

$$\frac{V_o(s)}{V_i(s)} = \frac{g_{m1} R_{o1}}{1 + R_{o1} C_{o1} s} \times \frac{g_{m2} R_{o2}}{1 + R_{o2} C_{o2} s}$$

$$= \frac{A_0}{(1 + s/\omega_{p1})(1 + s/\omega_{p2})}$$

$$A_0 = g_{m1} R_{o1} \cdot g_{m2} R_{o2}$$

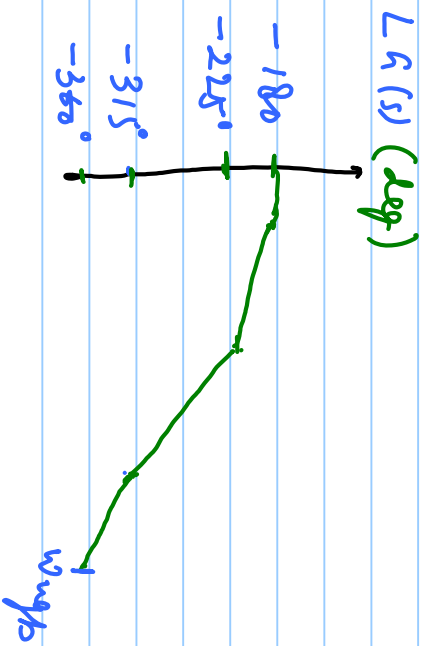
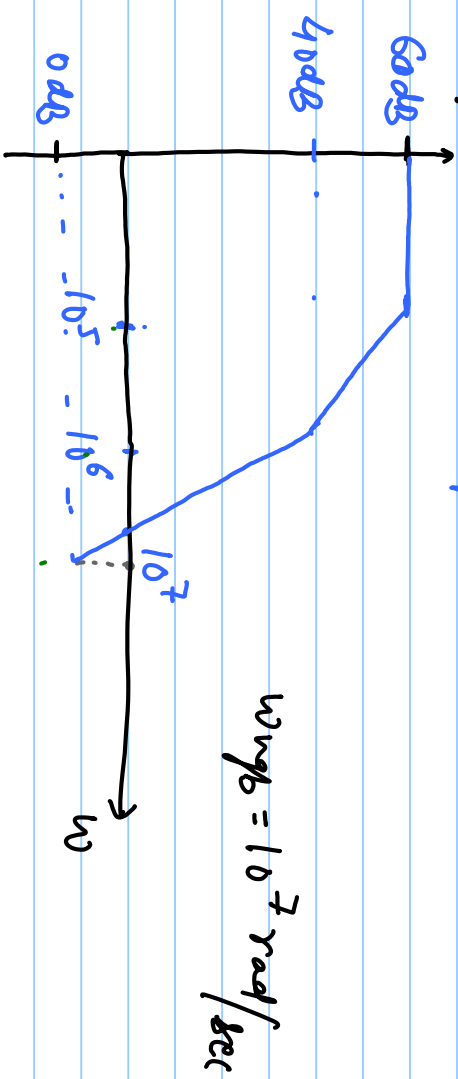
$$\omega_{p1} = \frac{1}{R_{o1} C_{o1}} \quad ; \quad \omega_{p2} = \frac{1}{R_{o2} C_{o2}}$$

Assume,  $A_0 = 1000$ ;  $g_{m1} = 100 \mu\text{A/V}$ ,  $R_{01} = 1\text{M}\Omega$ ,  $g_{m2} = 100 \mu\text{A/V}$ ,  $R_{02} = 100\text{k}\Omega$   
 $g_{m1}, R_{01} = 100$ ,  $g_{m2}, R_{01} = 10 \rightarrow A_0 = 1000$   
 $C_{01} = 10\text{pF}$  &  $C_{02} = 10\text{pF}$

$$\omega_{p1} = \frac{1}{R_{01}C_{01}} = \frac{1}{10^6 \times 10^{-11}} = 10^5 \text{ rad/sec}$$

