# EC201-ANALOG CIRCUITS : PROBLEM SET 3

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## Problem 1

The MOSFET in Fig. 1 has  $V_T = 0.7 V$ , and  $\mu_n C_{ox} = 500 \,\mu A/V^2$ . The drain current in the device is 1 mA.

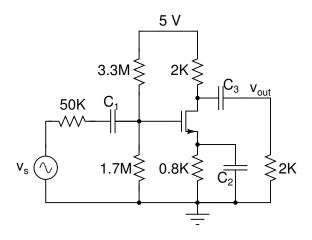


Figure 1: Problem 1

- Determine the small signal gain from  $v_s$  to  $v_{out}$ .
- Determine the (W/L) of the device and the quiescent  $V_{GS}$  and  $V_{DS}$ .
- The lowest frequency contained in  $v_s$  is 100 rad/s. Determine the minimum values of  $C_1$ ,  $C_2$  and  $C_3$  required so that the natural frequencies associated with their charging/discharging is atleast 10 times smaller than the smallest input frequency.
- Determine the voltage swing limits at *v*<sub>out</sub>. What is the amplitude of the largest sinusoidal input signal that can be applied before the output begins to clip ?
- The supply voltage is changed to 5.5 V. Determine the small signal gain of the amplifier.
- Due to a change in temperature, *V*<sub>T</sub> increases by 100 mV. What is the new small signal gain of the amplifier ?

### Problem 2

The MOSFETs in Fig. 2 have  $V_T = 0.7 V$ , and  $\mu_n C_{ox} = 500 \,\mu A/V^2$ . Like in Problem 1, the drain current in M2 is 1 mA, and has the same (W/L) as in that problem.

- Determine the small signal gain from  $v_s$  to  $v_{out}$ .
- Determine the (W/L) of M1 and the quiescent  $V_{GS}$  and  $V_{DS}$ .

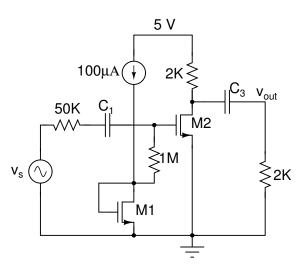


Figure 2: Problem 2

- The lowest frequency contained in  $v_s$  is 100 rad/s. Determine the minimum values of  $C_1$  and  $C_3$  required so that the natural frequencies associated with their charging/discharging is atleast 10 times smaller than the smallest input frequency.
- Determine the voltage swing limits at *v*<sub>out</sub>. What is the approximate amplitude of the largest sinusoidal input signal that can be applied before the output begins to clip ?
- The supply voltage is changed to 5.5 V. Determine the small signal gain of the amplifier. How does this compare with the results of Problem 1 ? Why ?
- What is the small signal gain of the amplifier if (a)  $V_{T,M1} = 0.8 V, V_{T,M2} = 0.7 V$  (b)  $V_{T,M1} = 0.7 V, V_{T,M2} = 0.8 V$  and (c)  $V_{T,M1} = 0.8 V, V_{T,M2} = 0.8 V$ ? How does this compare with the results of Problem 1? Why?

### Problem 3

The MOSFETs in Fig. 3 have  $V_T = 0.7 V$ , and  $\mu_n C_{ox} = 500 \,\mu A/V^2$ . Like in Problem 1, the drain current in M2 is 1 mA, and has the same (W/L) as in that problem.

- Determine the small signal gain from  $v_s$  to  $v_{out}$ .
- Determine the (W/L) of M1 and the quiescent  $V_{GS}$  and  $V_{DS}$ .
- The lowest frequency contained in  $v_s$  is 100 rad/s. Determine the minimum values of  $C_1$  and  $C_3$  required so that the natural frequencies associated with their charging/discharging is atleast 10 times smaller than the smallest input frequency.

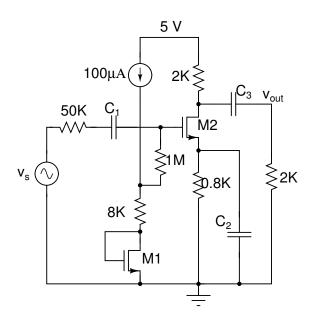


Figure 3: Problem 3

- Determine the voltage swing limits at *v*<sub>out</sub>. What is the amplitude of the largest sinusoidal input signal that can be applied before the output begins to clip ?
- The supply voltage is changed to 5.5 V. Determine the small signal gain of the amplifier. How does this compare with the results of Problem 1 & 2 ? Why ?
- What is the small signal gain of the amplifier if (a)  $V_{T,M1} = 0.8 V, V_{T,M2} = 0.7 V$  (b)  $V_{T,M1} = 0.7 V, V_{T,M2} = 0.8 V$  and (c)  $V_{T,M1} = 0.8 V, V_{T,M2} = 0.8 V$ ? How does this compare with the results of Problem 1 & 2? Why?

