

## EE2025 Engineering Electromagnetics: July-Nov 2019

### Tutorial 6: Waveguides

1. A section of a rectangular waveguide of cross-section  $2\text{ cm} \times 1.5\text{ cm}$  is to be used as a delay line in a radar at  $10\text{ GHz}$ . What should be the length of the section to realize a delay of  $10\text{ nsec}$  ?
2. (a) Derive an expression for the conductive loss in a rectangular waveguide for the fundamental mode.  
(b) In a  $5\text{ cm} \times 3\text{ cm}$  waveguide the  $TE_{10}$  mode is propagating at  $10\text{ GHz}$ . The total power carried by the waveguide is  $10\text{ W}$ . If the conductivity of the waveguide walls is  $2 \times 10^7\text{ U/m}$ , find the attenuation constant of the waveguide in  $\text{dB/m}$ .
3. In an air-filled rectangular waveguide with  $a = 2.286\text{ cm}$  and  $b = 1.016\text{ cm}$ , the  $y$  component of the TE mode is given by

$$E_y = \sin(2\pi x/a) \cos(3\pi y/b) \sin(10\pi \times 10^{10}t - \beta z) V/m$$

Find

- (a) the operating mode
  - (b) the propagation constant  $\gamma$
  - (c) the intrinsic impedance  $\eta$
  - (d) Find the dielectric loss  $\alpha_d$  of the mode when the waveguide is filled with water( Complex permittivity of water at  $50\text{ GHz}$  is  $\epsilon_0(16.40 - j26.31)$ )
4. A frequency of  $9.5\text{ GHz}$  is used to excite all possible modes in a hollow rectangular waveguide of dimensions  $3\text{ cm} \times 2\text{ cm}$ . The length of the waveguide is  $100\text{ m}$ . Find the difference between time of arrivals of the fastest mode and the slowest mode.
  5. A  $240$  degree phase shift is produced by a  $4\text{ GHz}$  signal when traveling along a dielectric filled waveguide  $3\text{ cm}$  long. If the cutoff frequency of the waveguide when air-filled is  $10\text{ GHz}$ , calculate the relative permittivity of the dielectric.
  6. For a square waveguide, show that attenuation  $\alpha_c$  is minimum for  $TE_{10}$  mode when  $f = 2.962f_c$
  7. A  $4\text{ cm}$  square waveguide is filled with a dielectric with complex permittivity  $\epsilon_c = 16\epsilon_0(1 - j10^{-4})$  and is excited with the  $TM_{21}$  mode. If the waveguide operates at  $10\%$  above the cutoff frequency, calculate attenuation  $\alpha_d$ . How far can the wave travel down the guide before its magnitude is reduced by  $20\%$  ?