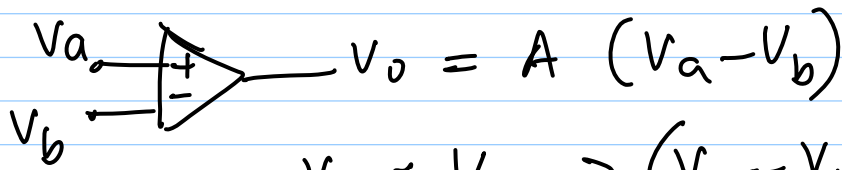
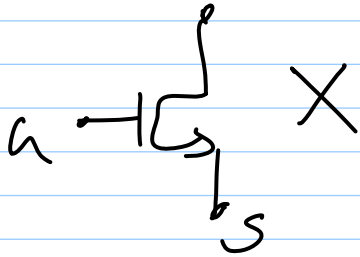


17-10-12

Lec 33



$$V_a \approx V_b \Rightarrow (V_a - V_b) \text{ small}$$



$$V_a = \frac{V_a + V_b}{2} + \frac{V_a - V_b}{2}$$

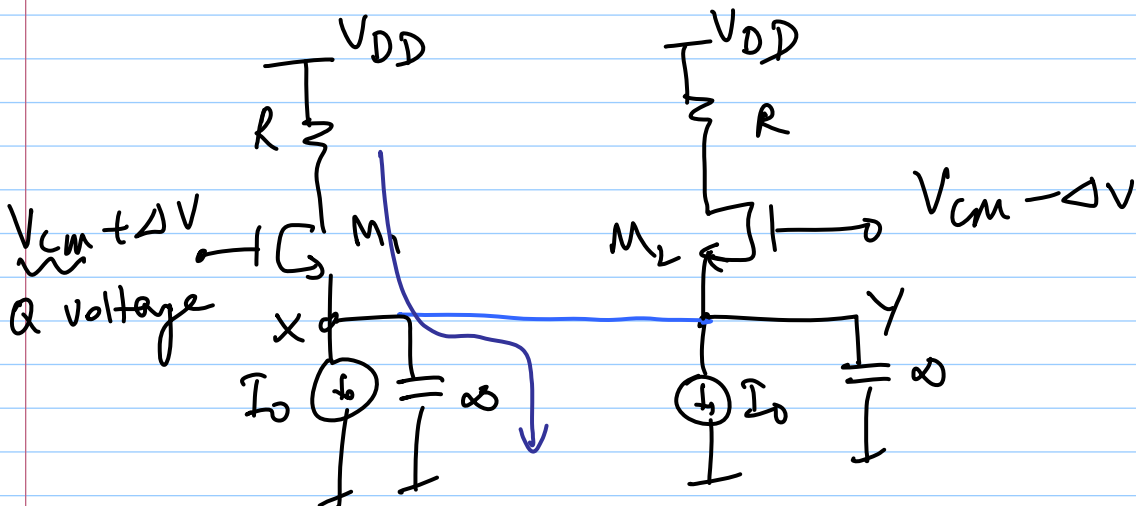
$$V_b = \frac{V_a + V_b}{2} - \frac{V_a - V_b}{2}$$

avg. (CM voltage)

