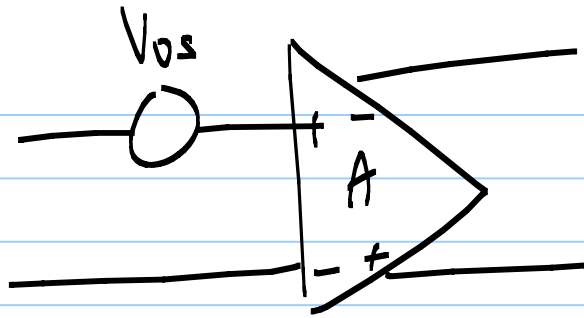
$$V_{os} = \Delta V_T + V_{Dsat_{nom.}} \left[\left(1 + \frac{\Delta I}{2 I_0} \right) \left(1 - \frac{\Delta W/L}{2 W/L} \right) - \left(1 - \frac{\Delta I}{2 I_0} \right) \left(1 + \frac{\Delta W/L}{2 W/L} \right) \right]$$

$$= \Delta V_T + V_{Dsat.} \left[- \frac{\Delta W/L}{W/L} + \frac{\Delta I}{I_0} \right]$$

$$V_{os} = \Delta V_T - V_{Dsat.} \left(\frac{\Delta W/L}{W/L} + \frac{\Delta R}{R} \right)$$

$$\sigma_{os}^2 = \sigma_{V_T}^2 + V_{Dsat.}^2 \left[\sigma_{\frac{\Delta W/L}{W/L}}^2 + \sigma_{\frac{\Delta I}{I_0}}^2 \right]$$

$$= \frac{A_{V_T}^2}{W \cdot L} + V_{Dsat.}^2 \left(\frac{A_{W/L}^2}{W \cdot L} + \frac{A_R^2}{W R L R} \right)$$



$$I_0 = g_m \Delta V_T$$

$$V_{T2} - V_{T1} = \Delta V_T$$

e.g. $V_{T1} < V_{T2}$

$$V_{T1} = V_T - \frac{\Delta V_T}{2}$$

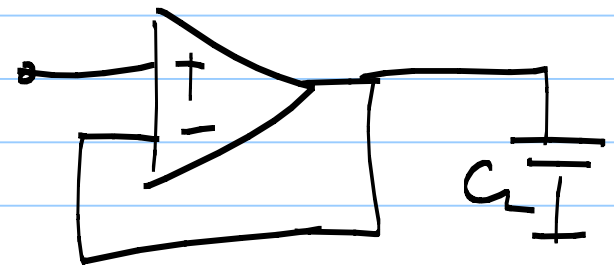
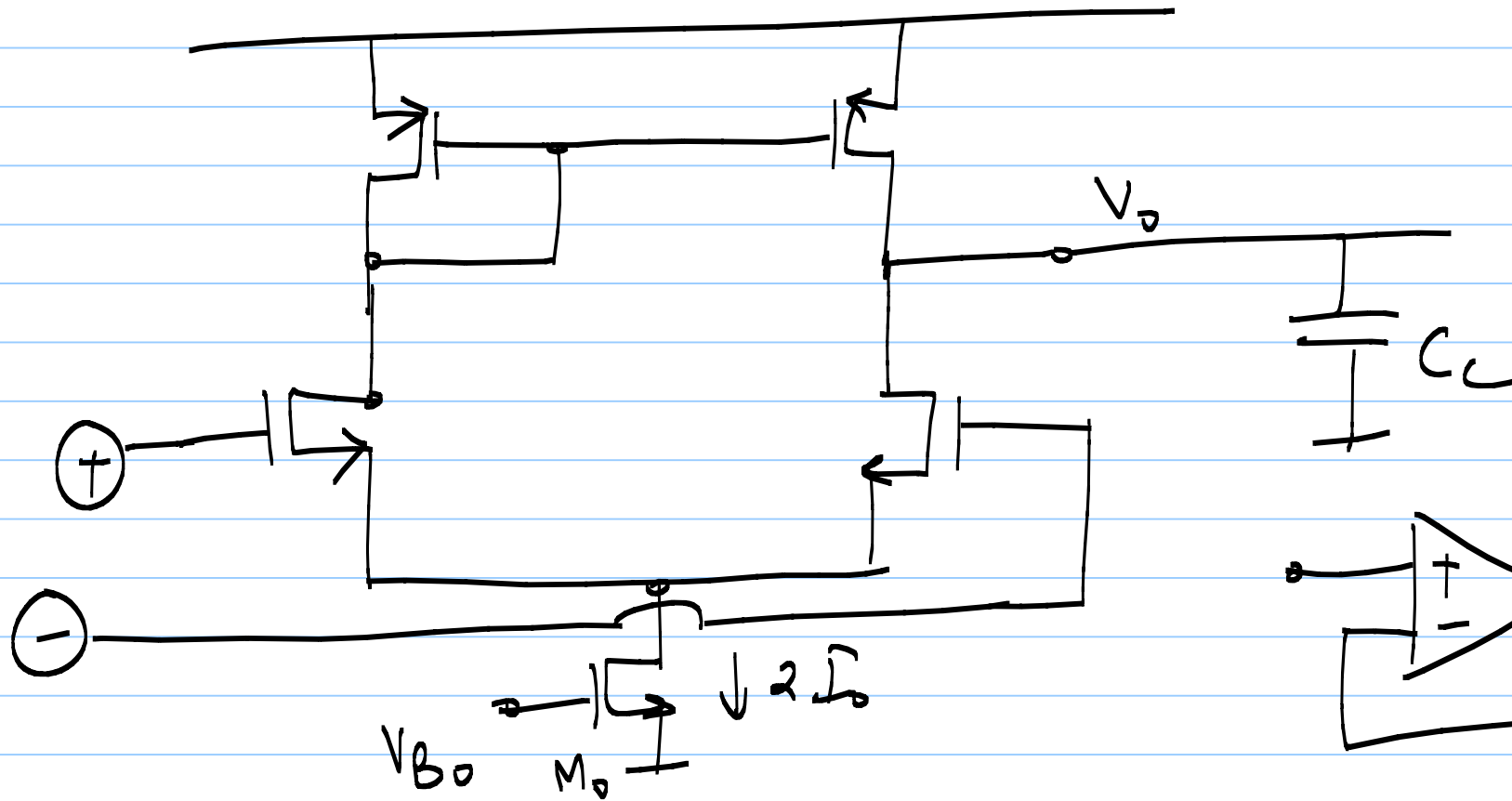
$$I_0 - \frac{g_m \Delta V_T}{2}$$

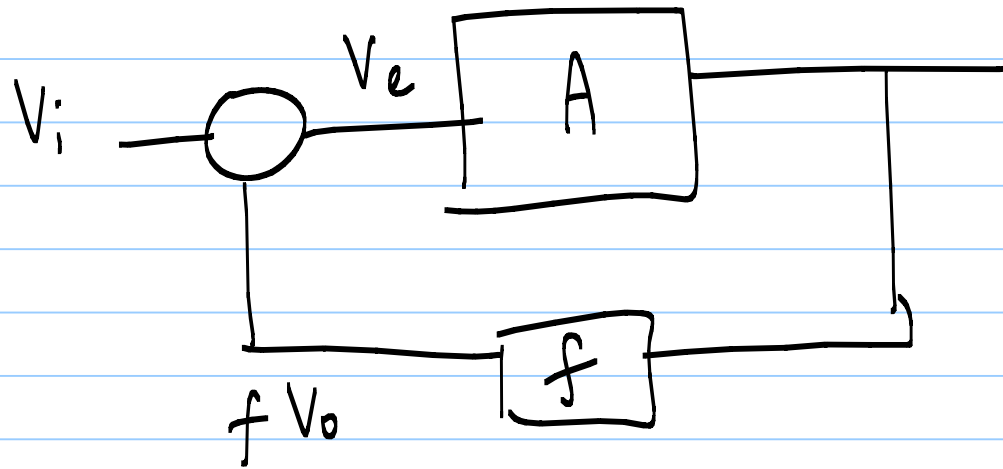
$$\Delta V_{out} = g_m \Delta V_T \cdot r_{out}$$

expected $V_{out} = V_{DD} - V_{SA34}$

V_{os} = voltage to be applied @ input so that $\Delta V_{out} = 0$

HW : V_{os} for 1-stage opamp assuming mismatch in $V_{T1} \leftrightarrow V_{T2}$ & $V_{T3} \leftrightarrow V_{T4}$ only





$$\left| \frac{V_o}{V_i} \right| \approx \frac{1}{f}$$

$$L_h = A_f$$

stability depends
on $|A_f|$ & $\angle A_f$

$f = 1$ is worst-case

3/2/20

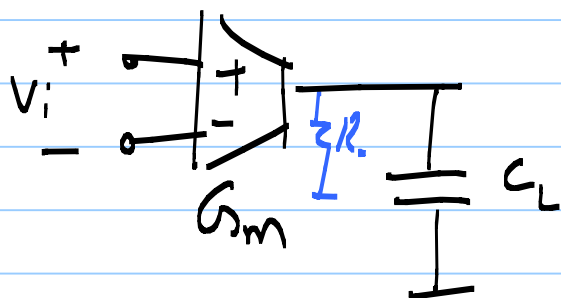
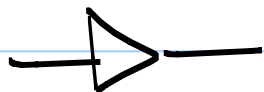
Lec 11

1-stage opamp datasheet
(Not rewired)

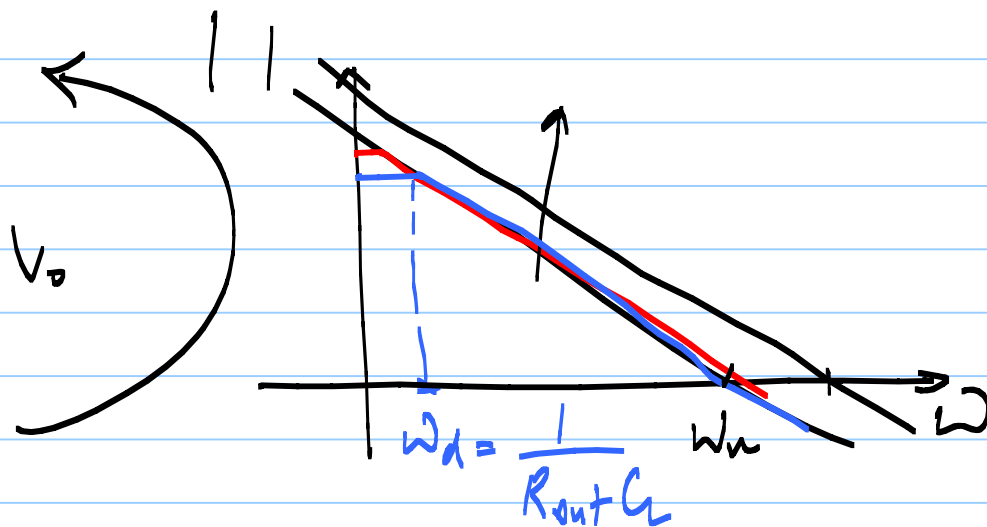
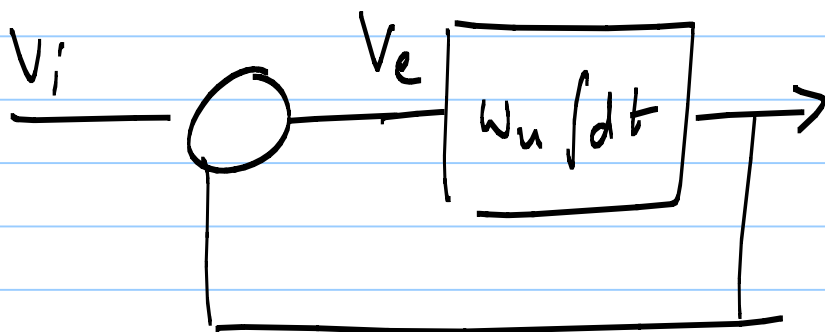
4/2/20

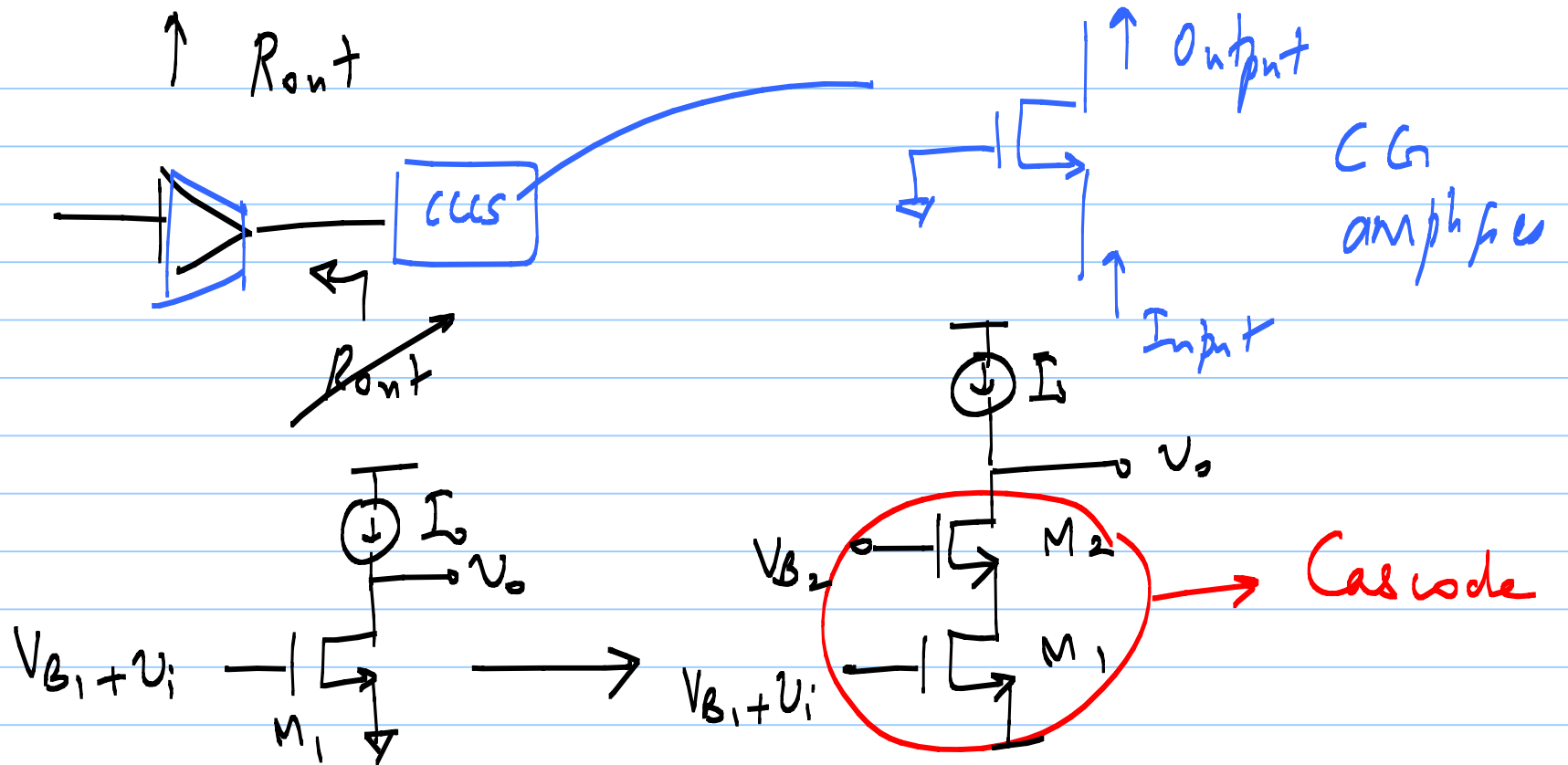
Lec 12

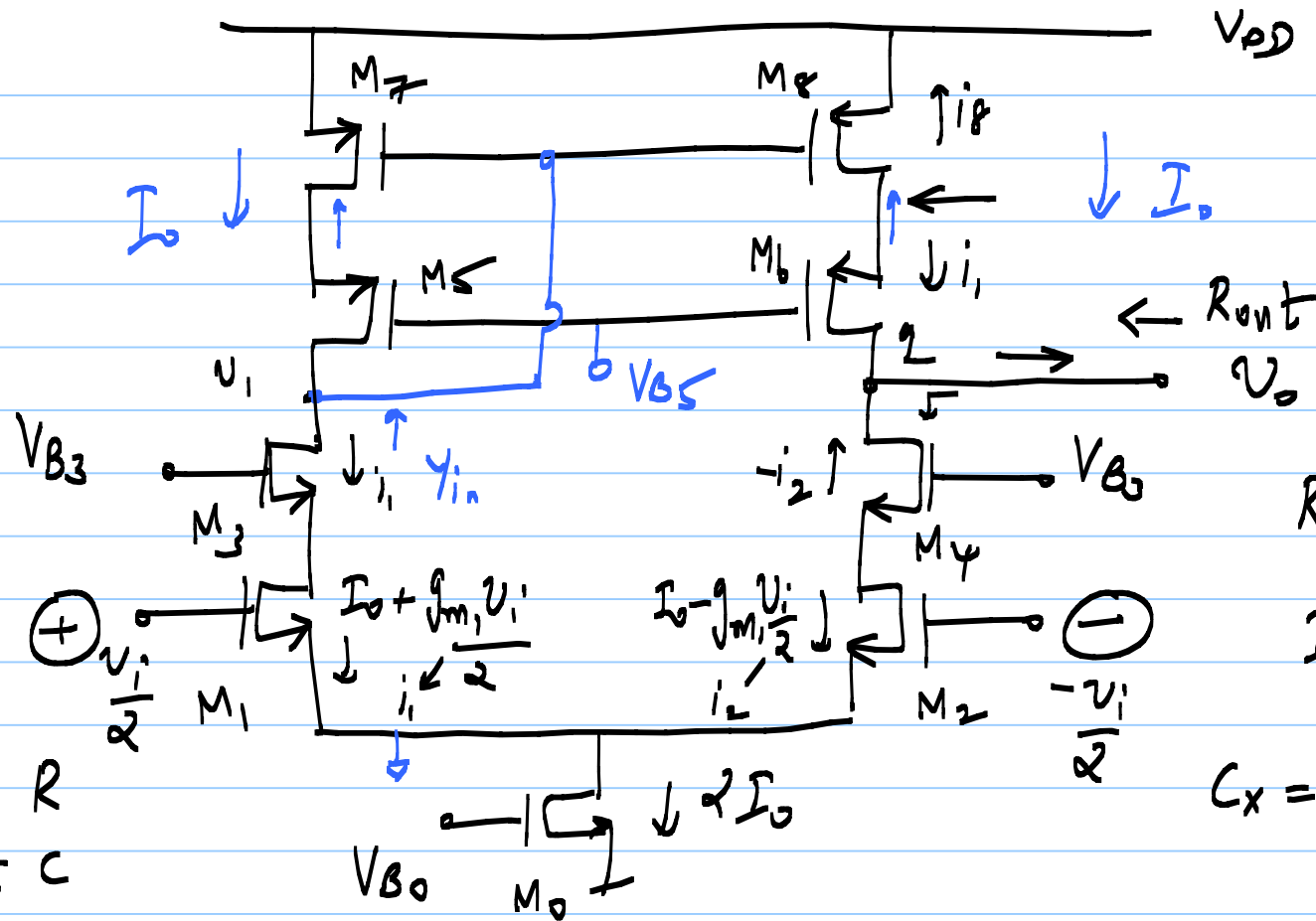
Telescopic opamp data sheet



$$\omega_u = \frac{g_m}{C_L}$$







$$V_{B5} \leq V_{DD} - V_{SDsat8} - V_{S41}$$

$$Re(Y_{in}) = g_{m7}$$

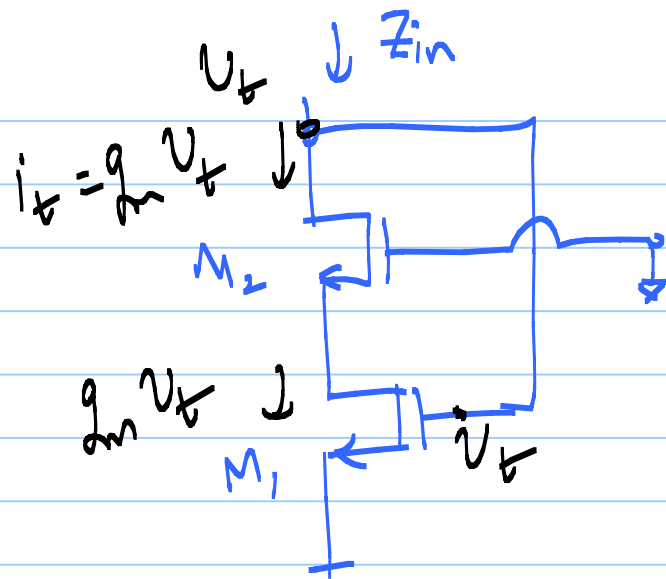
$$Im(Y_{in}) = sC_x$$

$$C_x = C_{gs7} + C_{gs8} + C_{db3} + C_{db5}$$

(a) low freq., $v_i = -\frac{i_1}{g_{m7}}$

$$i_p = g_{m8} \cdot v_i = -i_1$$

$$i_{out} = i_1 - i_2 = g_{m1} v_i \Rightarrow g_m = g_{m1}$$



$$Z_{in} \approx \frac{1}{g_{m1}}$$

$$R_{out} = r_{up} \parallel r_{dn} \approx (g_{mb} r_{dsb} r_{ds8}) \parallel (g_{m4} r_{ds4} r_{ds2})$$

R_{out} (telescopic) $\rightarrow$ R_{out} (1-stage)

Data sheet

1) DC gain = $g_{m1} R_{out}$

$$R_{out} = r_{up} \parallel r_{dn} \approx (g_{mb} r_{dsb} r_{ds8}) \parallel (g_{m4} r_{ds4} r_{ds2})$$

2) $\omega_u = g_{m1} / C_L$

3) Dominant pole $\omega_d = \frac{1}{R_{out} C_L}$

4) ND poles & zeroes (next class)

5) $ICMR = \left\{ \left. \frac{V_{DSat_0}}{2I_0} + \frac{V_{as1}}{I_0} \right|_{I_0}, \left. \frac{V_{B3} - V_{as3}}{I_0} + V_{T1} \right\}$

$$6) \text{ OCMR} = \left\{ V_{B3} - V_{T3}, V_{B5} + V_{T6} \right\}$$

$$7) \overline{e_n} = \frac{16kT}{3g_{m1}^2} [g_{m1} + g_{m7}]$$

Same as 1-stage opamp @ low freq.

@ high freq., noise of M_3-M_4 & M_5-M_6
add to $\overline{e_n}$

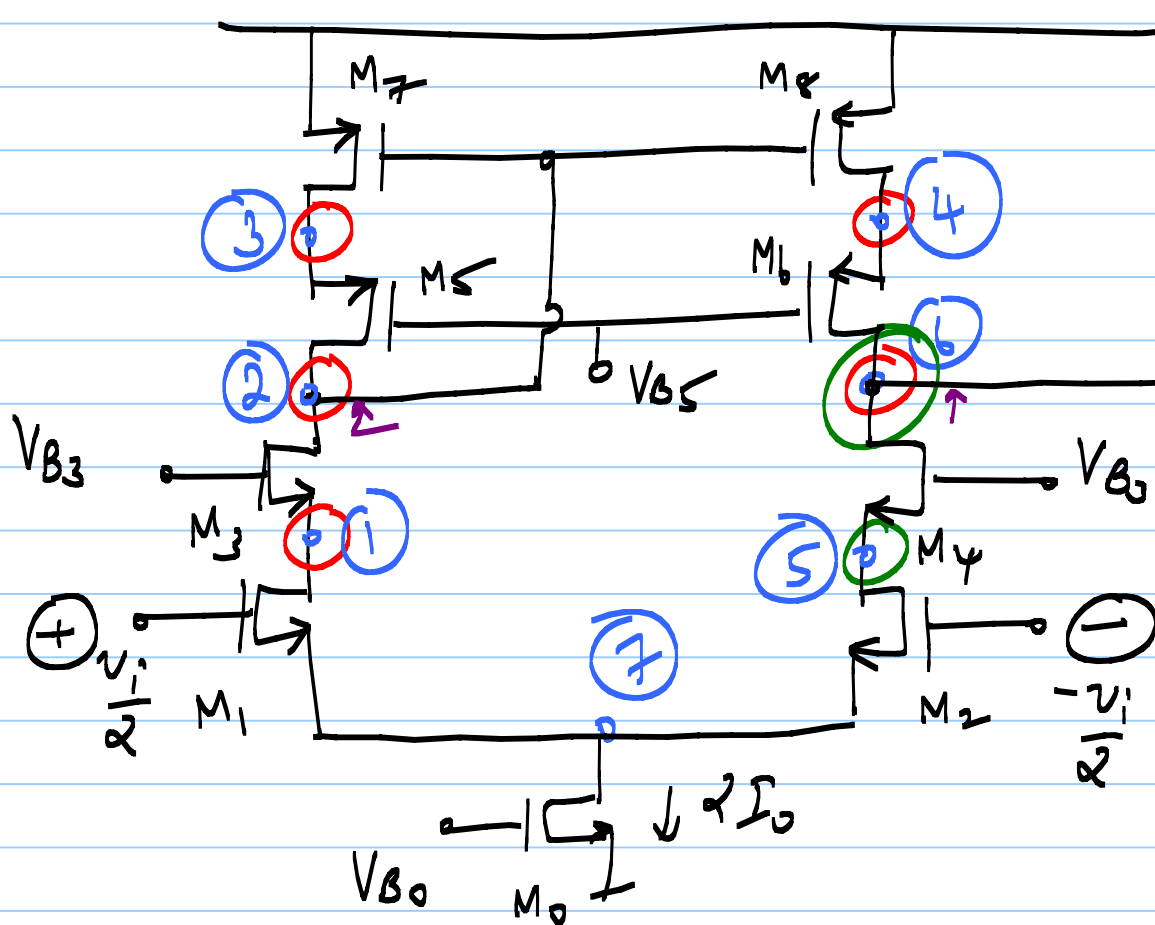
$$8) \sigma_{os}^2 = \sigma_{V_{T1,2}}^2 + \frac{g_{m7}^2}{g_{m1}^2} \cdot \sigma_{V_{T7-8}}^2$$

$$9) \text{ slew rate} = \pm \frac{2I_0}{C_L}$$

05/2/20

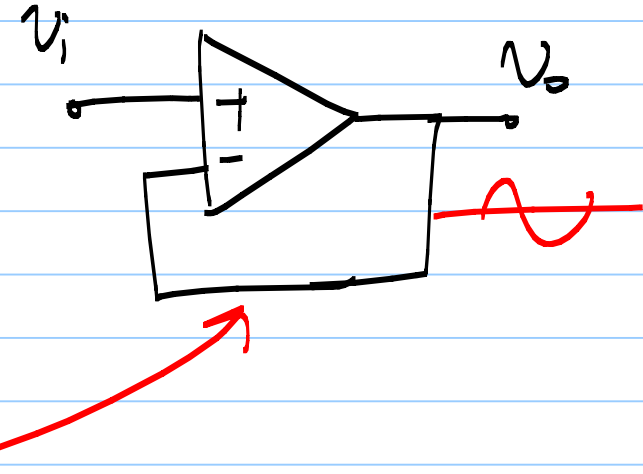
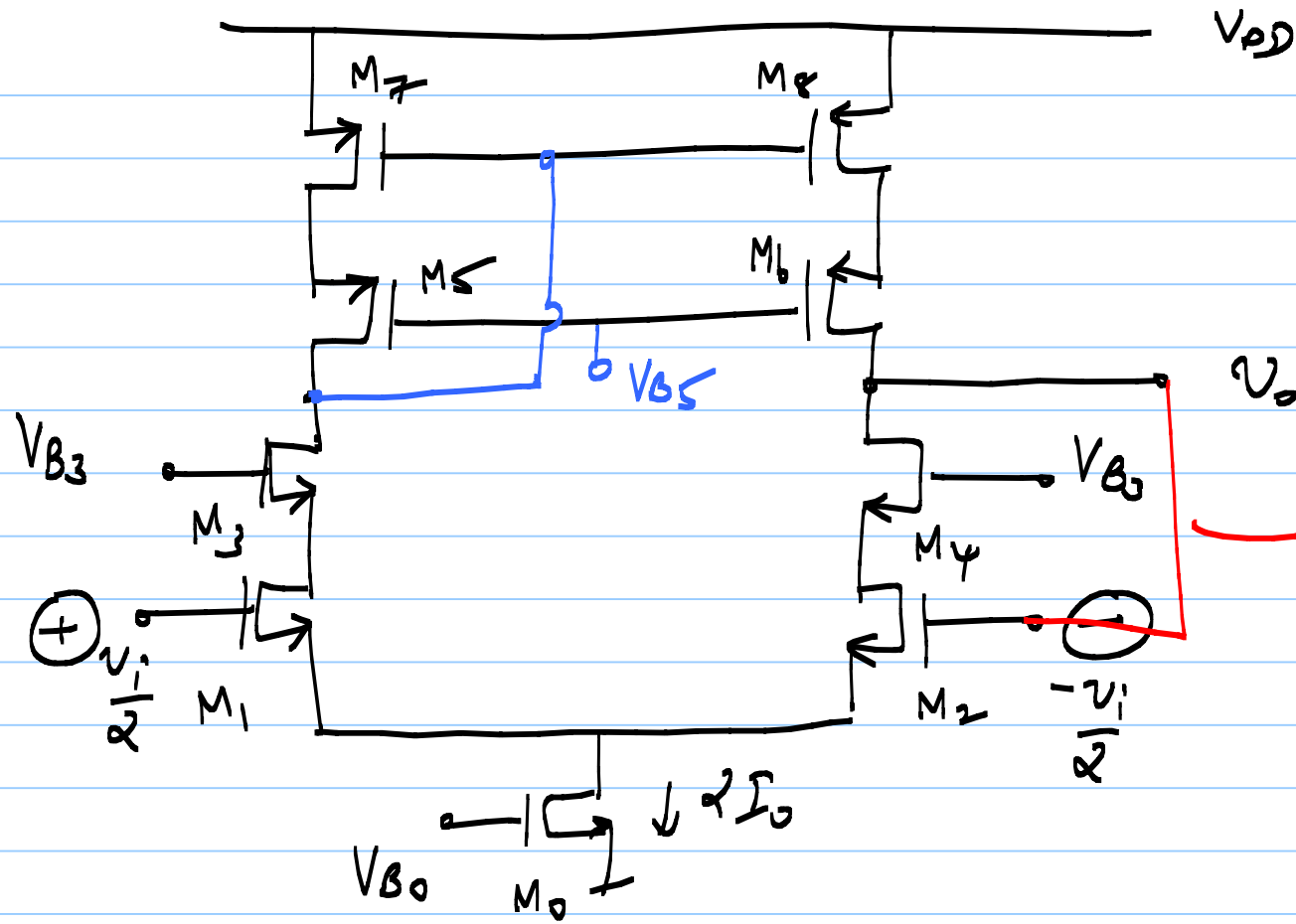
Lec 13

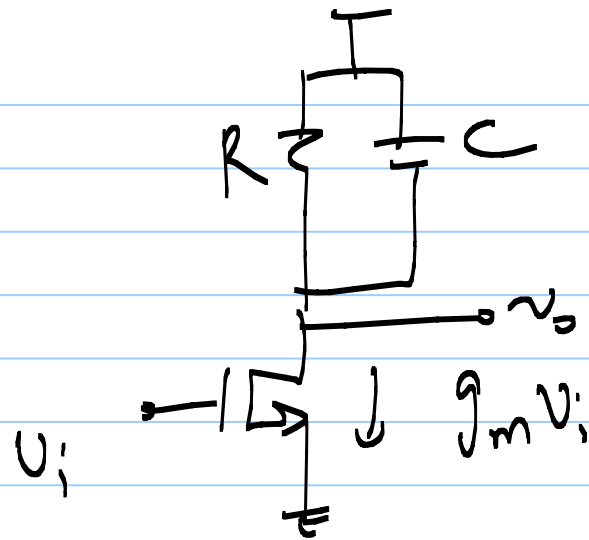
4) ND poles & zeroes of telescopic opamp



V_{DD}
 C_{par} @
Node 7 : affects
 A_{cm} &
 $CMRR$

$$\frac{v_o}{v_{id}}(s) = \frac{N(s)}{D(s)}$$





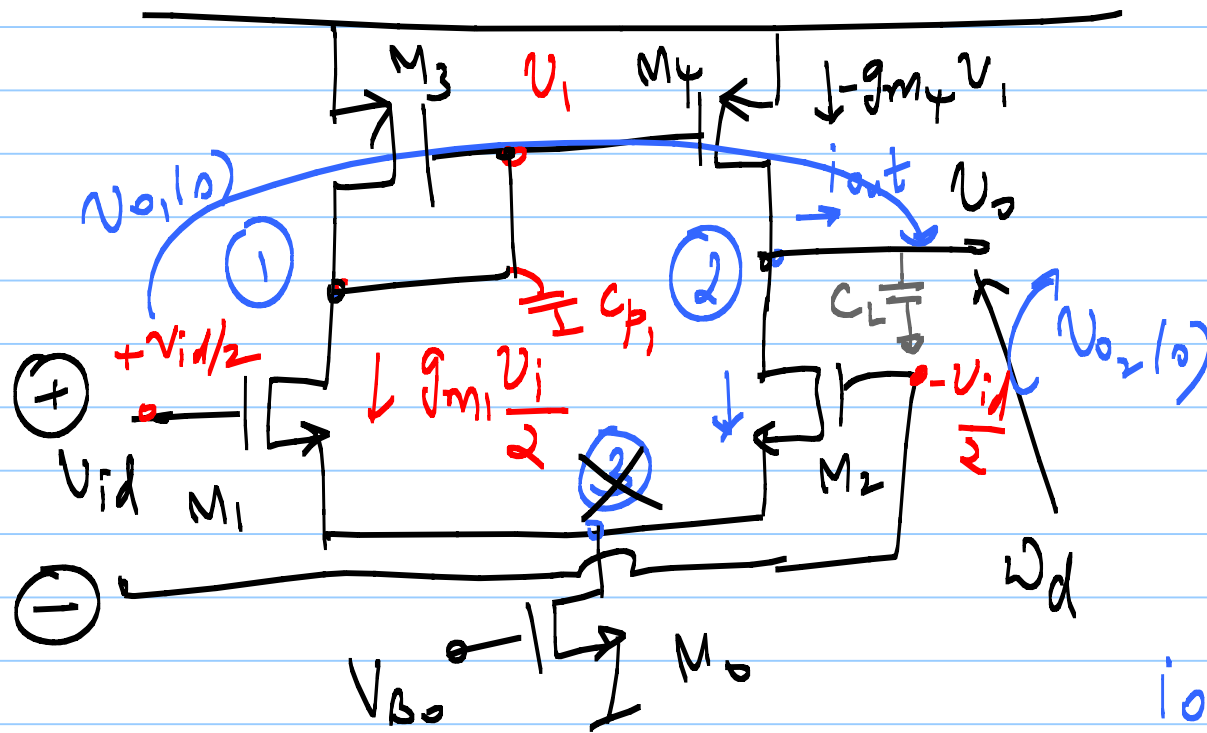
$$\frac{v_o}{v_i}(s) = - \frac{A}{1 + \frac{s}{\omega_p}}$$

$\nearrow g_m \cdot R$
 $\nearrow \omega_p$

$$\omega_p = \frac{1}{RC}$$

$$v_o = -g_m v_i \cdot \frac{R \cdot \frac{1}{sC}}{R + 1/sC}$$

$$= -g_m v_i \cdot \frac{R}{1 + \underbrace{sCR}_{1/\omega_p}}$$

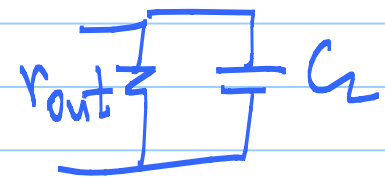


$$\frac{V_o}{V_i}(s) = \frac{N(s)}{D(s)} \quad \begin{matrix} \downarrow \text{zero} \\ \uparrow \text{pole} \end{matrix}$$

degree 2

i_{out} flows through

$$V_o(s) = V_{o1}(s) + V_{o2}(s)$$



$$V_{o2}(s) = +g_{m2} \frac{V_i}{2} \times \underbrace{\left(\frac{r_{out}}{1 + s r_{out} C_L} \right)}_{\omega_{p2}}$$

$$\begin{aligned}
 v_{o1}(s) &= -g_{m1} \frac{v_i}{2} \cdot \frac{\frac{1}{g_{m3}} - \frac{1}{sC_{p1}}}{\frac{1}{g_{m3}} + \frac{1}{sC_{p1}}} \\
 &= -\frac{g_{m1}}{g_{m3}} \frac{v_i}{2} \cdot \frac{1}{1 + \underbrace{\frac{sC_{p1}}{g_{m3}}}} \\
 &\qquad\qquad\qquad \omega_{p1} = \frac{g_{m3}}{C_{p1}}
 \end{aligned}$$