$$\omega_{p2} = \frac{1}{R_{02}C_{02}} = \frac{1}{10^5 \times 10^{-11}} = 10^6 \text{ rad/sec}$$

$$|A(s)| = L_G(s) \text{ for } \beta = 1$$



Total Phase shift due to poles =  $-180^\circ$

$-180^\circ$  comes from -ve feedback

So if -ve of -amp is considered in -ve feedback then

total loop phase shift =  $-360^\circ \Rightarrow$  +ve feedback  $\rightarrow$  unstable.

In order to compensate 2-stage op-amp, we target  $m \geq 60^\circ$

Before compensation

$$\omega_{p_1} = 10^5 \text{ rad/sec} \quad \omega_{p_2} = 10^6 \text{ rad/sec}$$

$$PM = 180^\circ - \tan^{-1} \frac{\omega \omega_{gb}}{\omega_{p1}} - \tan^{-1} \frac{\omega \omega_{gb}}{\omega_{p2}}$$

$$\downarrow 90^\circ$$

$$= 90^\circ - \tan^{-1} \frac{\omega \omega_{gb}}{\omega_{p2}}$$

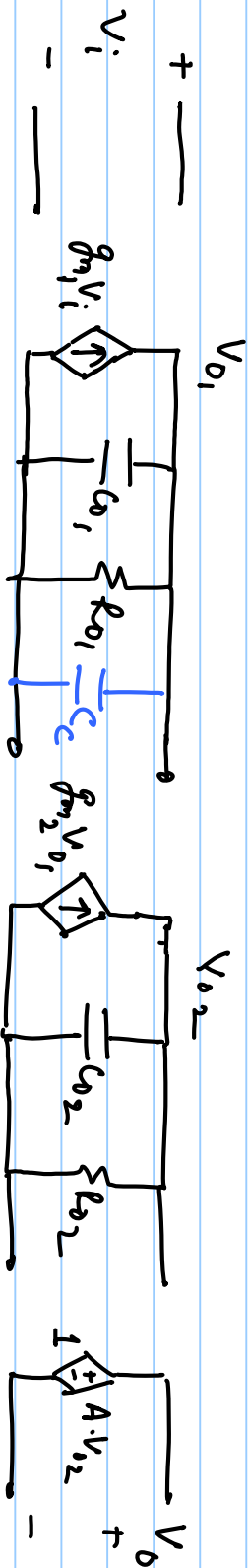
$$PM = 60^\circ$$

$$\tan^{-1} \frac{\omega \omega_{gb}}{\omega_{p2}} = 30^\circ \Rightarrow \omega \omega_{gb} = \frac{\omega_{p2}}{\sqrt{3}}$$

$$\omega_{p1} = \frac{\omega \omega_{gb}}{A_0} = \frac{\omega_{p2}}{A_0 \sqrt{3}} = \frac{10^6}{10^3 \times \sqrt{3}} = \frac{10^3}{\sqrt{3}}$$

