

## Analogy Systems &amp; Lats

$$\xi = \frac{1}{2\sqrt{A_0}} \sqrt{\frac{\omega_{p1}}{\omega_{p2}} + \frac{\omega_{p2}}{\omega_{p1}}}$$

$\xi \rightarrow 0$  if  $\omega_{p1} = \omega_{p2} \rightarrow$  system is undamped

$$\omega_{p1} = \frac{\omega_{ngb}}{A_0}, \quad \omega_{p2} = \omega_{ngb}$$

$$\xi = \frac{1}{2\sqrt{A_0}} \sqrt{\frac{\omega_{ngb}}{A_0 \times \omega_{ngb}} + \frac{\omega_{ngb}}{\omega_{ngb}/A_0}} = \frac{1}{2\sqrt{A_0}} \sqrt{\frac{1}{A_0} + A_0}$$

$\sim 0$

$$\xi = \frac{1}{2}$$

Now assume,  $\omega_2 = 2\omega_1$

$$H(s) = \frac{1}{1 + s/\omega_p}$$

$$|H(s)| = \frac{1}{\sqrt{1 + (\omega/\omega_p)^2}} \quad ; \quad \angle H(s) = -\tan^{-1} \frac{\omega}{\omega_p}$$

$$= \frac{\omega_p}{\omega} \quad \text{for } \omega/\omega_p \gg 1$$

$$\angle G(s) = \frac{K_0}{(1 + s/\omega_{p1})(1 + s/\omega_{p2})}$$

$$\angle G(s) = -\tan^{-1} \frac{\omega}{\omega_{p1}} - \tan^{-1} \frac{\omega}{\omega_{p2}}$$

$$\omega = \omega_{\text{cgl}}$$

$$\omega_{p1} = \frac{\omega_{\text{cgl}}}{A_0}, \quad \omega_{p2} = 2\omega_{\text{cgl}} A_0$$

$$\angle G(s) = -\tan^{-1} A_0 - \tan^{-1} \frac{1}{2}$$

$$A_0 \gg 1$$

$$= -90^\circ - 27^\circ = -117^\circ$$

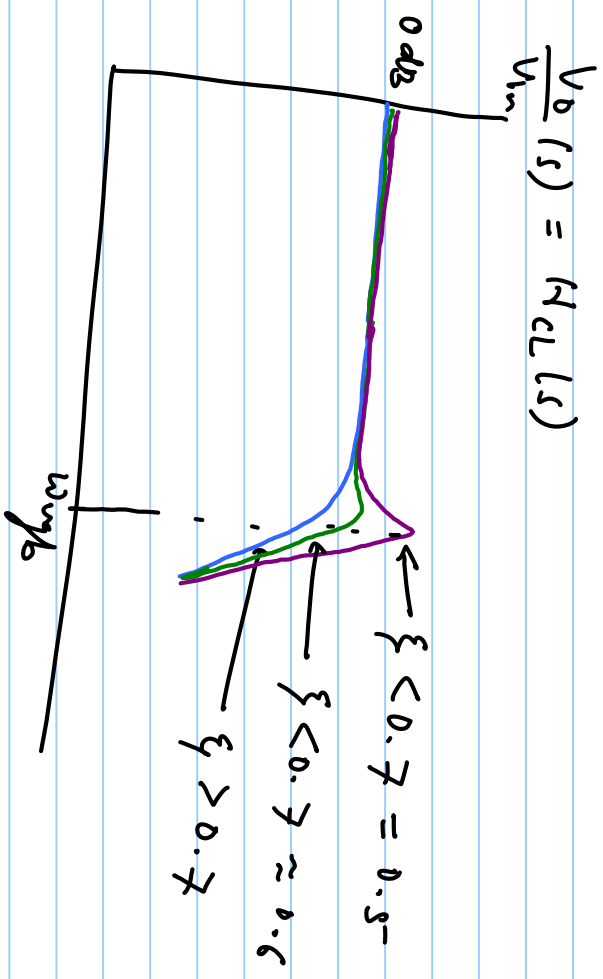
$$\phi_M = 180^\circ + \angle G(s) = 180^\circ - 117^\circ = 63^\circ$$

$$\zeta = \frac{1}{2\sqrt{A_0}} \sqrt{\frac{1}{2A_0} + 2A_0}$$

↖ 0

$$= \frac{1}{\sqrt{2}} = 0.7$$

- $\zeta = 0.5$  ,  $PM = 95^\circ$
- $\zeta = 0.7$  ,  $PM = 63^\circ$
- $\zeta = 0$  ,  $PM \approx 0$



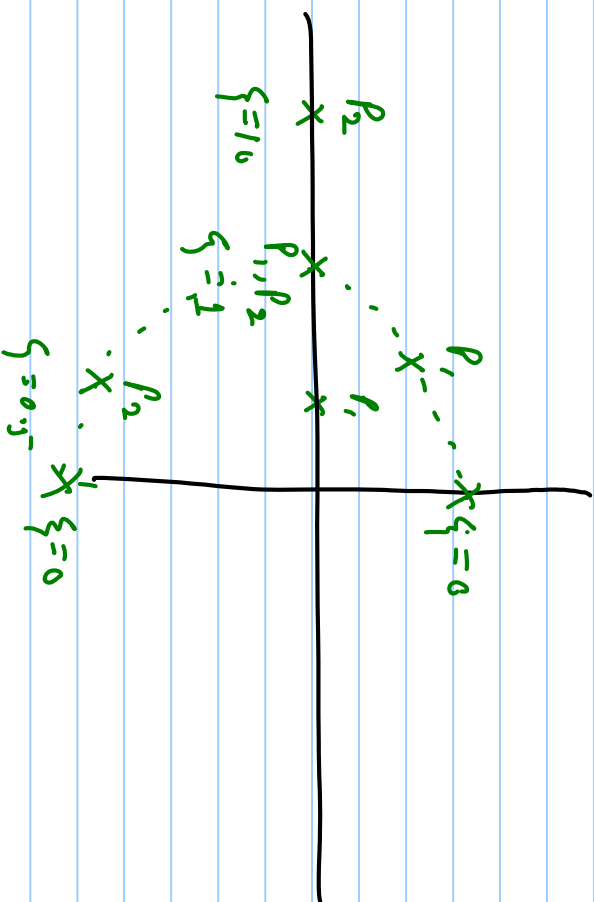
$$\zeta = \infty, \quad \varphi_M \approx 90^\circ$$

$$\zeta = \frac{1}{2\sqrt{A_0}} \sqrt{\frac{\omega_{p1}^2}{\omega_{p2}^2} + \frac{\omega_{p2}^2}{\omega_{p1}^2}}$$

$$\zeta = 1, \quad \omega_{p1} = \omega_{np0}/A_0$$

$$1 = \frac{1}{2\sqrt{A_0}} \sqrt{\frac{\omega_{np0}^2}{A_0 \omega_{p2}^2} + \frac{A_0 \omega_{p2}^2}{\omega_{np0}^2}}$$

$$\Rightarrow 1 = \frac{1}{2\sqrt{A_0}} \times \sqrt{A_0 \frac{\omega_{p2}^2}{\omega_{np0}^2}}$$



$$\omega_{p2} = 4 \text{ rad/s}$$

$$\zeta = 1, \quad PM = 76^\circ$$

PM (loop gain)