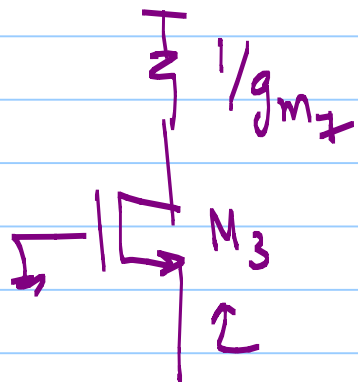
$$v_{o1}(s) = g_{m1} \frac{v_i}{2} \cdot \frac{1}{1 + s/\omega_{p1}} \cdot \frac{r_{out}}{1 + s/\omega_{p2}}$$

$$v_o(s) = g_{m1} r_{out} \frac{v_i}{2} \left[\frac{1}{1 + s/\omega_{p2}} + \frac{1}{(1 + s/\omega_{p1})(1 + s/\omega_{p2})} \right]$$

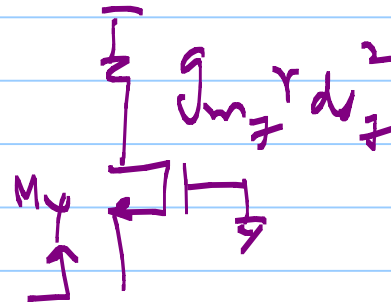
$$\frac{v_o}{v_i} = \frac{A_o}{2} \left[\frac{1}{(1 + s/p_1)(1 + s/p_2) \dots} + \frac{1}{() ()} \right]$$

Telescopic opamp :

$$\frac{v_o}{v_i}(s) = k \left[\underbrace{\frac{1}{(1 + s/p_1) \dots}}_{+ \frac{v_i}{2} \text{ has } p_1, p_2, p_3, p_4, p_5} + \frac{1}{(1 + s/p_5)(1 + \frac{s}{p_6})} \right]$$

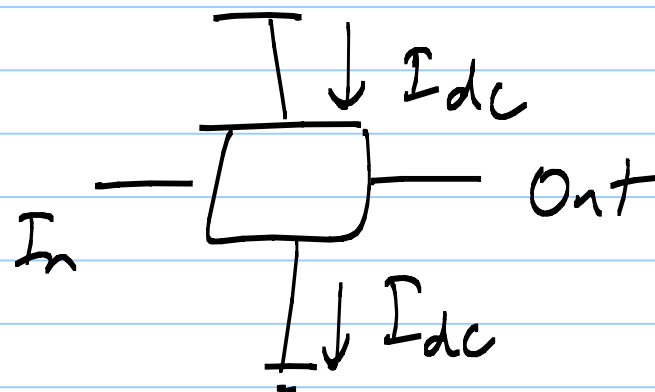
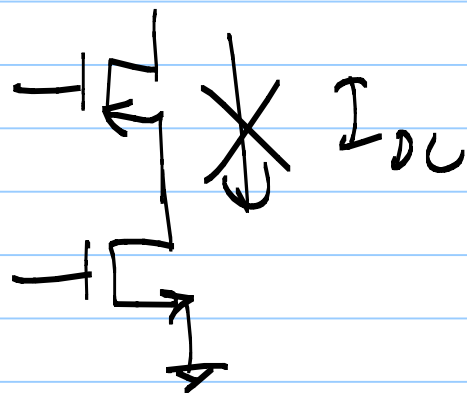
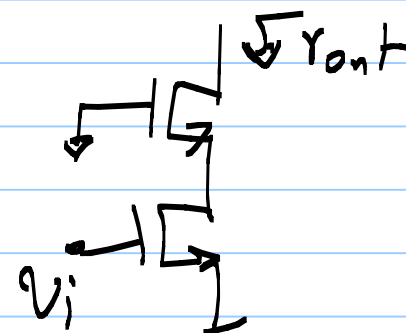
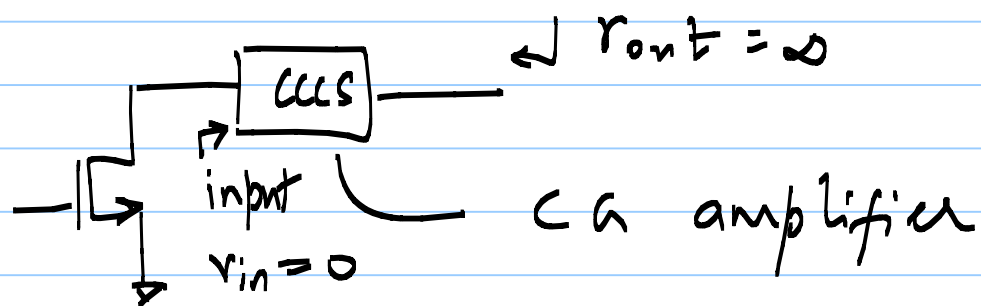
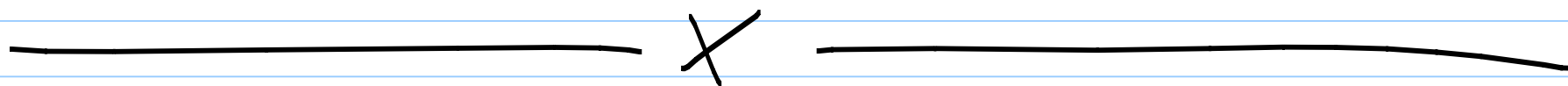


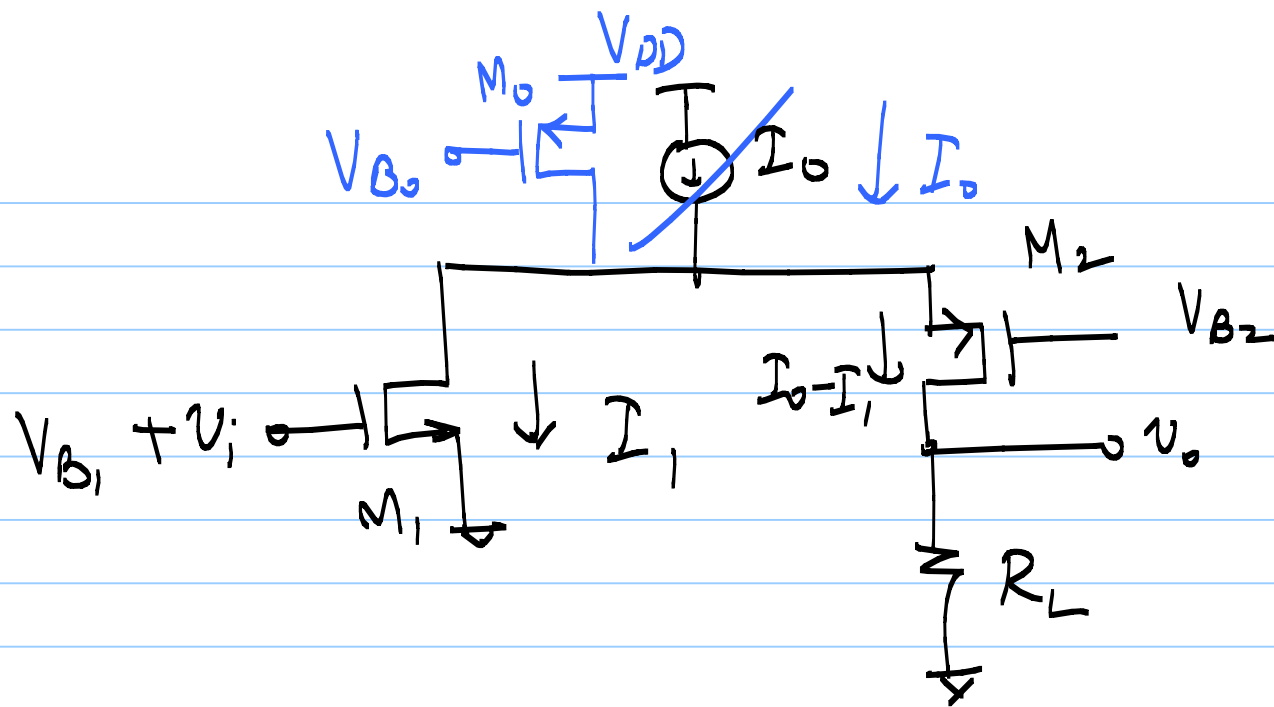
$$p_1 \neq p_5$$



* 6 poles, 4 zeroes

↳ 5 ND poles & 4 ND zeroes



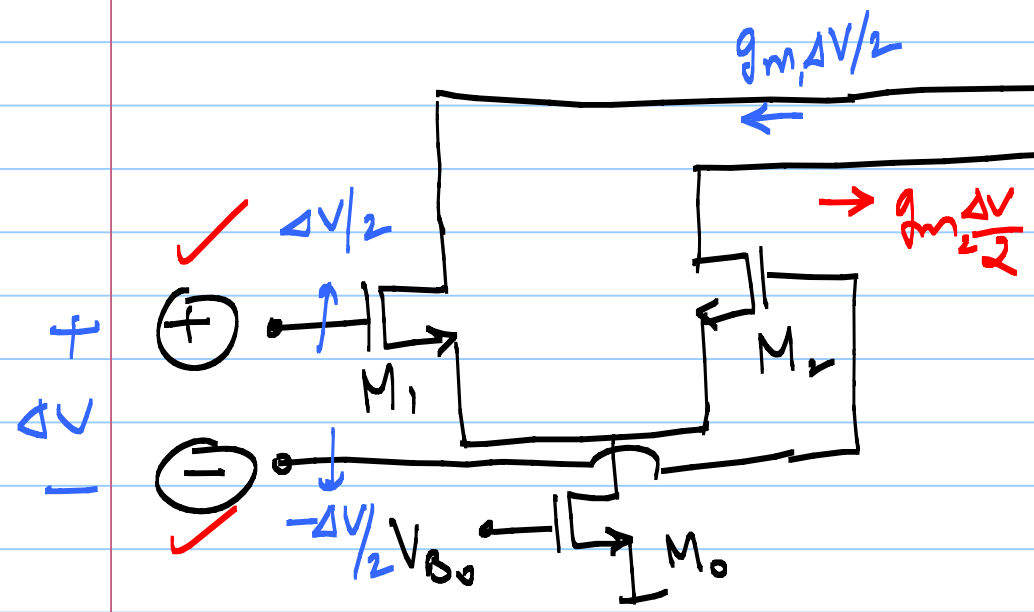


Folded
cascode
amplifier

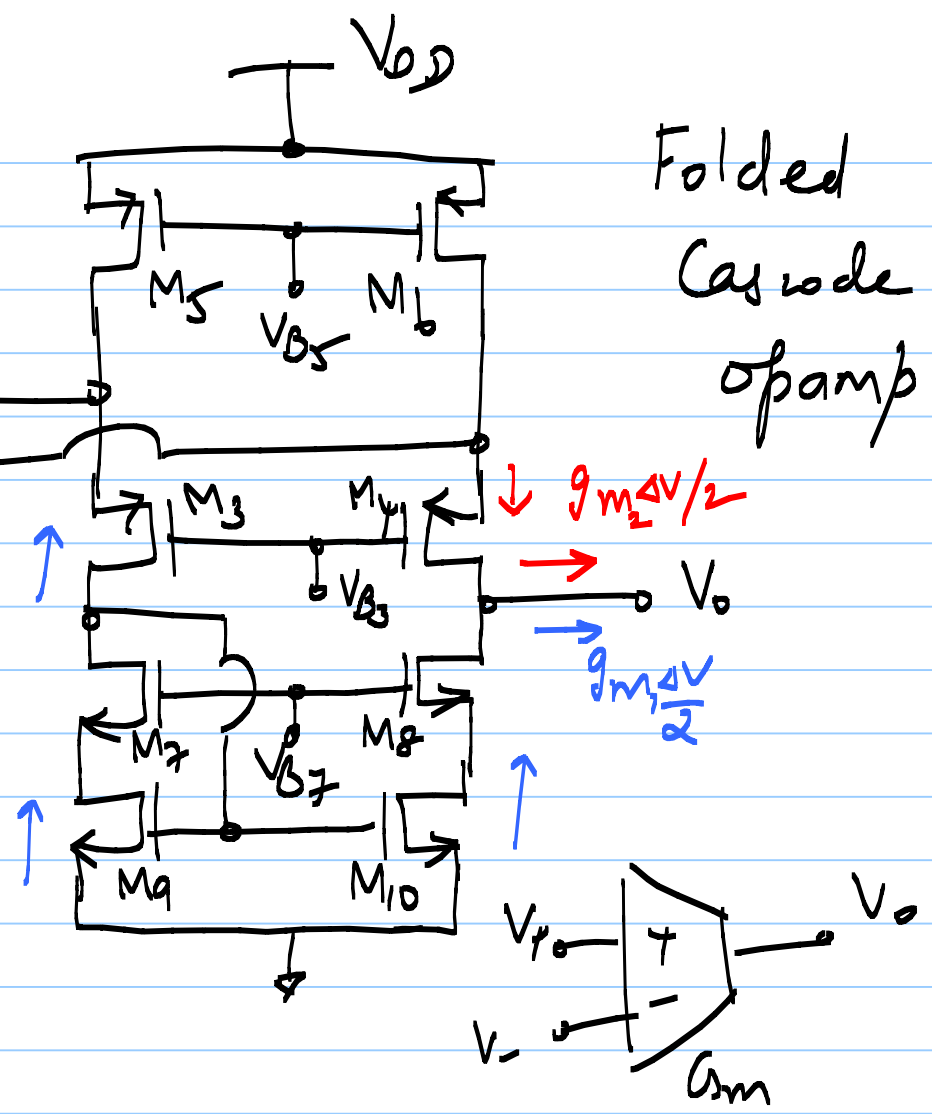
7/2/20

Lec 14

Folded
Cascode
opamp



$G_m = g_{m1}$

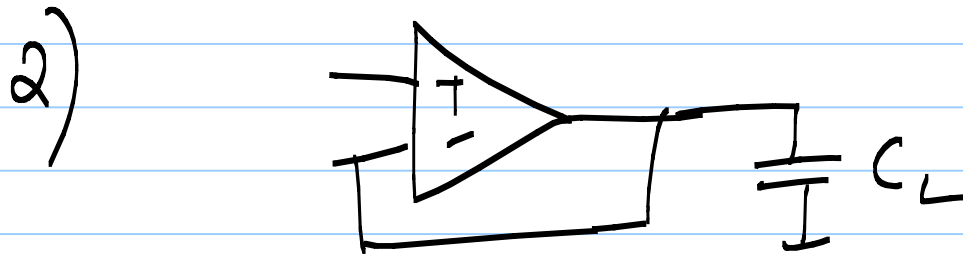


Folded Cascode Opamp datasheet

1) $G_m = g_{m1}$;
 $r_{out} = \left[g_{m4} r_{ds4} (r_{ds2} \parallel r_{ds6}) \right] \parallel \left[g_{m8} r_{ds8} r_{ds10} \right]$

↳ additional term

gain = $g_{m1} r_{out}$ - slightly lower than that of telescopic opamp



$$\omega_u = \frac{g_{m1}}{C_L}$$

3) Dominant pole

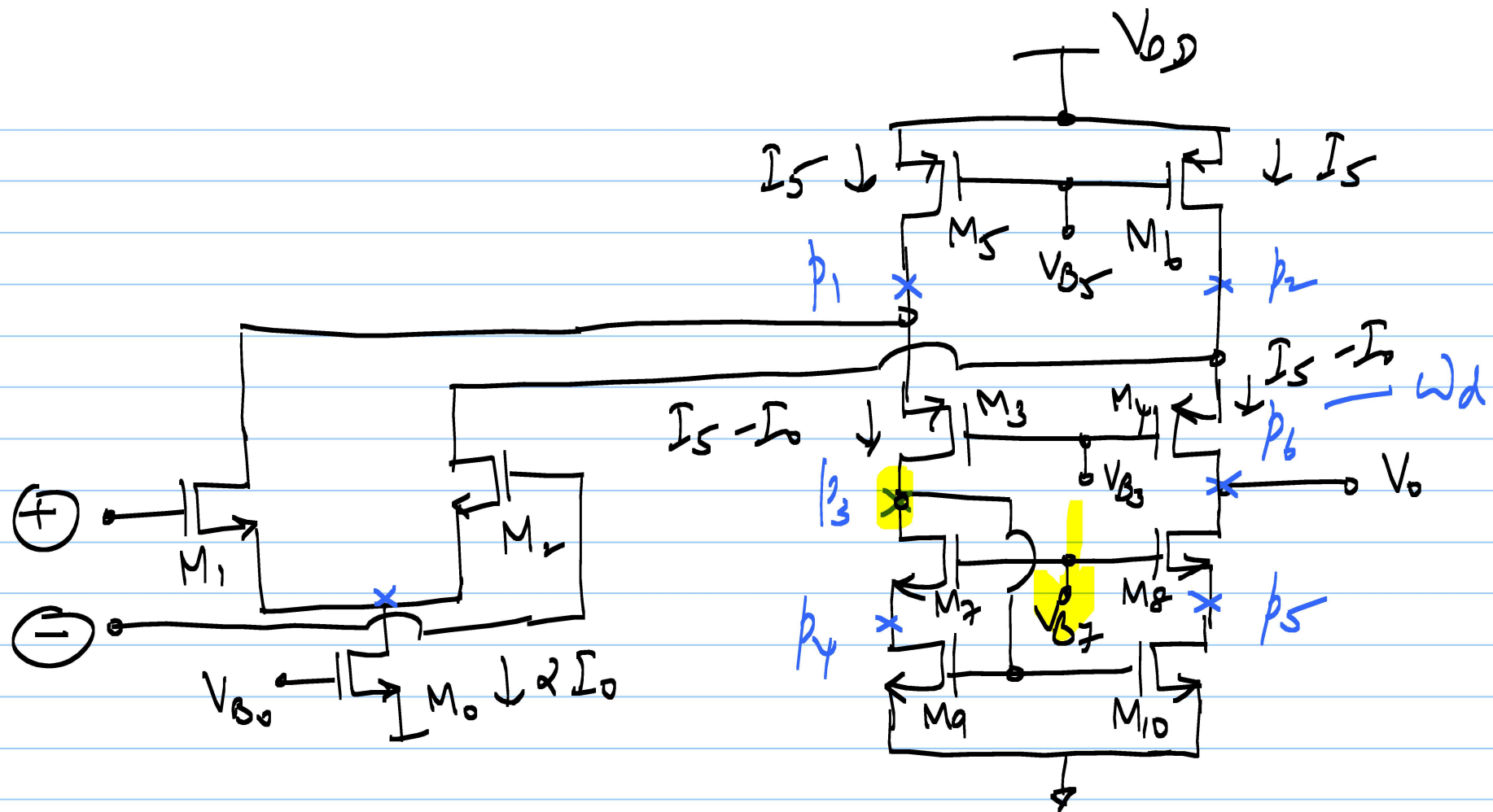
$$\omega_d = \frac{1}{r_{out} C_L}$$

4) ND poles & zeroes: 5 nm-dominant
pole @ $p_1 - p_5$

zeros: 4 ND zeros

$+1/2$ path: p_1, p_3, p_4, p_5, p_6

$-1/2$ path: p_2, p_4



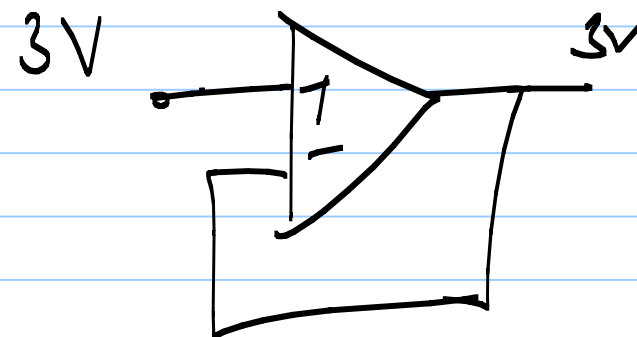
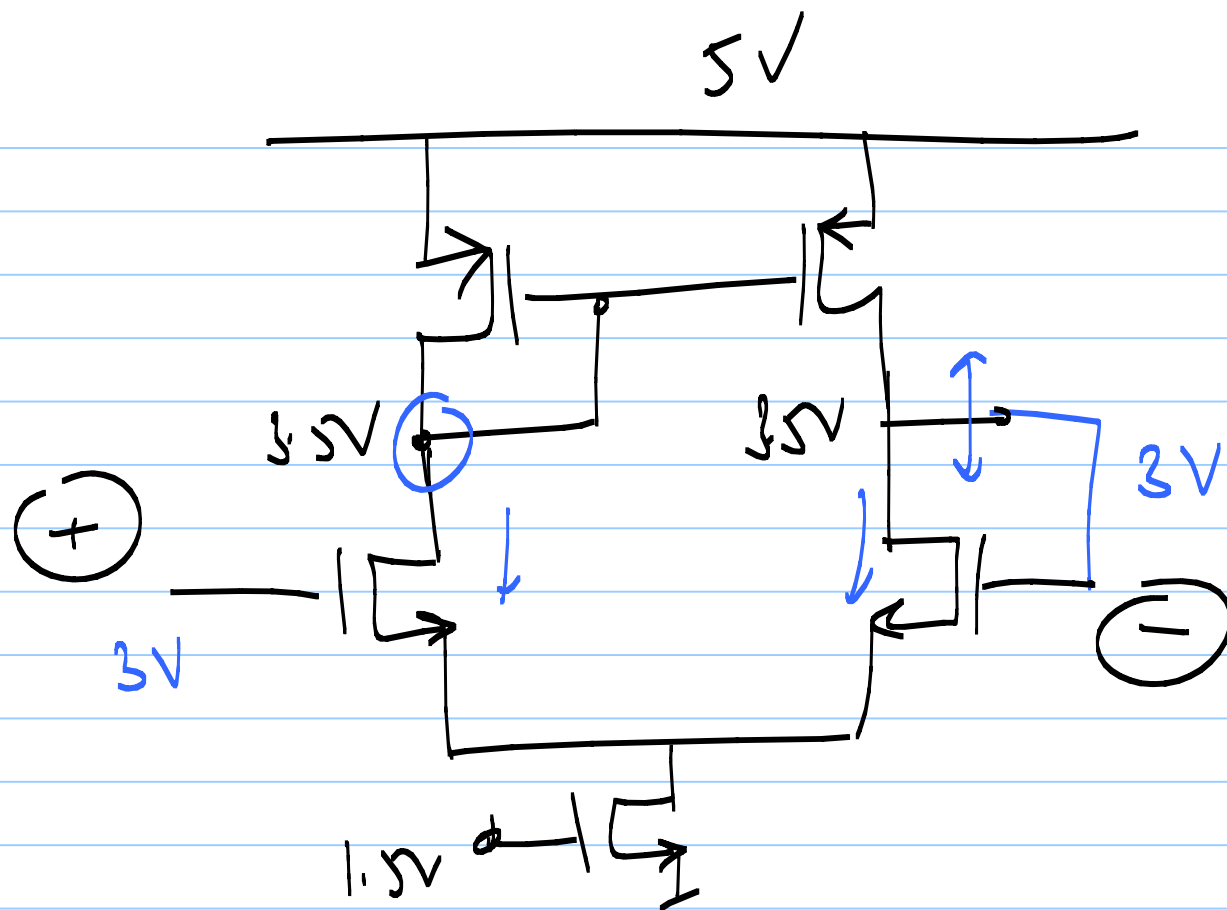
$$5) \text{ ICMR} = \left\{ V_{DSat0} \mid 2I_0 + V_{AS1} \mid I_0, \right. \\ \left. V_{B3} + V_{S43} \mid I_5 - I_0 + V_{T1} \right\}$$

$$b) \underline{DCMR}: \{ V_{B7} - V_{T8}, V_{B3} + V_{T4} \}$$

$$V_{B7 \min} = V_{DSat_{10}} + \frac{V_{h_{S8}}}{I_S - I_0} - I_0$$

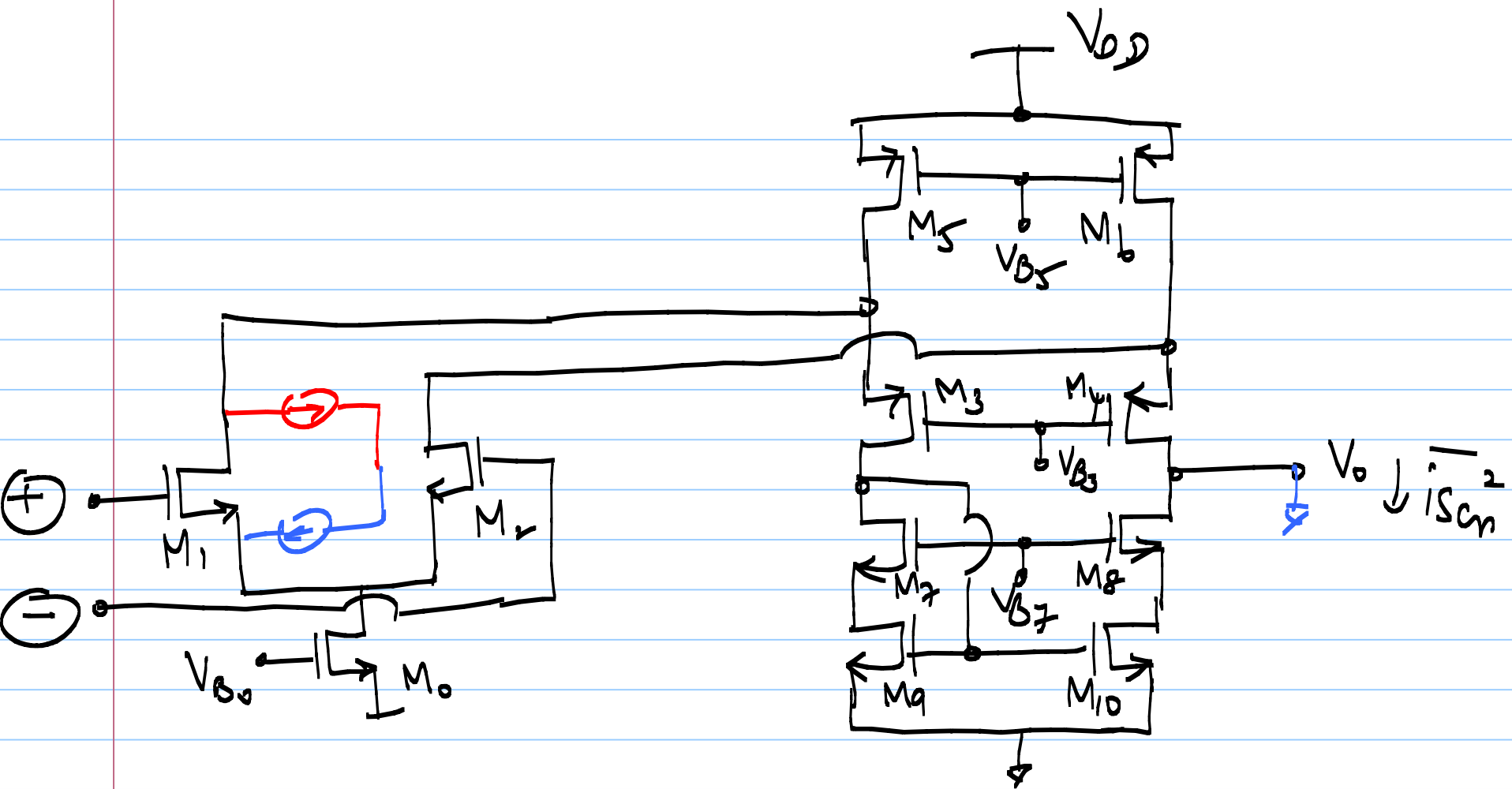
$$V_{B3 \max} = V_{DD} - V_{SDsat_6} - V_{SA4}$$

$$\rightarrow DCMR = \{ V_{DSat_{T8}} + V_{DSat_{10}}, V_{DD} - V_{SDsat_6} - V_{SDsat_4} \}$$



$$7) \quad \overline{e_n^2} = \frac{\overline{i_{sc_n}^2}}{g_{m_1}^2}$$

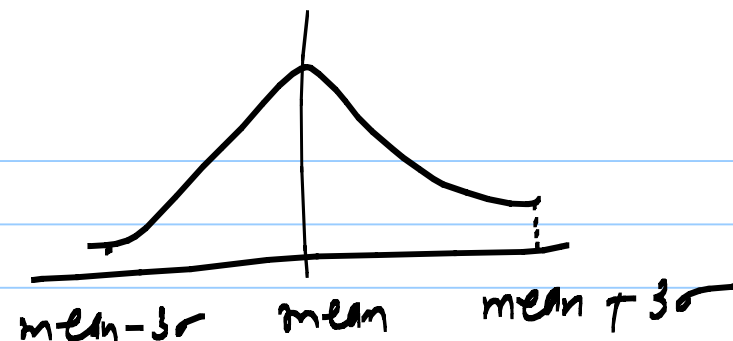
$$\overline{i_{sc_n}^2} = \overline{i_{n_1}^2} + \overline{i_{n_2}^2}$$



10/2/20

Lec 15

1) "Process Corners" :



s

t

f

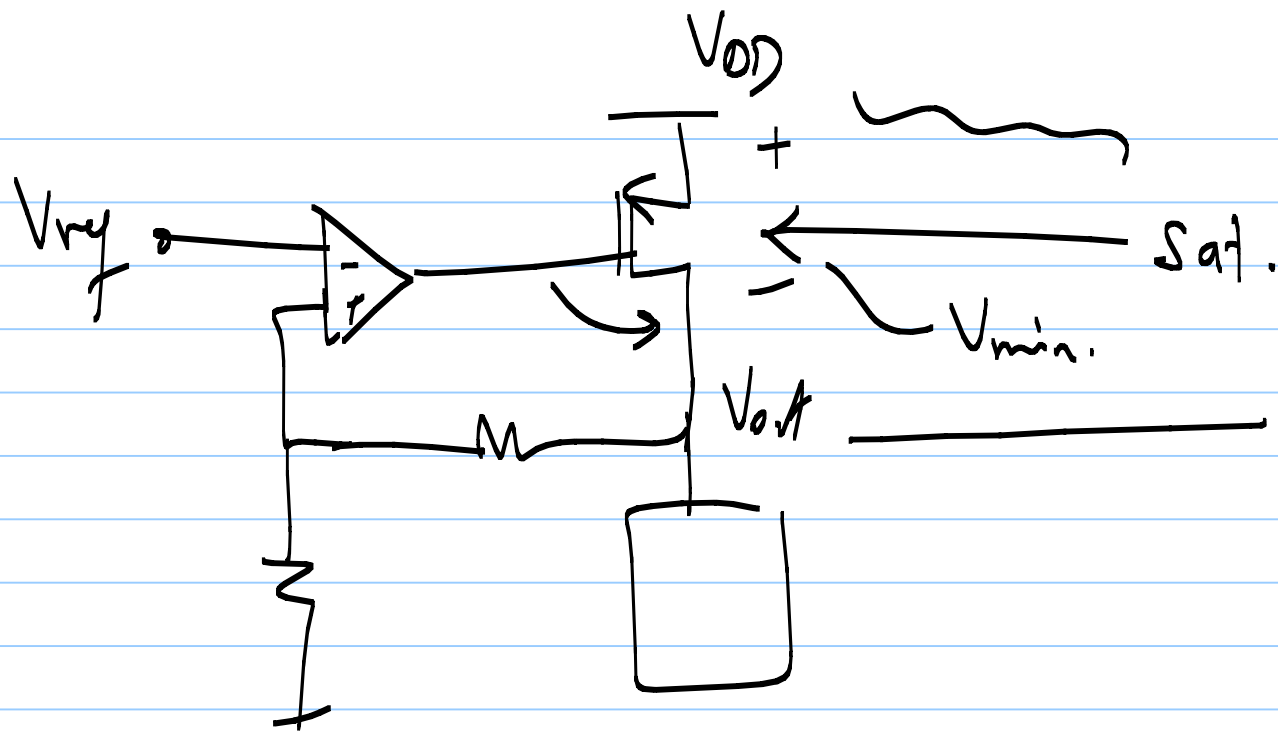
ss

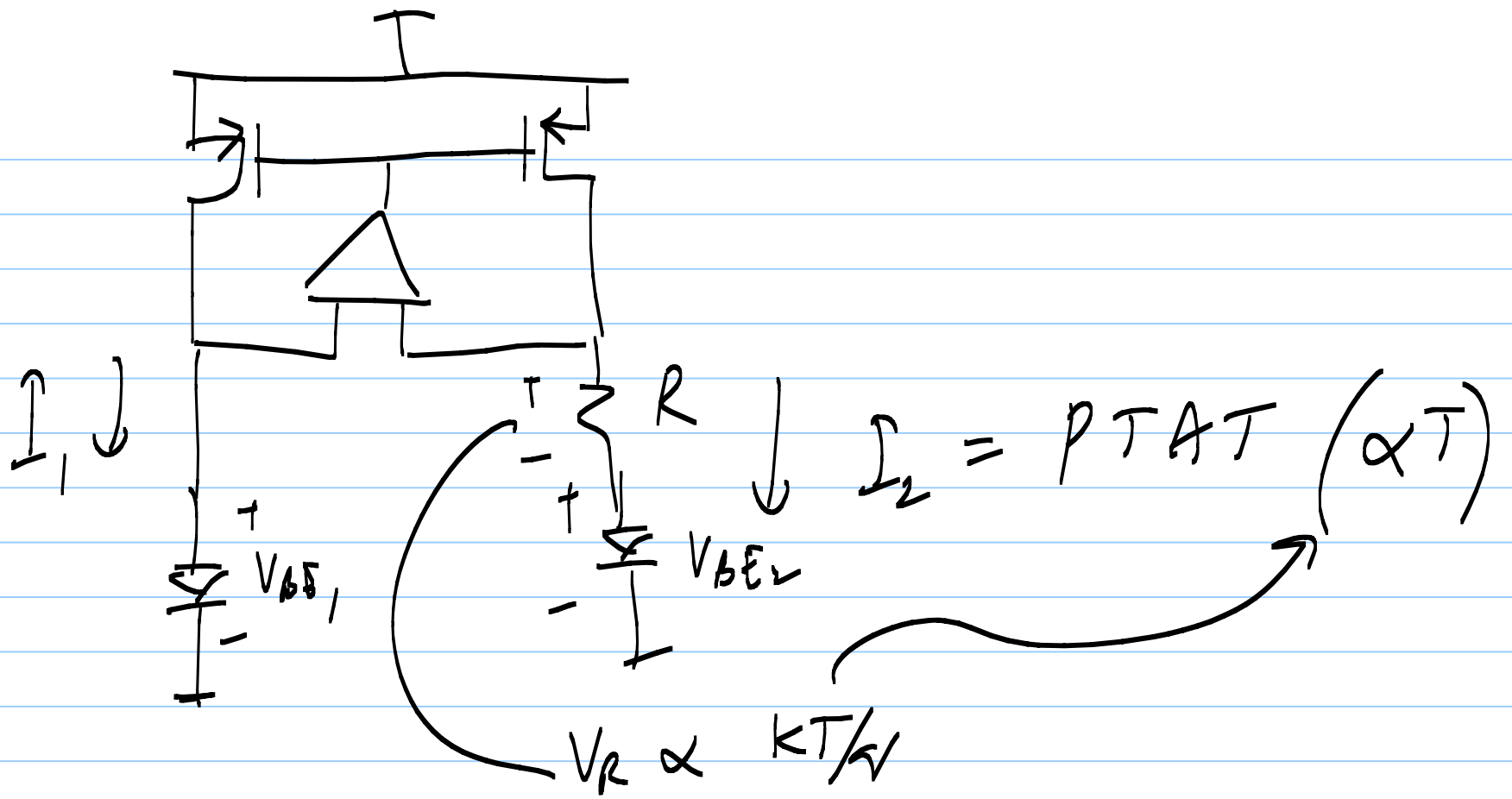
tt

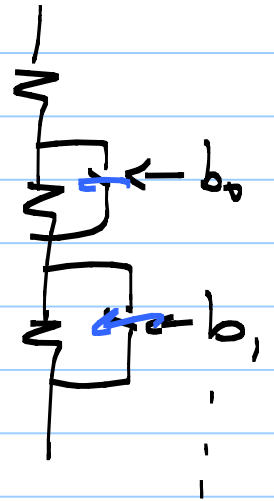
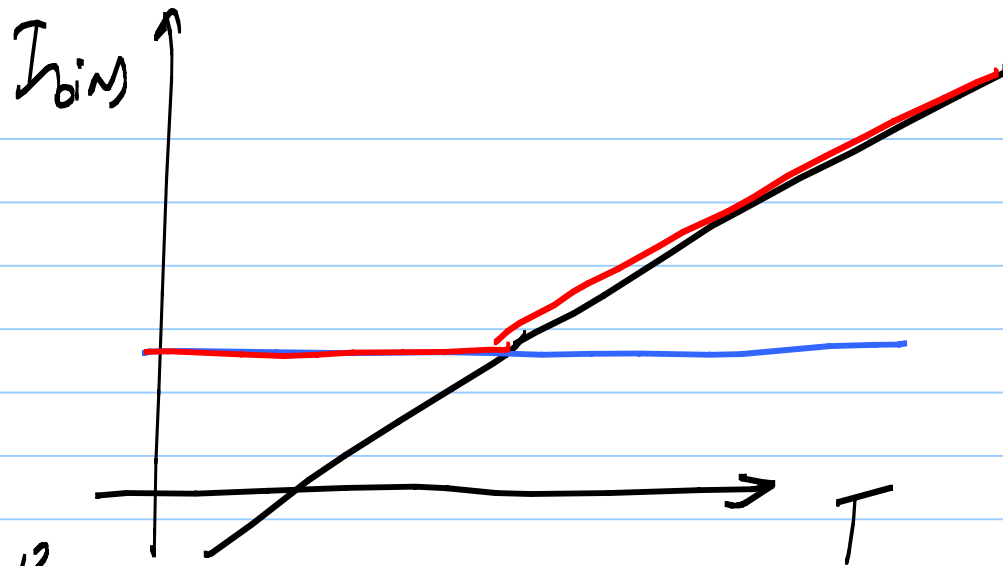
ff

sf

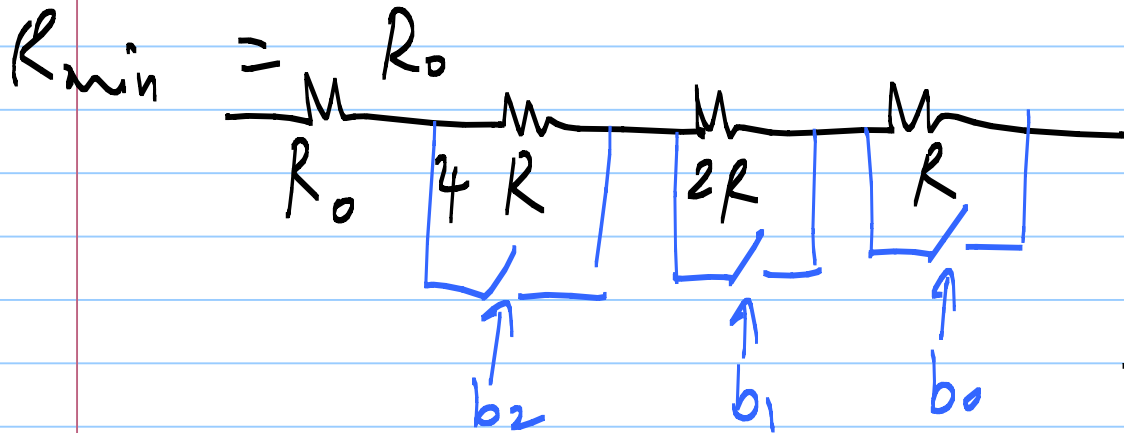
fs







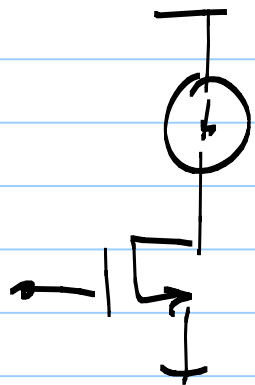
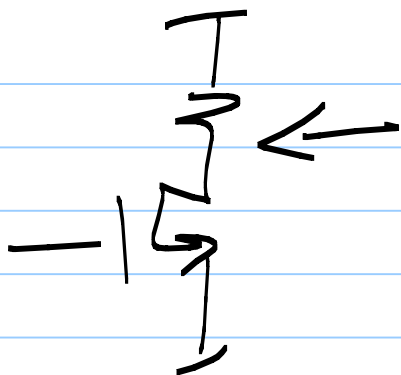
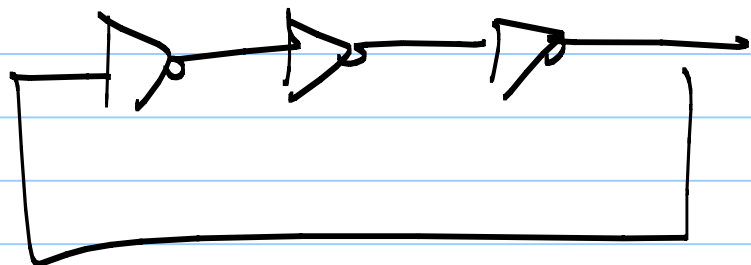
$$R_{max} = R_0 + 7R$$