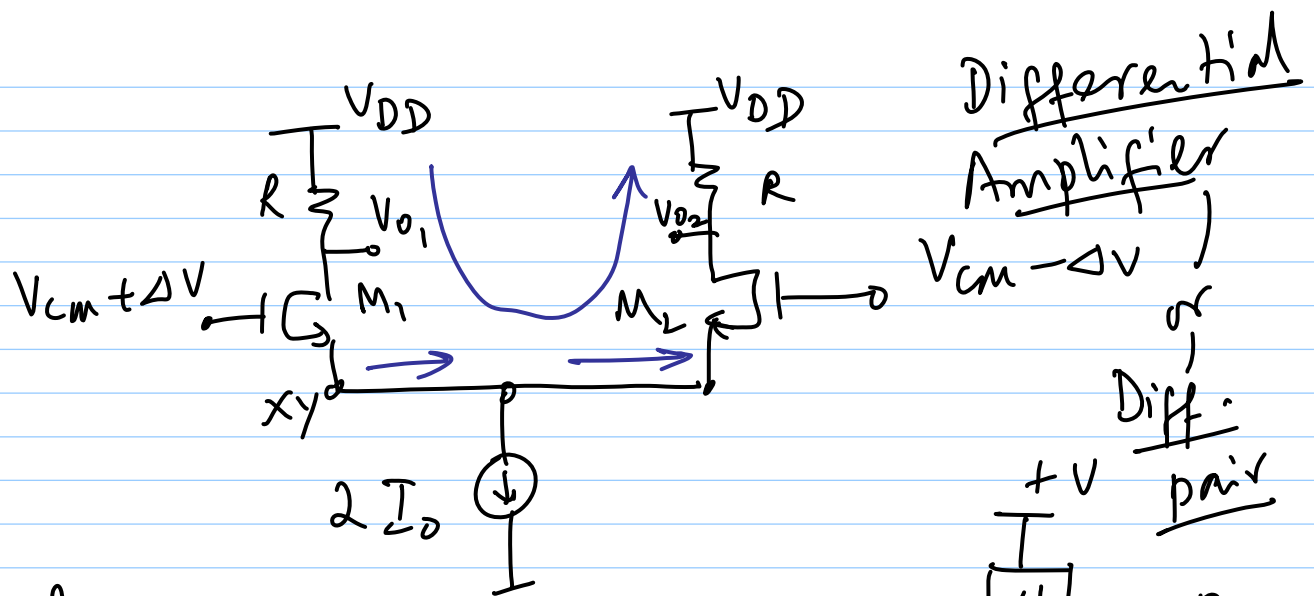
diff. (DM voltage)

$$V_{cm} + \Delta V \rightarrow k(V_{cm} + \Delta V)$$

$$V_{cm} - \Delta V \rightarrow k(V_{cm} - \Delta V)$$

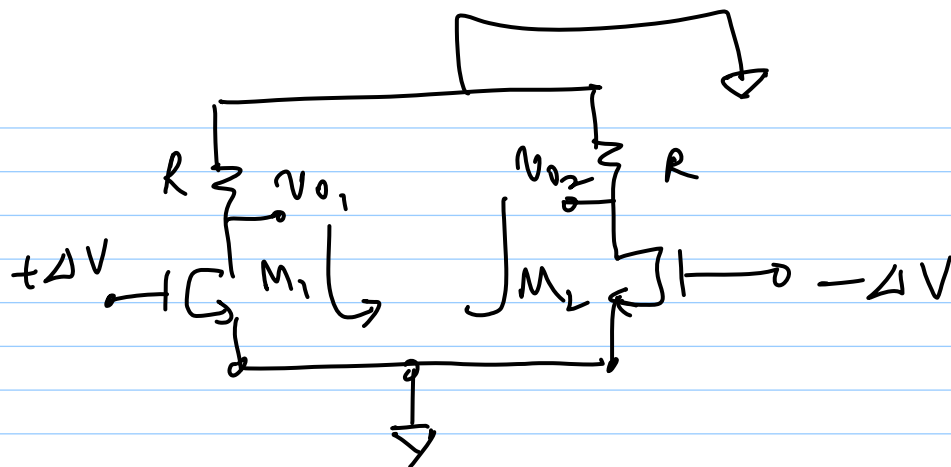


$$V_x = V_{cm} - V_{as_1}; \quad V_y = V_{cm} - V_{as_2} = V_x$$



Small signal $v_{xy} = 0$ (symmetry)

$V_{xy} = V_{cm} - V_{as}$ (total voltage)

