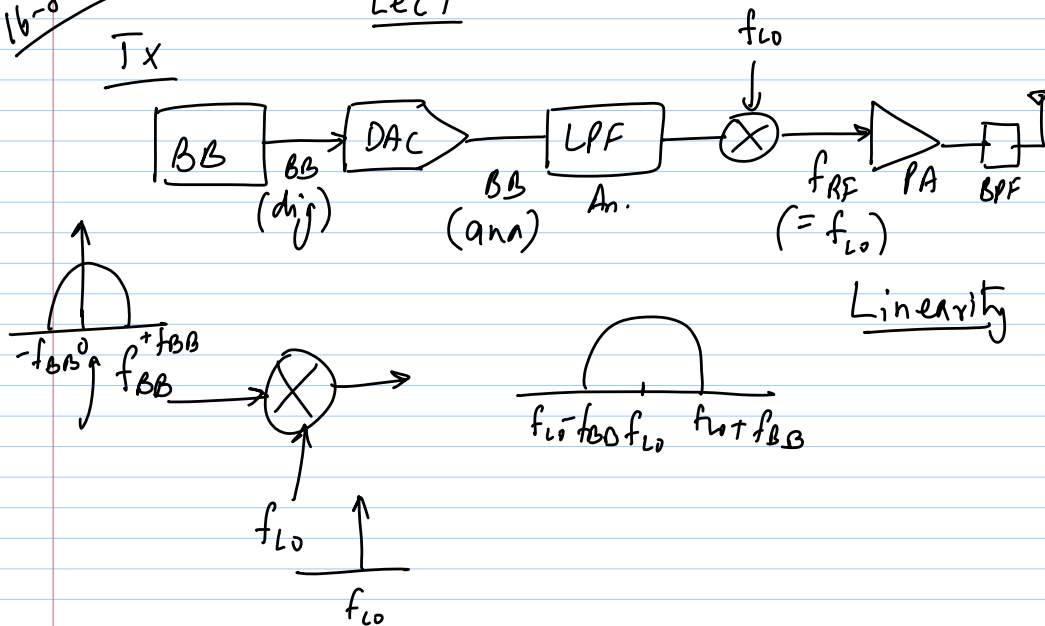


16-8-13

Lec 7



Basic RF concepts

1) Linearity

* HD in amplifier

$$f_o \rightarrow \sum_{k=1}^n k f_i \quad \sum_{k=2}^n P_{kf_i}$$

$$x(t) \rightarrow \boxed{} \rightarrow y(t) \quad \begin{aligned} x_1(t) &\rightarrow y_1(t) \\ x_2(t) &\rightarrow y_2(t) \\ ax_1(t) + bx_2(t) &\rightarrow ay_1(t) + by_2(t) \end{aligned}$$

* No offsets

* Non-zero initial conditions

2) Time invariance

$$x(t) \rightarrow y(t)$$

$$x(t-\tau) \rightarrow y(t-\tau) \quad \forall \tau$$

time variant system:



Mixer
NL & TV

Effects of Nonlinearity

$$x(t) = A \cos(\omega t) \quad x(t) \rightarrow \boxed{NL} \rightarrow y(t)$$

$$y(t) \approx \alpha_1 x(t) + \alpha_2 x^2(t) + \alpha_3 x^3(t)$$

$$= \alpha_1 A \cos(\omega t) + \alpha_2 A^2 \cos^2(\omega t) + \alpha_3 A^3 \cos^3(\omega t)$$

$$= \alpha_1 A \cos(\omega t) + \frac{\alpha_2 A^2}{2} [1 + \cos(2\omega t)]$$

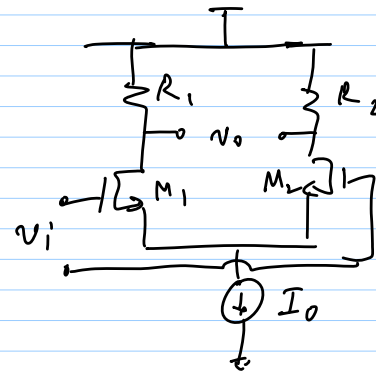
$$+ \frac{\alpha_3 A^3}{4} [3\cos(\omega t) + \cos(3\omega t)]$$

$$= \underbrace{\frac{\alpha_2 A^2}{2}}_{\text{DC offset}} + \underbrace{\left(\alpha_1 A + \frac{3\alpha_3 A^3}{4} \right)}_{\text{gain}} \cos(\omega t)$$

$$+ \underbrace{\frac{\alpha_2 A^2}{2} \cos(2\omega t)}_{\text{2nd harmonic}} + \underbrace{\frac{\alpha_3 A^3}{4} \cos(3\omega t)}_{\text{3rd harmonic}}$$

- * even harmonics result from even order NL
- differential symmetry will knock these out
- mismatches lead to residual even harmonic

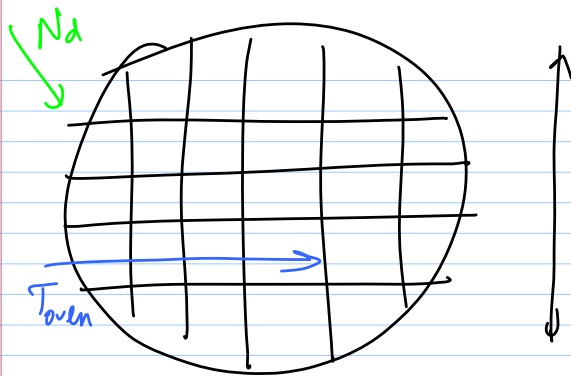
Diff. symmetry



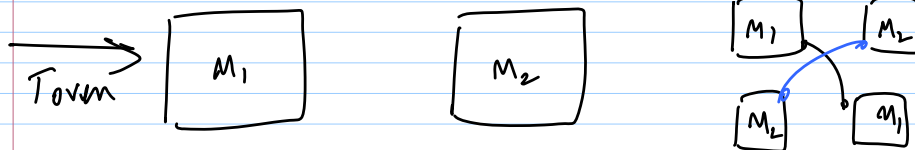
$$M_1 \equiv M_2$$

$$R_1 \equiv R_2$$

* Corner - across dies
 $\mu - f(\text{doping}, T, V)$



dia = 12 inches
 1000's of chips



* Amplitude of n^{th} harmonic