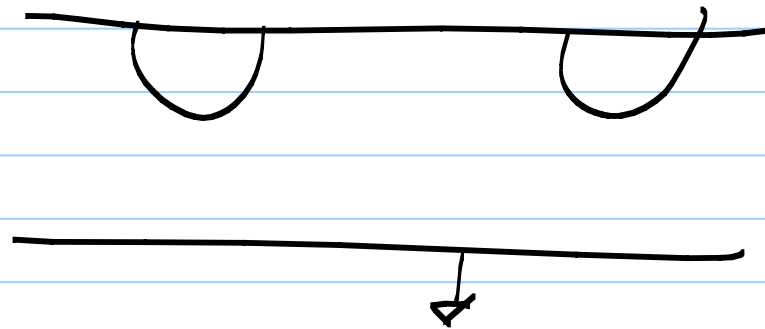
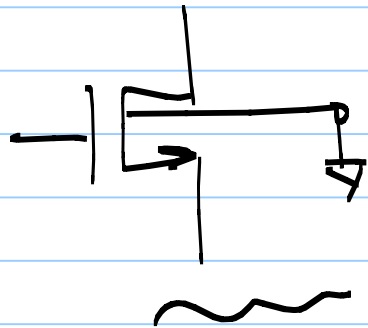
$$b_{n-1} \dots b_0 \downarrow$$

$$1 \ 0 \ 0 \ 0 \dots 0$$

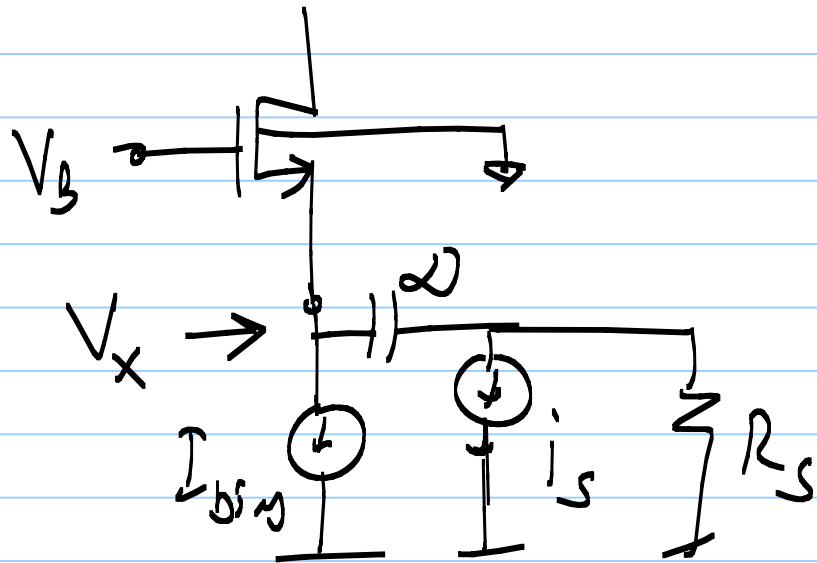
$$= 011 \quad R_{nom} = R_0 + 4R$$



2) $\frac{g_{mb}}{V_T} = V_{T0} + \gamma \left[\sqrt{2\phi_f + V_{SB}} - \sqrt{2\phi_f} \right]$

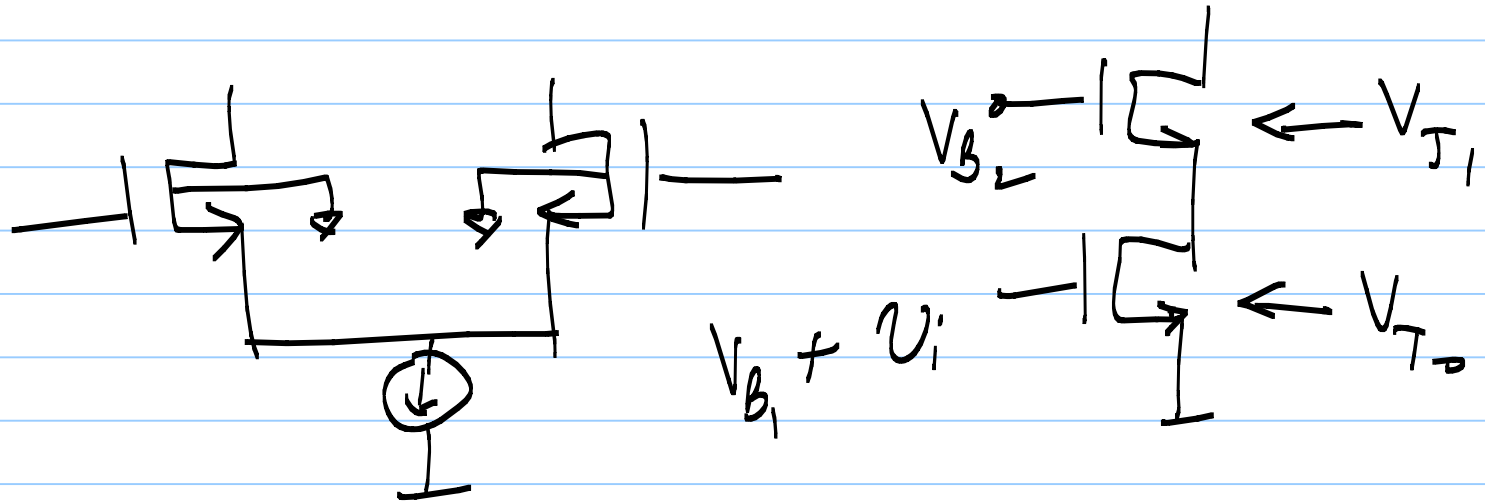


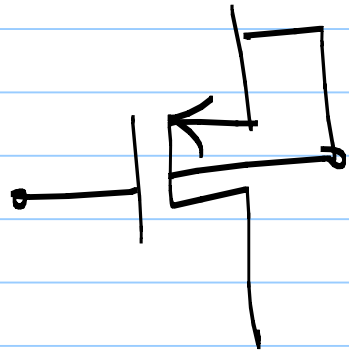
$V_{SB} > 0 \Rightarrow V_T > V_{T0}$



$$V_{SB} = V_X$$

$$V_T > V_{T_0}$$

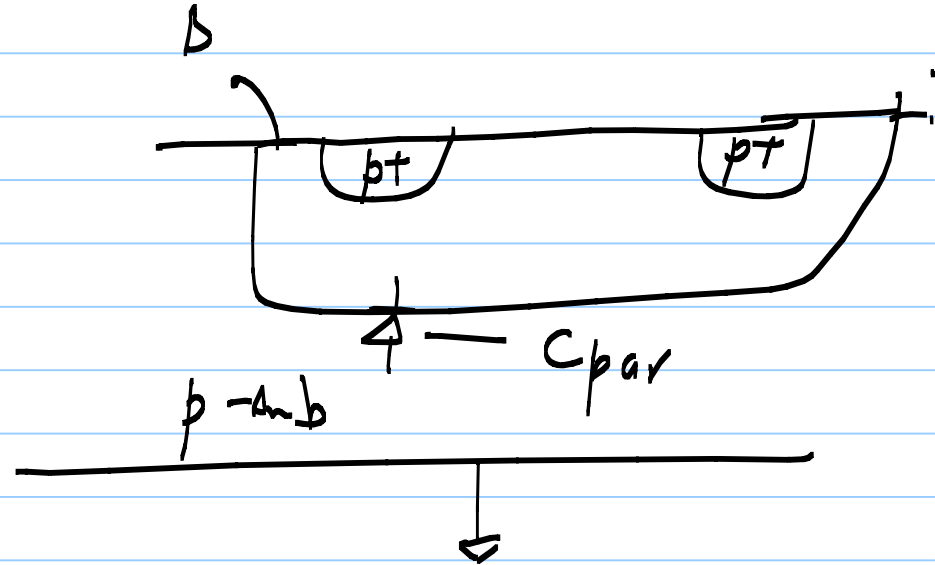
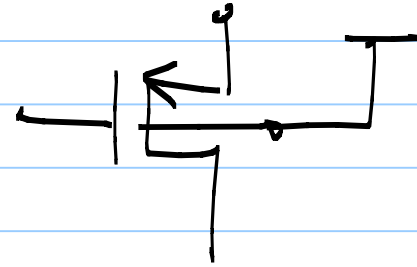


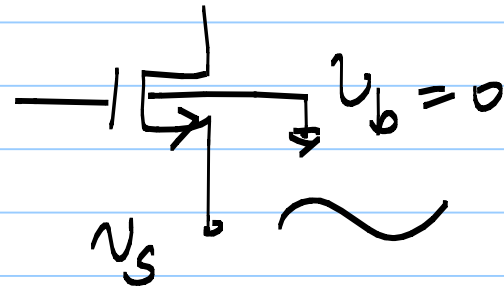
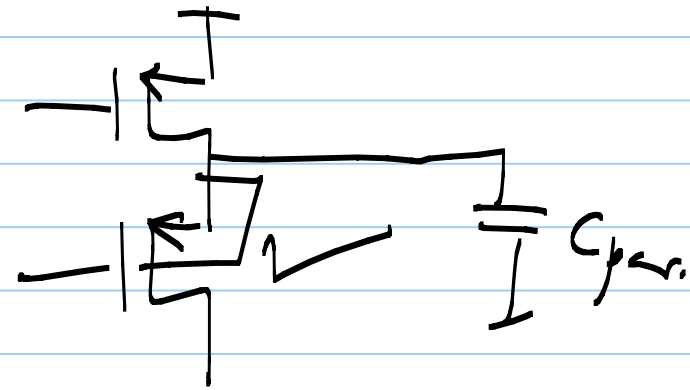
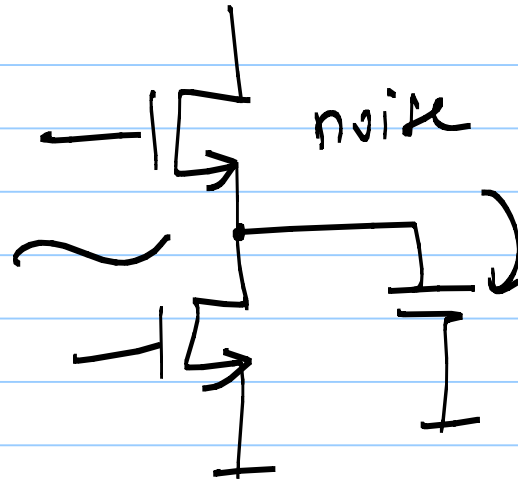


✓
DC
biasing
circuits

or

low-freq. ckt



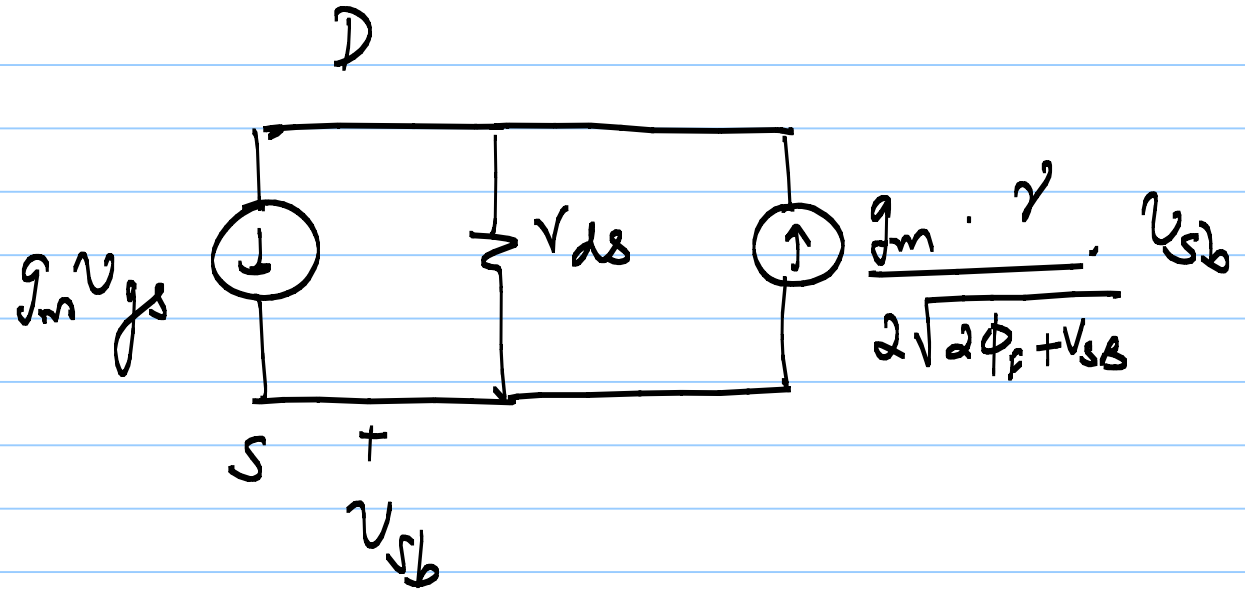


$$\frac{\partial V_T}{\partial V_{SB}} = \frac{\partial}{\partial \sqrt{V_{SB} + 2\phi_F}}$$

$$\frac{\partial I_D}{\partial V_{SB}} = \frac{\partial I_D}{\partial V_T} \cdot \frac{\partial V_T}{\partial V_{SB}} = \frac{-g_m \cdot \partial}{\partial \sqrt{V_{SB} + 2\phi_F}}$$

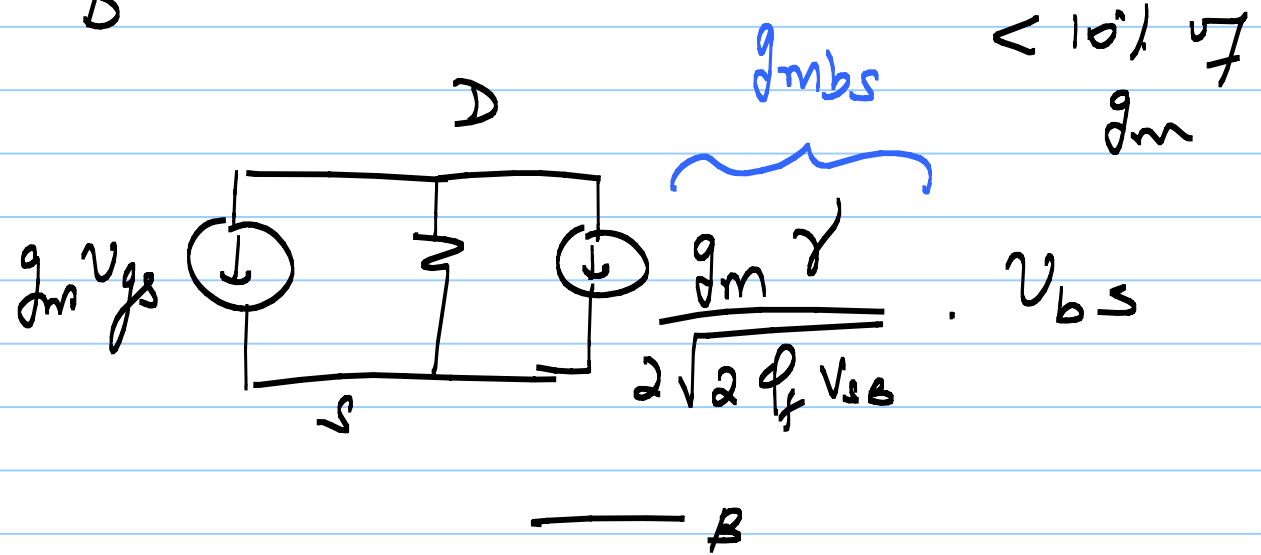
$$i_d = \frac{\partial I_D}{\partial V_{SB}} \cdot v_{sb}$$

G



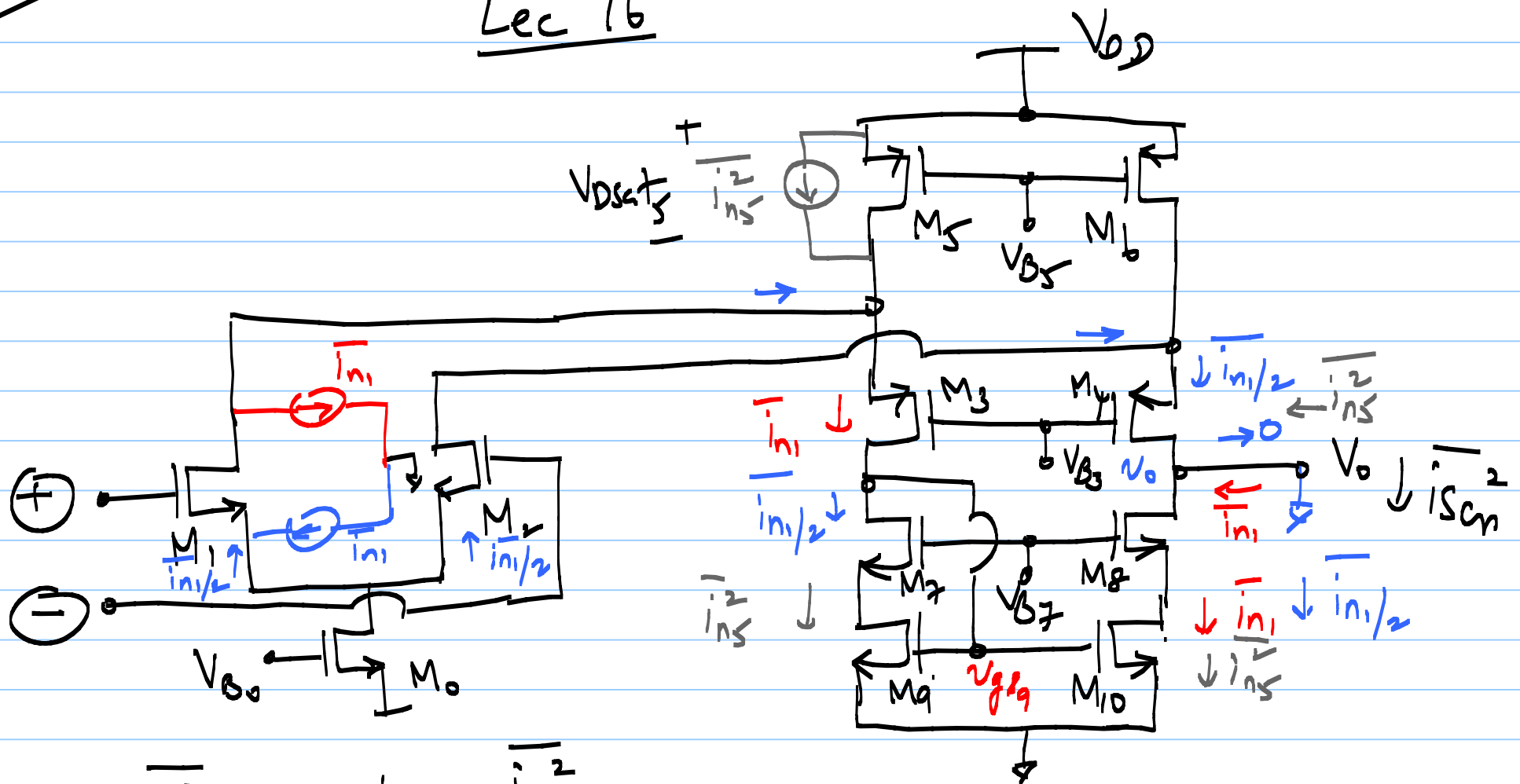
B

g



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Lec 16



$$7) e_n^2 = \frac{1}{g_{m1}^2} \cdot i_{scn}^2$$

$$= \frac{1}{g_{m1}^2} \left[i_{n1}^2 + i_{n2}^2 + i_{n5}^2 + i_{n6}^2 + i_{n7}^2 + i_{n8}^2 + i_{n9}^2 + i_{n10}^2 \right]$$

$$\frac{\overline{e_n^2}}{\Delta f} = \frac{16kT}{3g_{m1}} + \frac{16kT g_{m5}}{3g_{m1}^2} + \frac{16kT g_{m9}}{3g_{m1}^2}$$

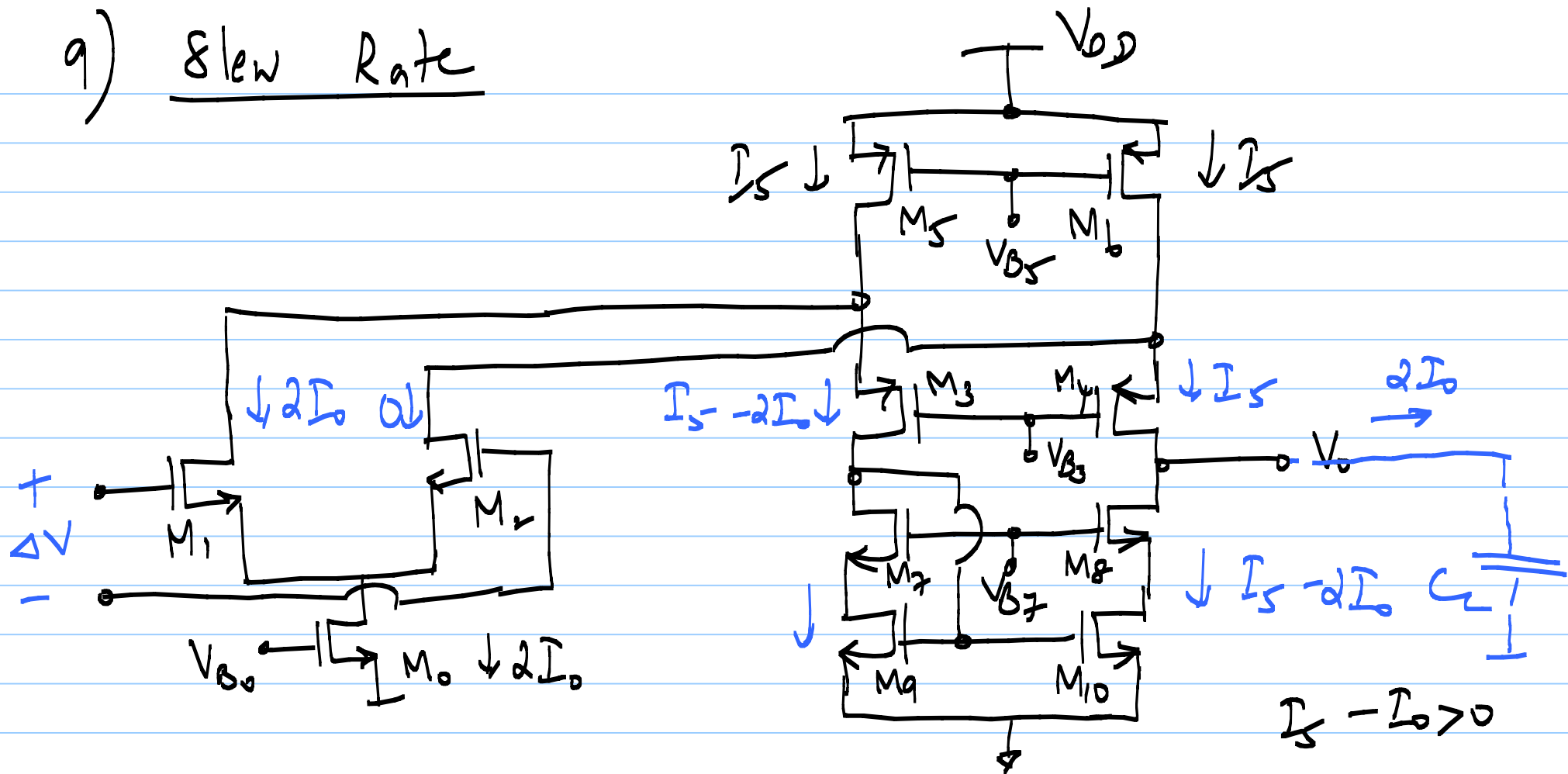
noise of folded cascode is worse than

1-stage or telescopic opamps

$$8) \quad \sigma_{os}^2 = \sigma_{V_{T1/2}}^2 + \sigma_{V_{T5,1}}^2 \cdot \frac{g_{m5}^2}{g_{m1}^2} + \sigma_{g_{10}}^2 \cdot \frac{g_{m9}^2}{g_{m1}^2}$$

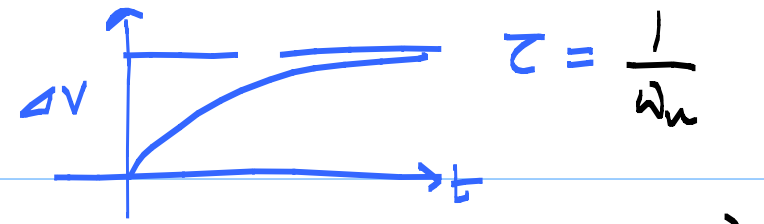
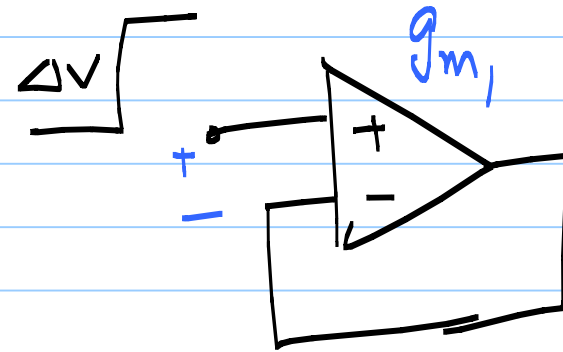
offset is worse

9) Slew Rate



case 1 : $SR = \pm 2I_0/C_2$ if $I_5 > 2I_0$

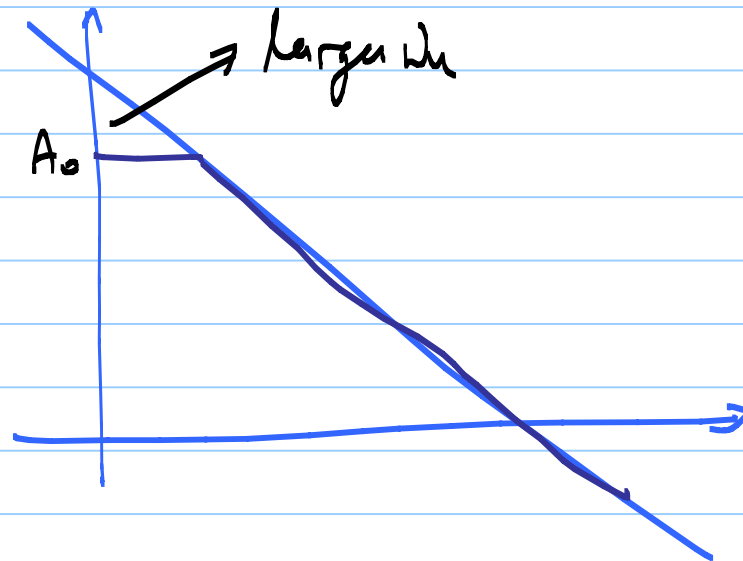
case 2 : If $I_5 < 2I_0$?



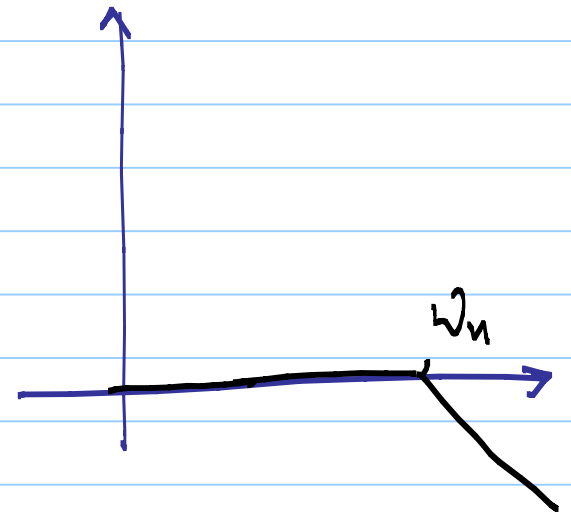
$$V(t=0^-) = V(t=0^+)$$

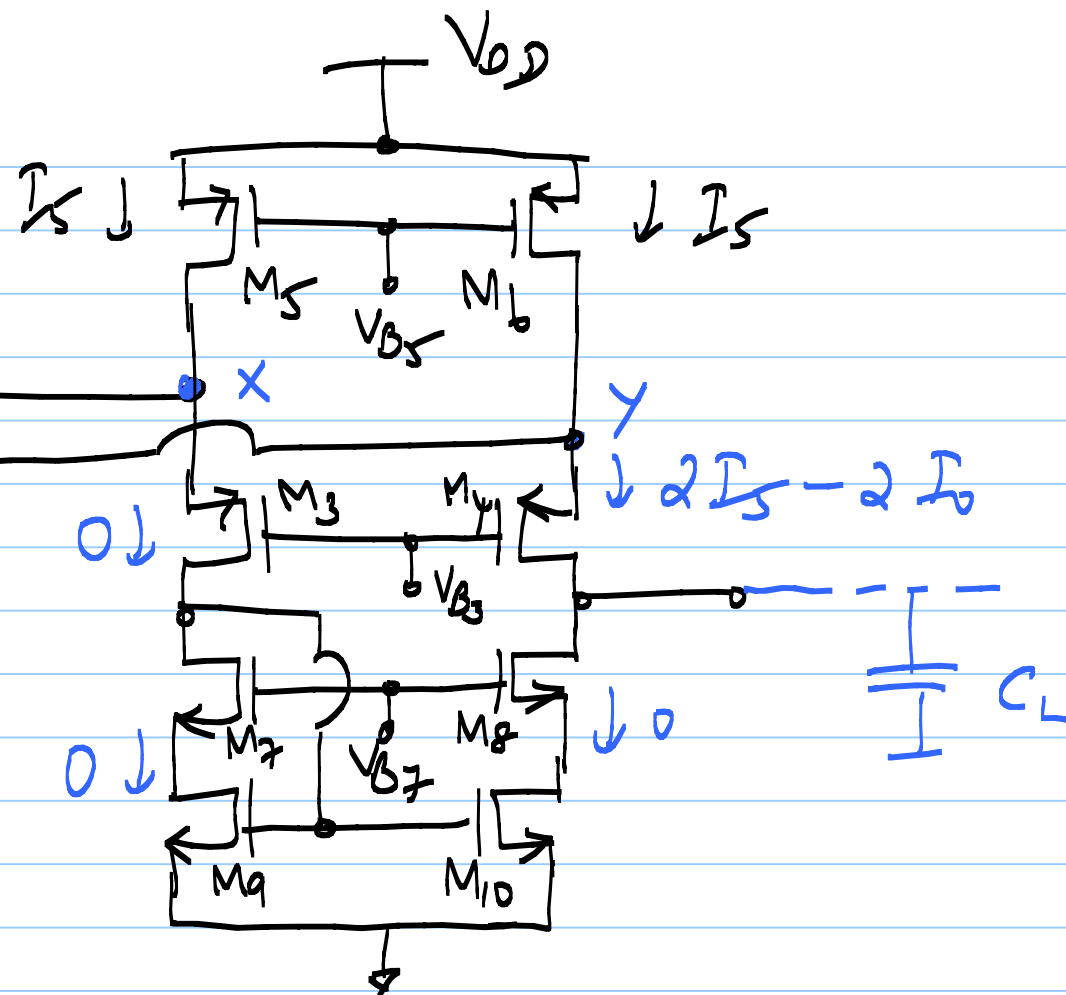
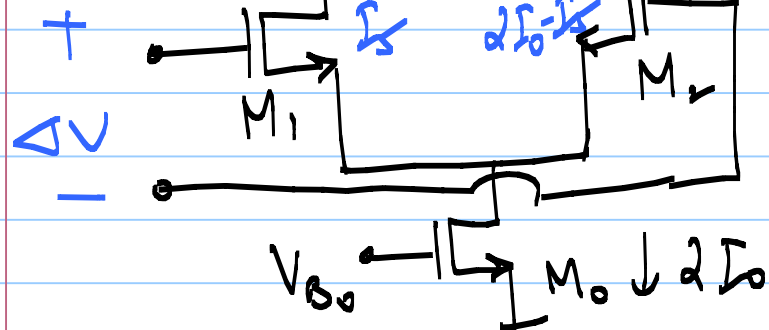
$$(V_+ - V_-)(t=0^+) = \Delta V$$

$$|LG| = |A|$$



$$|CLG|$$





KCL @ x: $I_{D_1} = I_S$; $I_{D_2} = 2I_0 - I_S$

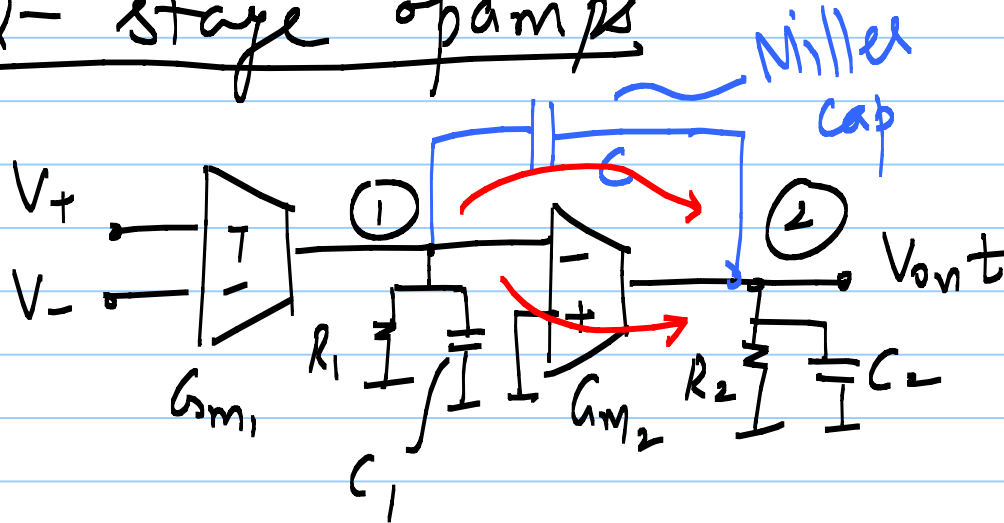
KCL @ y : $I_{xy} = I_x - (2I_x - I_x) = 2I_x - 2I_x$

