## Solutions to Problem Set 9

## EE419: Digital Communication Systems

Check the solutions for possible bugs!

2. (a) The relations between the input sequence  $\{u_n\}$  and the output sequences  $\{v_n^{(1)}\}$  and  $\{v_n^{(2)}\}$  are as follows:

$$\begin{aligned} v_n^{(1)} &= u_n^{(1)} + u_{n-3}^{(1)}, \\ v_n^{(2)} &= u_n^{(1)} + u_{n-1}^{(1)} + u_{n-2}^{(1)} + u_{n-3}^{(1)}. \end{aligned}$$

(b) The trellis is shown in Fig. 1.

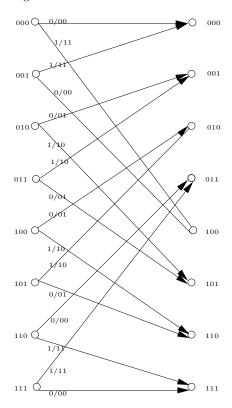


Figure 1: One stage of the trellis.

(c) Encoding of (111111....):

$$v_n^{(1)} = 111000000.....$$
  
 $v_n^{(2)} = 101000000.....$ 

3. (a) The relations between the input sequence  $\{u_n\}$  and the output sequences  $\{v_n^{(1)}\}$  and  $\{v_n^{(2)}\}$  are as follows:

$$v_n^{(1)} = u_n^{(1)},$$
 
$$v_n^{(2)} = u_n^{(1)} + u_{n-1}^{(1)}.$$

The trellis for 4 message bits is shown in Fig. 2.

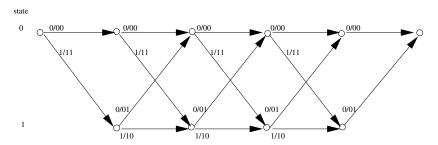


Figure 2: Trellis Diagram for 4 message bits with zero termination.

- (b) Number of codewords = Number of possible messages =  $2^4 = 16$ .
- (c) Viterbi decoding over a BSC is shown in Fig. 3. The final survivor is shown in red. The ML decoded message is seen to be 1000.

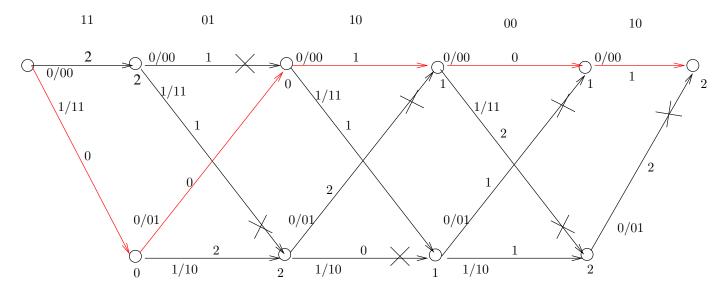


Figure 3: Viterbi Decoding over BSC.

(d) Viterbi Decoding over AWGN is shown in Fig. 4. The final survivor is shown in red. The ML decoded message is seen to be 0111.

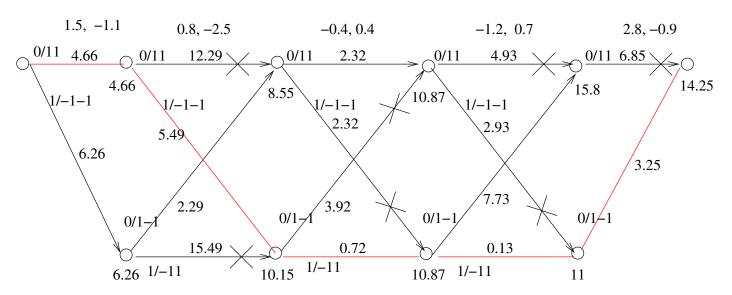


Figure 4: Viterbi Decoding over AWGN.