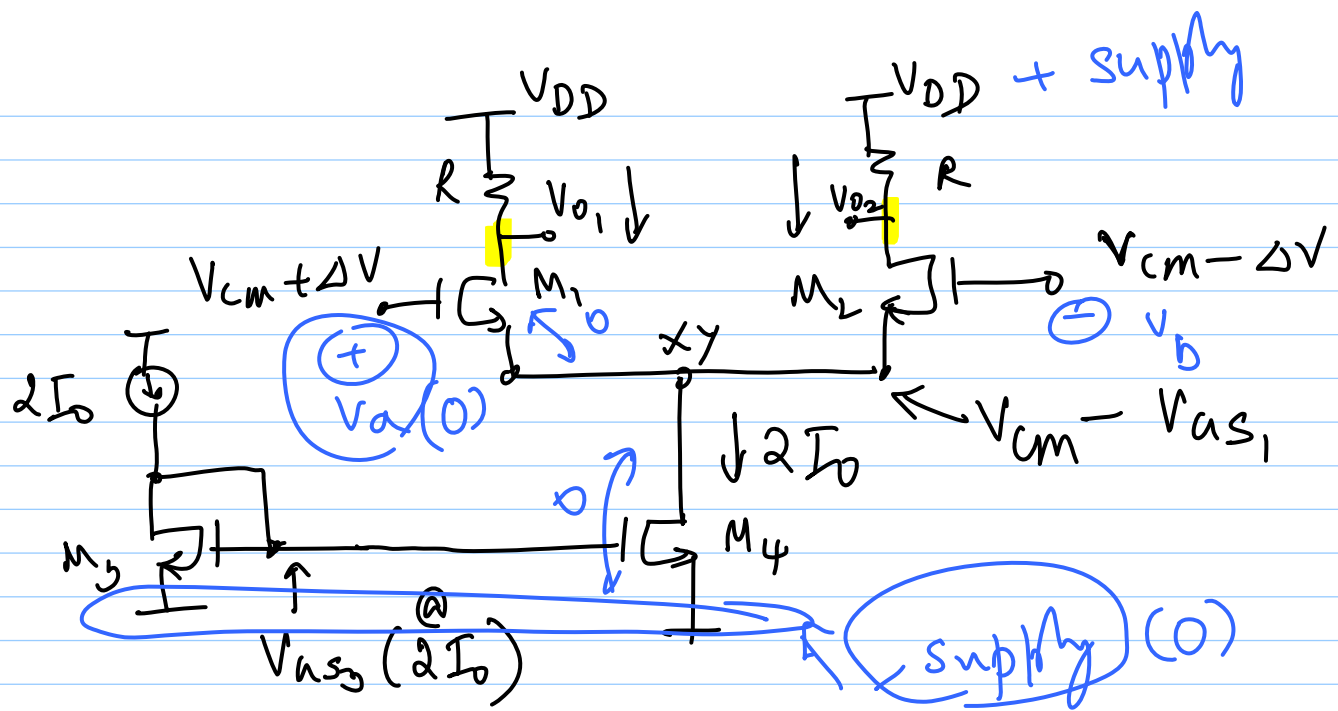


$$i_{d1} = g_m \Delta V ; \quad i_{d2} = -g_m \Delta V$$

$$v_{01} = -g_m R \Delta V ; \quad v_{02} = g_m R \Delta V$$

$$V_{01} = V_{DD} - I_0 R - g_m R \Delta V$$

$$V_{02} = V_{DD} - I_0 R + g_m R \Delta V$$



* $V_{cm} \downarrow \Rightarrow V_{xy} \downarrow \Rightarrow M_4$ goes into triode

$$\Rightarrow V_{cm} - V_{ds1} \geq V_{D,sat4}$$

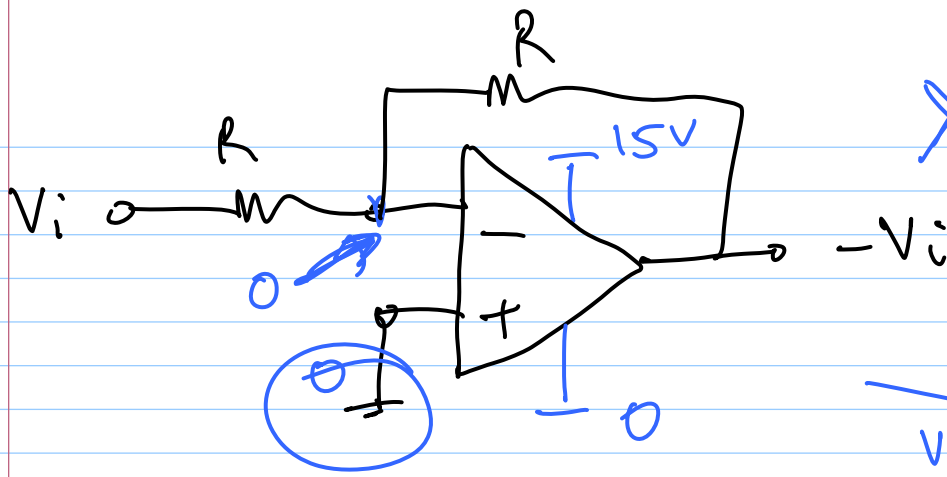
$$\Rightarrow V_{cm,min} = V_{ds1} + V_{D,sat4}$$