$$s_k = \frac{+ 2 I_5 - 2 I_6}{C_L}$$

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Lec 17

2-stage opamps



$$\text{gain} = G_{m1} R_1 G_{m2} R_2$$

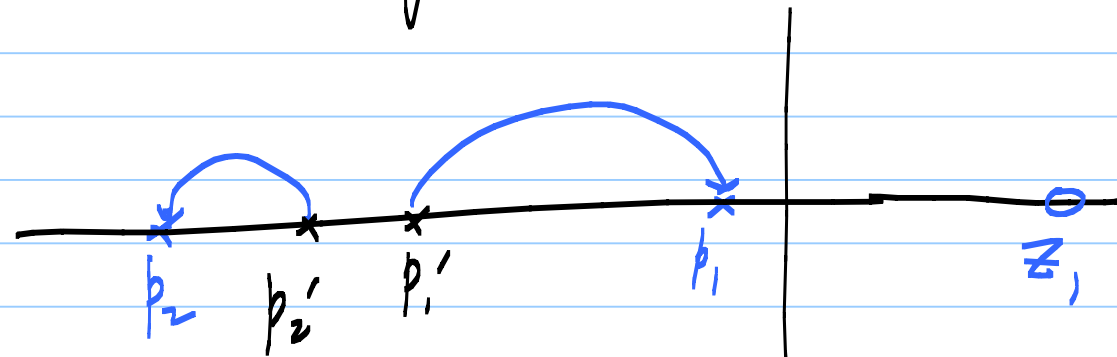
If you drive R_L

$$\text{gain} = G_{m1} R_1 G_{m2} (R_L \parallel R_2)$$

2 poles
LHP

$$p_1' = \frac{-1}{R_1 C_1}$$

$$p_2' = \frac{-1}{R_2 C_2}$$



phase margin
gain margin

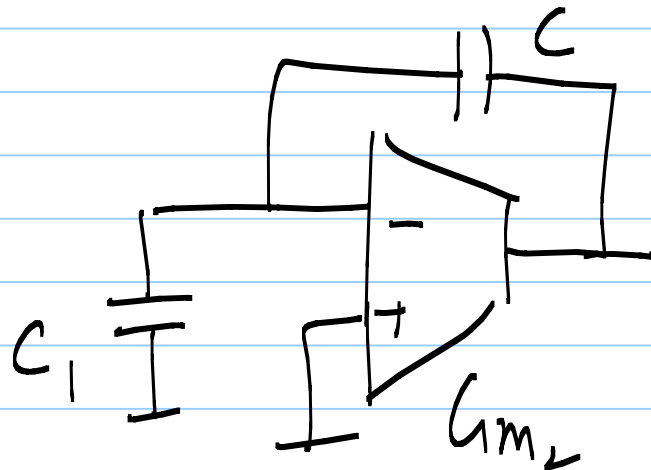
pole splitting improves PM

$$C @ \text{Node 1} = C_1 + G_{m2} R_2 C \approx G_{m2} R_2 C$$

$$R @ \text{node 1} = R_1$$

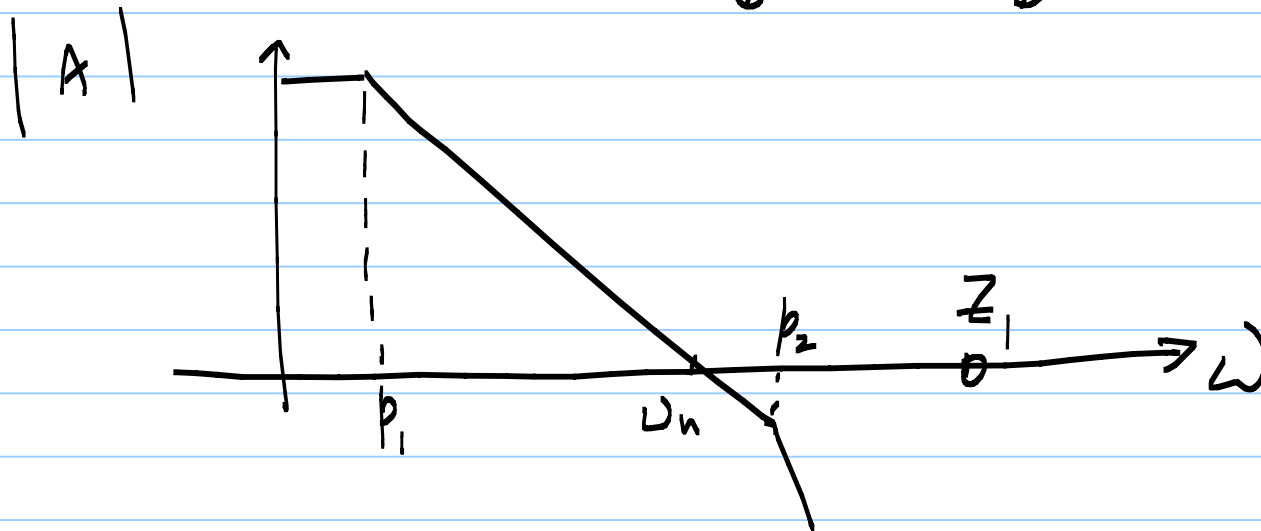
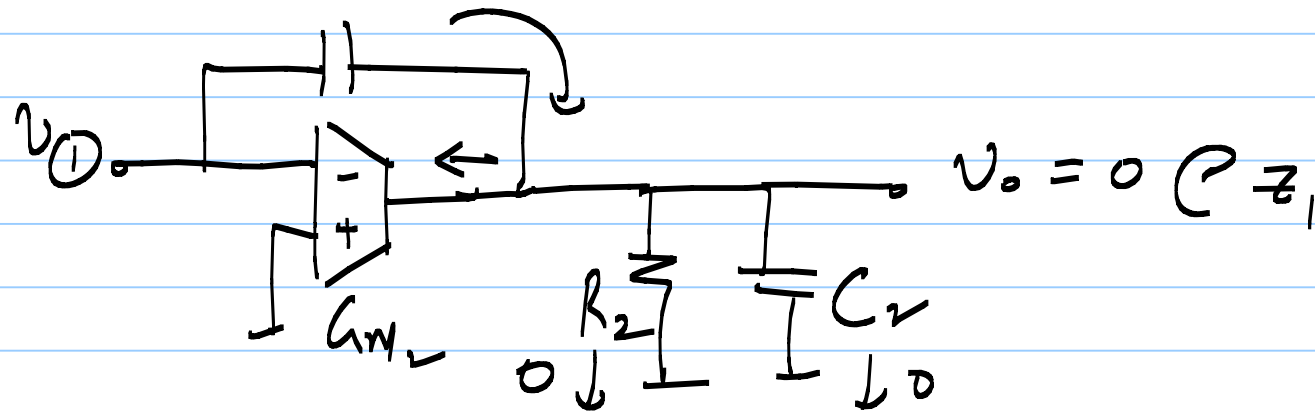
$$p_1' \rightarrow \text{moves to } p_1 = \frac{-1}{R_1 G_{m2} R_2 C}$$

$$p_2' \rightarrow \text{moves to } p_2 = \frac{-1}{\left[R_2 \parallel \frac{1}{G_{m2}} \cdot \frac{C_1 + C}{C} \right] \left[C_2 + \frac{C C_1}{C + C_1} \right]}$$



$$\leftarrow R_{out} = \left(\frac{C_1 + C}{C} \right) \frac{1}{G_{m2}}$$

$$Z_{\text{ero}} \quad Z_1 @ + \frac{G_{m2}}{C}$$

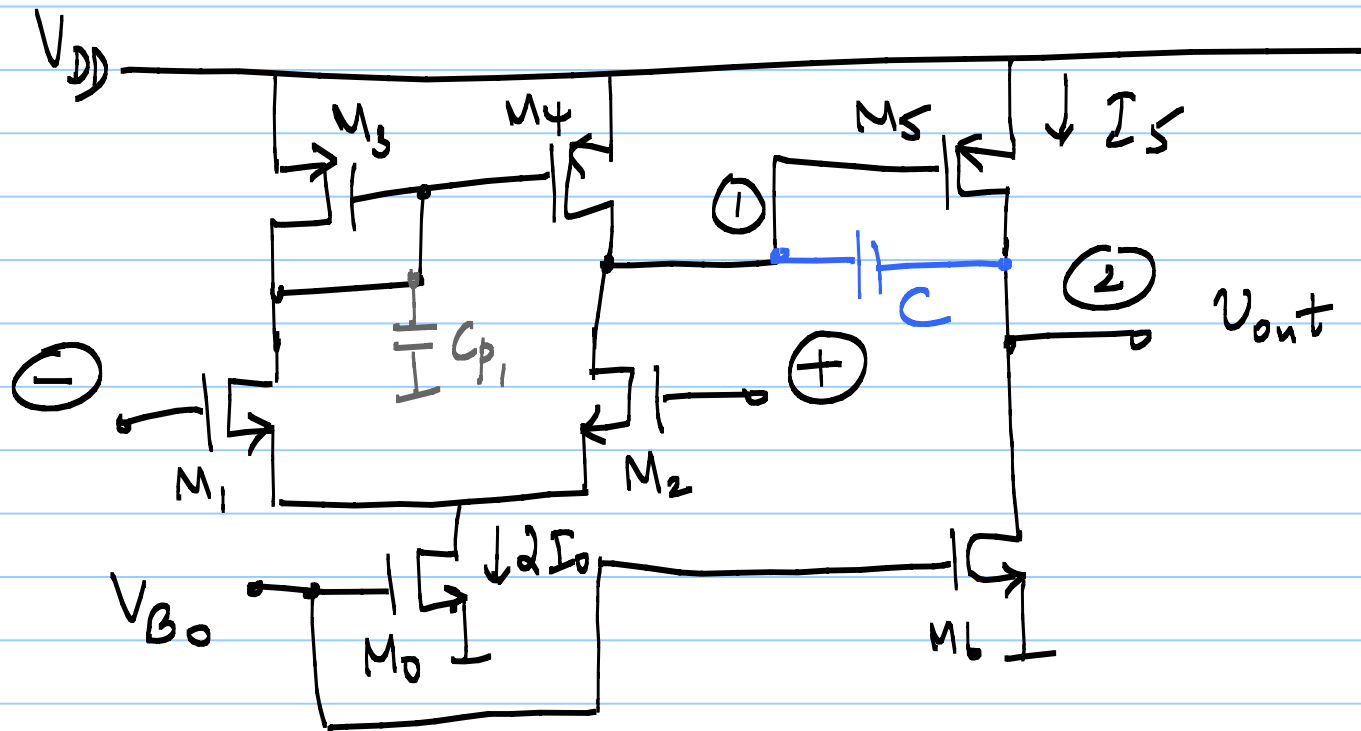


$$Z_1 \Rightarrow \omega_u$$

$$\omega_u = A_o \cdot v_d = \frac{G_{m1} R_1 G_{m2} R_2}{R_1 G_{m1} R_2 C}$$

$$\omega_n = \frac{G_{m1}}{C}$$

$$Z_1 \gg \omega_n \Rightarrow G_{m2} \gg G_{m1}$$



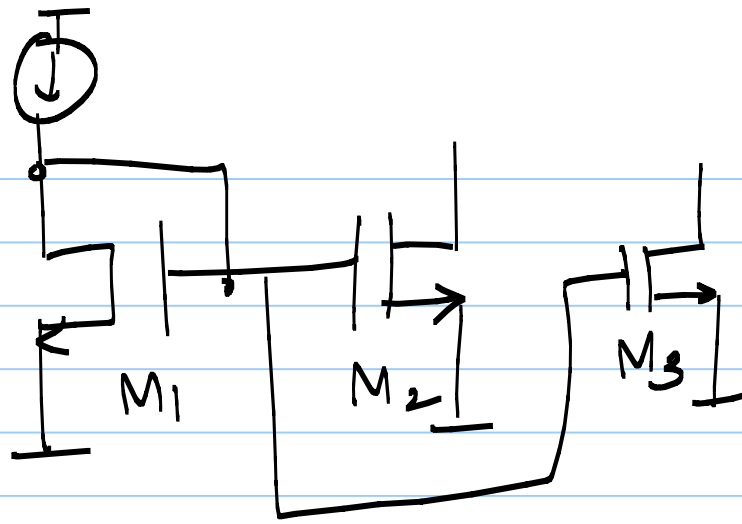
$$1) \quad V_{GS0} \Big|_{2I_0} = V_{GS6} \Big|_{I_5}$$

$$L_0 = L_6$$

$$\frac{2I_0}{(W/L)_0} = \frac{I_5}{(W/L)_6}$$

$$2) \quad V_{DD} - V_{GS3} \Big|_{I_0} = V_{DD} - V_{GS5} \Big|_{I_5}$$

$$\frac{I_0}{(W/L)_3} = \frac{I_5}{(W/L)_5}$$



$$L_1 = L_2 = L_3$$

2-stage opamp datasheet

$$1) \quad G_m = G_{m1} R_1 \cdot G_{m2} = g_{m1} (r_{ds2} \parallel r_{ds4}) \cdot g_{m5}$$
$$G_{m1} = g_{m1} ; \quad G_{m2} = g_{m5}$$
$$R_1 = r_{ds2} \parallel r_{ds4} ; \quad R_2 = r_{ds5} \parallel r_{ds6}$$

$$(A.) \text{ DC gain} = G_{m1} R_1 G_{m2} R_2$$
$$= g_{m1} (r_{ds2} \parallel r_{ds4}) \cdot g_{m5} (r_{ds5} \parallel r_{ds6})$$

$$2) \quad \omega_u = \frac{G_{m1}}{C} = \frac{g_{m1}}{C}$$

$$3) \quad \omega_d = \frac{1}{G_{m2} R_2 R_1 C} = \frac{1}{(r_{ds2} \parallel r_{ds4}) (g_{m5} (r_{ds5} \parallel r_{ds6})) C}$$

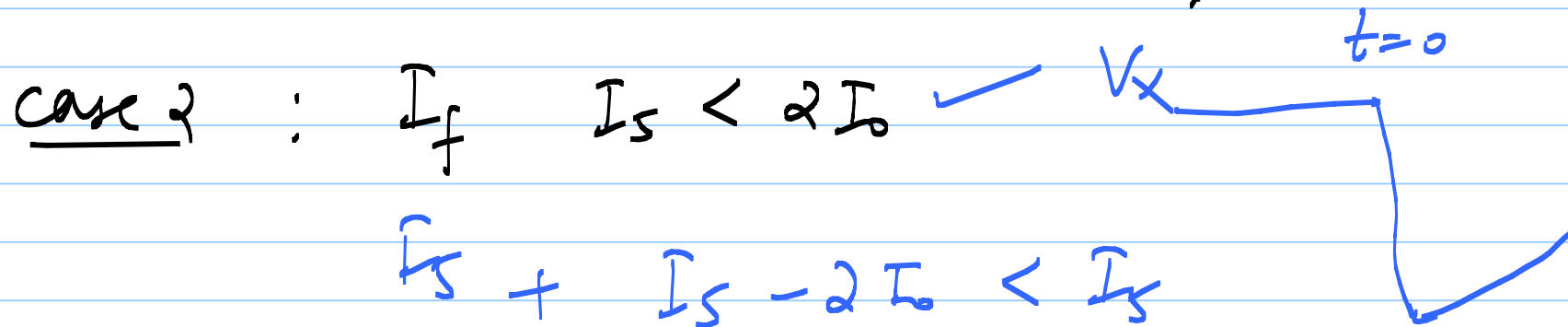
(p₁)

4) Non dominant poles & zeroes:

$$p_2 = \frac{-1}{\left[R_2 \parallel \frac{1}{g_{m2}} \cdot \frac{C_1 + C_2}{C} \right] \left[C_2 + \frac{C C_1}{C + C_1} \right]} ; z_1 = + \frac{g_{m2}}{C}$$

$$\begin{array}{l} \text{Mirror} \\ M_3, M_4 \end{array} \left\{ \begin{array}{l} p_3 = - g_{m3} / C_{p1} \\ z_2 = - 2 g_{m3} / C_{p1} \end{array} \right.$$

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$$I_S + I_S - 2I_0 < I_S$$

2-stage opamp datasheet

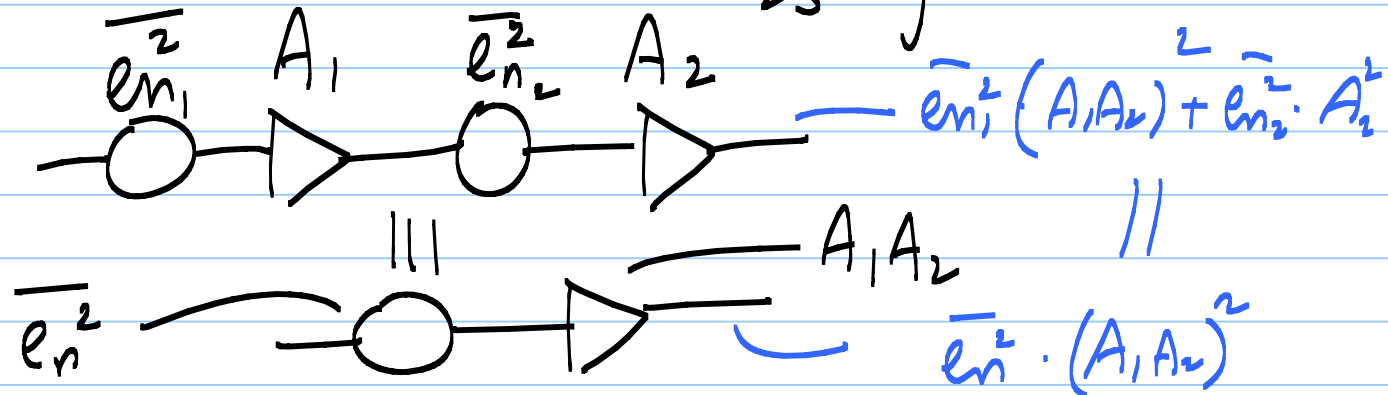
5) ICMR :

$$V_{CM,in} = \left\{ V_{DSatb} \Big|_{2I_b} + V_{GS1} \Big|_{I_b}, V_{DD} - V_{GS3} \Big|_{I_b} + V_{T1} \right\}$$

6) OCMR :

$$V_{CM,out} = \left\{ V_{B0} - V_{Tb}, V_{DD} - V_{SDSat5} \Big|_{I_s} \right\}$$

7) $\overline{e_n^2} = ?$



$$\overline{e_n^2} = \overline{e_{n_1}^2} + \frac{1}{A_1^2} \cdot \overline{e_{n_2}^2}$$

$$A_1 = g_{m_1} (r_{out_1}) ; A_2 = g_{m_5} (r_{out_2})$$

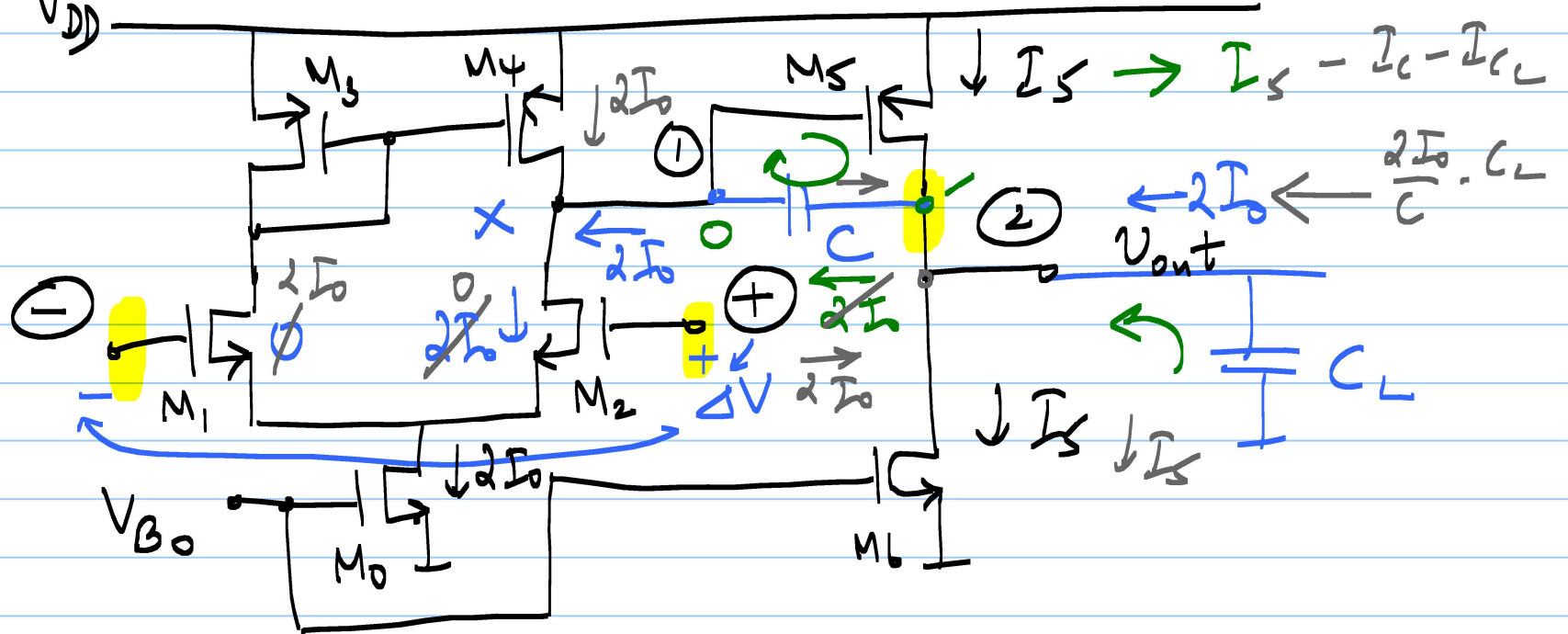
$$\overline{e_{n_1}^2} = \frac{16kT}{3g_{m_1}^2} [g_{m_1} + g_{m_3}]$$

$$\overline{e_{n_2}^2} = \frac{8kT}{3g_{m_5}^2} [g_{m_5} + g_{m_1}]$$

$$\overline{e_n^2} = \frac{16kT}{3g_{m_1}^2} [g_{m_1} + g_{m_3}] + \left(\frac{1}{g_{m_1} r_{out_1}} \right)^2 \cdot \frac{8kT}{3g_{m_5}^2} [g_{m_5} + g_{m_1}]$$

$$8) \quad g_{03}^2 = g_{V_{T_{1-2}}}^2 + \frac{g_{M_3}^2}{g_{M_1}^2} \cdot g_{V_{T_{3-4}}}^2 + (\quad)$$

9) $\frac{\text{Slew rate}}{V_{DD}}$



@ $t = 0^+$, $V_x(t=0^+) = V_x(t=0^-)$
 $\Rightarrow I_L(t=0^+) = 2I_0$

$$② \quad t = 0^+ \quad , \quad s_R = - \frac{2I_0}{C_L}$$

↓

$$- \frac{2I_0}{C_L}$$

$$\frac{I_{C_L}}{C_L} = \frac{2I_0}{C} \Rightarrow I_{C_L} = \frac{2I_0 \cdot C_L}{C}$$

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Lec 19

Design Example

Specs: $A_0 \gg 80 \text{ dB}$; $f_u \gg 5 \text{ MHz}$; $V_{op-p} = 4 \text{ V}$;
 $SR \gg 10 \text{ V}/\mu\text{s}$; $PM = 60^\circ$ for unity gain;

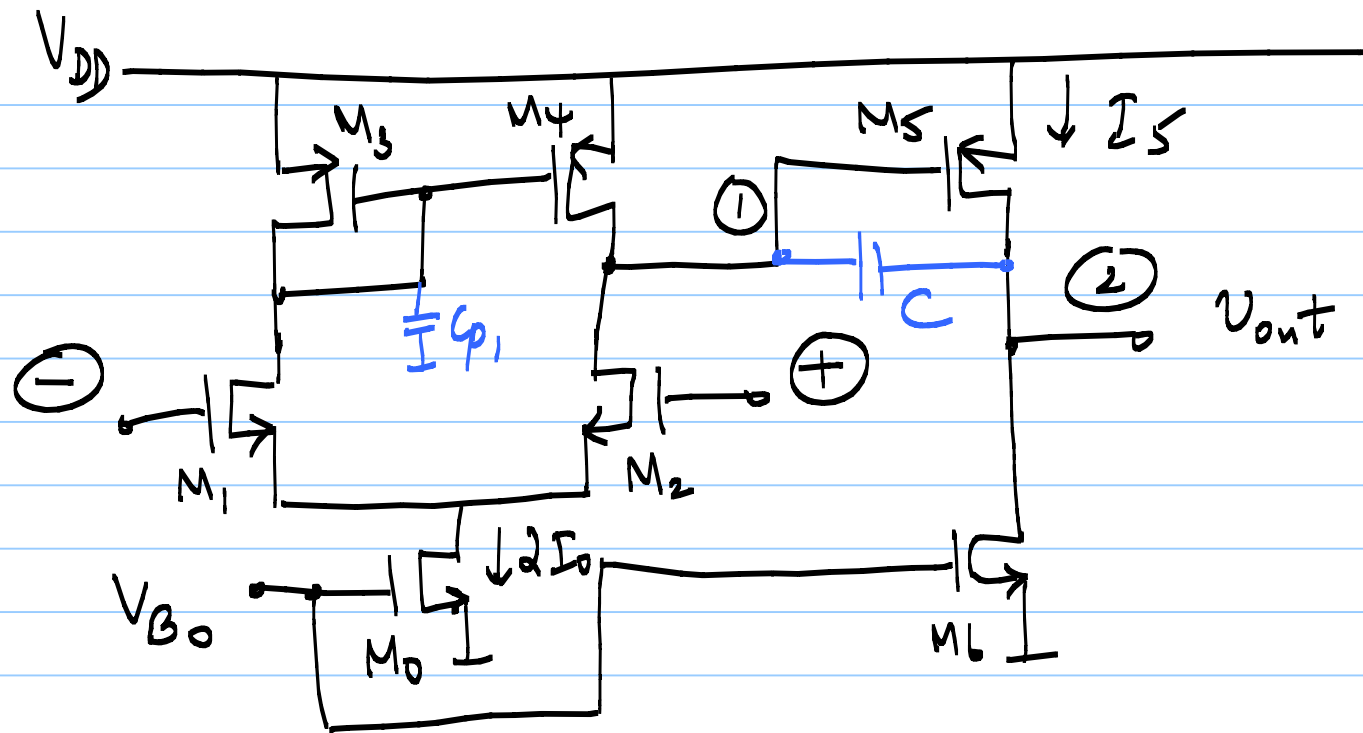
Design parameters

$$V_{DD} = 5 \text{ V}; \quad C_L = 10 \text{ pF}; \quad \mu_n C_{ox} = 50 \mu\text{A}/\text{V}^2$$

$$\mu_p C_{ox} = 25 \mu\text{A}/\text{V}^2; \quad V_{Tn} = V_{Tp} = 1 \text{ V};$$

$$L_{min} = 2 \mu\text{m}; \quad C_{ox} = 1.5 \text{ fF}/\mu\text{m}^2;$$

$$(\lambda L)_n = 0.04 \mu\text{m}/\text{V}; \quad (\lambda L)_p = 0.1 \mu\text{m}/\text{V}$$



1) Set all $L = L_{min.} = 2\mu m$

2) $\frac{2I_o}{C} = SR$

3) $\frac{g_{m1}}{C} = 2\pi f_n$

4) $g_{m5} = 10 g_{m1}$

$$5) \quad PM = 60^\circ \Rightarrow \quad p_2 = \sqrt{3} \omega_n \\ = -54.4 \text{ Mrad/s}$$

$$6) \quad p_2 \approx -\frac{gm_2}{C_L} = -\frac{gm_5}{C_L}$$

$$gm_5 = 544 \mu S$$

$$gm_1 = 54.4 \mu S$$

$$\frac{gm_1}{C} = 2\pi f_n \Rightarrow C = 1.73 \text{ pF}$$

$$\frac{2I_0}{C} = s/r \Rightarrow 2I_0 = 17.32 \mu A \\ I_0 = 8.66 \mu A$$

$$\left(\frac{W}{L}\right)_1 = 3.4$$

$$7) \quad V_{opp} = 4V$$

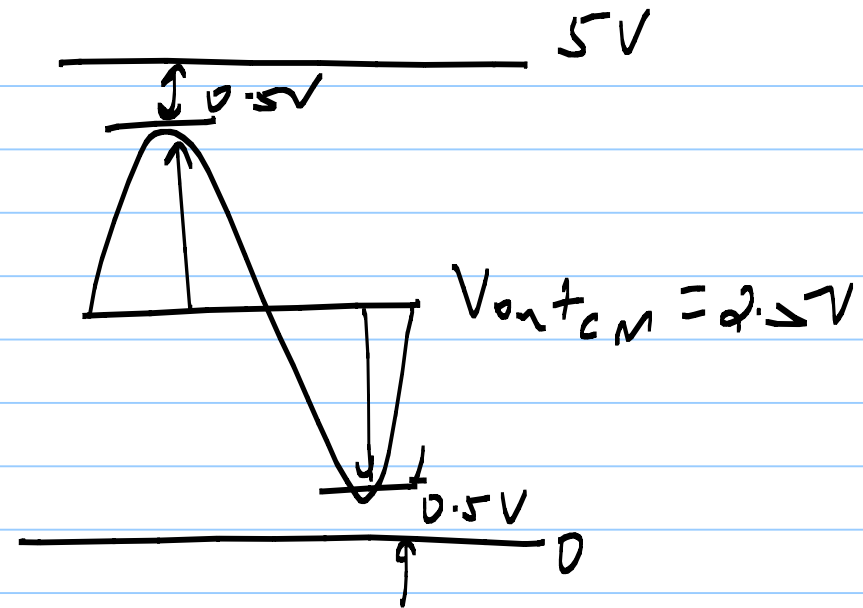
$$V_{dsat5} = V_{dsat6} = 0.5V$$

$$g_{m5} = \frac{2I_5}{V_{dsat5}} \Rightarrow I_5 = 136 \mu A$$

$$\Rightarrow \left(\frac{W}{L}\right)_5 = 43.5 \quad \checkmark$$

$$\left(\frac{W}{L}\right)_6 = 21.7 \Rightarrow \left(\frac{W}{L}\right)_0 = 2.8$$

$$\left(\frac{W}{L}\right)_{3,4} = \frac{I_0}{I_5} \left(\frac{W}{L}\right)_5 = 2.8 \quad \checkmark$$



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$$\lambda_n = 0.02 \text{ V}^{-1}$$

$$\lambda_p = 0.05 \text{ V}^{-1}$$

$$I_0 = 8.66 \mu\text{A}$$

$$r_{ds2} = 5.75 \text{ M}\Omega$$

$$r_{ds4} = 2.3 \text{ M}\Omega$$

$$\left. \begin{array}{l} r_{ds2} = 5.75 \text{ M}\Omega \\ r_{ds4} = 2.3 \text{ M}\Omega \end{array} \right\} r_{out1} = 1.64 \text{ M}\Omega$$

$$I_5 = 136 \mu\text{A}$$

$$r_{ds5} = 0.15 \text{ M}\Omega$$

$$r_{ds6} = 0.36 \text{ M}\Omega$$

$$\left. \begin{array}{l} r_{ds5} = 0.15 \text{ M}\Omega \\ r_{ds6} = 0.36 \text{ M}\Omega \end{array} \right\} r_{out2} = 0.11 \text{ M}\Omega$$

$$g_{m1} = 54.4 \mu\text{S} \quad , \quad g_{m2} = 544 \mu\text{S}$$

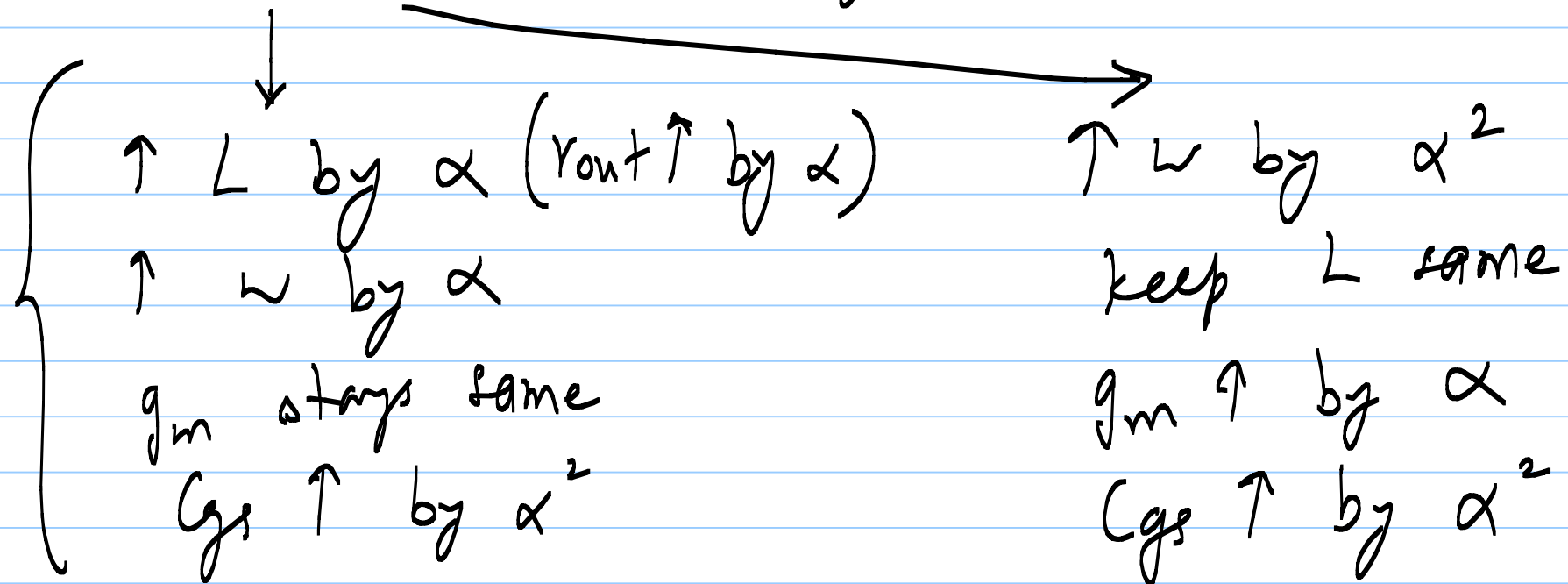
$$A_1 = g_{m1} r_{out1} = 89.2 \text{ V/V}$$

$$A_1 A_2 = 5334 \text{ V/V}$$

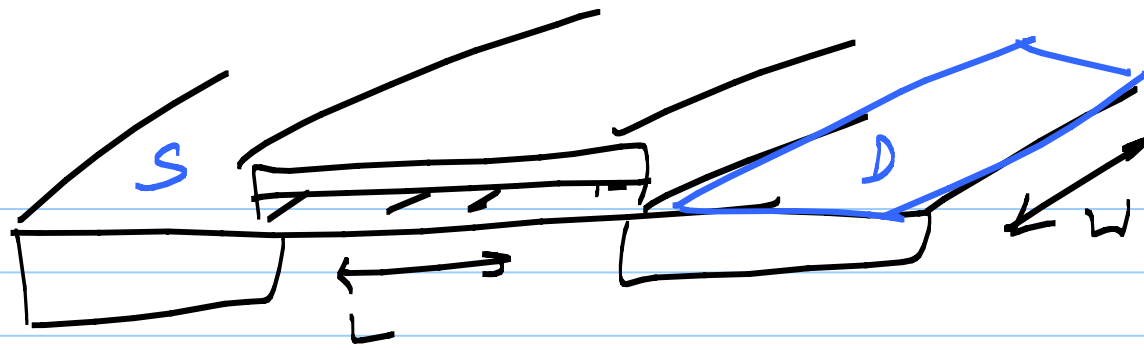
$$A_2 = g_{m2} r_{out2} = 59.8 \text{ V/V}$$

$$C_{gs} = \frac{2}{3} WL C_{ox}$$

A_i needs to $\uparrow$ by α



as $I \uparrow$ by α , $g_m \uparrow$ by $\sqrt{\alpha}$
 $r_{ds} \downarrow$ by α



Instead, equate r_{up} & r_{dn} @ outputs of 1st & 2nd stages.

