

# EE658: VLSI Data Conversion Circuits; HW6

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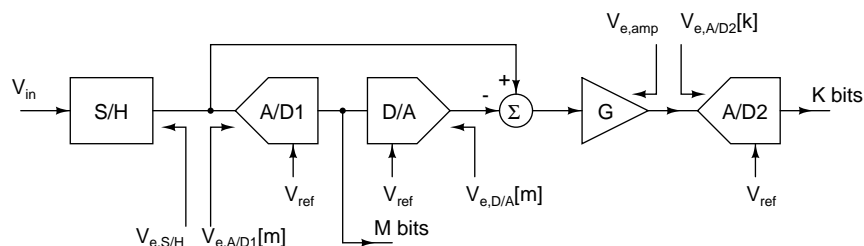


Figure 1:

1. Fig. 1 shows a two step flash converter with error correction. The overall resolution is  $N = M + K - 1$  bits. The error in each block is shown as an analog voltage referred to either the input or the output. i.e. The  $m^{\text{th}}$  transition of A/D1 occurs at  $mV_{LSB1} + V_{e,A/D1}[m]$  and the  $m^{\text{th}}$  output of D/A is  $mV_{LSB1} + V_{e,D/A}[m]$ .  $0 \leq m \leq 2^M - 1$  and  $0 \leq k \leq 2^K - 1$ .  $V_{LSB} = V_{ref}/2^N$  is the LSB voltage of the overall converter.
  - (a) Derive the value of the input  $V_{in}$  which corresponds to  $m^{\text{th}}$  transition of A/D1. You should get an expression that combines the errors from different components.
  - (b) Derive the value of the input  $V_{in}$  which corresponds to  $k^{\text{th}}$  transition of A/D2. Assume that A/D1 is between  $m^{\text{th}}$  and  $(m + 1)^{\text{th}}$  transitions.
  - (c) In the result from (a) above, assume that the different terms contribute equally to the total error, which is constrained to  $0.5V_{LSB}$ . Calculate the individual errors in terms of  $V_{ref}$ .
  - (d) Calculate the allowable errors in each component for a 8 bit converter, for  $M = 5, K = 4$  and  $M = 4, K = 5$ . Express the accuracy as an effective number of bits (A component with a voltage range  $V_{ref}$  has an  $L$  bit accuracy if its error magnitude is less than  $V_{ref}/2^{L+1}$ , i.e. half LSB at  $L$  bits).
2. Assume that you have a 2 step flash A/D converter (no digital error correction) with 2 bits in each stage. All components other than the residue amplifier are ideal. Plot INL and DNL for the following cases. Compare it with the ideal characteristics.
  - (a) (2 pts.) The amplifier has a gain  $G > 4$
  - (b) (2 pts.) The amplifier has a gain  $G < 4$
  - (c) (2 pts.) The amplifier has an input referred offset  $V_{os} > 0$
  - (d) (2 pts.) The amplifier has an input referred offset  $V_{os} < 0$