#### Problem 4

This problem illustrates the effects of battery internal resistance on the small signal performance of an amplifier. The MOSFETs in Fig. 4 have  $V_T = 0.7 V$ , and  $\mu_n C_{ox} = 500 \,\mu A/V^2$ . Like in Problem 1, the drain current in M2 is to be 1 mA.  $R_b$  represents the internal resistance of the battery. To determine the operating point, neglect the drop across  $R_b$  due to the current flowing through the gate-bias resistors. For the first three parts, set Cb = 0.

- For  $R_b = 0$ , determine the (W/L) of the FET and the quiescent  $V_{GS}$  and  $V_{DS}$ . Determine the small signal y-parameters of the two port enclosed in the box. What do you observe about  $y_{12}$ ? Why? Is there *any* AC negative feedback around M2?
- Repeat the above exercise for  $R_b = 500 \,\Omega$ . Comment on the results.
- To avoid degradation in performance due to the DC drop across  $R_b$ , a student deliberately increases the battery voltage to 5.5 V, so that the device operating point is identical to that in the first part of this problem. Determine the small signal y-parameters of the two port enclosed in the box. What do you observe about  $y_{12}$ ? Why? Is there *any* AC negative feedback around M2?

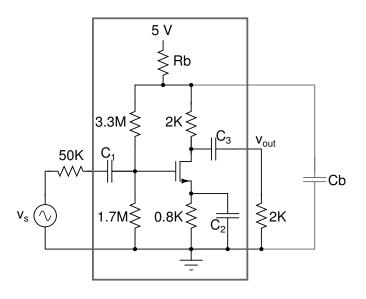


Figure 4: Problem 4

• Based on the observations above, the student adds a **huge** capacitor *Cb* between the battery output and ground. Does this solve the problem(s) faced in part 3 above? Why ?

#### Problem 5

The MOSFET in Fig. 5 has  $V_T = 0.7 V$ , and  $\mu_n C_{ox} = 500 \,\mu A/V^2$ .