$$\text{Set } L_{3,4,5} = \left(\frac{\lambda_p}{\lambda_n} \right) \cdot L_{min} = 5 \mu m$$

Set $W_{3,4,5}$ so that $(W/L)_{3,4,5}$ stays the same

$$r_{out1} = 2.88 M\Omega$$

$$r_{out2} = 0.18 M\Omega$$

$$A_1 = 156.6 \text{ V/V} ; A_2 = 97.9 \text{ V/V}$$

$$A_0 = 15334 \text{ V/V} \approx 84 \text{ dB}$$

Check :

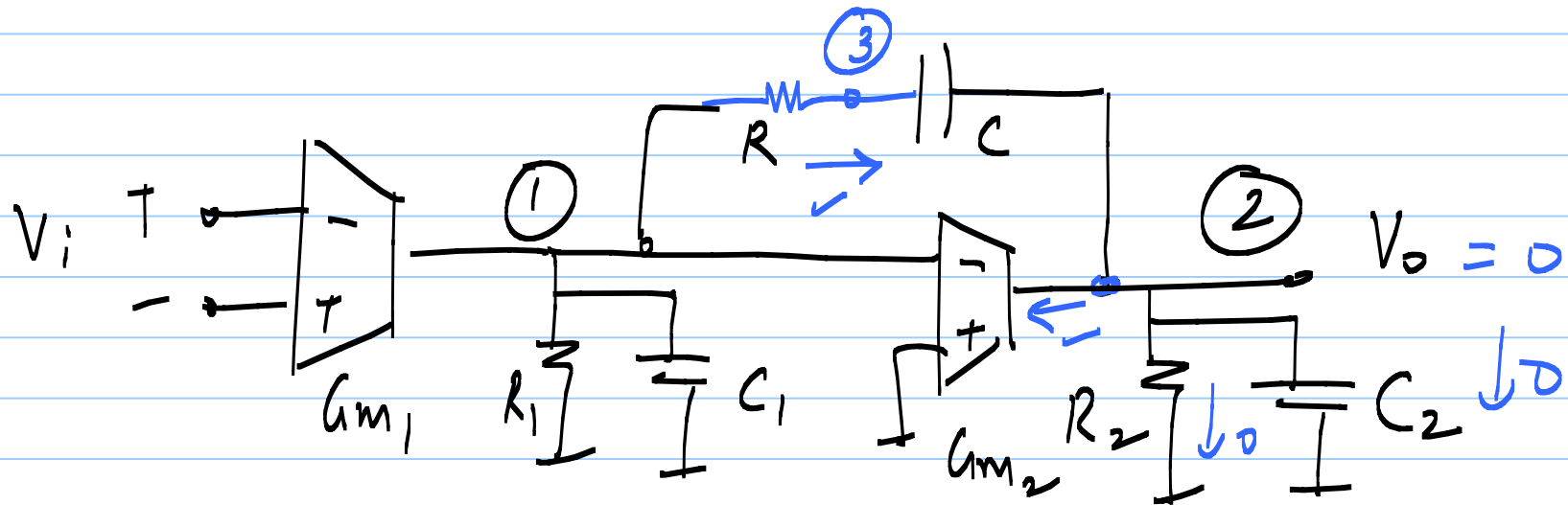
$$1) \quad \text{Mirror pole} = \frac{g_{m_3}}{C_{p_1}} \Rightarrow p_2$$

$$\text{Mirror zero} \approx \frac{2g_{m_3}}{C_{p_1}} \Rightarrow p_2$$

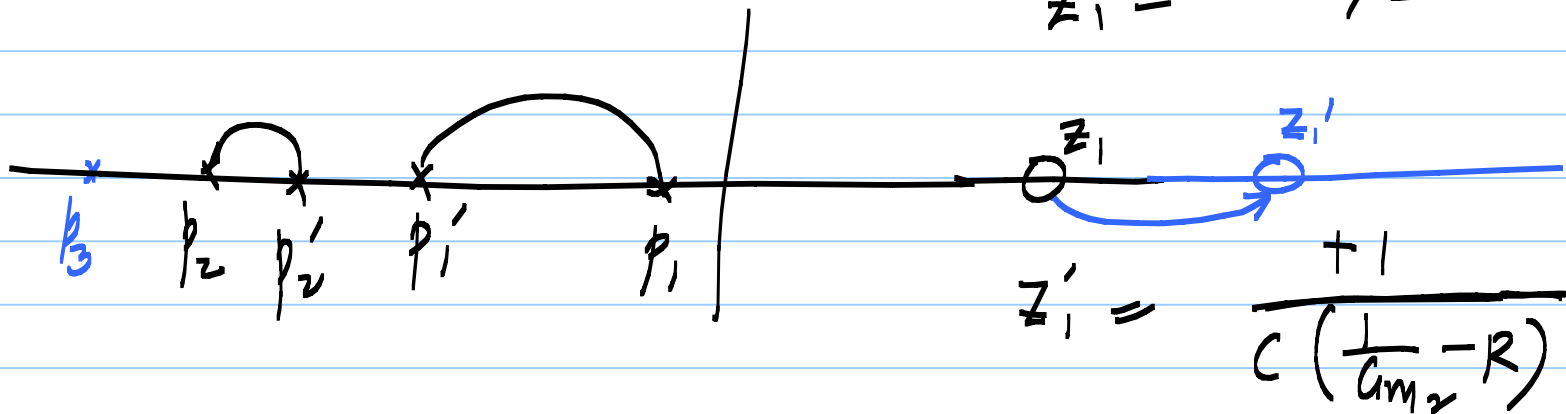
$$2) \quad g_{m_5} r_{out_2} \cdot C \gg C_{gs}$$

$$3) \quad C_{gd} \ll \text{all } C_{par.}$$

Pole-zero cancellation compensation



$$Z_1 = +G_{m2}/C$$



$$p_3 \approx \frac{-1}{R \cdot C_1}$$

1) Case 1: Set $z_1' = \infty$ (very large)

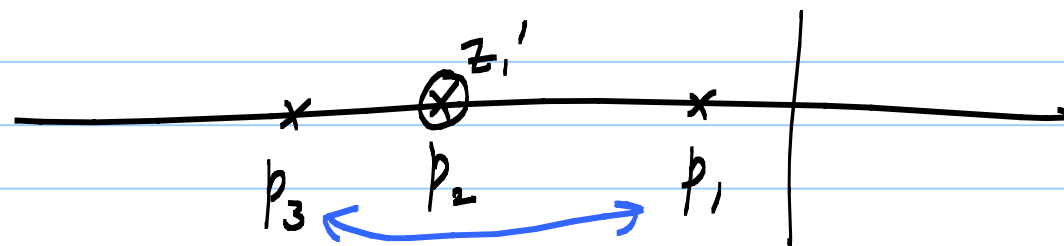
$$\Rightarrow R = \frac{1}{G_{m2}}$$

$$p_3 \approx -\frac{G_{m2}}{C_1}$$

2) Choose $R > \frac{1}{G_{m2}} \Rightarrow$ zero moves into LHP (from $-\infty$ side)

Set z_1' to cancel p_2

$\Rightarrow$ larger PM or larger BW



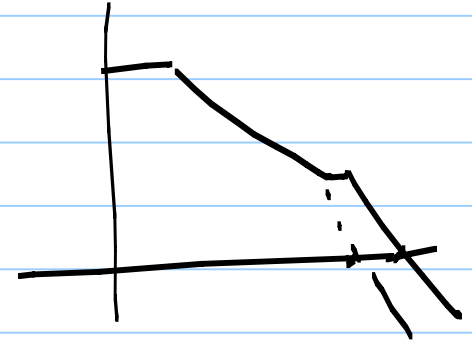
21/2/20

2)

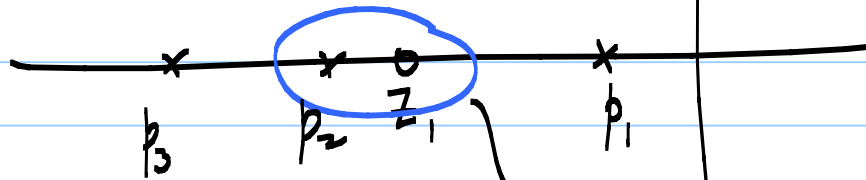
Lec 21

$$p_2 = \frac{1}{C_m \cdot ()}$$

still need $R \propto \frac{1}{C_m}$



pole zero
doublet



slow settling component

We want $p_2 - z_1$ on top of each other
& track each other (due to process variations)
temp.

We want R to track $\frac{1}{g_{m2}}$

Technique 1)

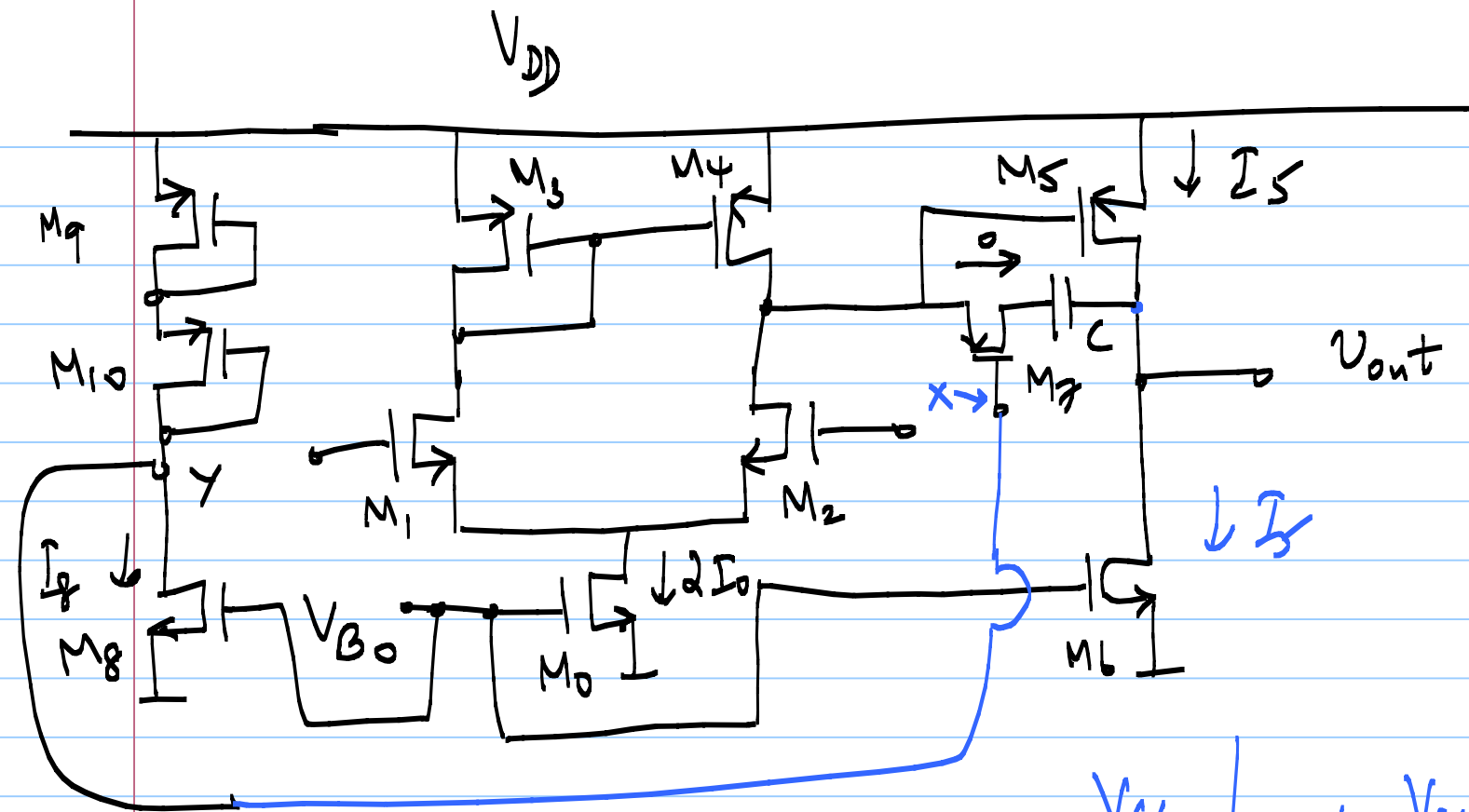
Use MOSFET in linear region to realize R

$$I_D = \mu C_{ox} \left(\frac{W}{L} \right) \left\{ (V_{gs} - V_T) (V_{ds}) - \frac{V_{ds}^2}{2} \right\}$$

$$g_{ds} = \frac{\partial I_D}{\partial V_{ds}} = \mu C_{ox} \left(\frac{W}{L} \right) (V_{gs} - V_T - V_{ds})$$

$$r_{ds} \Big|_{V_{ds} \rightarrow 0} = \frac{1}{g_{ds}} = \frac{1}{\mu C_{ox} \left(\frac{W}{L} \right) (V_{gs} - V_T)}$$

$$g_{ds} \Big|_{V_{ds} \rightarrow 0} = g_m \Big|_{sat}$$



$$V_x = V_{DD} - V_{S45} - V_{S47}$$

$$V_y = V_{DD} - V_{S49} - V_{S410}$$

$$V_{S45} \Big|_{I_5} + V_{S47} = V_{S49} \Big|_{I_8} + V_{S410} \Big|_{I_8}$$

e.g. set $V_{S45} \Big|_{I_5} = V_{S49} \Big|_{I_8} \Rightarrow \frac{I_5}{(W/L)_5} = \frac{I_8}{(W/L)_9}$

$$V_{S47} = V_{S410} \Big|_{I_8}$$

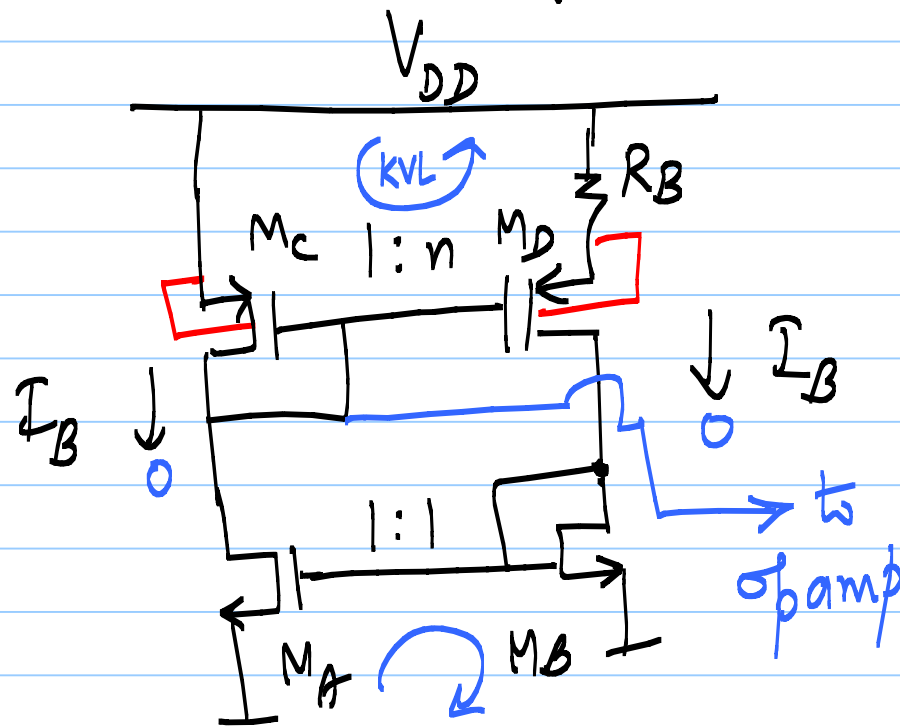
$$\tau \uparrow \Rightarrow g_{m5} \downarrow \Rightarrow r_{ds7} \uparrow \Rightarrow V_{S4} \downarrow$$

$$V_{sg7} = V_{sg1} + \Delta V_g - V_{sg5} - \Delta V_{10} + \Delta V_5 = + \Delta V_7$$

$$g_{ds} = \mu_p C_{ox} \left(\frac{W}{L} \right) \left(V_{sg7_{inj}} + \Delta V_7 - V_{T7} \right)$$

Technique 2) Use passive resistor R , force

g_{m5} to track $1/R$



$$V_{SGC} = V_{SGD} + I_B R_B$$

$$\cancel{V_{TC}} + V_{DSATC} = \cancel{V_{TD}} + V_{DSATD} + I_B R_B$$

$$\frac{2I_B}{g_{m_c}} = V_{DSATC}$$

$$\frac{2I_B}{g_{m_D}} = V_{DSATD}$$

$$g_{m_D} = \sqrt{n} g_{m_c}$$

$$\frac{2I_B}{g_{m_c}} = \frac{2I_B}{g_{m_D}} + I_B R_B$$

* $I_B = 0$ is a valid state of the circuit
 $\Rightarrow$ need a startup circuit

* If $I_B \neq 0$,

$$\frac{2}{g_{mc}} = \frac{2}{g_{mD}} + R_B$$

$$\frac{2}{g_{mc}} = \frac{2}{g_{mc} \sqrt{n}} + R_B$$

$$\frac{1}{g_{mc}} \left[2 - \frac{2}{\sqrt{n}} \right] = R_B$$

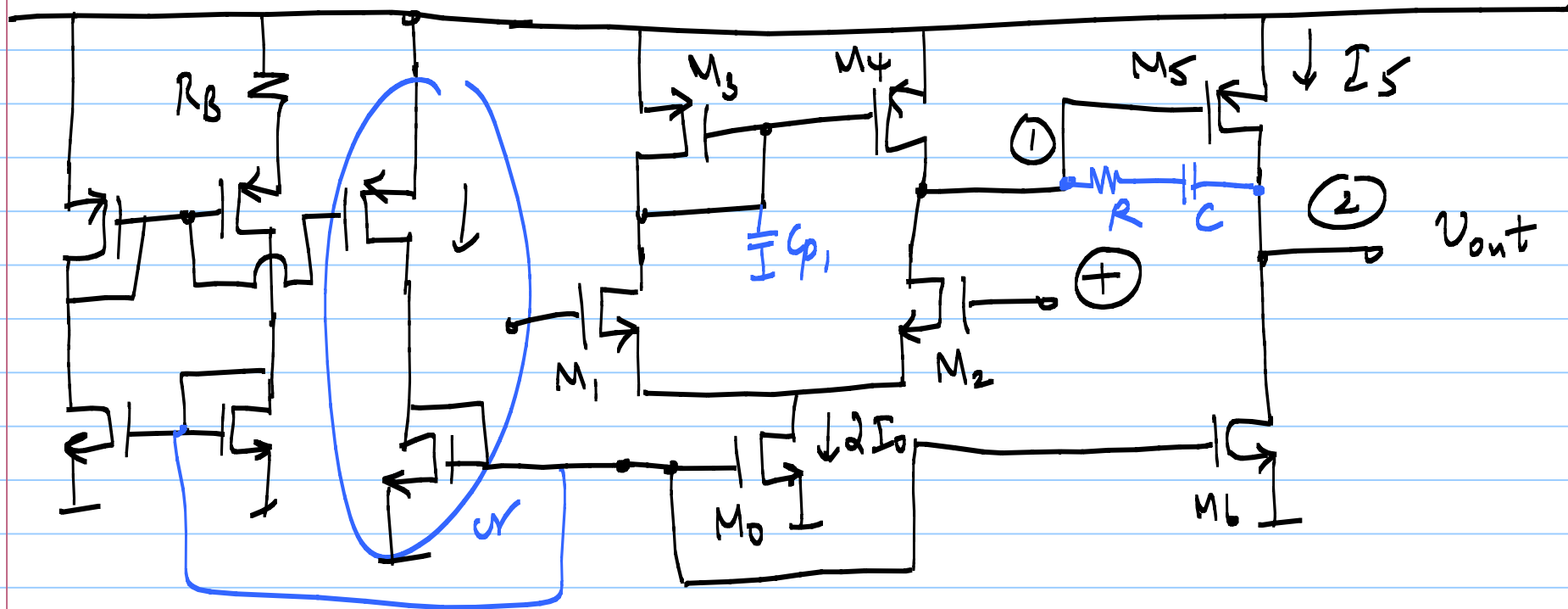
$$\frac{1}{g_{mc}} \propto R_B$$

$\leftarrow$ choose same type
of resistor so that
 R_B tracks R

$$I_B \propto \frac{1}{R_B^2}$$

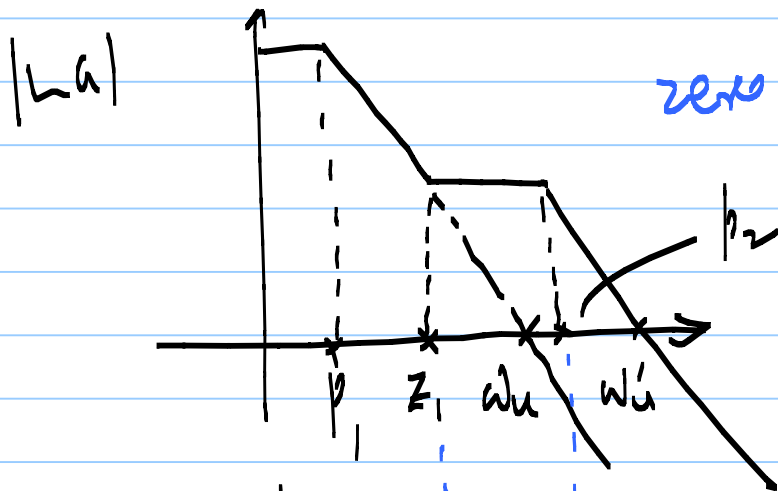
We want $I_S \propto \frac{1}{R_D^2} \propto \frac{1}{R^2}$

$$g_{m5} \propto \frac{1}{R}$$

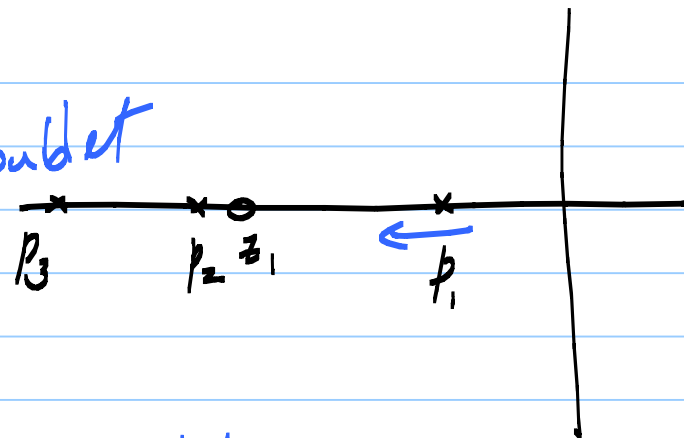


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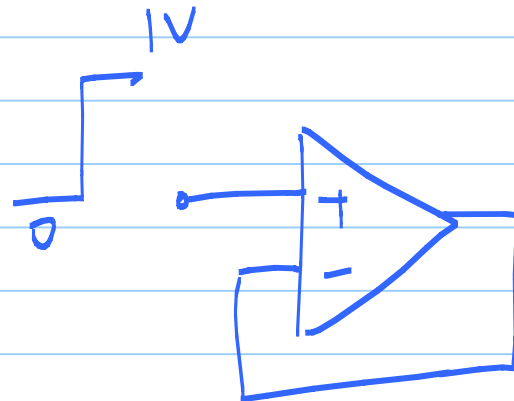
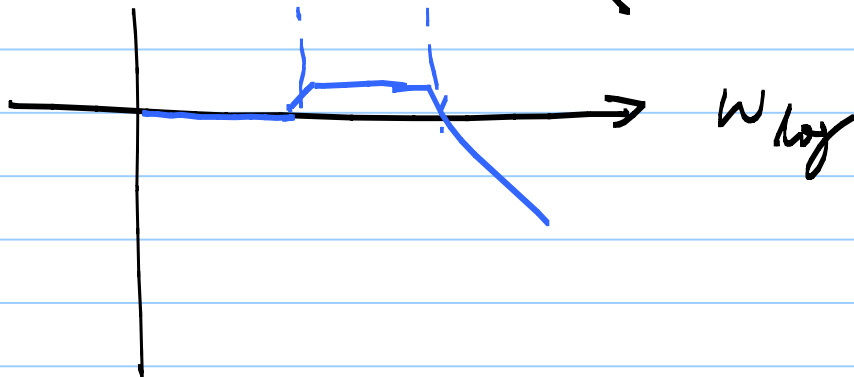
Lec 22



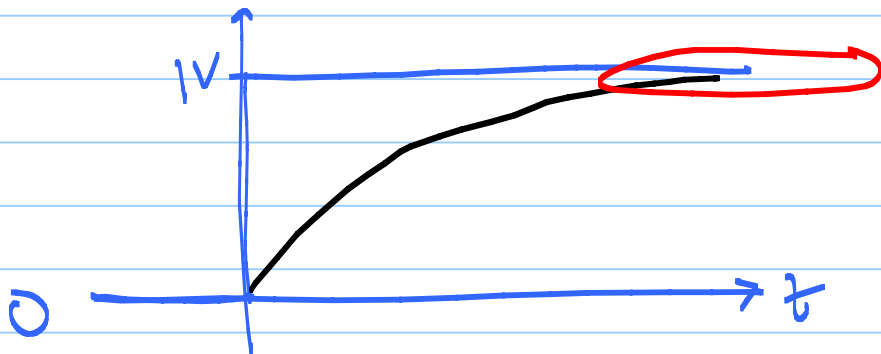
zero-pole doublet



$|CL_a|$



HW



$$\underset{\substack{| \\ \text{large}}}{()} (e^{-w_u t}) + \underset{\substack{\uparrow \\ \text{small}}}{()} e^{(-z_1 t)}$$

Example : $A_0 = 80 \text{ dB} = 10^4 \text{ V/V}$

$$A_1 = 156 \text{ V/V} \quad A_2 = 98 \text{ V/V}$$

$$g_{m2} = 0.5 \text{ mS}$$

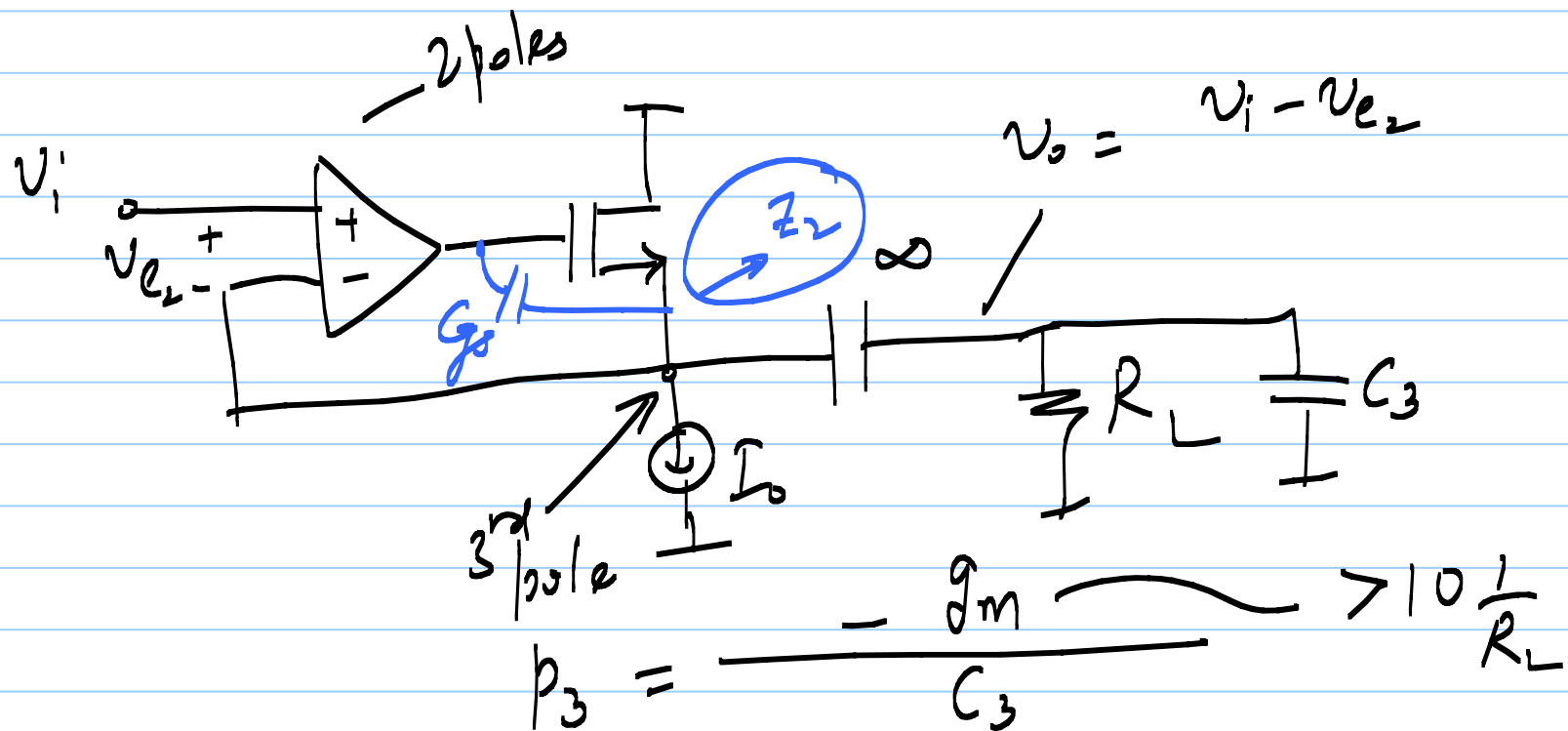
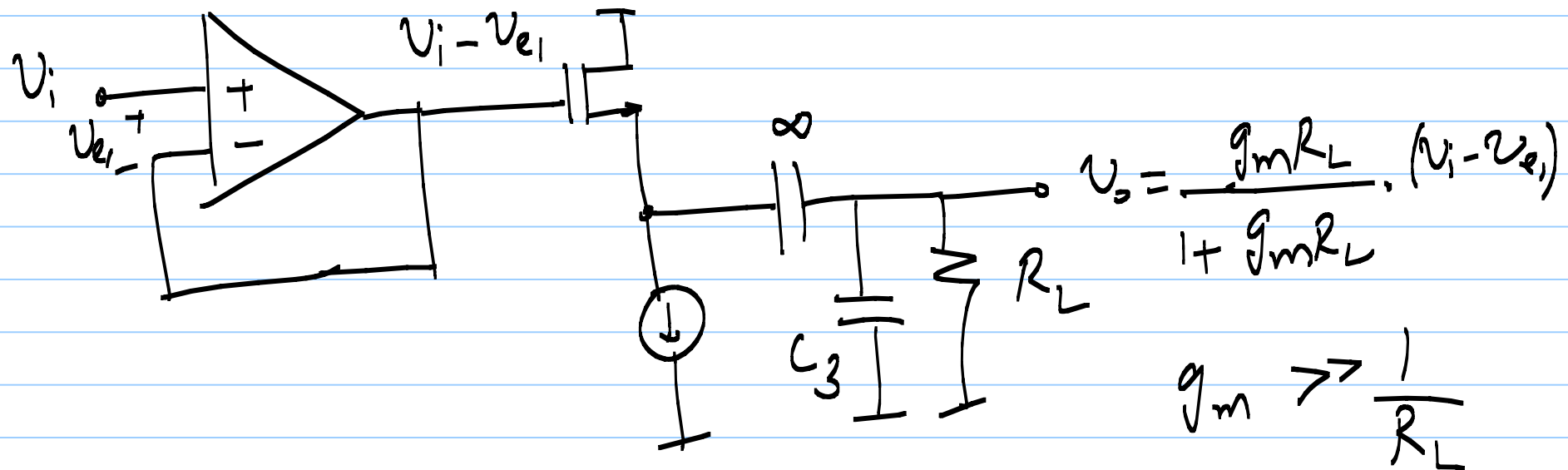
resistive load $R_L \downarrow$:

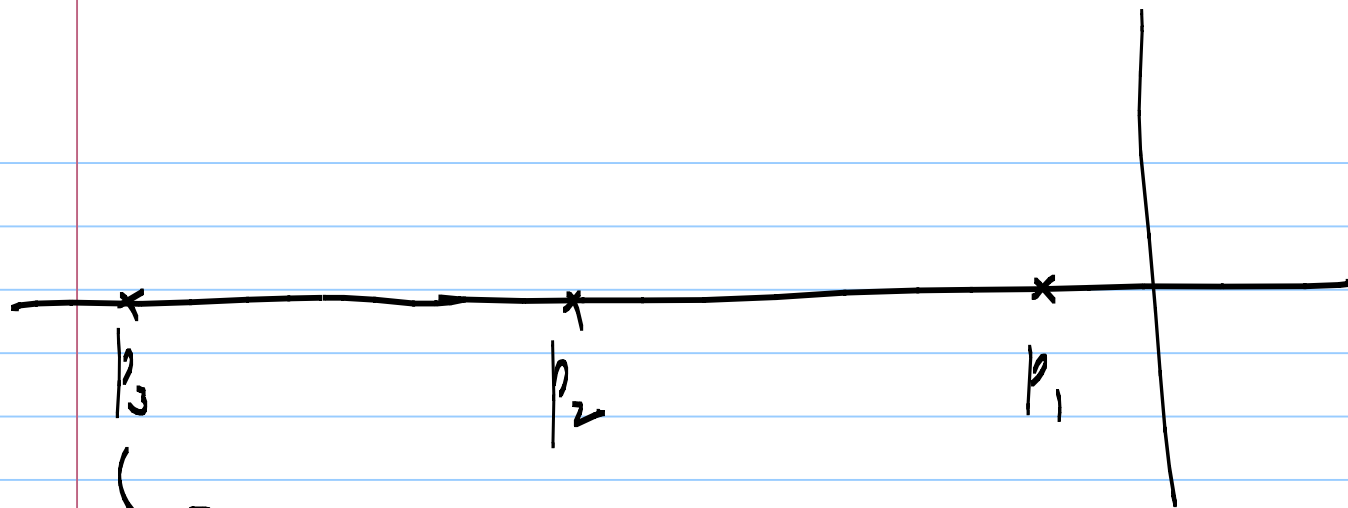
$$A_2 = g_{m5} (r_{out2} \parallel R_L) \approx g_{m5} R_L$$

e.g. if $R_L = 2 \text{ k}\Omega \Rightarrow A_2 = 1 \text{ V/V}$

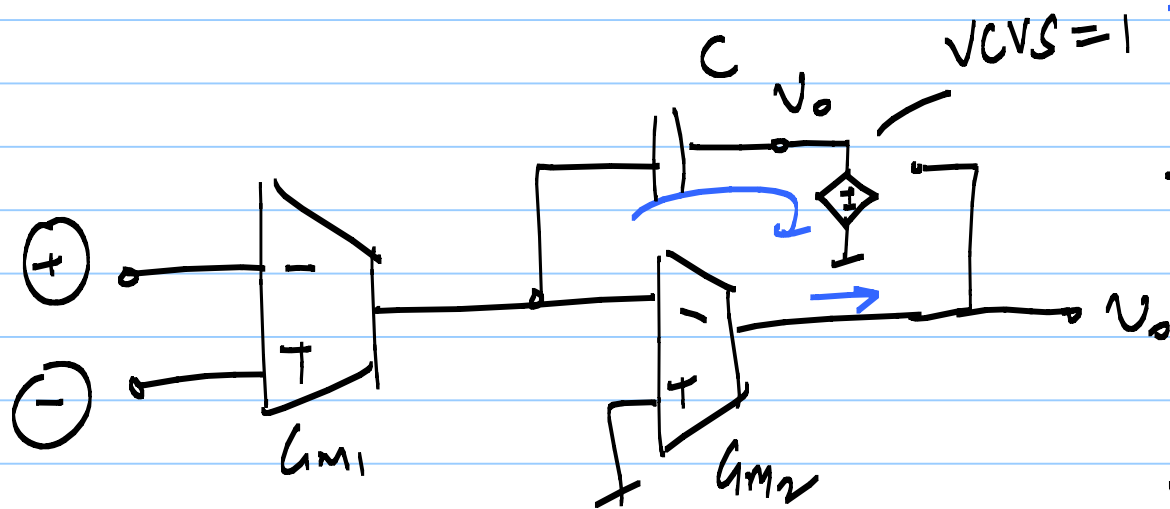
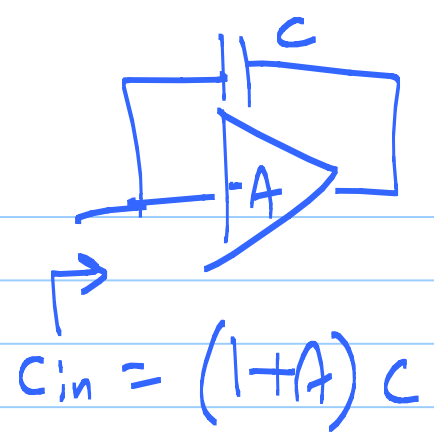
$$A_1 = 156 = A_0$$