* $V_{cm} \uparrow \Rightarrow M_{1,2}$ approach triode

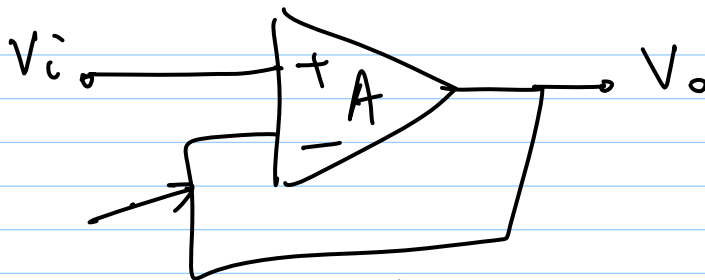
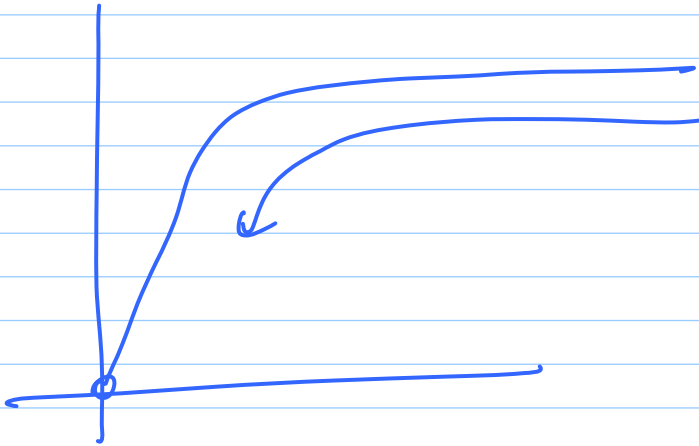
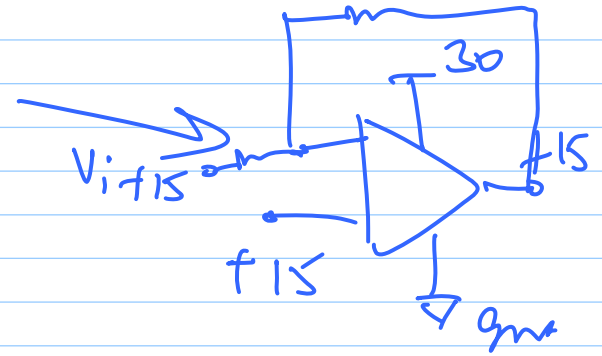
$$V_{cm} - V_T \leq V_{DD} - I_O R$$

$$\Rightarrow V_{cm,max} = V_{DD} - I_O R + V_T$$

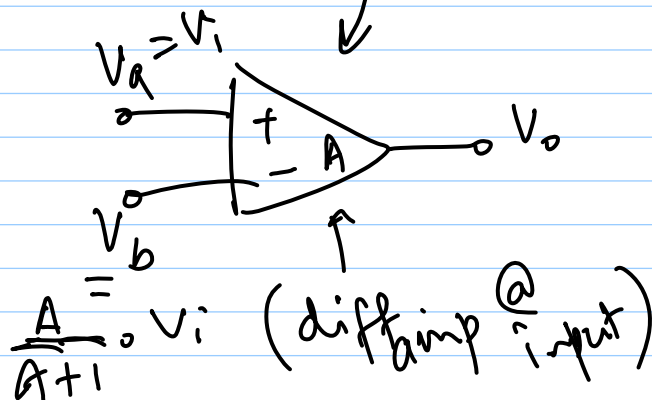
$$\left\{ V_{cm,min}, V_{cm,max} \right\} \quad \frac{\text{Input}}{\text{Common-mode range}}$$