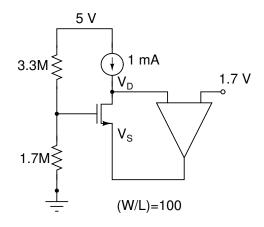


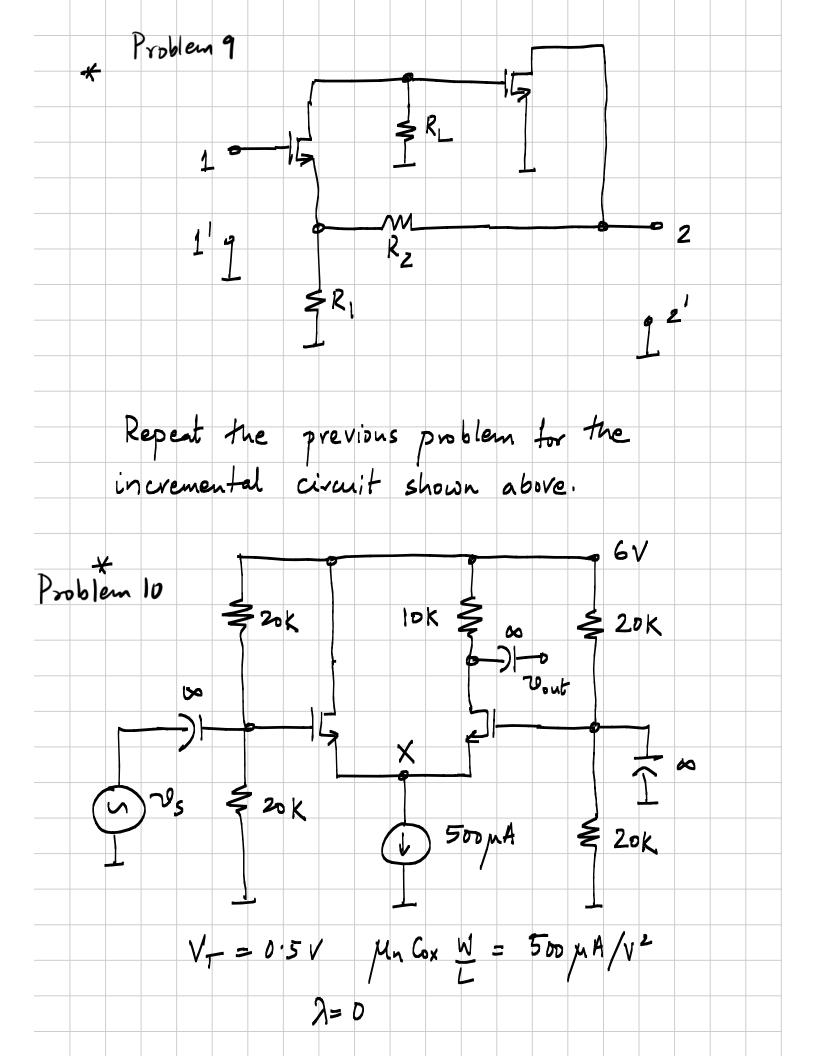
Figure 5: Problem 5

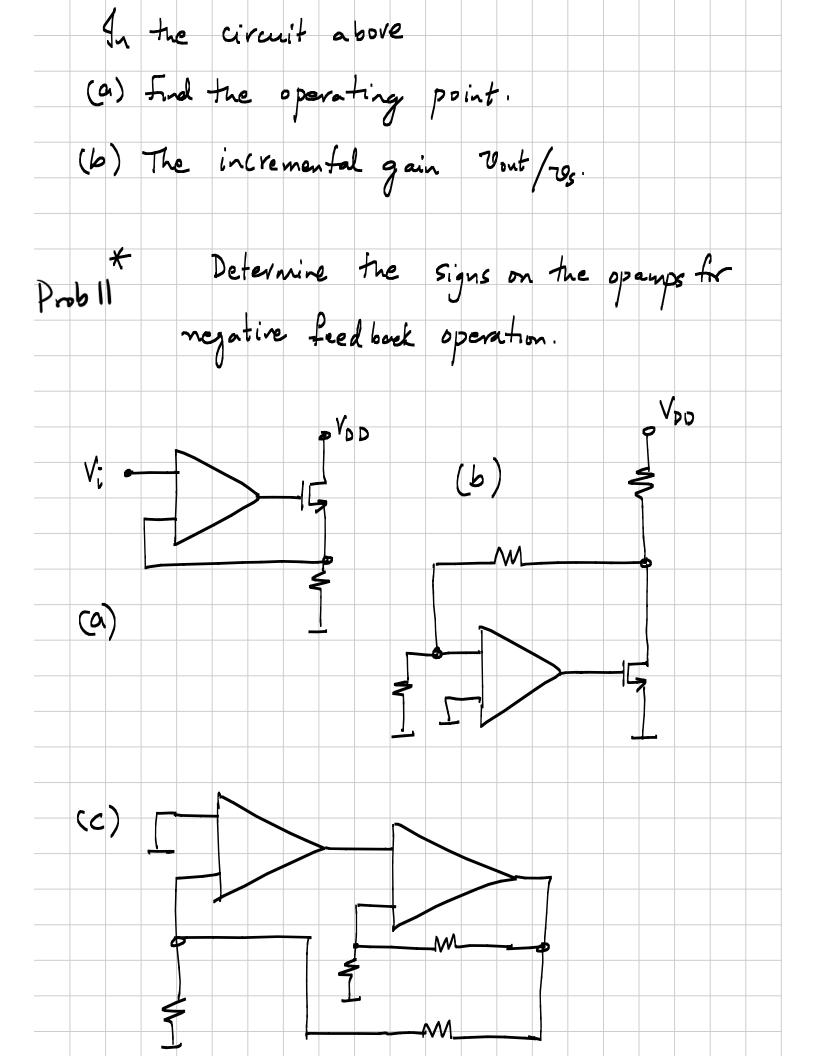
- Reason through the circuit of Fig. 5 and figure out *why* this makes sense.
- Determine the signs on the opamp for negative feedback operation.
- Determine the potentials at nodes *V*<sub>D</sub> and *V*<sub>S</sub>.

Problem 6 For this problem, both transistors are identical,  $\star$ with  $V_{T} = 0.5 V$ ,  $\lambda = D$ ,  $\mu_{L} C_{OX} \frac{V}{L} = 500 \mu k/V^{2}$ \$ 500 mA Rx Cout 8 20 Vin (T 5 18 K Rin Vec The quiescent currents through both transistors are Cqual. Determine Rx, Vss, R, & R2 so that (a) Vin can be coupled without using CI (b)  $Rin = |M\Omega|$ (c) <u>Vout</u> = 2, after accounting for finite 9 m of the Vin transistors After determining the values above, find the quiescent voltage at node Y and the maximum Sinusoidal amplitude one can use at the input so that

the output is not distorted. Now, an infinite capacitor is connected from node Z to ground what is yout now? Vin Problem 7 V Vod \* 250 mA + I, 20K  $\begin{array}{c} M_{1} \\ M_{2} \\ M_{3} \\ M_{3}$  $\lambda = 0 \quad , \quad \sqrt{\tau} = \quad 0.5 \checkmark$ (a) Determine the quiescent current of MI. (5) Assuming large 3m, what gain do you expect from Vin to Vout ? What is the actual gain? (1) Determine the input & output impedances Rin & Rout. (d) Determine I, so that the output sinusoid just clips at both extremes for an input amplitude of 1 V. For this port, assume Im is very large. (e) An infinite capacitor is now connected between the node marked X and ground. Determine the incremental gain from Vi to Vout.

\* Problem 8 2 Ź R\_ \_\_\_\_\_R\_\_\_ 1'9 ZR2 The circuit above is the incremental equivalent of an amplifier. The transistors have transconductances denoted by gm. (a) Determine the input impedance @ port 1 when port 2 is shorted (b) Determine the output impedance @ purt 2 when port 1 is shorted. (c) What kind of controlled source is this Z (d) If gn - , determine the transfer function of the above controlled source.





Problem 12 101 SIOK 40K -) - vout 20K IL MI SIONK 5 ) 29 i 51 10 20Қ ≤ (a) Determine the signs on the opomp for negative feedback operation (+) Determine the quiescent potential Q the gate of MI. (c) What is the incremental gain vont 2