We want to drive $R_L < 2 \text{ k}\Omega$





$\rightarrow \approx 100 \times p_2$

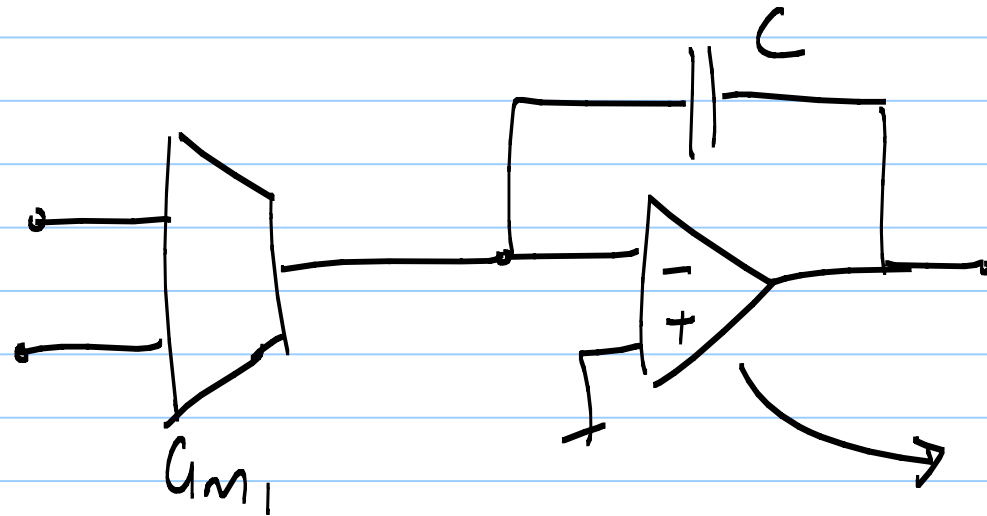
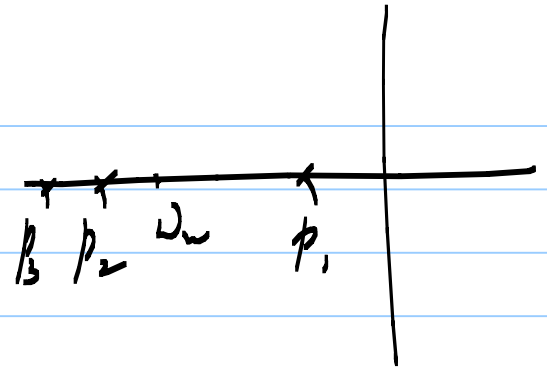
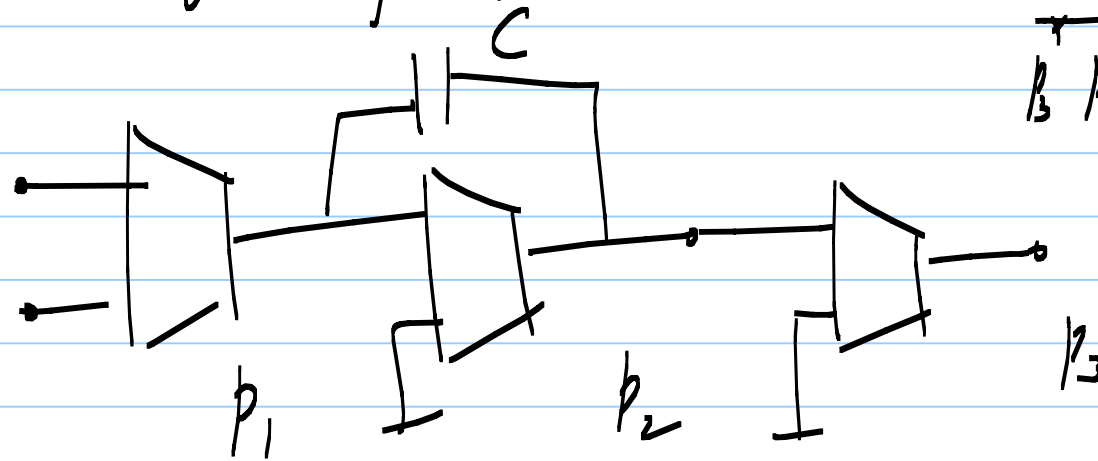


$\rightarrow$ Source follower

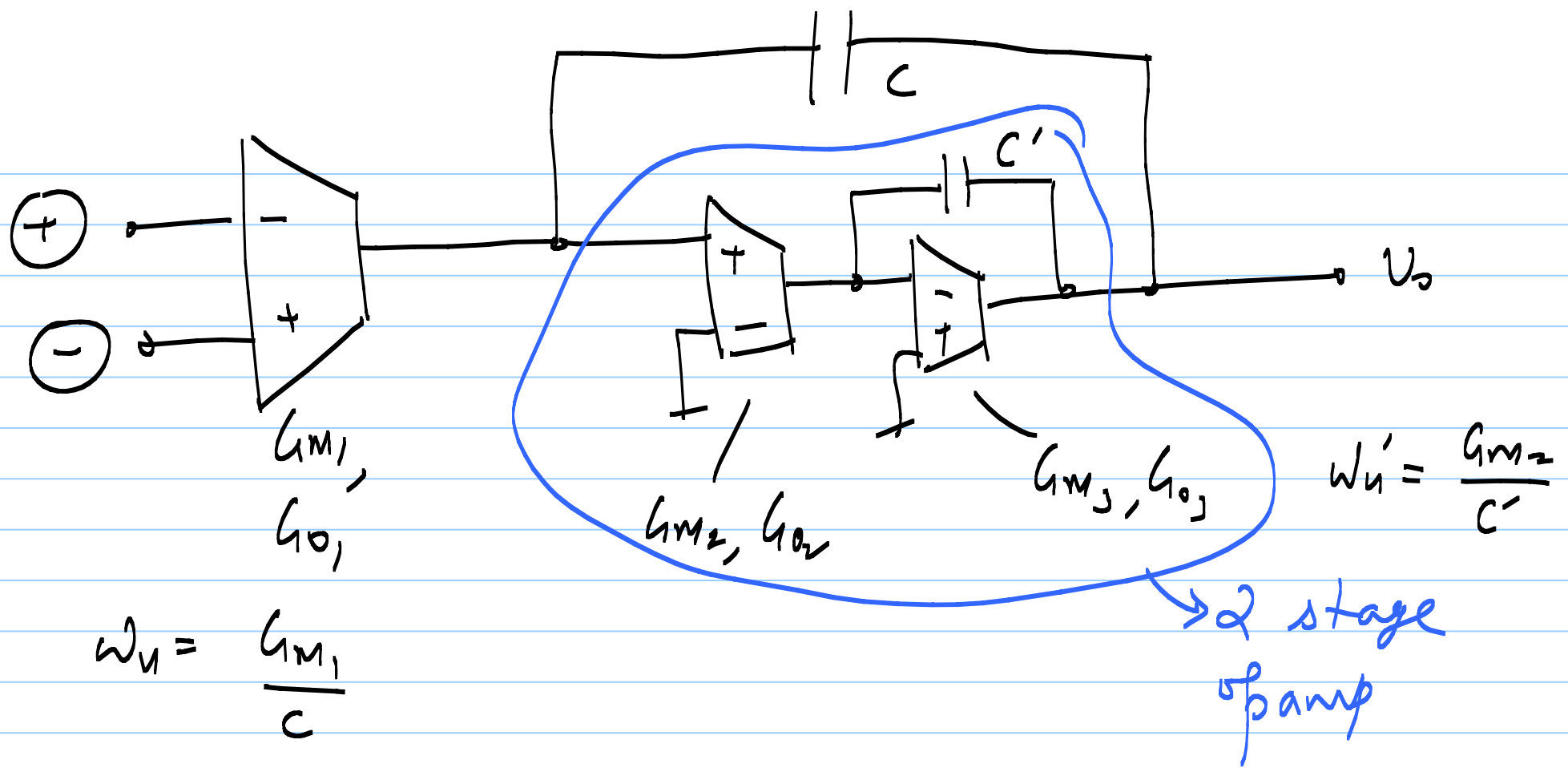
$\rightarrow p_1, p_2, \cancel{z_1}$

$\swarrow$ stays the same
 $\searrow$

3-stage amp



→ 2-stage amp



$$\omega_u = \frac{G_{m1}}{C}$$

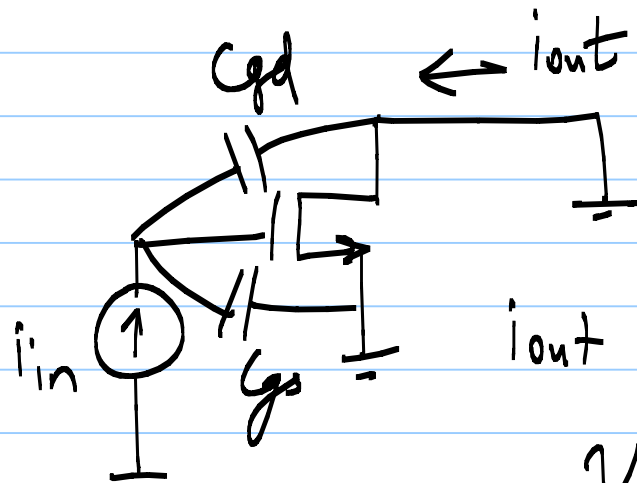
$$\omega_u' \gg \omega_u$$

"Nested Miller" Configuration

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Lec 23

plot



$$\left| \frac{i_{out}}{i_{in}} \right| \text{ vs. } f$$

$$i_{out} = g_m v_{gs}$$

$$v_{gs} = \frac{i_{in}}{s(C_{gs} + C_{gd})}$$

$$\frac{i_{out}}{i_{in}} = \frac{g_m}{s(C_{gs} + C_{gd})} \quad \left| \frac{i_{out}}{i_{in}} \right|$$



f_T = transition frequency

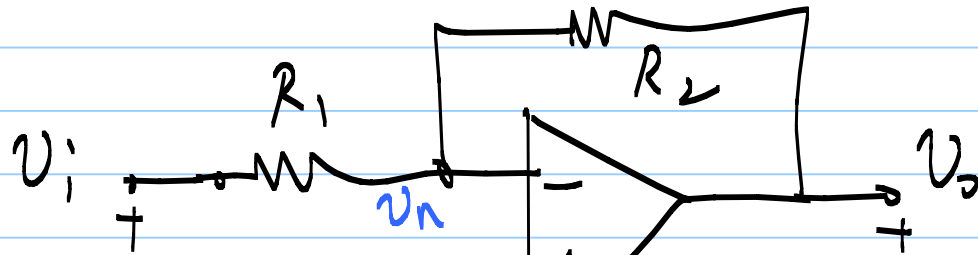
$$2\pi f_T = \frac{g_m}{C_{gs} + C_{gd}} \approx \frac{g_m}{C_{gs}} \propto \frac{\sqrt{I_{bias}}}{\sqrt{W} L^{3/2}}$$

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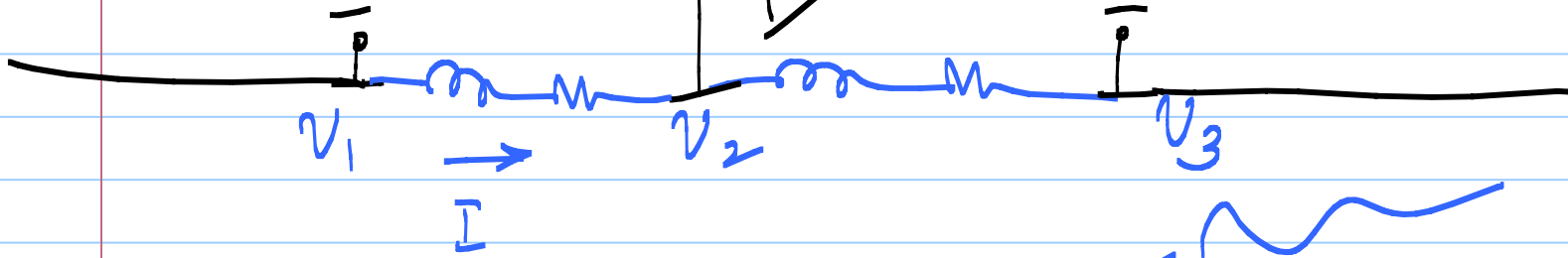
Lec 24

Fully Differential Opamps

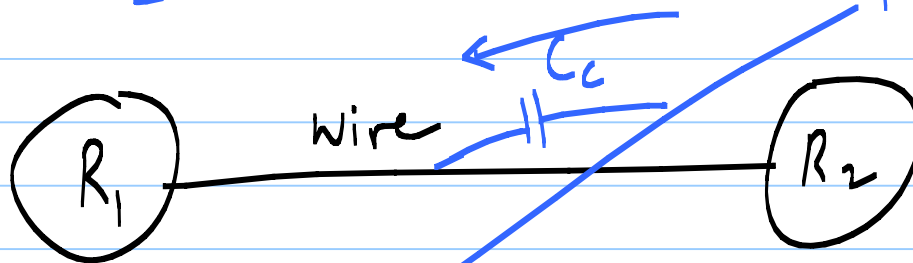
1)

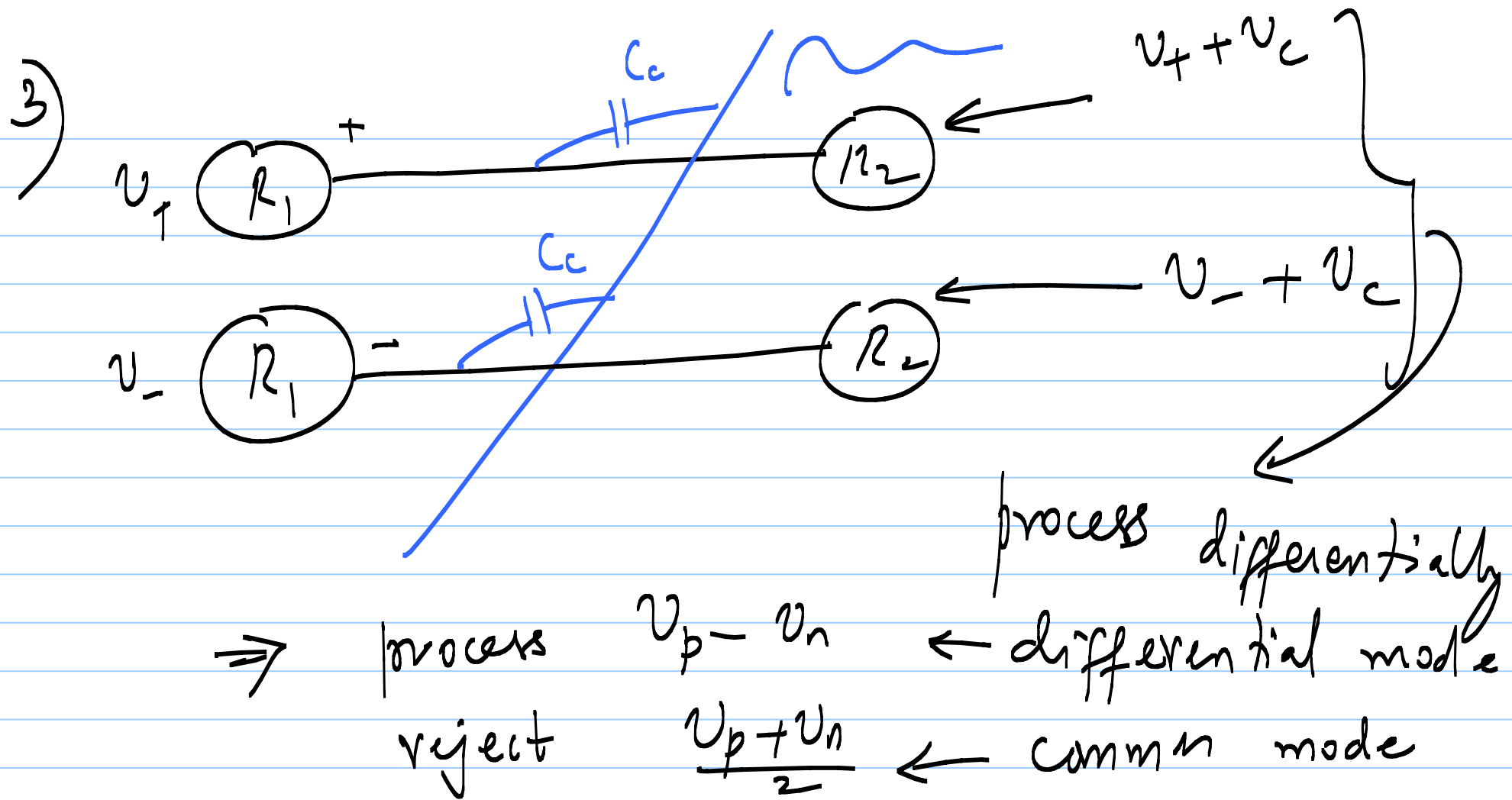


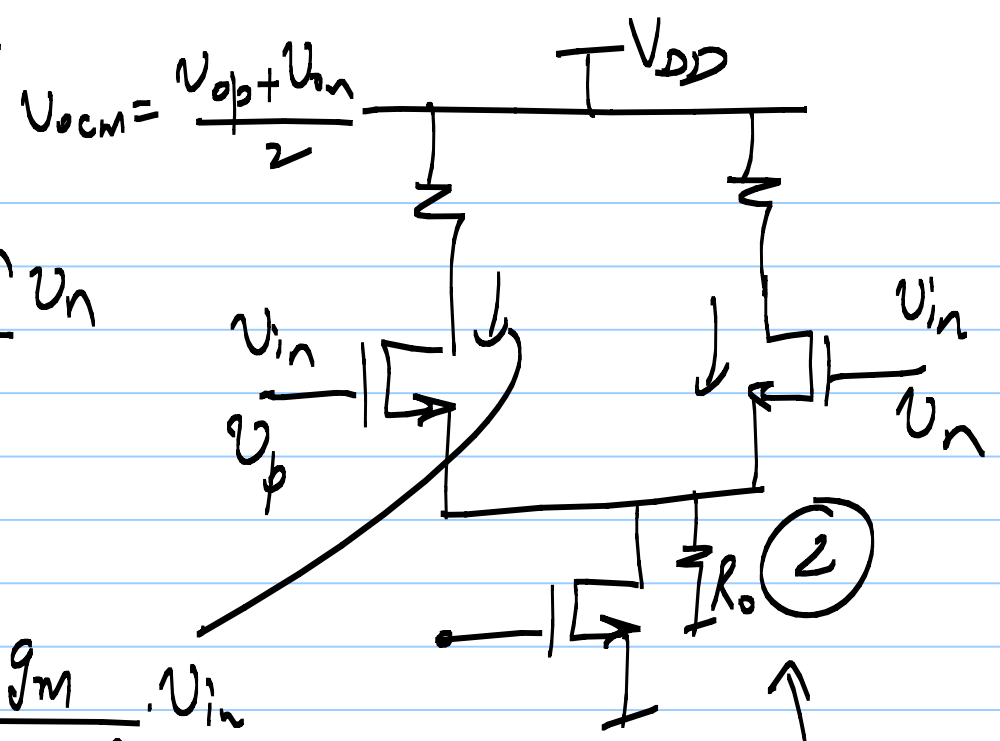
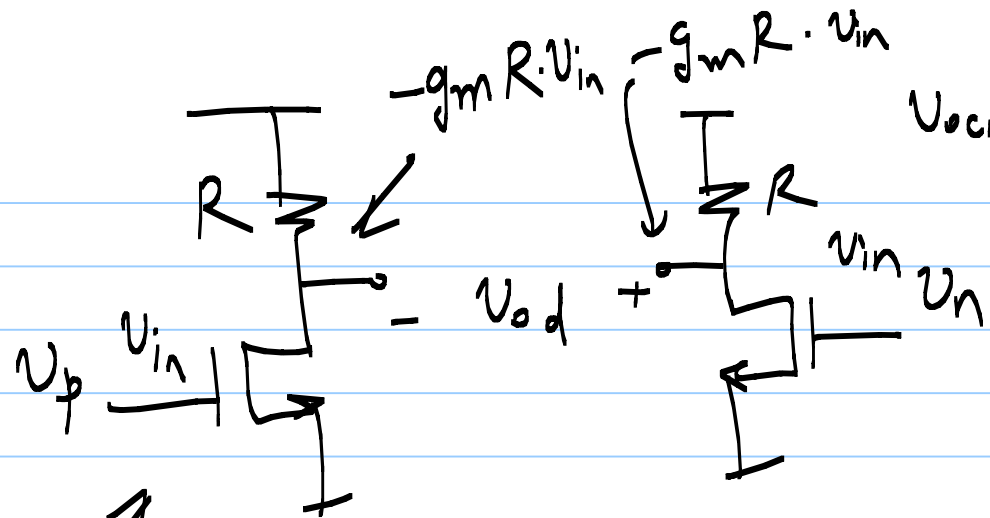
$$\frac{v_o}{v_i} = -\frac{R_2}{R_1}$$



2)





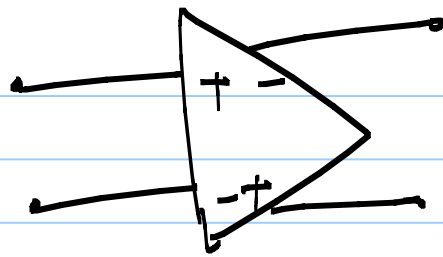


has
no
CMRR

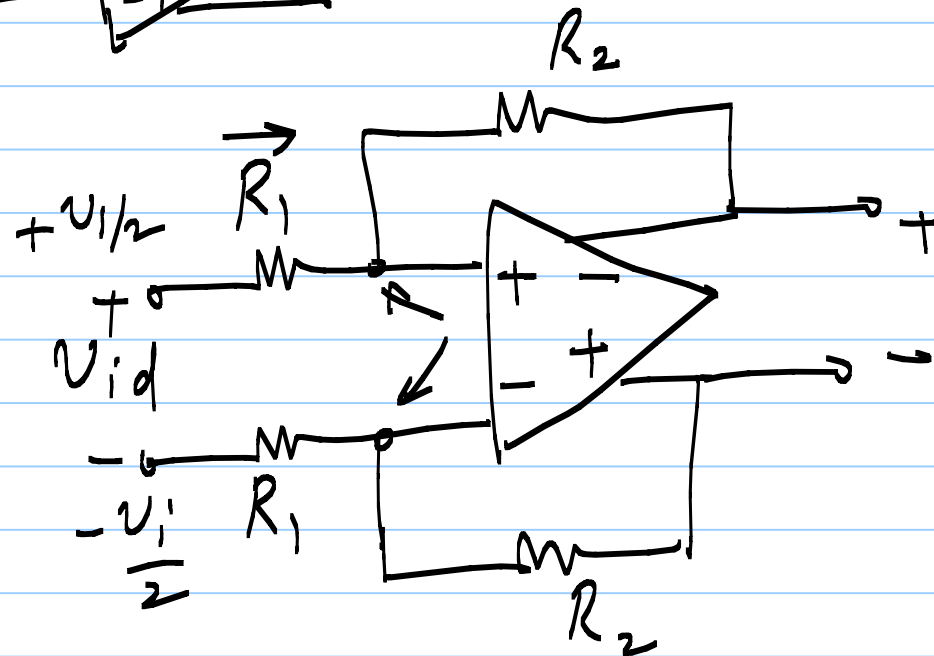
①
 $A_{dm1} = A_{dm2}$
 $A_{cm1} = A_{dm1}$
 "pseudo differential"
 amplifier

$$\frac{g_m}{1+2g_m R_o} \cdot v_{in}$$

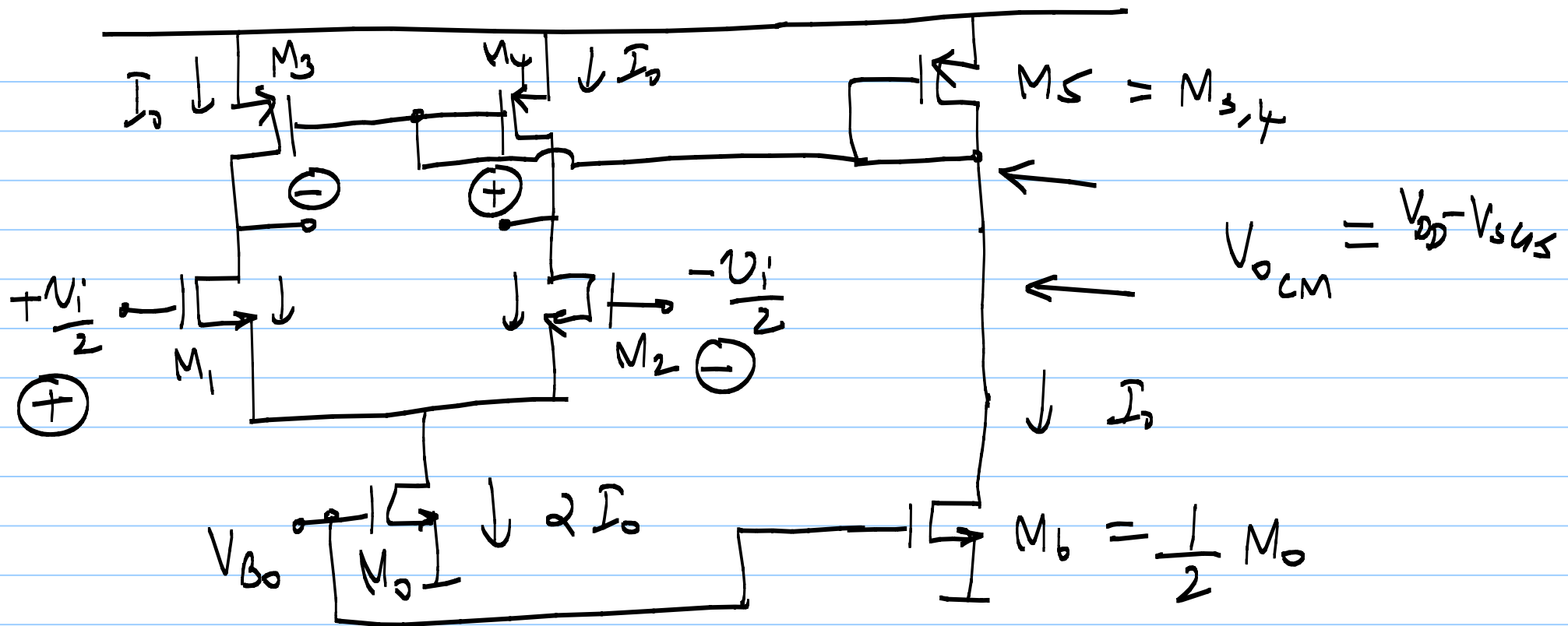
$A_{cm2} \approx 0$ has
 large CMRR
 "Differential"
 amplifier



← fully differential amp

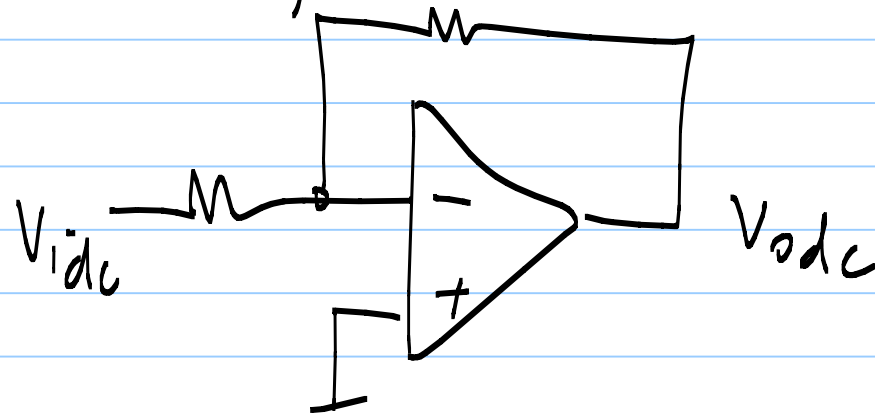


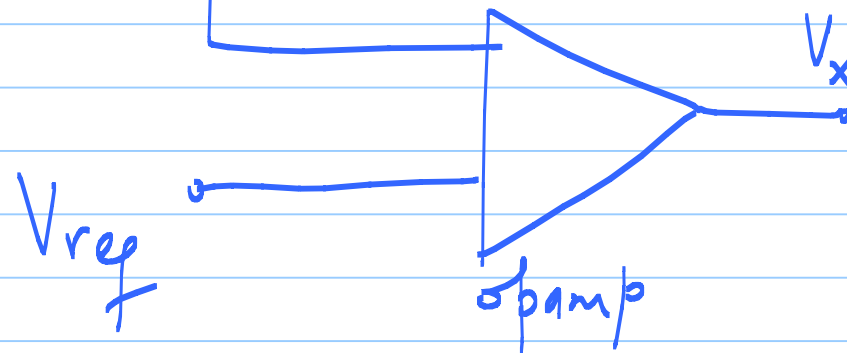
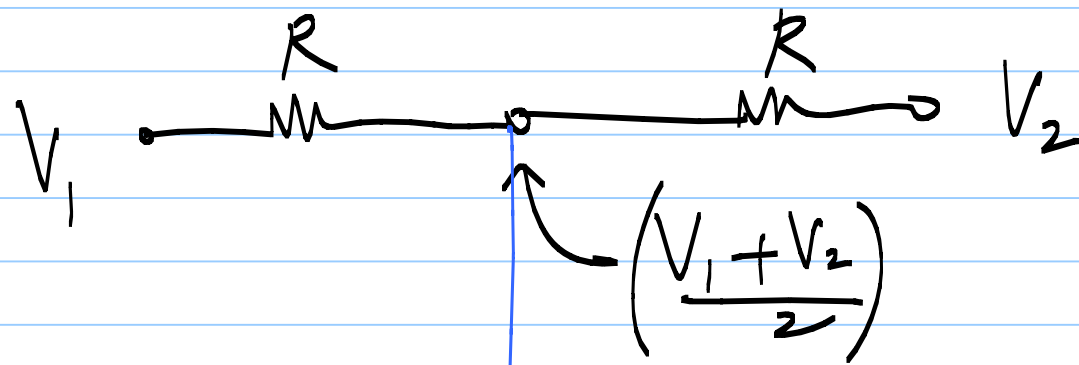
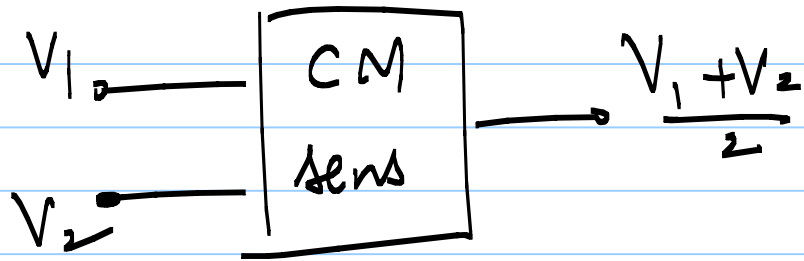
$$v_{od} = \left(-\frac{R_2}{R_1} \right) \cdot v_{id}$$



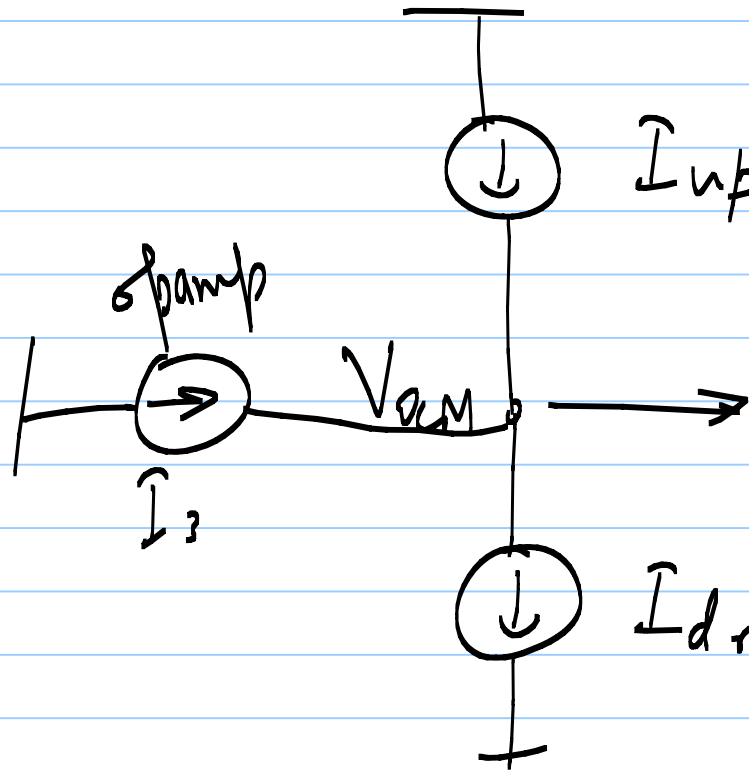
* Ill biased because output DC is not set properly

* Need common mode feedback (CMFB) to set output common mode properly





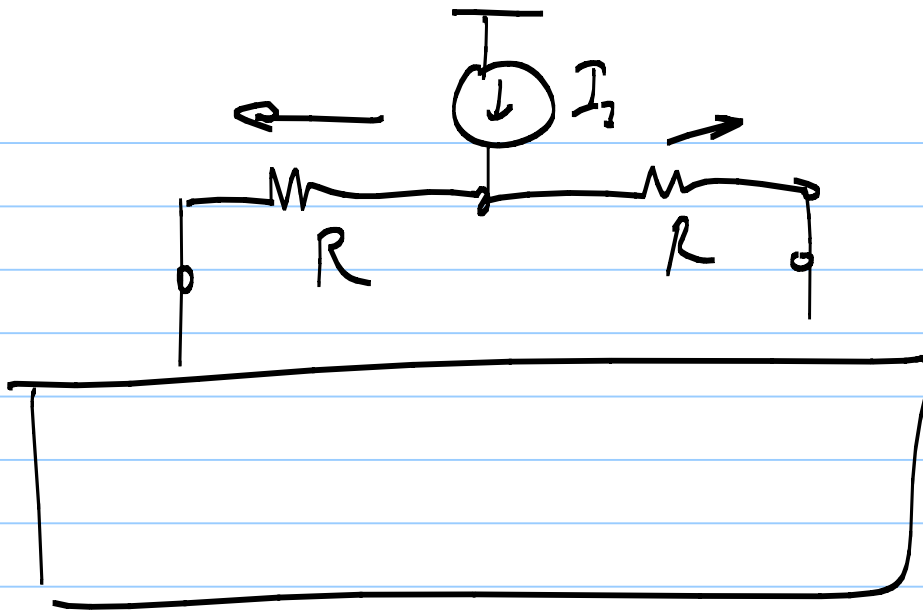
$V_x \leftarrow$ connect V_x
to a node in
the ckt that
changes V_{cm}