~~X~~ not possible



$$\frac{V_o}{V_i} = ? \quad \left. \begin{array}{l} (V_i - V_o) A = V_o \\ V_o = \frac{A}{A+1} V_i \end{array} \right\}$$



$$\left. \begin{array}{l} V_a = V_i \\ V_b = \frac{A}{A+1} V_i \end{array} \right\}$$

$$V_{cm}$$

$$= \frac{V_i + \frac{A}{A+1} V_i}{2}$$

$$= \frac{2A+1}{2(A+1)} V_i \approx V_i$$

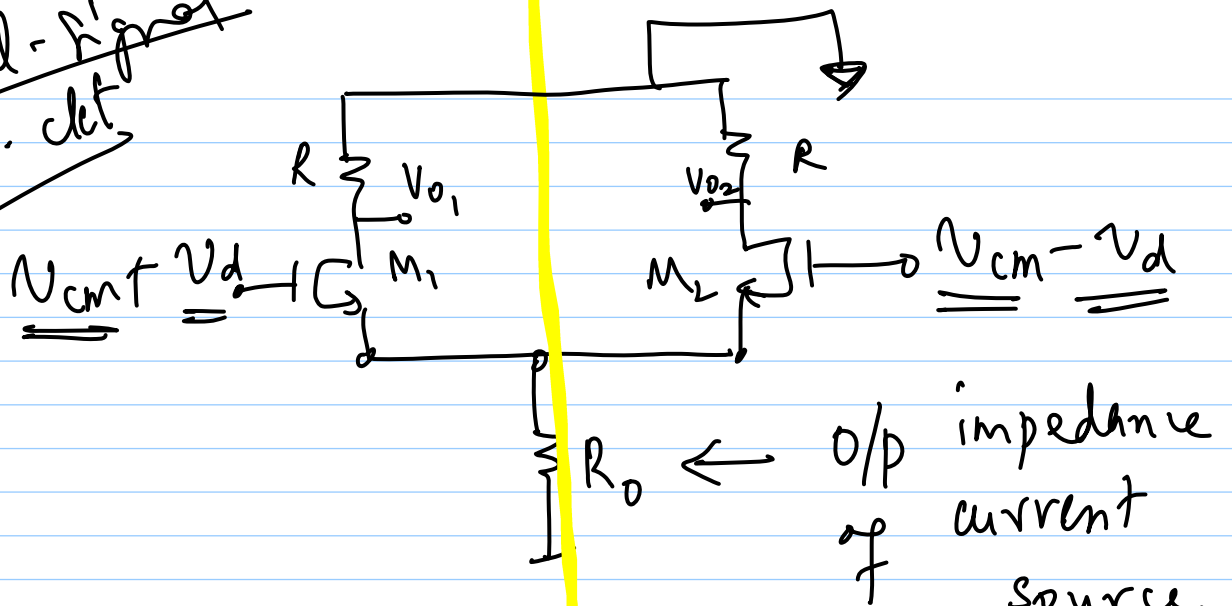
✓ "CM mode" $\approx f(V_i)$

$$V_{dm} = \frac{V_i - \frac{A}{A+1} V_i}{2}$$

$$= \frac{V_i}{2(A+1)}$$

✓ "dm signal"