$$\omega_{p1} = \frac{1}{R_{o1}C_{o1}}$$

For compensation, we need to increase cap of  $V_{o2}$



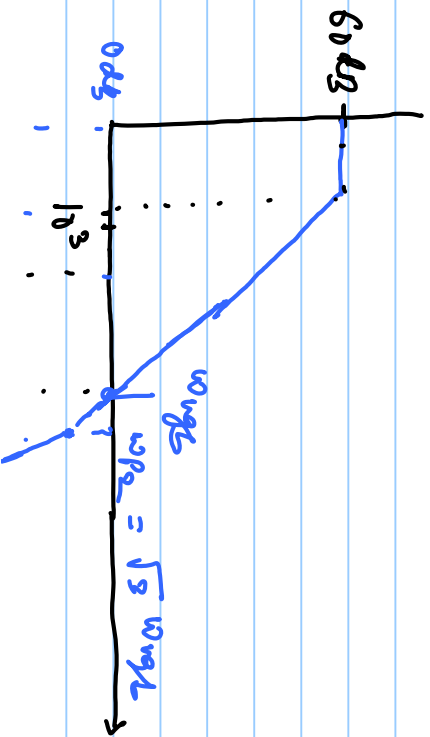
$\omega_{p1}$  after compensation

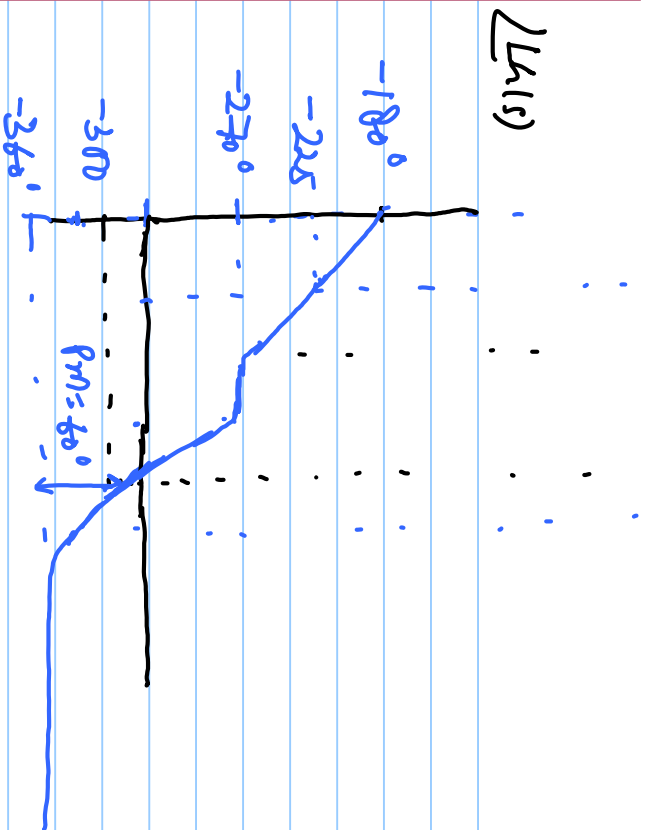
$$\omega_{p1} = \frac{1}{R_{o1}(C_{o1} + C_c)} = \frac{10^3}{\sqrt{3}}$$

$$R_{01} (\omega_1 + C_c) = \frac{\sqrt{3}}{10^3} \Rightarrow C_{01} + C_c = \frac{\sqrt{3}}{10^3} \left( \frac{1}{R_{01}} \right)$$

$$= \frac{\sqrt{3}}{10^3} \times \frac{1}{10^6} = \sqrt{3} \times 10^{-9} \approx 1.7 \text{ nF}$$

$$|L_{410}| \quad C_c = 1.7 \text{ nF} - 10 \text{ pF} \approx 1.7 \text{ nF}$$

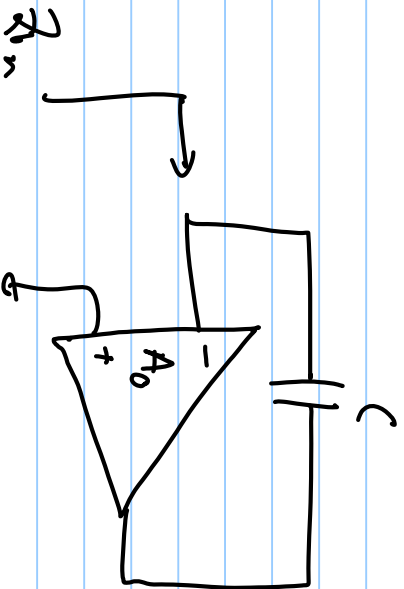




When we compensate 2-stage op-amp by adding cap, it is called Lead compensation



## Miller compensation



$$R_{in} = \frac{1}{(1+A_0)C}$$