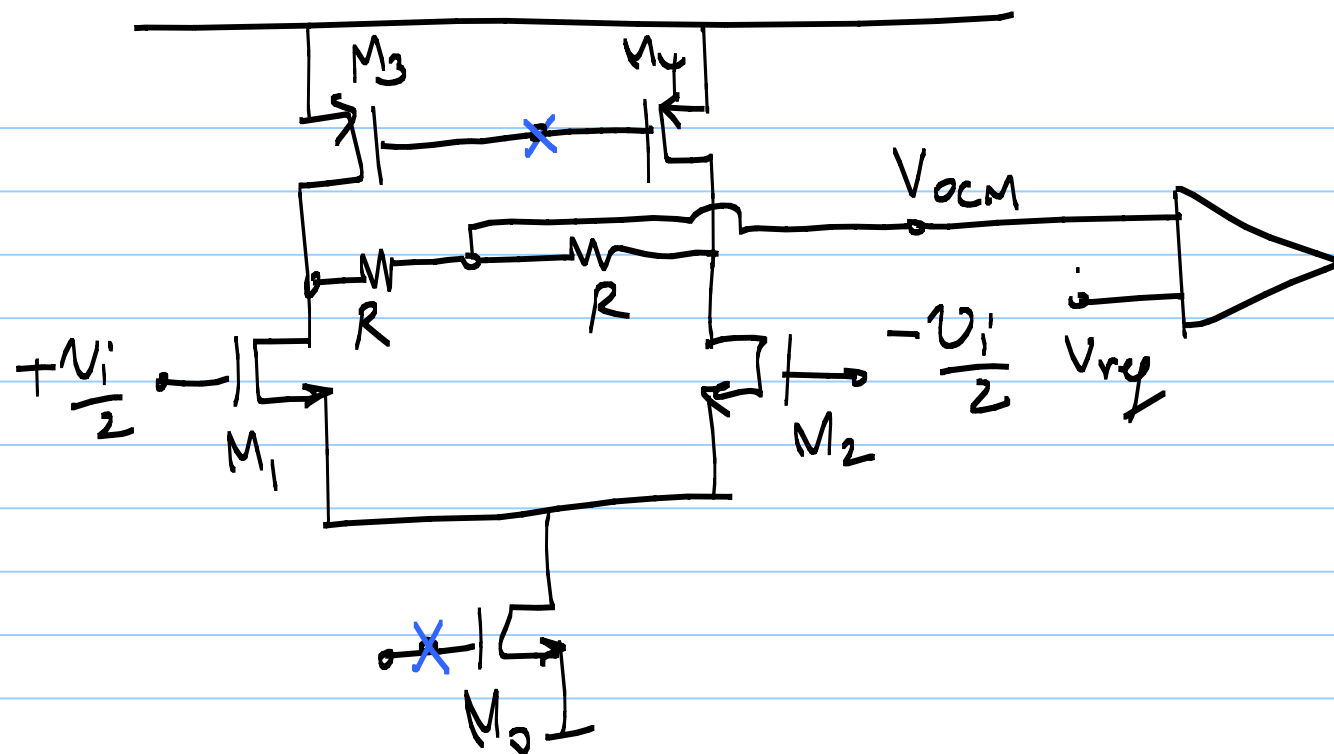


I_f $I_{up} > I_{dn}$, $V_{out} \uparrow$

$I_{up} < I_{dn}$, $V_{out} \downarrow$

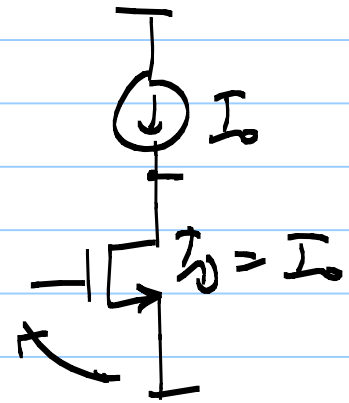
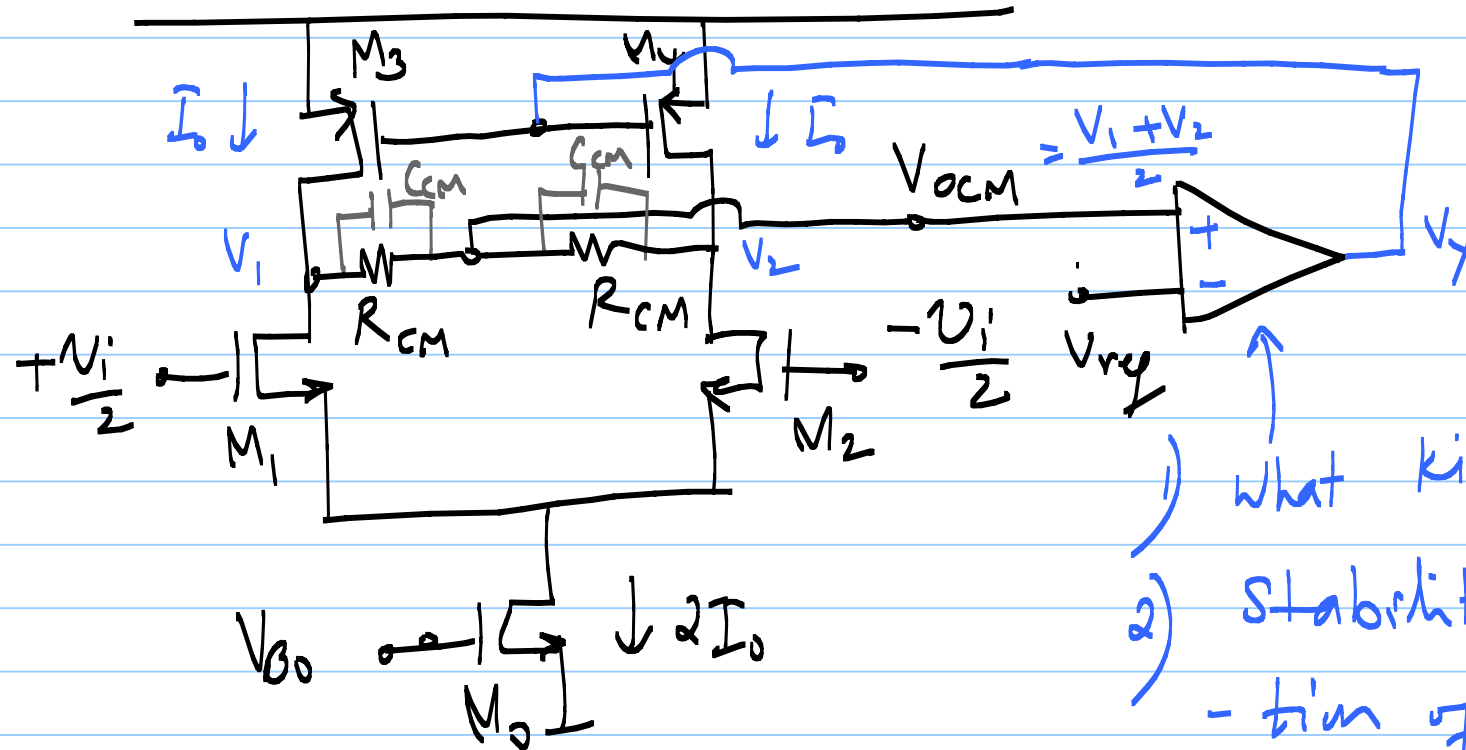
In steady state, $I_{up} = I_{dn}$



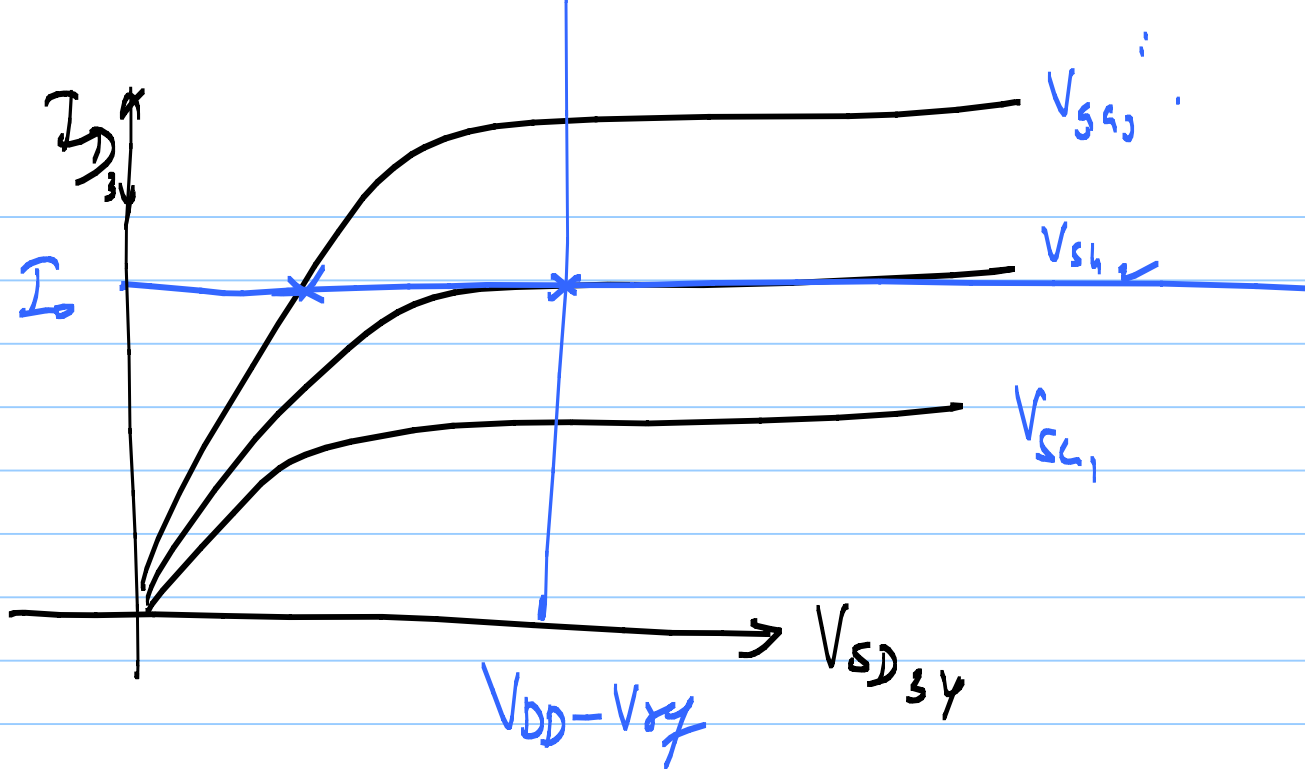


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Lec 25



- 1) What kind of opamp?
- 2) Stability & compensation of CMFB
- 3) Does CMFB affect diff. operation?
- 4) Use other types of CM sensors?



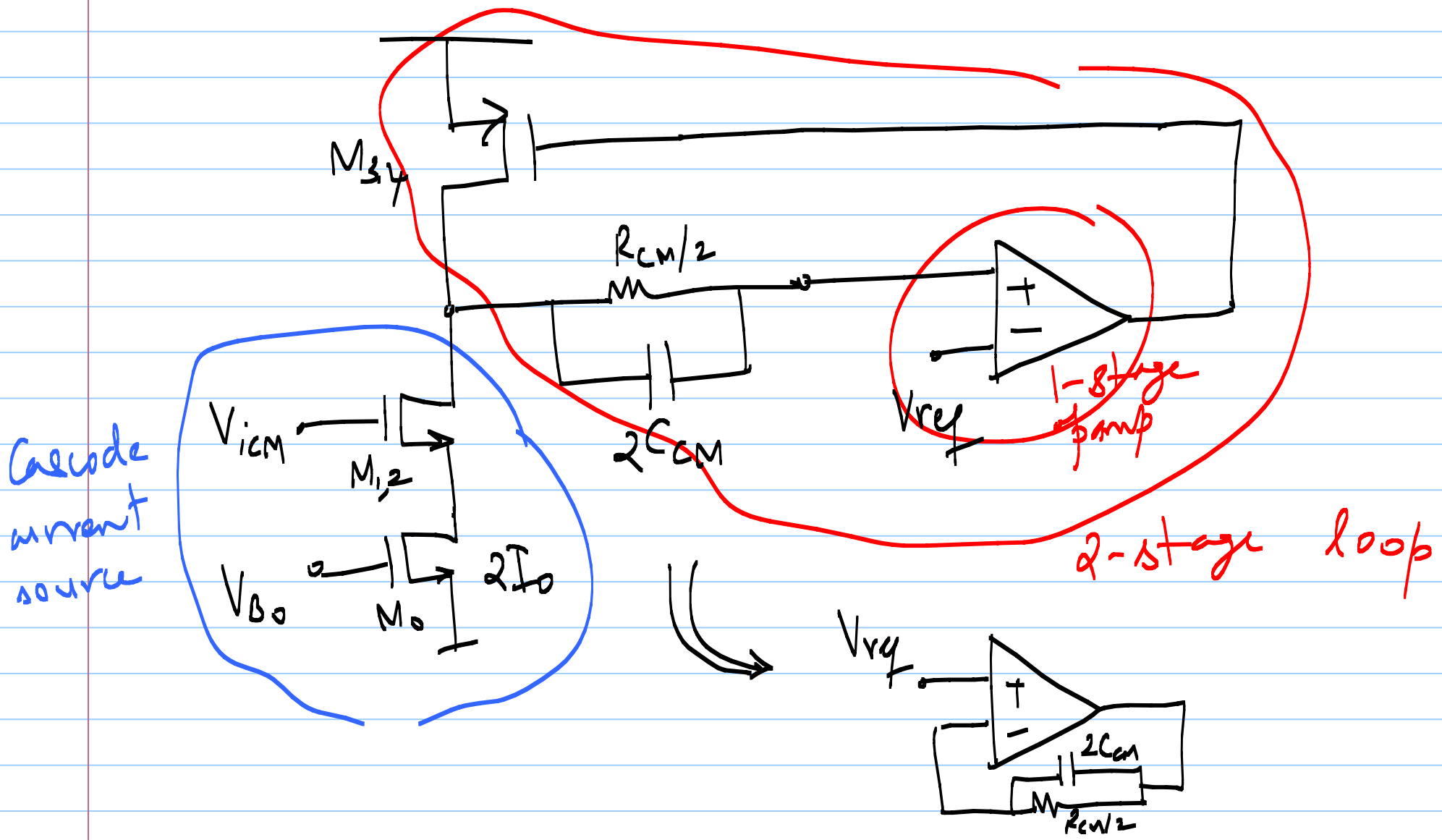
4) CM sensor:
 → passive (linear) — use this for 1-stage FD opamp.
 → active

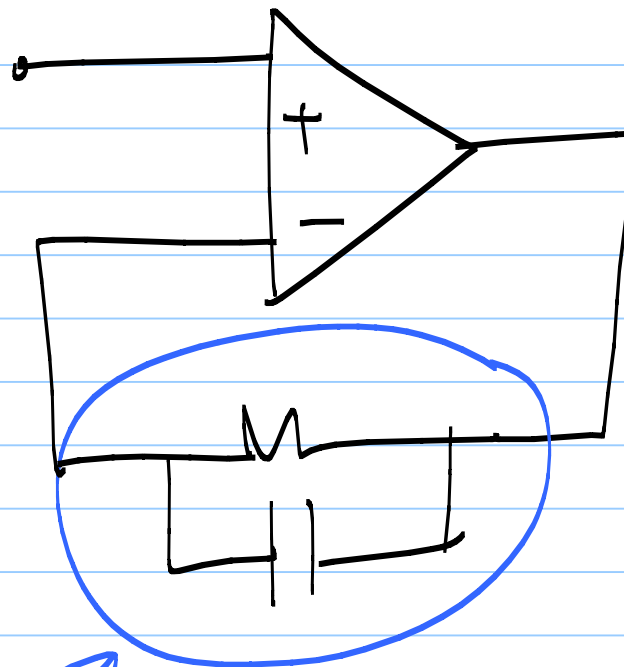
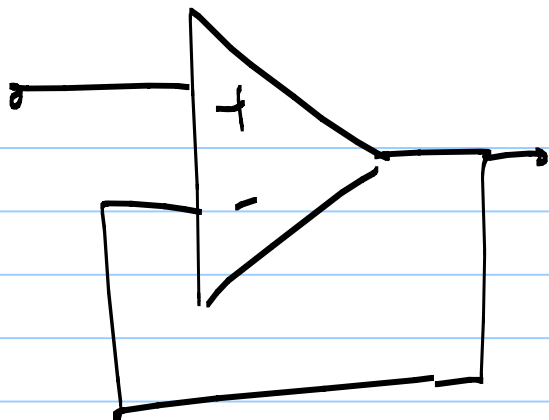
3) Diff'l. operation: $\frac{V_{od}}{V_{id}} = g_{m1} (r_{ds2} \parallel r_{ds4} \parallel R_{cm})$

$R_{CM} \Rightarrow r_{ds2}, r_{ds4}$

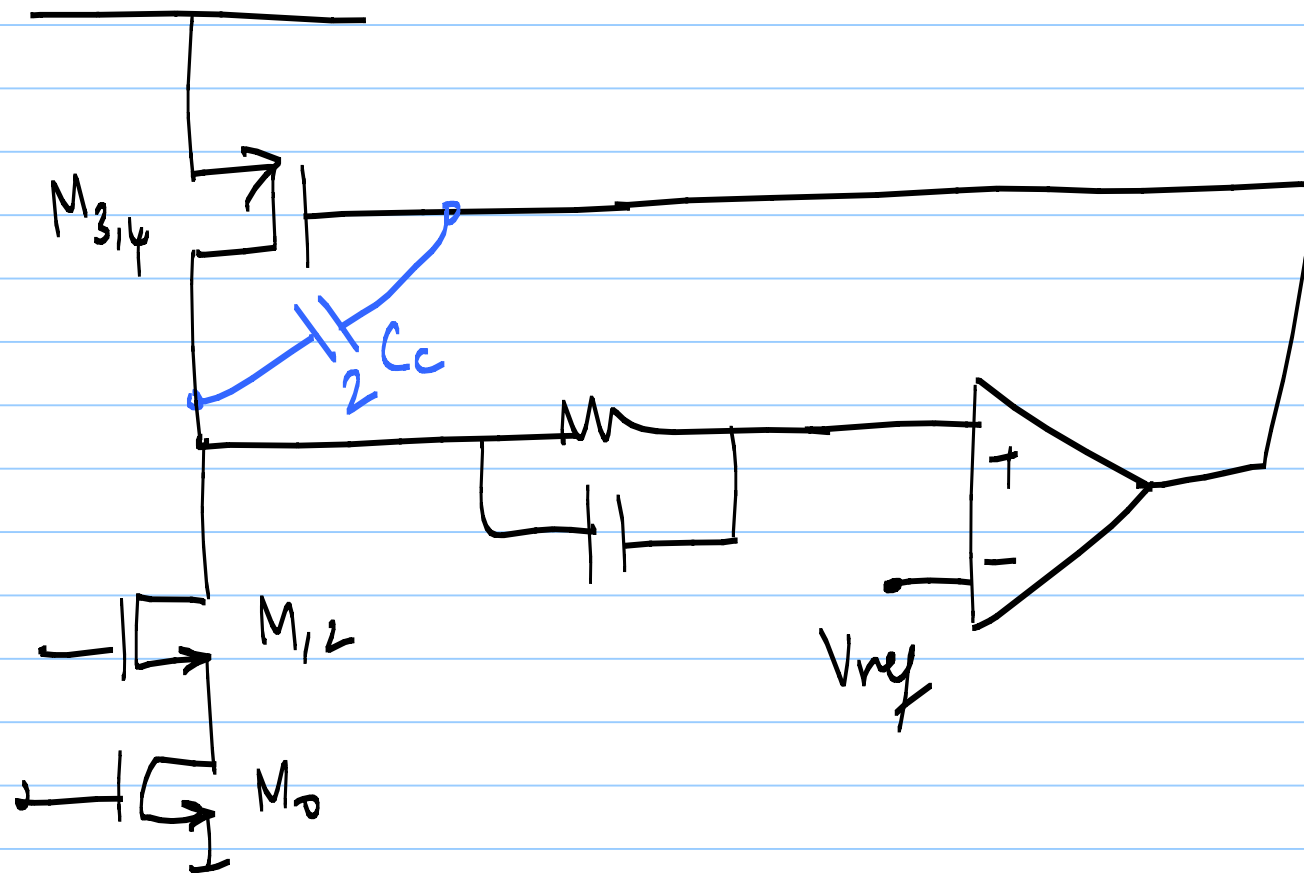
$\sim M \Omega$
 comes with parasitic cap C_{cm}

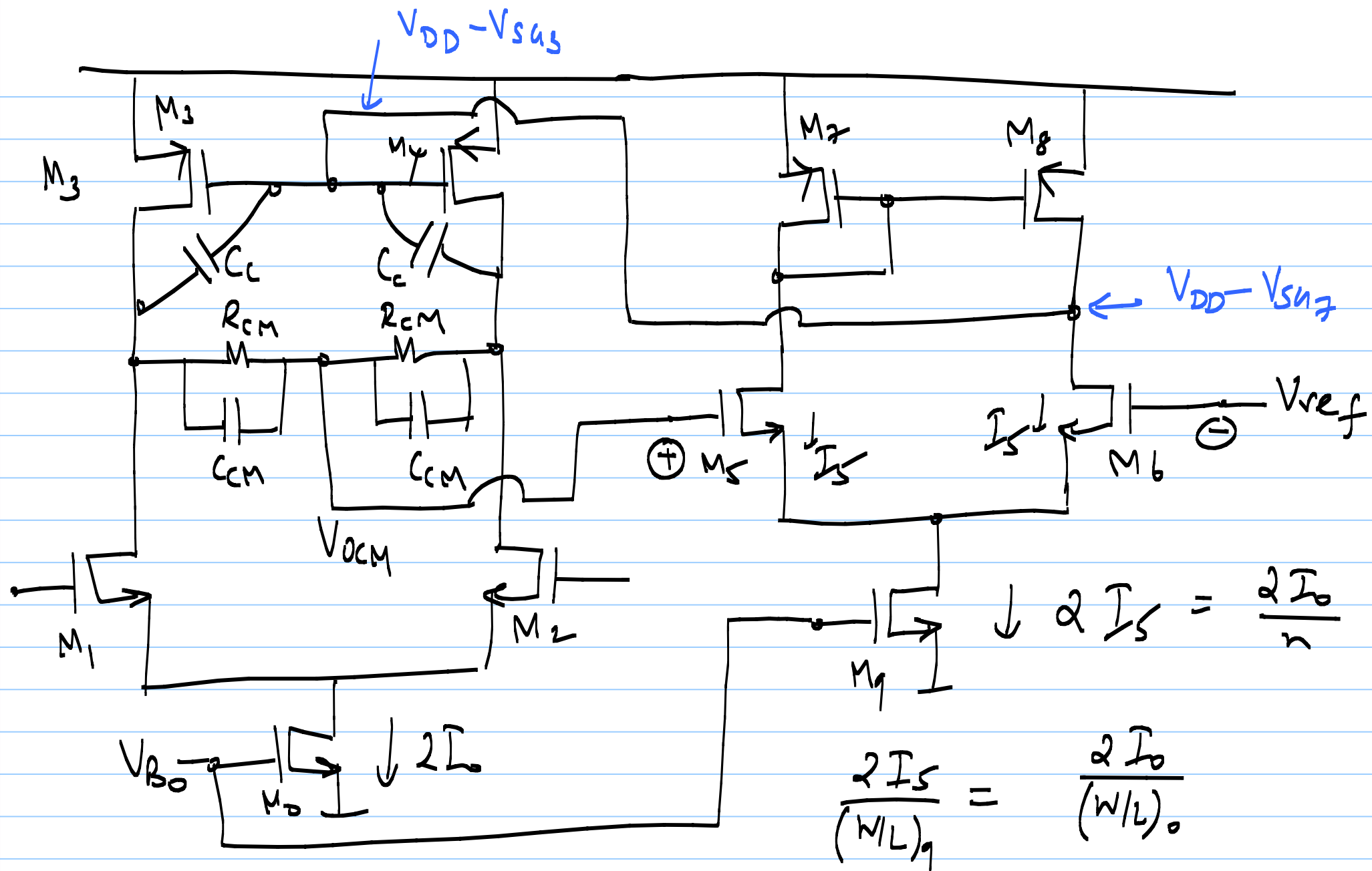
- 1) choose 1-stage opamp for simplicity
- 2) stability





add/subtract $\rightarrow$ phase shift } changes PM
 }



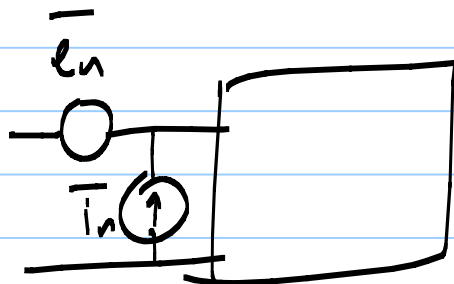


$$\underline{\text{Set}} \quad V_{DD} - V_{S_{u3}} \Big|_{I_0} = V_{DD} - V_{S_{u7}} \Big|_{I_5}$$

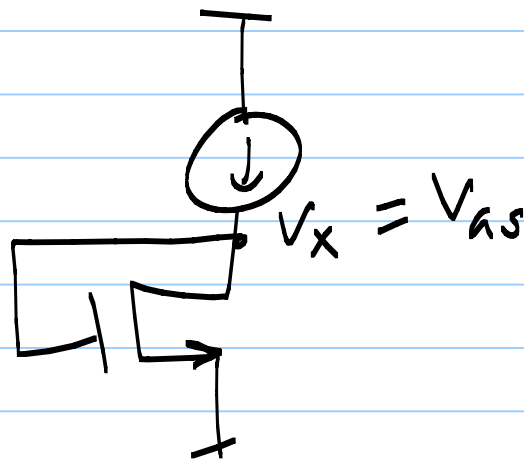
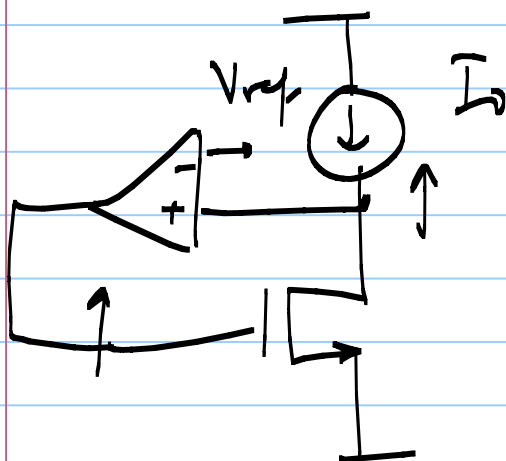
$$V_{OCM} = V_{r4} \quad \text{in absence of mismatch}$$

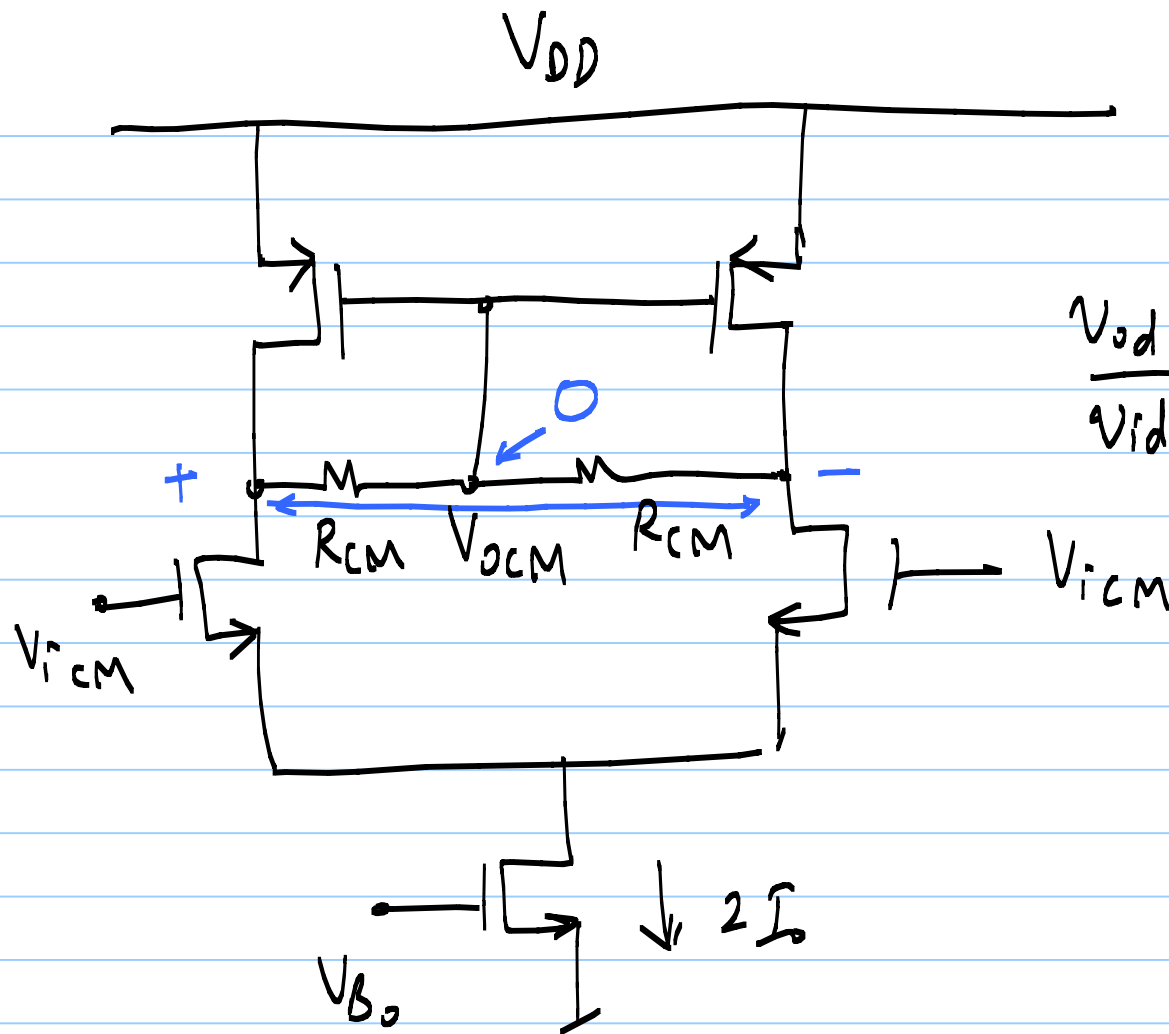
2/3/20

Lec 26



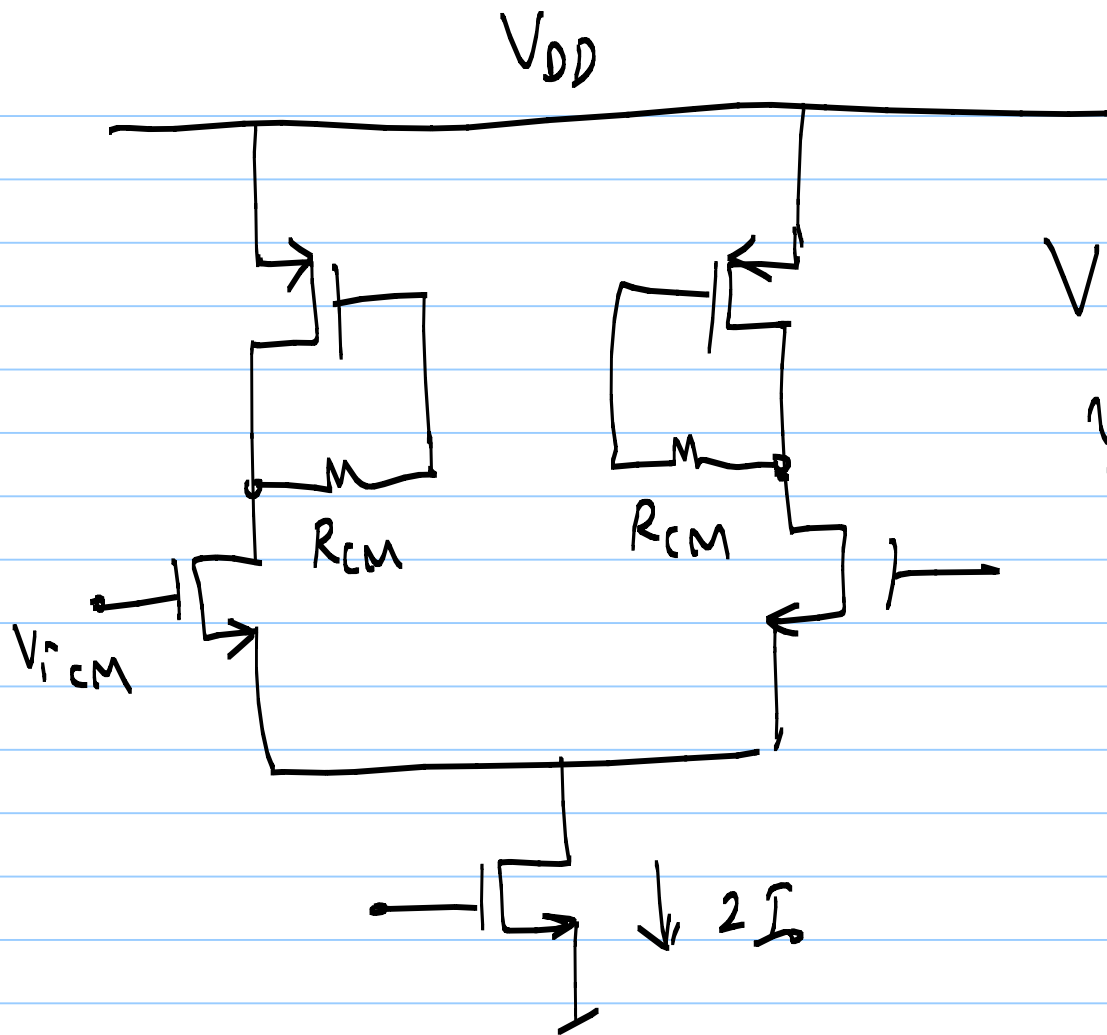
- Ans 3
- 1) V_{ov} - cannot be kept constant
 - 2) Input steping.





$$V_{ocm} = V_{DD} - V_{S4,54}$$

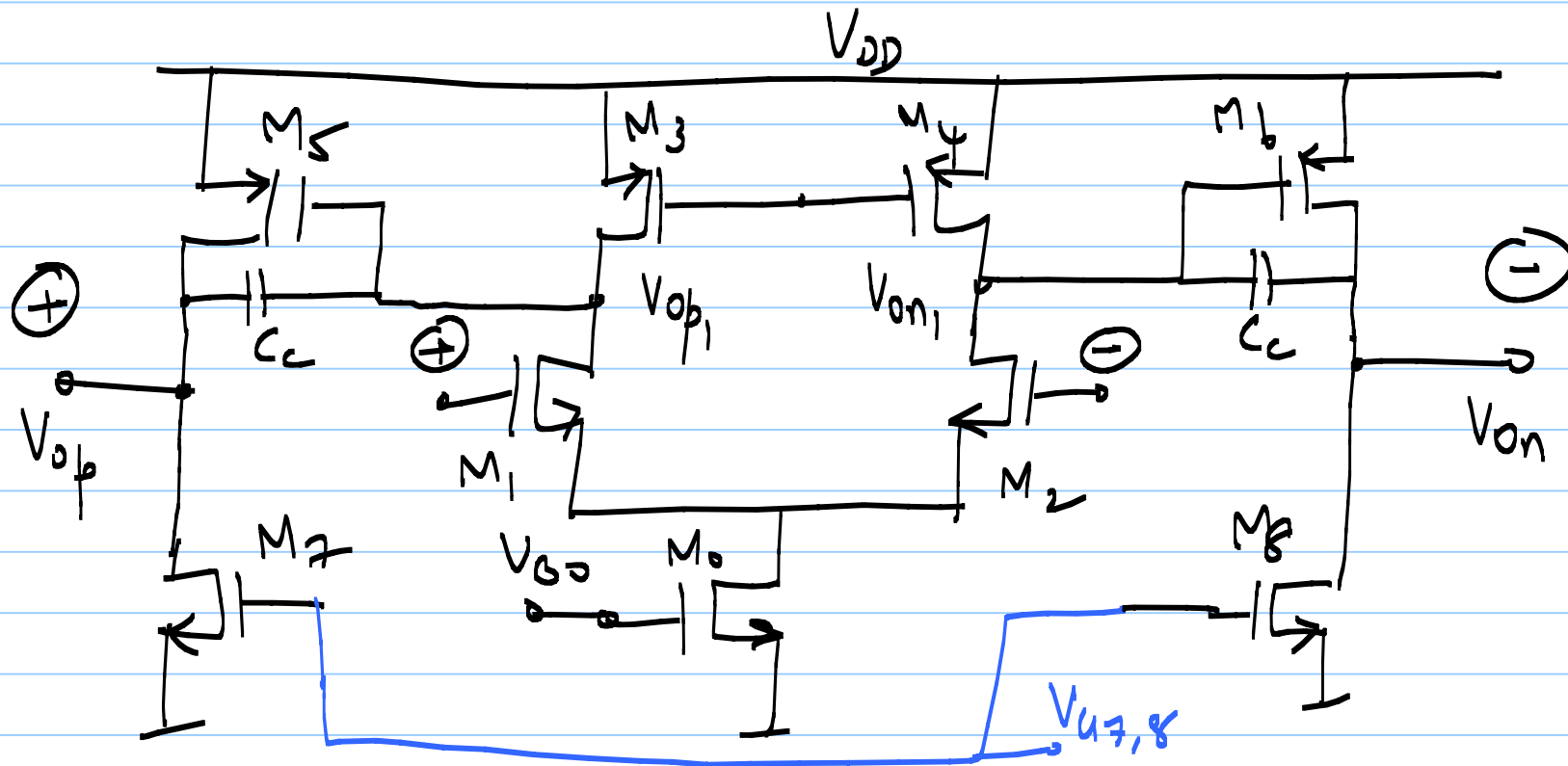
$$\frac{v_{od}}{v_{id}} = g_{m1} (r_{ds2} \parallel r_{ds4} \parallel R_{cm})$$



$$V_{OCM} = V_{DD} - V_{SA34}$$

$$\frac{V_{od}}{V_{id}} \approx \frac{g_{m1}}{g_{m3} + g_{ds2} + g_{ds4}}$$

Two-stage fully differential opamp



need to set $V_{CM1} = \frac{V_{op1} + V_{on1}}{2}$

and $V_{CM} = \frac{V_{op} + V_{on}}{2}$

* $M_5 - M_6$ stage is a pseudo-differential amplifier — has CM gain

* changing $V_{a3,4} \rightarrow$ change $V_{ocm1} \rightarrow$ change V_{ocm}

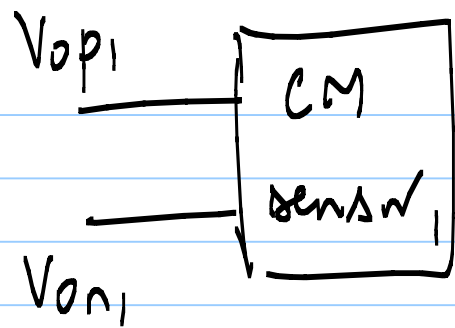
1) Sense V_{ocm} — feedback to $V_{a3,4}$

→ sets both V_{ocm1} & V_{ocm} with a single CMFB

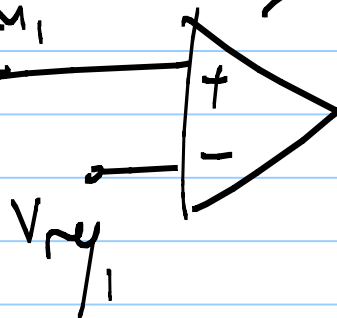
→ may end up with a 3-stage loop

→ stabilizing may be tricky.