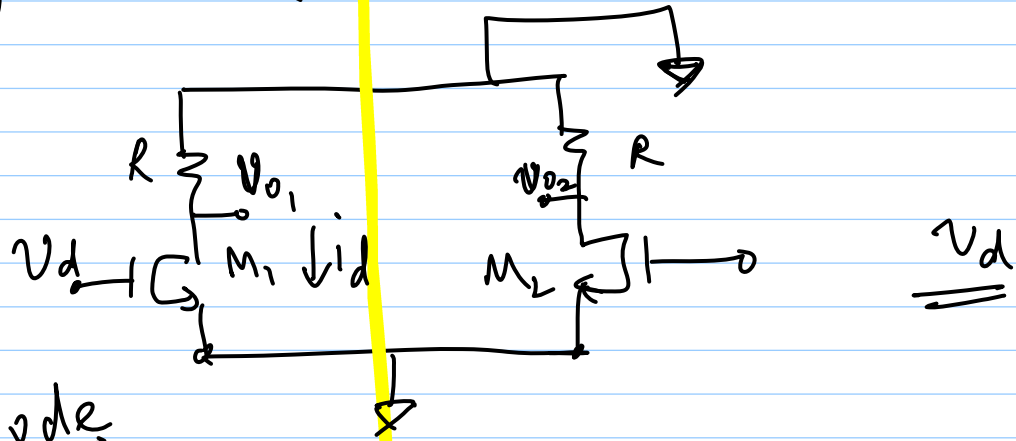
Small-Signal
ser. ckt



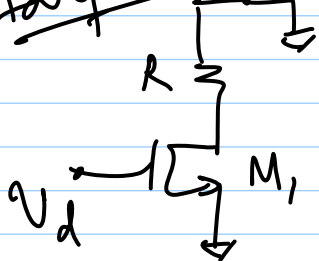
* linear, symmetric network

* v_{cm} = inc. CM component

Only v_d



Diff. mode
Half ckt



$$i_{d1} = g_m v_d$$

$$v_{o1} = -g_m R v_d$$

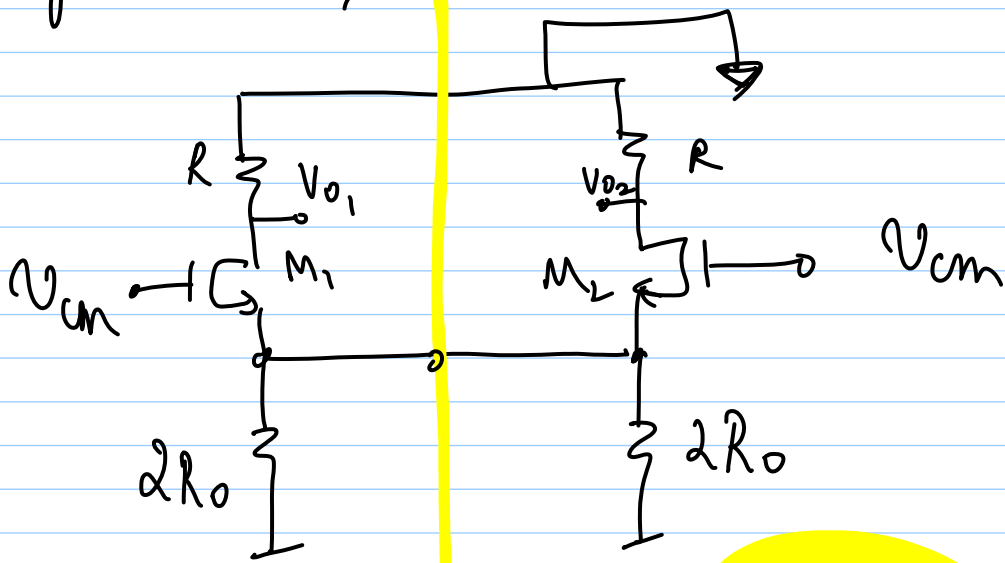
other half

$$i_{d2} = -g_m v_d$$

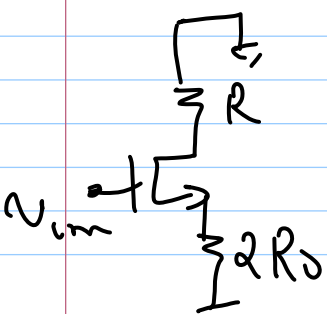
$$v_{o2} = +g_m R v_d$$

$\{x(-1)\}$

Only v_{cm} (x1)



CM
Half ckt



$$i_{d1} = \frac{g_m}{1 + 2g_m R_o} v_{cm}$$

$$v_{o1} = -i_{d1} R$$