2) Have 2 CMFB, one around each stage



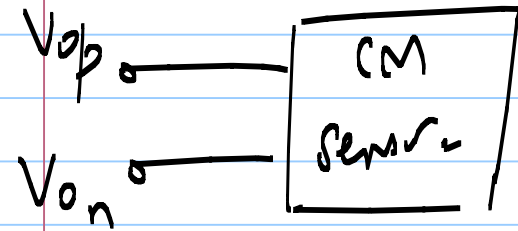
V_{ocm1}



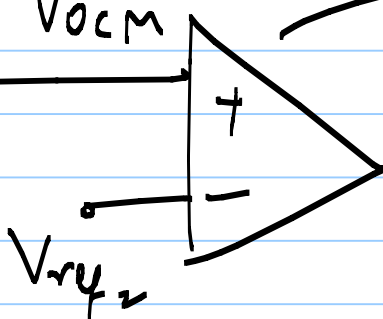
→ one stage opamp

$V_{a3,4}$

- 1) nmos input pair
- 2) pmos CM load
- 3) same current density in pmos as $M_{5,6}$



V_{ocm}



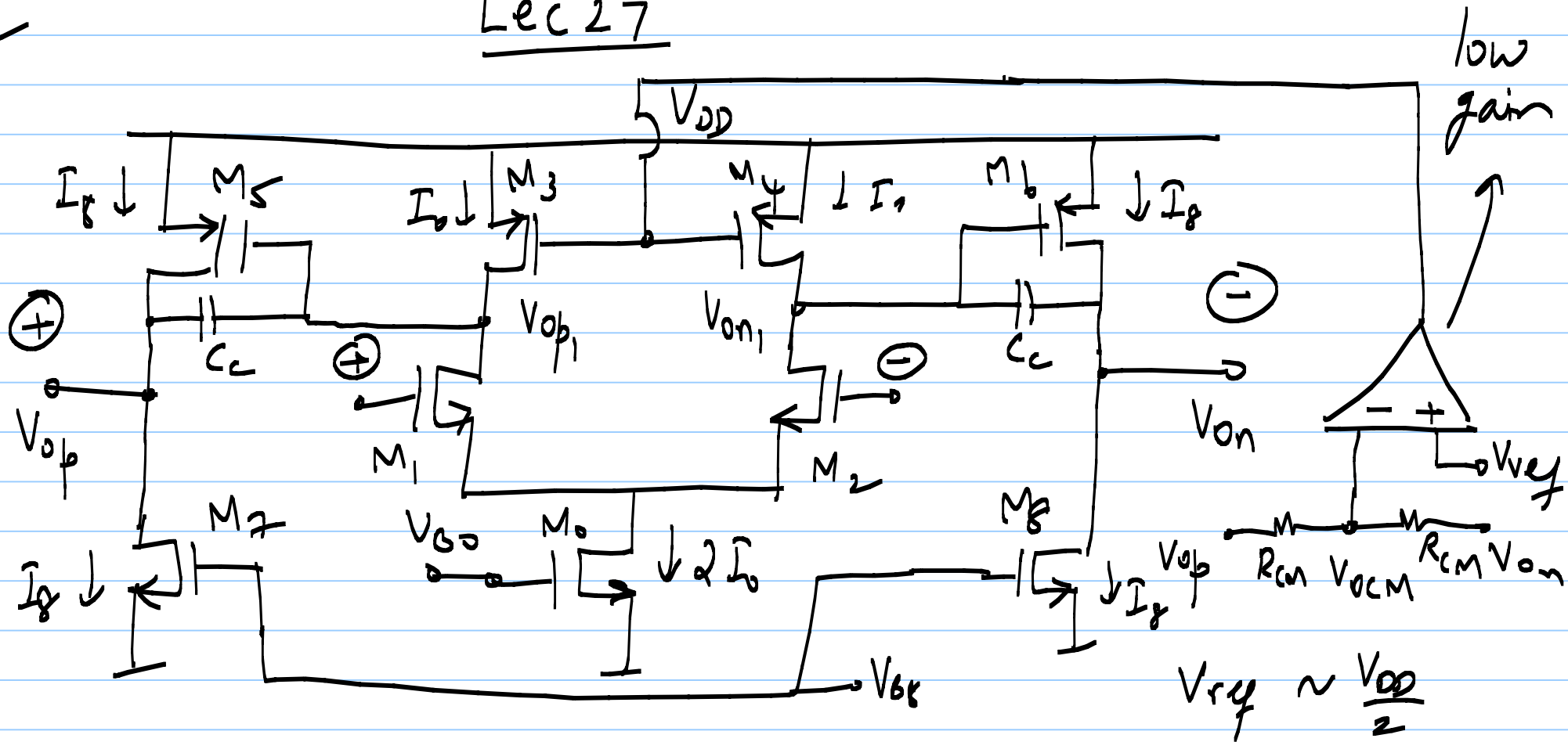
→ 1-stage opamp

$V_{a7,8}$

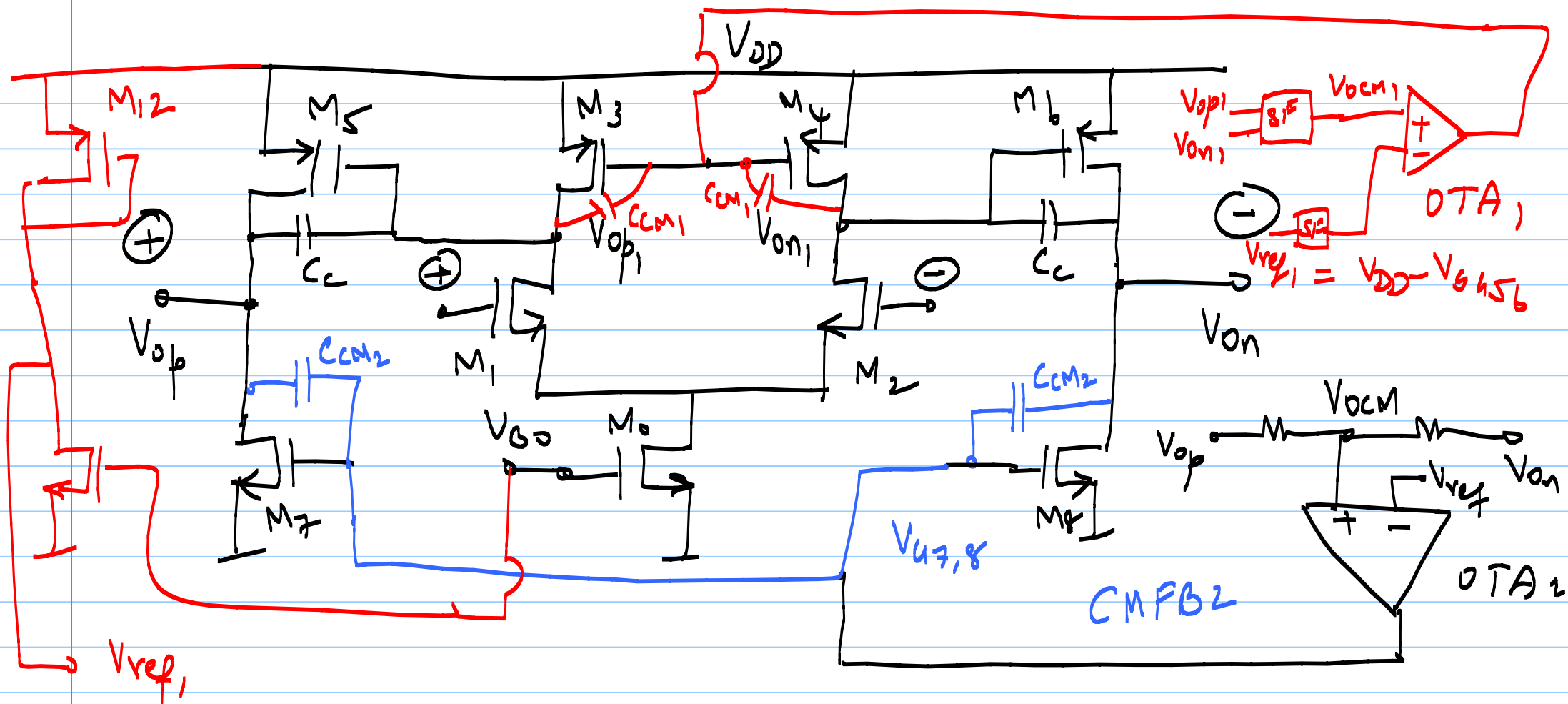
- 1) pmos input pair
- 2) nmos CM load
- 3) same current density in nmos CM as $M_{7,8}$

3/3/20

Lec 27



C_c - can compensate for CMFB also
(in certain cases)

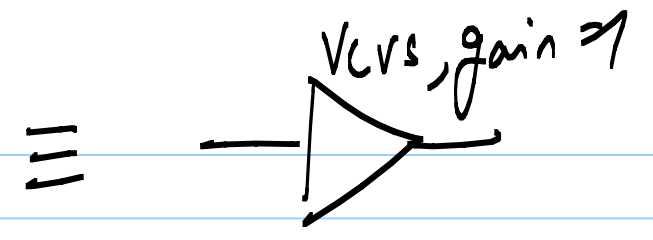
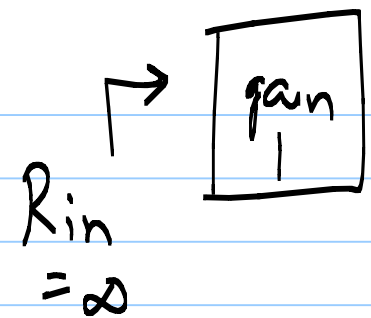


OTA 2 - pmos input pair + nmos CM load

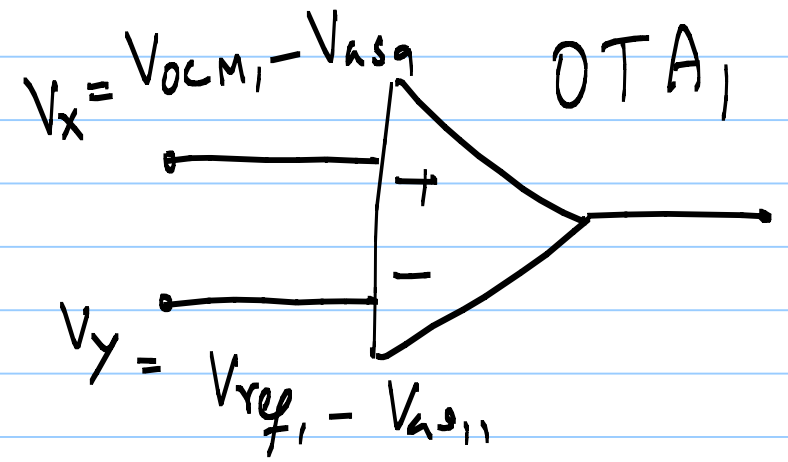
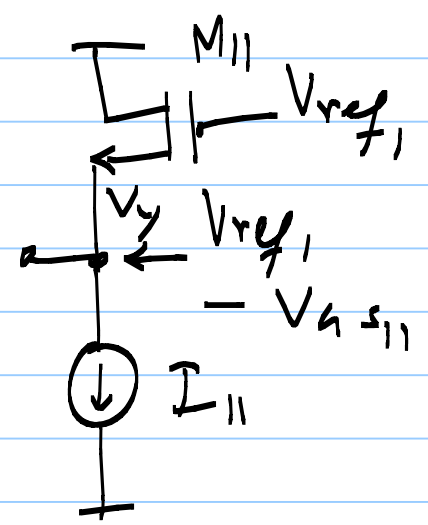
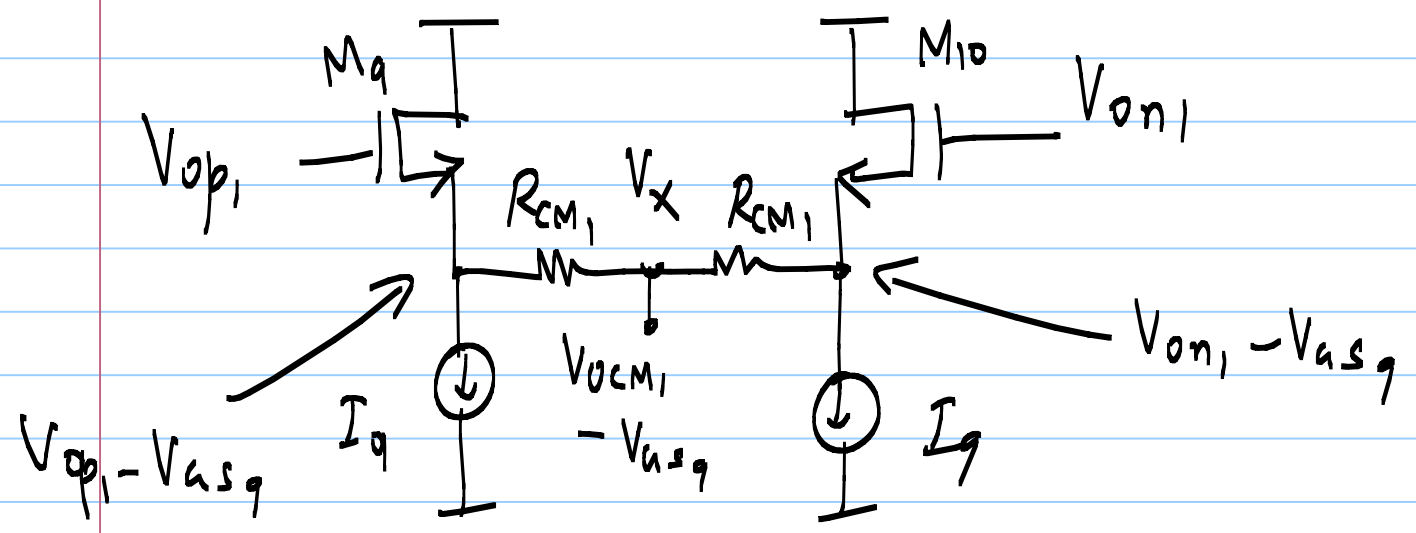
same current density
as M_7-8

$M_{1,2}$ & M_5-M_6 need to have same current density

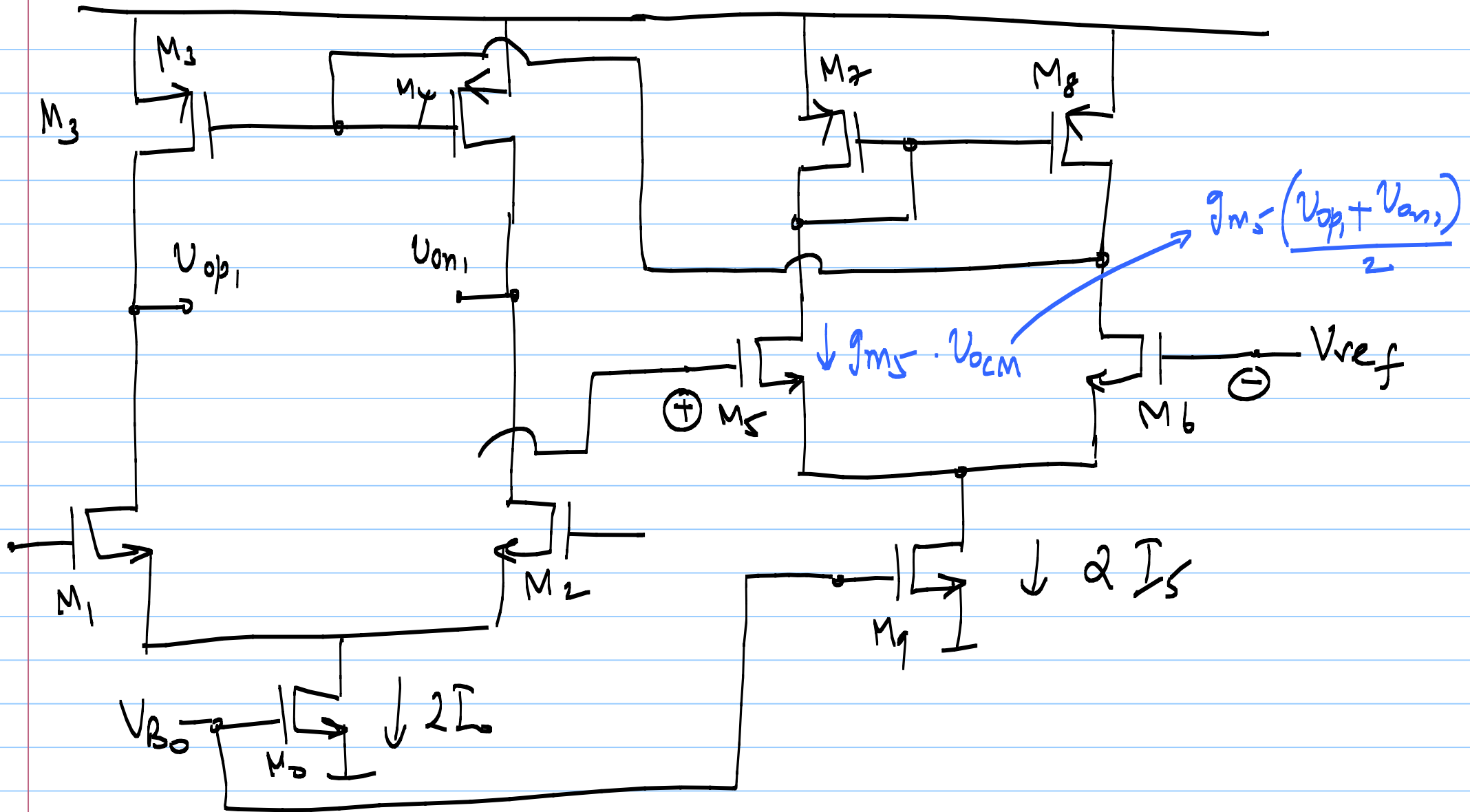
$$V_{OCM1} = \frac{V_{op1} + V_{on1}}{2}$$



$M_9, M_{10}, M_1 \rightarrow$ same current densities

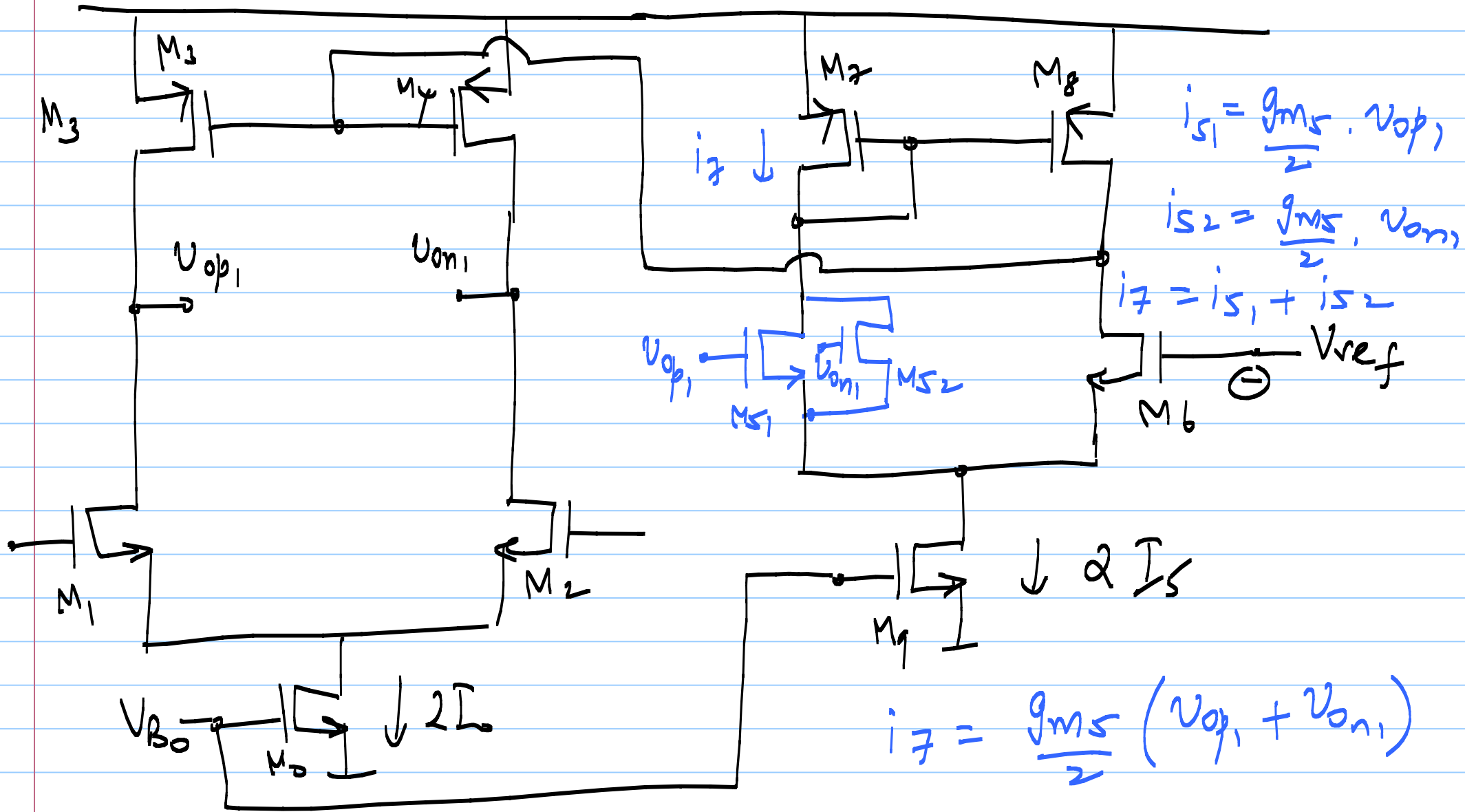


$\rightarrow$ nmos input pair + pmos CM load (same I density as $M_{3,4}$)



$$M_{S1} = M_{S2} = \frac{M_5}{2}$$

$$g_{m_{S1}} = g_{m_{S2}} = \frac{g_{m_5}}{2}$$

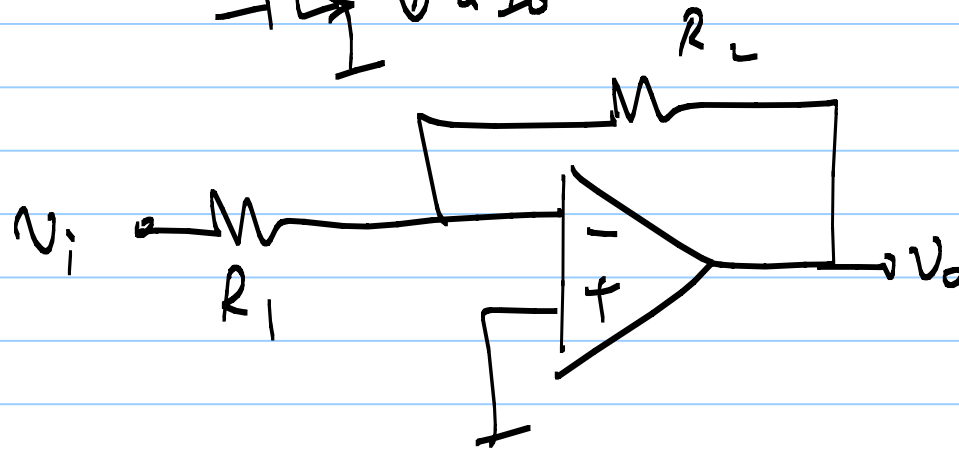
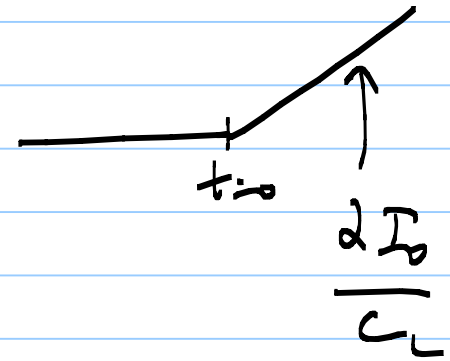
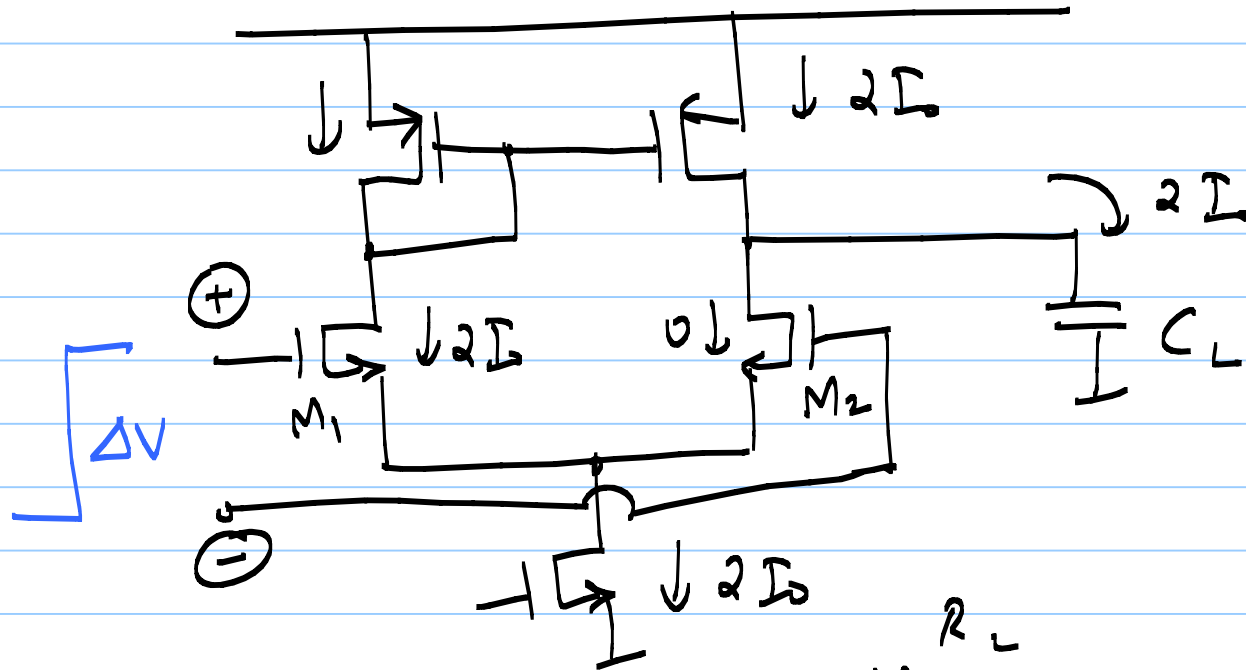


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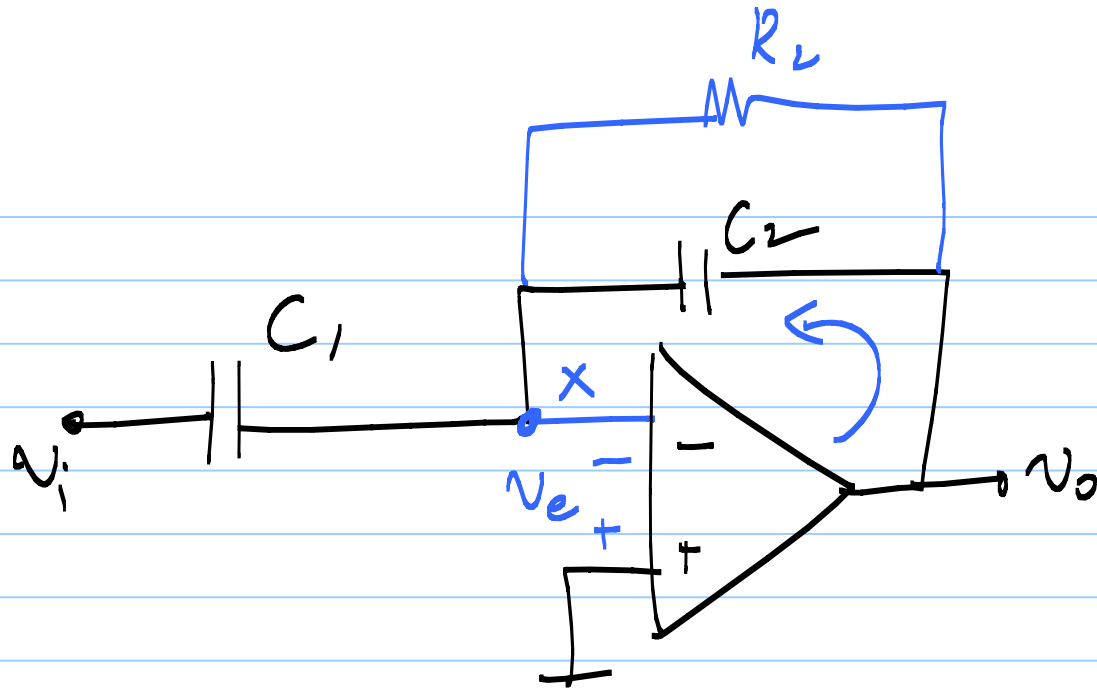
Lec 28

Review Class

Slew rate



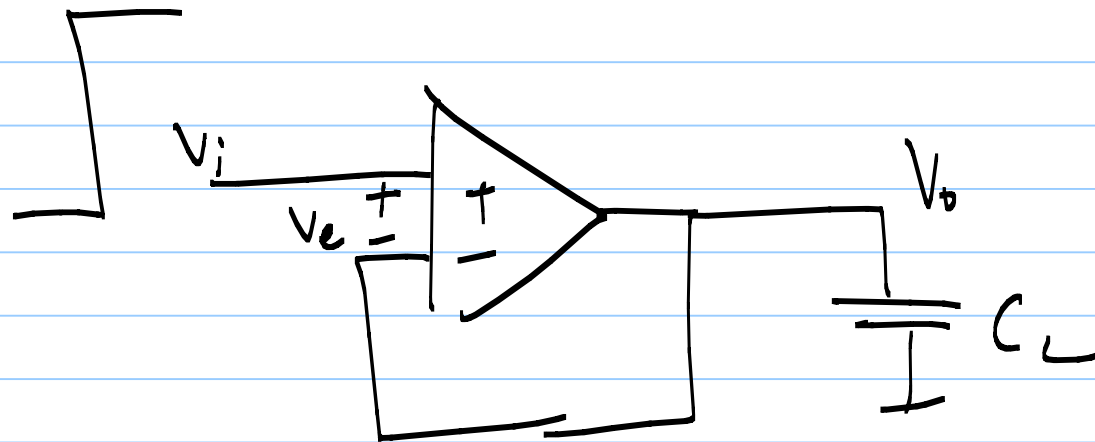
$$\frac{V_O}{V_i} = -\frac{R_2}{R_1}$$

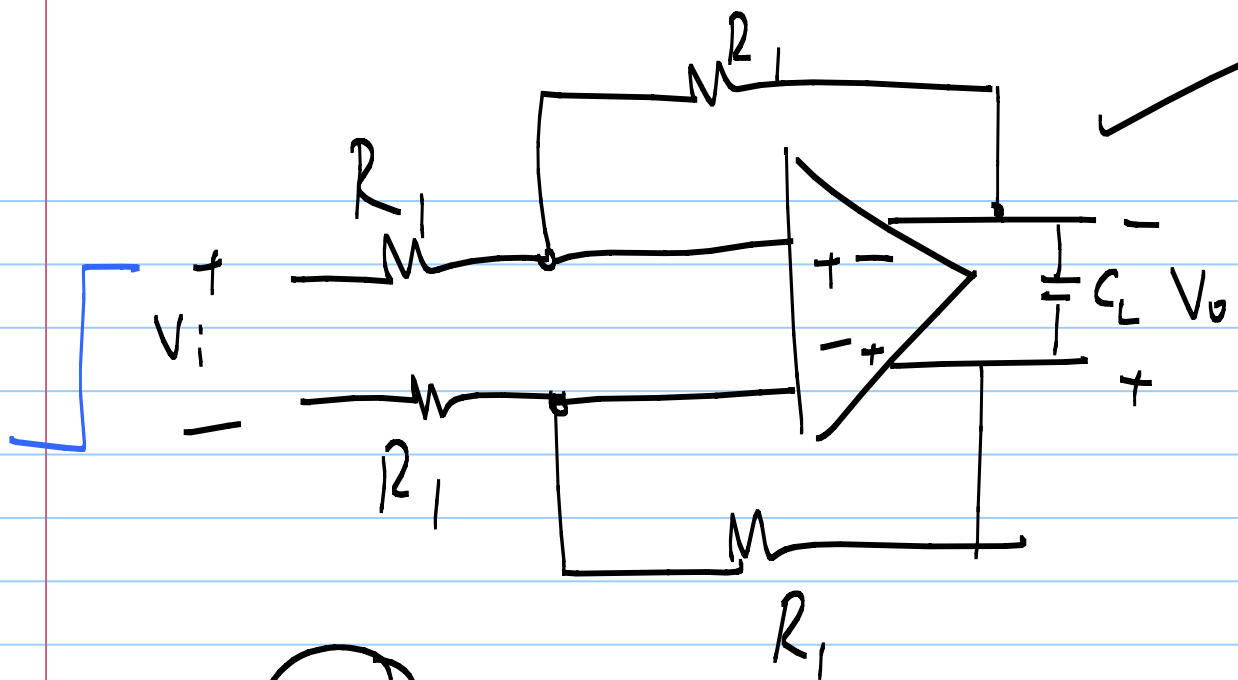


$$\frac{v_o}{v_i} = -\frac{C_1}{C_2}$$

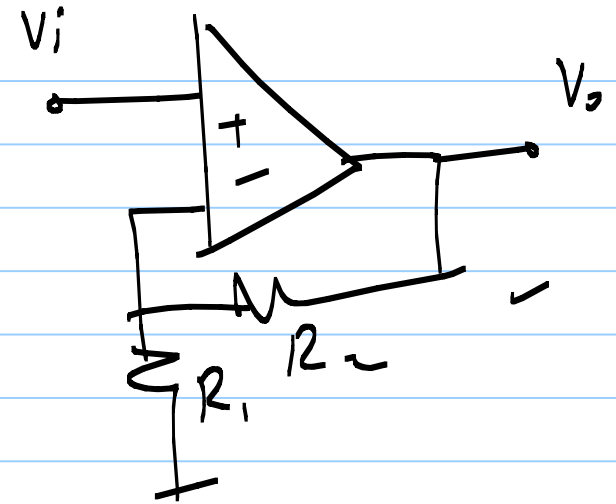
$$R_2 \gg \frac{1}{sC_2}$$

$$I_f \approx \frac{1}{R_2 C_2}$$

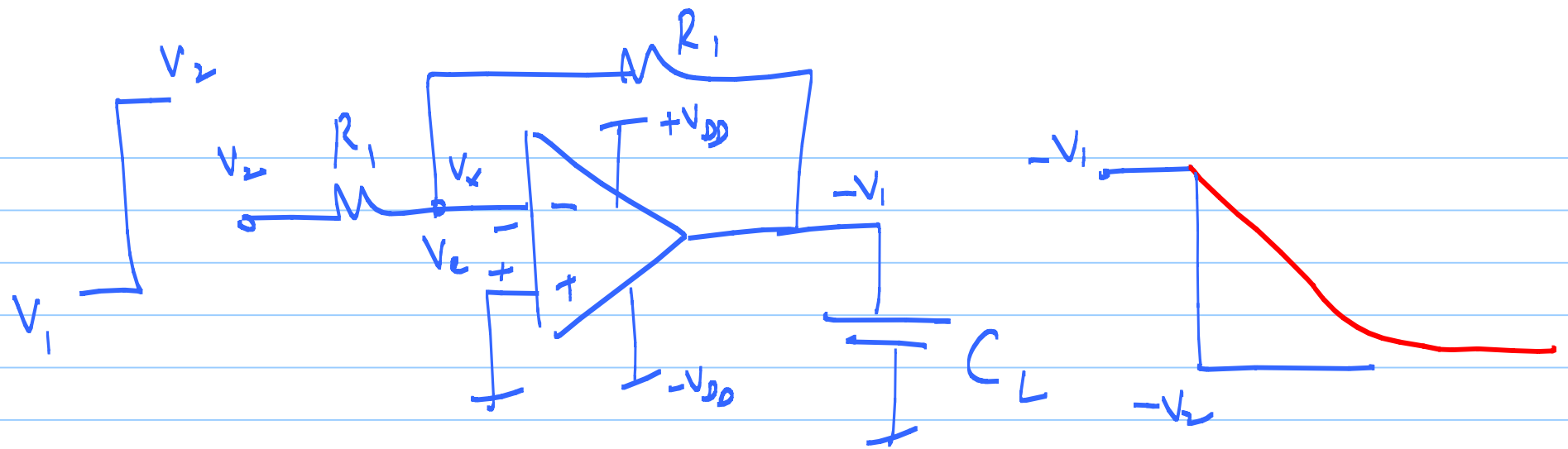




(Hv)



$$\frac{V_o}{V_i} = 1 + \frac{R_2}{R_1} \rightarrow \infty$$



$$V_x = V_2 - \left(\frac{V_2 + V_1}{2R_1} \right) R_1 = \frac{V_2 - V_1}{2} = -V_e$$

$$V_e = \frac{V_1 - V_2}{2}$$